

31 the outer tubes, to take due account of outward-only local buckling, and the effective
32 compressive strength of the infilled concrete, to reflect the reduced relative effectiveness of
33 higher concrete grades, are considered. The modified design rules are shown to improve the
34 accuracy and consistency of the design capacity predictions. Finally, statistical analyses were
35 carried out to demonstrate the reliability of the modified design approaches.

36

37 **1. Introduction**

38 The use of concrete-filled steel tubular (CFST) cross-sections for compression members has
39 become increasingly widespread in construction, owing primarily to their superior strengths,
40 stiffnesses and ductility over plain concrete or hollow steel tubes [1,2]. The interaction between
41 the concrete infill and the outer metal tube leads to efficient utilisation of both constituent
42 materials by confining the concrete core and delaying local buckling of the metal tube, thereby
43 improving the cost-effectiveness of the system. Recently, research efforts have turned towards
44 concrete-filled double skin tubular (CFDST) cross-sections, comprising two metal tubes and
45 sandwiched concrete filled between the tubes [3-7]. CFDST cross-sections share most of the
46 benefits of CFST cross-sections, but will typically be lighter owing to the absence of the inner
47 concrete core. This facilitates assembly and deconstruction and reduces foundation costs,
48 making CFDST cross-sections an attractive choice for heavy structural applications. Such
49 potential applications include offshore structures [3] and bridge piers [4]; an early example of
50 the use of CFDST columns in a transmission tower is described in [5].

51

52 Stainless steel members possess a unique combination of excellent mechanical properties for
53 structural applications and corrosion resistance, and have been utilised in construction
54 increasingly over the past few decades [8]. An innovative form of CFDST cross-section,
55 utilising stainless steel for the outer tube, was recently proposed [9–12], with the aim of

56 exploiting the most favourable properties of the constituent materials to the greatest possible
57 extent. CFDST columns using stainless steel for the outer tubes were found to exhibit a rather
58 more rounded and ductile load–deformation response compared to their carbon steel
59 counterparts [10–12]. These observations mirror the findings for concrete-filled stainless steel
60 tubular stub columns in a number of recent studies, including concrete-filled stainless steel stub
61 columns with circular [13], rectangular [14–16] and square [14–17] cross-sections. This
62 behaviour is directly linked to the rounded stress–strain response and substantial strain
63 hardening that characterises stainless steel alloys. The combined advantages of the composite
64 action seen in CFDST members, alongside the durability and ductility associated with stainless
65 steel, make this section type potentially suitable for applications in demanding and aggressive
66 environments, such as in offshore and marine structures, bridges and the nuclear industry.

67

68 Research into CFDST members dates back about 20 years and has mainly focussed on CFDST
69 sections employing carbon steel tubes and sandwiched concrete grades up to 72 MPa [18].
70 CFDST sections with stainless steel outer tubes have been the subject of only a few studies,
71 where their structural performance has been examined through experimentation and numerical
72 analysis. Han et al. [9] carried out a preliminary experimental investigation to examine the
73 behaviour of CFDST stub columns with austenitic stainless steel outer tubes. Further tests were
74 conducted by the authors of the present paper [10] to examine the cross-sectional behaviour and
75 resistances of CFDST stub columns with lean duplex and ferritic stainless steel outer tubes in
76 pure compression. Meanwhile, the authors [11,12] also examined CFDST stub columns
77 comprising austenitic stainless steel outer tubes and high strength steel inner tubes
78 experimentally and numerically. FE analyses were employed by Hassanein and Kharoob [19]
79 and Wang et al. [20] with the focus on CFDST cross-sections with circular hollow section (CHS)
80 inner tubes. To date, investigations into the structural performance of CFDST members

81 employing stainless steel as the outer tubes have been rather limited, and the design of these
82 members is not explicitly covered by current codes of practice. This prompted a thorough
83 programme of research performed by the authors, aimed at examining the behaviour and
84 capacity of CFDST structural members with stainless steel outer tubes of varying cross-section
85 shape and devising efficient structural design rules to support their application in practice. The
86 present paper focuses on the compressive behaviour and design of CFDST cross-sections with
87 square or rectangular hollow section (SHS/RHS) lean duplex or ferritic stainless steel outer
88 tubes and SHS carbon steel inner tubes.

89

90 A finite element (FE) investigation into the compressive behaviour of the examined CFDST
91 cross-sections is reported. The numerical modelling programme comprises a validation study
92 to replicate the structural response observed in available experiments described in the literature,
93 and a parametric study to generate further FE data on CFDST sections of varying local
94 slendernesses and material strengths. Based on the generated FE results, the influence of the
95 local slendernesses of the outer and inner tubes, the concrete strength and the grade of stainless
96 steel, on the ultimate response of the studied CFDST sections in compression is examined. The
97 combined set of FE and test data is then adopted to assess the applicability of current design
98 rules for concrete-filled members set out in the European Code EN 1994-1-1 (EC4) [21],
99 Australian Standard AS5100 [22] and American Specifications AISC 360 [23] and ACI 318
100 [24] to the design of the studied CFDST cross-sections. Modifications to the design treatment
101 in relation to the effective areas of the outer tubes and the effective compressive strength of the
102 concrete are considered. Finally, the reliability of the modified design approaches is evaluated
103 through statistical analyses.

104

105 **2. Review of existing experimental data**

106 A number of experimental investigation into the compressive behaviour of CFDST cross-
107 sections with stainless steel outer tubes have been carried out [9–12], but the only previous
108 experiments on CFDST cross-sections with SHS carbon steel inner tubes and SHS/RHS lean
109 duplex and ferritic stainless steel outer tubes (see Fig. 1), which are the focus of the present
110 study, were reported in Wang et al. [10]. In the study of Wang et al. [10], stub column tests
111 were conducted on eight different cross-sections with lean duplex stainless steel (Grade 1.4062)
112 RHS 150×80×3 (depth × width × thickness in mm) and SHS 100×100×3 or ferritic stainless
113 steel (Grade 1.4003) RHS 120×80×3 and 100×80×4 as the outer tubes, and carbon steel (Grade
114 S275) SHS 20×20×2.5, 20×20×1.5, 40×40×4 and 40×40×1.5 as the inner tubes. For each cross-
115 section, three concrete grades with nominal concrete cylinder compressive strengths of 40, 80
116 and 120 MPa were employed. A total of 28 stub column tests was carried out employing the
117 experimental rig shown in Fig. 2(a); a full description of the stub column tests is provided in
118 Wang et al. [10]. The observed failure modes featured outward-only local buckling of the
119 stainless steel outer tubes, crushing of the infill concrete, as well as local buckling of the carbon
120 steel inner tube, as displayed in Fig. 3. A summary of the measured geometric and material
121 properties, as well as the obtained experimental failure load for each stub column specimen is
122 reported in Table 1, where D_o/t_o and D_i/t_i are the overall depth-to-thickness ratios of the outer
123 and inner tubes respectively, in which D_o and D_i correspond to the overall depths of the outer
124 and inner tubes, t_o and t_i are the corresponding thicknesses, $\sigma_{0.2,o}$ and $\sigma_{0.2,i}$ correspond to the
125 material 0.2% proof stresses of the outer and inner tubes, f_c is the cylinder compressive strength
126 of the concrete and N_{exp} is the experimental failure load.

127

128 **3. Numerical modelling programme**

129 A comprehensive numerical modelling programme was performed employing the general-
130 purpose finite element (FE) analysis package ABAQUS [25]. FE models were established with

131 the aim of (i) replicating the compressive behaviour of the CFDST stub column test specimens
132 reported in [10] and (ii) performing a parametric study to derive further FE data and investigate
133 the influence of key variables on the structural performance of the studied CFDST cross-
134 sections in compression. The main features of the FE models are described in Section 3.1, while
135 the validation and parametric study are reported in Sections 3.2 and 3.3, respectively.

136

137 **3.1 Development of finite element models**

138 ***3.1.1. Element types and discretisation***

139 FE models of all test specimens presented in Section 2 were established employing C3D8R [25]
140 solid elements for the concrete and S4R [25] shell elements for the metal tubes, in line with
141 previous numerical modelling of concrete-filled tubular members [11,12,26–29]. A systematic
142 mesh sensitivity study was undertaken to decide upon suitable mesh settings for the FE models,
143 in order to produce accurate yet computationally efficient results. For the cold-formed metal
144 tubes, the element size for the flat portions was chosen to be equal to the respective cross-
145 section thickness, while each corner of the cross-section was uniformly discretised into at least
146 four elements to ensure a precise representation of the curved corner geometry. For the
147 sandwiched concrete, the element sizes were selected to match those of the adjacent metal tubes
148 in order to facilitate numerical convergence.

149

150 ***3.1.2. Material Modelling***

151 The material constitutive properties of the metal tubes were represented by multi-linear elastic-
152 plastic stress–strain curves with isotropic hardening in ABAQUS [25]. The input true stress–
153 true plastic strain data set was derived from the measured engineering stress–strain curves,
154 characterised by at least 100 intervals to ensure the full range of the response was accurately
155 captured. The cold-formed metal tubes experienced plastic deformations during the cold-rolling

156 process, causing an increase in strength and a loss in ductility. This is particularly pronounced
157 in the corner regions and more significant in stainless steel, as observed from the coupon test
158 results reported by Wang et al. [10]. The yield strengths of the corner materials were found to
159 be about 50%, 35% and 10% higher, on average, than those of the flat materials for the lean
160 duplex stainless steel, ferritic stainless steel, and carbon steel sections, respectively. Hence,
161 allowance for this was made in the current FE models by assigning the corner material
162 properties to the respective curved corner regions and the adjacent flat regions beyond the
163 corners by a distance of two times the cross-section thickness, following the recommendations
164 of [30].

165

166 The material properties of the sandwiched concrete were characterised by the built-in concrete
167 damage plasticity (CDP) model in ABAQUS [25]. The Poisson's ratio of the concrete and
168 modulus of elasticity E_c were set respectively equal to 0.2 and $4733 \sqrt{f_c}$, respectively, in
169 accordance with ACI 318 [24]. For the compressive properties of the concrete used in the CDP
170 model, a confined concrete stress–strain curve was adopted to take due account of the
171 confinement afforded to the concrete by the metal tubes. The confined stress–strain curve was
172 originally calibrated against test data on carbon steel CFST stub columns with concrete cylinder
173 compressive strengths ranging from 13 to 164 MPa by Tao et al. [28], and modified by the
174 authors [11,12] for application to CFDST stub columns with stainless steel outer tubes. The
175 modifications were concerned primarily with the confinement factor (ξ_c), as defined by Eq. (1),

176

$$\xi_c = \frac{A_o \sigma_{0.2,o}}{A_{ce} f_c} \quad (1)$$

177 where A_o is the cross-sectional area of the outer tube and A_{ce} is an equivalent cross-sectional
178 area of the sandwiched concrete, defined as the full area enclosed by the outer tube, as given
179 by Eq. (2), where $r_{int,o}$ is the internal corner radius of the outer tube.

180
$$A_{ve} = (D_o - 2t_o)^2 - (4 - \pi)r_{int,o}^2 \quad (2)$$

181 For the tensile properties of the concrete used in the CDP model, a stress–strain curve
182 comprising a linear response up to the ultimate tensile strength, taken as $0.1f_c$, and a descending
183 branch characterised by fracture energy (G_F) [25,28], was adopted throughout the numerical
184 modelling programme.

185

186 ***3.1.3. Boundary conditions and interactions***

187 The geometry, loading and experimentally observed failure modes of the studied CFDST
188 specimens were doubly symmetric. Hence, to enhance computational efficiency, only one-
189 quarter of the cross-sections and half of the stub column lengths were modelled, with suitable
190 boundary conditions assigned to the planes of symmetry, as depicted in Fig. 2(b). For ease of
191 application of boundary conditions, the end sections of the three constituent parts of the CFDST
192 stub columns were coupled to three reference points, which were restrained against all degrees
193 of freedom except longitudinal translation in order to attain fixed-ended boundary conditions.
194 The same value of longitudinal displacement was applied at the three reference points to mimic
195 the displacement-controlled compressive loading scheme used in the experiments.

196

197 The interaction between the outer and inner tubes and the concrete was modelled using surface-
198 to-surface contact. “Hard contact” was employed in the normal direction, while the Coulomb
199 friction model was adopted to simulate the tangential behaviour. A value of 0.6 was selected
200 for the friction coefficient, though a prior sensitivity study had revealed that the compressive
201 response of the studied CFDST cross-sections was relatively insensitive to variation in this
202 parameter [31]. This is primarily due to the nature of the loading (i.e. axial compression), under
203 which the slip at the interfaces was negligible since the concrete and the metal tubes largely
204 deform together.

205

206 ***3.1.4. Initial imperfections and residual stresses***

207

208 Local geometric imperfections and residual stresses have negligible influence on the behaviour
209 of CFDST stub columns, owing principally to the fact that (i) the lateral pressure applied to the
210 steel tubes from the expansion of the concrete obviates the need to assign any geometric
211 perturbation to induce local buckling, and (ii) the support afforded to the metal tubes by the
212 concrete lessens the sensitivity of the tubes to local instabilities [11,12]. Therefore, local
213 geometric imperfections and residual stresses were not explicitly included in the current FE
214 models. The suitability of this treatment is confirmed through the validation of the FE models
215 reported in Section 3.2.

216

217 ***3.1.5. Solution schemes***

218 The modified Riks method (Riks) is commonly adopted for solving static numerical problems
219 with geometrical and material nonlinearities [25], and was generally employed in the present
220 study for the displacement-controlled nonlinear numerical analyses of the CFDST stub columns.
221 However, for some of the models, particularly those with more slender metal tubes,
222 convergence problems inhibited attainment of the peak loads or tracing of the post-ultimate
223 responses. In these cases, an adaptive automatic stabilisation scheme [25], which allows the
224 model to be stabilised by implementing an artificial viscous damping force, was employed in
225 the FE simulations. This approach has been successfully utilised for cold-formed steel members
226 and systems in [32,33], and shown to achieve satisfactory results provided that a sufficient
227 number of increments are achieved before the peak load is reached and that the ratio of the
228 energy dissipated by viscous damping (ALLSD) to the total strain energy (ALLIE) remains low.
229 In this study, at least 50 successful increments prior to reaching the peak load were achieved

230 and the ratios of ALLSD/ALLIE remained below 2%. The load versus average axial strain
231 (defined as the axial shortening divided by the stub column length) curve obtained using the
232 automatic stabilisation scheme is compared with that obtained using the modified Riks method
233 in Fig. 4 for a typical FE model featuring an SHS 600×600×12 lean duplex outer tube, an SHS
234 300×300×5 carbon steel inner tube and a concrete strength of 40 MPa; this specimen is denoted
235 LS600×12-NS300×5-C40 herein. The comparison reveals that similar results are achieved
236 using the two solution schemes with a maximum discrepancy of approximately 1% at the peak
237 load.

238

239 **3.2. Validation of FE model**

240 The developed FE model was validated with reference to the results of the tested CFDST stub
241 columns presented in Section 2; comparisons were made of the ultimate loads, load–
242 displacement curves and failure modes. Table 1 reports the numerical to experimental ultimate
243 compressive capacity ratio (N_{FE}/N_{exp}) for each tested CFDST specimen. A mean value of
244 N_{FE}/N_{exp} of 1.02 with a coefficient of variation (COV) of 0.035 was achieved, indicating that
245 the FE ultimate strengths are in close agreement with those obtained from the tests. The FE
246 models were also found to reproduce accurately the full load–deformation histories of the
247 respective stub column tests, examples of which are displayed in Fig. 5. The exhibited failure
248 modes were also well replicated numerically, as shown in Fig. 3. Overall, it may be concluded
249 that the established FE models can accurately and reliably simulate the experimental structural
250 responses of the examined CFDST stub columns.

251

252 **3.3. Parametric study**

253 The successfully validated FE models were utilised to acquire further FE data on CFDST cross-
254 sections with varying cross-section slendernesses and material strengths. The CFDST cross-

255 sections included in the parametric study cover compact, noncompact and slender cross-
256 sections, with reference to the classification limits for composite cross-sections in AISC 360
257 [23]. Regarding the geometric properties of the modelled cross-sections, the inner and outer
258 tubes were SHS with overall widths fixed at 300 and 600 mm, respectively, while the
259 thicknesses were varied to generate a wide spectrum of local slenderness values (d_i/t_i and d_o/t_o)
260 from 6 to 146, where d_i and d_o are the flat element widths of the inner and outer tubes. Note
261 that the studied d_o/t_o ratios cover the practical range of available rolled stainless steel sections
262 but also extend to more slender sections, which could be produced by press-braking, to assess
263 their performance in concrete-filled tubular construction. The internal corner radii of the outer
264 and inner tubes were set equal to the respective section thicknesses. The length of each FE
265 model was equal to $2.5D_o$, mirroring the test specimens. Throughout the parametric study, the
266 measured material properties of the tested lean duplex stainless steel SHS 100×100×3 and
267 ferritic stainless steel RHS 120×80×3 were used for the outer tubes, while those of the tested
268 carbon steel SHS 40×40×4 were used for the inner tubes. Three concrete grades with concrete
269 compressive strengths of 40, 80 and 120 MPa were adopted. Table 2 lists the ranges of variation
270 of the aforementioned parameters considered herein. Overall, a total of 311 CFDST specimens
271 was simulated in the parametric study.

272

273 The derived FE results were employed to examine the influence of the key variables on the
274 ultimate strength of the studied CFDST stub columns (N_u), including the local slendernesses of
275 the outer and inner tubes, the concrete grade and the stainless steel grade. Note that the load–
276 axial strain curves for some compact specimens did not reach their peak loads despite large
277 plastic deformations. For these specimens, the ultimate strength was defined as the load at
278 which the tangent stiffness of the load–axial strain curve at increment i , K_i , reached 1% of its
279 initial stiffness, K_{ini} — i.e. failure was taken at the point when $K_i/K_{ini} = 0.01$, a typical example

280 of which is illustrated in Fig. 6. This approach was proposed by dos Santos et al. [34] and has
281 been employed for the definition of the ultimate strengths of concrete-filled tubular members
282 in [11,12,14].

283

284 **3.3.1 Influence of local slenderness of metal tube**

285 The influence of the local slenderness of the outer tube on the ultimate response is assessed
286 through comparisons among specimens with the same inner tubes and concrete grades but
287 varying local slenderness values for the outer tube (d_o/t_o). In the comparisons presented, the
288 ultimate strength (N_u) obtained from the CFDST stub column FE simulations are normalised
289 by the respective plastic strength (N_{pl}) of the cross-sections, as defined by Eq. (3), which is a
290 simple summation of the plastic resistances of the outer tube, concrete and inner tube.

$$291 \quad N_{pl} = A_o \sigma_{0.2,o} + A_c f_c + A_i \sigma_{0.2,i} \quad (3)$$

292

293 The results are displayed in Fig. 7, where the normalised strength (N_u/N_{pl}) is plotted against the
294 local slenderness of the outer tube d_o/t_o . A total of 10 groups of data, differentiated by the local
295 slenderness of inner tube d_i/t_i , are compared, each comprising a spectrum of d_o/t_o ratios ranging
296 from 4 to 146. It can be observed that the specimens with the more compact outer tubes
297 exhibited the higher values of N_u/N_{pl} ; this is attributed to the reduced susceptibility to local
298 buckling and the improved confinement afforded to the concrete. Typical load–axial strain
299 curves, shown for specimens LS600×5-NS300×10-C40, LS600×20-NS300×10-C40 and
300 LS600×30-NS300×10-C40, are presented in Figs 8(a)–(c), while the load–carrying
301 contributions from the outer tube, concrete and inner tube, normalised by their corresponding
302 plastic loads (denoted $A_o \sigma_{0.2,o}$, $A_c f_c$ and $A_i \sigma_{0.2,i}$), are compared in Figs 8(d)–(f). It can be seen
303 that the slender stainless steel outer tube (LS600×5) was prone to local buckling and failed to
304 attain its yield load ($A_o \sigma_{0.2,o}$), while the more compact outer tubes (LS600×20 and LS600×30)

305 were able to exceed their yield loads and exhibit the pronounced strain hardening that
306 characterises stainless steel materials. The performance of the sandwiched concrete, in terms of
307 both strength and ductility, was also found to improve when a more compact outer tube was
308 used due to the greater confinement afforded to the concrete, as depicted in Fig 8(e).

309

310 Compared to the local slenderness of the outer tube, that of the inner tube was found to be less
311 influential on the ultimate response of the studied CFDST cross-sections. This can be seen in
312 Fig. 7, where, for a given d_o/t_o value, the difference in results between the CFDST stub columns
313 with varying d_i/t_i values is minimal. This is also evident in Fig. 9, where the normalised strength
314 N_u/N_{pl} can be seen to remain almost unaltered across the range of d_i/t_i ratios from 6 to 146.
315 Typical examples are shown in Fig. 10 for the examined CFDST stub columns with d_i/t_i ratios
316 of 26, 56 and 96. It can be seen that the performance of the outer tube and concrete appears not
317 to be greatly influenced by the compactness of the inner tube; in addition, despite the inner tube
318 failing by local buckling at a relatively low average axial strain for specimen LS600×3-
319 NS300×3-C40, the ultimate strength of the cross-section, which is dominated by the outer tube
320 and the concrete, is reached at a much later stage. Overall, it is concluded that the compactness
321 of the stainless steel outer tube has a substantial influence on the ultimate response of the
322 CFDST cross-sections, while the local slenderness of the carbon steel inner tube, which
323 represents only a relatively small contribution to the plastic resistance of the overall CFDST
324 cross-section, is less influential.

325

326 **3.3.2 Influence of concrete grade**

327 Three concrete grades were assessed in the parametric study, with nominal compressive
328 concrete strengths of 40, 80 and 120 MPa. The confined strength of the concrete is directly
329 linked to the cross-sectional compactness and is mainly governed by the local slenderness of

330 the outer tube. Comparisons of normalised strength (N_u/N_{pl}) were therefore made with respect
331 to the local slenderness of the outer tube (d_o/t_o), as shown in Fig. 11. It can be seen that the
332 lower concrete grades result in better normalised ultimate performance in the case of lower
333 outer tube slenderness values, revealing that lower concrete grades can benefit to a greater
334 extent from the confinement offered by the outer tube, provided that the tube is sufficiently
335 stocky.

336

337 **3.3.3 Influence of stainless steel grade**

338 Two stainless steel grades, lean duplex stainless steel (Grade 1.4062) and ferritic stainless steel
339 (Grade 1.4003), were examined in this study. The ultimate performance of CFDST cross-
340 sections utilising the two different grades of stainless steel for the outer tube are compared in
341 Fig. 12(a), revealing improved structural performance associated with the use of the lean duplex
342 grade, particularly in the case of the more compact outer tubes. This is attributed to the more
343 pronounced strain hardening and higher ductility of lean duplex stainless steel over ferritic
344 stainless steel, as displayed in Fig. 12(b).

345

346 **4. Evaluation of current international design codes**

347 **4.1 General**

348 The applicability of the European Code EN 1994-1-1 (EC4) [21], the Australian Standard AS
349 5100 [22] and the two American Specifications—AISC 360 [23] and ACI 318 [24] for
350 composite carbon steel members to the design of the studied CFDST cross-sections is appraised
351 in this section. Limitations on cross-sectional slenderness and material strengths specified in
352 the examined codes are summarised in Table 3. Note that although these code limitations are
353 exceeded for some of the tested [10] and modelled stub columns, comparisons and evaluations

354 are still presented to explore possible extension of the codes beyond their current range
355 applicability.

356

357 **4.2 European Code EN 1994-1-1 (EC4)**

358 The design expression for the axial compressive resistances of square or rectangular carbon
359 steel CFST cross-sections in EC4 [21] is a summation of the plastic resistance of the metal tubes
360 and concrete infill. Account is taken of the higher strength of the concrete infill as a result of
361 the confinement provided by the outer tube, by implementing a concrete coefficient of 1.0,
362 rather than 0.85. The analogous cross-section capacity (N_{EC4}) for a concrete-filled square or
363 rectangular CFDST cross-section in compression is thus given by Eq. (4).

$$364 \quad N_{EC4} = A_o \sigma_{0.2,o} + A_c f_c + A_i \sigma_{0.2,i} \quad (4)$$

365 A slenderness limit of $D_o/t_o \leq 52(235/f_y)^{0.5}$ for concrete-filled composite members is defined in
366 EC4 [21], beyond which the effects of local buckling need to be considered. In this study, this
367 slenderness limit is slightly modified to reflect the difference in Young's modulus between
368 stainless steel and carbon steel, thus: $D_o/t_o \leq 52\sqrt{(235/\sigma_{0.2,o})(E_o/210000)}$. For the CFDST cross-
369 sections exceeding this modified slenderness limit, the effective width formulation set out in
370 EN 1993-1-4 [35,36] for slender stainless steel internal plate elements, as given by Eq. (5), was
371 used for calculating the effective area of the outer tube, where ρ is the local buckling reduction
372 factor, and $\bar{\lambda}_p$ is the plate element slenderness and can be determined from Eq. (6), in which ν
373 is the Poisson's ratio, taken as 0.3, E_o is the Young's modulus of the outer tube, and k is the
374 buckling coefficient, taken equal to 4 for plates with simply supported boundary conditions in
375 pure compression [37,38].

$$376 \quad \rho = \frac{0.772}{\bar{\lambda}_p} - \frac{0.079}{\bar{\lambda}_p^2} \quad (5)$$

377
$$\bar{\lambda}_p = \sqrt{\frac{\sigma_{0.2,o}}{\sigma_{cr}}} = \sqrt{\frac{12(1-\nu^2)\sigma_{0.2,o}}{k\pi^2 E_o}} (d_o/t_o) \quad (6)$$

378
379 **4.3 Australian Standard AS 5100**

380 The Australian Standard AS 5100 [22] adopts the same approach to obtain the axial
381 compressive design resistances as given in EC4 [21], but with a different slenderness limit and
382 effective width expression. A yield slenderness limit of 40 is specified for the flat faces of the
383 outer tube (λ_e) in AS 5100, where the local slenderness λ_e was also modified for stainless steel,
384 as given by $(d_o/t_o)(\sigma_{0.2,o}/250)^{0.5}$. For the design strengths of the test specimens and FE models
385 that exceed this limit, effective areas were again used in place of the gross areas to account for
386 local buckling. The effective width expression for cold-formed stainless steel tubular cross-
387 sections set out in AS/NZS 4673 [39] was adopted for the comparisons with the Australian
388 design provisions, as given by Eq. (7), where λ is a local slenderness, as given by Eq. (8), in
389 which F_n is the overall buckling stress of the column, equal to $\sigma_{0.2,o}$ due to the short length of
390 the studied stub columns, and k is again taken as 4 according to AS/NZS 4673 [39]. Hence, the
391 slenderness λ is essentially the same as that employed in EN 1993-1-4 [35], denoted $\bar{\lambda}_p$ and
392 defined by Eq. (5).

393
$$\rho = \frac{1 - 0.22 / \lambda}{\lambda} \quad (7)$$

394
$$\lambda = \left(\frac{1.052}{\sqrt{k}} \right) \frac{d_o}{t_o} \left(\sqrt{\frac{F_n}{E_o}} \right) \quad (8)$$

395
396 **4.4 American design provisions AISC 360 and ACI 318**

397 The AISC 360 compressive cross-section strength (N_{AISC}) for a square or rectangular concrete-
398 filled column is presented as a function of the slenderness (compactness) of the flat faces of the
399 steel section ($\lambda=d_o/t_o$), as determined from Eq. (9),

$$N_{AISC} = \begin{cases} A_o \sigma_{0.2,o} + 0.85 A_c f_c + A_i \sigma_{0.2,i} & (\lambda < \lambda_p) \\ P_p - \frac{P_p - P_y}{(\lambda_r - \lambda_p)^2} (\lambda - \lambda_p)^2 + A_i \sigma_{0.2,i} & (\lambda_p \leq \lambda < \lambda_y) \\ A_o f_{cr} + 0.7 A_c f_c + A_i \sigma_{0.2,i} & (\lambda \geq \lambda_y) \end{cases} \quad (9)$$

400 where P_p and P_y are determined from Eq. (10) and (11) respectively, λ_p and λ_r correspond to
 401 the limits between compact/noncompact and noncompact/slender cross-sections, again
 402 modified for stainless steel herein, given by $2.26(E_o/\sigma_{0.2,o})^{0.5}$ and $3.00(E_o/\sigma_{0.2,o})^{0.5}$ respectively,
 403 and f_{cr} is the elastic critical local buckling stress of the outer tube, as given by Eq. (12). Note
 404 that the contribution from the inner tube in the resistance function is treated as an independent
 405 term, rather than a concrete dependent term as for reinforcing bars; further explanation has been
 406 provided in previous work by the authors [10–12].

$$408 \quad P_p = A_o \sigma_{0.2,o} + 0.85 A_c f_c + A_i \sigma_{0.2,i} \quad (10)$$

$$409 \quad P_y = A_o \sigma_{0.2,o} + 0.7 A_c f_c + A_i \sigma_{0.2,i} \quad (11)$$

$$410 \quad f_{cr} = \frac{9E_o}{(d_o/t_o)^2} \quad (12)$$

411 The American Concrete Institute design provisions for CFST cross-sections, as set out in ACI
 412 318 [24], are also assessed herein. The confinement afforded to the concrete from the steel tube
 413 is not explicitly considered in ACI 318. Hence, the cross-section resistance (N_{ACI}) is given by
 414 Eq. (13).

$$415 \quad N_{ACI} = A_o \sigma_{0.2,o} + 0.85 A_c f_c + A_i \sigma_{0.2,i} \quad (13)$$

416 The gross area of the outer tube may be used in Eq. (13) provided that the tube thickness satisfies
 417 $t_o \geq D_o(\sigma_{0.2,o}/3E_o)^{0.5}$ [24]. For the design strengths of the test and FE specimens outside this
 418 range, effective areas were again used in place of the gross areas to account for local buckling,
 419 and the effective width expression for cold-formed stainless steel tubular cross-sections given
 420 in the SEI/ASCE-8-02 [40] was utilised in the calculations. Note that SEI/ASCE-8-02 [40]
 421 employs the same effective width formulation as AS/NZS 4673 [40], as given by Eq. (7).

422

423 **4.5 Assessment of current design methods**

424 In this section, the accuracy of the predicted cross-section compressive strengths from the
425 described design methods is evaluated by comparisons against the test and FE failure loads.
426 The mean test and FE to design code prediction ratios N_u/N_{code} , as presented in Table 4, are
427 respectively equal to 1.20, 1.17, 1.27, and 1.27 for EC4, AS 5100, AISC 360 and ACI 318, with
428 COVs of 0.108, 0.100, 0.131, and 0.086, revealing that the current design rules result in rather
429 conservative and scattered compressive strength predictions for the studied CFDST cross-
430 sections. The high level of conservatism and scatter is also evident in Figs 13–16, where the
431 ratios of N_u/N_{code} are plotted against the normalised cross-section slenderness (λ) of each
432 examined code, together with the corresponding normalised cross-section slenderness limits; a
433 summary of the normalised cross-section slenderness measures and limits is reported in Table
434 3. It can be seen that the predictions for the CFDST cross-sections falling within the slenderness
435 limits are unduly conservative, especially in the lower cross-section slenderness range, which
436 may be attributed to the lack of consideration for the substantial strain hardening that the
437 stainless steel outer tube exhibits and the higher degree of confinement afforded to the concrete
438 infill from the stockier outer tubes.

439

440 **5. Modifications to design rules**

441 **5.1 Modification to high strength concrete**

442 The results from the parametric analyses have revealed that the degree of influence of the
443 concrete strength on the compressive capacities of the studied CFDST stub columns differs
444 among the concrete grades, particularly for CFDST stub columns with compact outer tubes. It
445 is therefore suggested that this difference is reflected in the design formulations. It can also be
446 seen in Table 5 that the accuracy of the compressive strength predictions varies with concrete

447 grade for all the examined design codes. Specifically, the design predictions of CFDST cross-
448 sections with lower grade concrete were found to be more conservative than their counterparts
449 with higher grade concrete. This observation echoes the experimental results for the studied
450 CFDST cross-sections in [10], and also mirrors the findings for CFST cross-sections [14] and
451 other CFDST cross-sections [11,12]. To address this, it is proposed that the concrete strength
452 (f_c) in the design expressions is modified by multiplying by a reduction factor η , as specified in
453 EN 1992-1-1 [41] and given by Eq. (14), to account for the effective compressive strength of
454 high grade concrete (greater than 50 MPa). Note that the reduction factor η in EN 1992-1-1 [41]
455 only covers concrete strengths up to 90 MPa, beyond which a constant value of 0.8, as proposed
456 by Liew et al. [42], is employed herein.

$$457 \quad \eta = 1.0 - \frac{f_c - 50}{200} \quad (14)$$

458 The accuracy of the modified capacity predictions is assessed in Table 5, where the mean test
459 and FE to design code prediction ratios (N_u/N_{EC4*} , $N_u/N_{AS5100*}$, N_u/N_{AISC*} , and N_u/N_{ACI*}) and the
460 corresponding COVs for the three concrete grades are presented. The results from the
461 assessment reveal that with the inclusion of the reduction factor η , the modified capacity
462 predictions are more consistent and less scattered across the range of concrete grades from C40
463 to C120.

464

465 **5.2 Modification to design of steel tube**

466 The existing design codes were generally found to result in excessively conservative
467 compressive capacity predictions for the CFDST cross-sections exceeding the specified code
468 slenderness limits. This is can be primarily attributed to the neglect of the beneficial restraining
469 effect of the concrete on the local buckling of the stainless steel outer tubes. Unlike in hollow
470 SHS/RHS members, the local buckling failure mode of the outer tube in the examined CFDST
471 cross-sections features outward-only deformation of all four faces, rather than alternating

472 inward and outward deformations of adjacent faces. It has been shown that the elastic buckling
473 coefficient k [37,38] increases from 4 for conventional (two-way) local buckling of uniformly
474 compressed simply-supported plates to 10.67 for outward-only local buckling [43]. A modified
475 local buckling coefficient k equal to 10.67, rather than 4, has therefore been employed by the
476 authors [10,12] in previous studies to reflect the restraining effect of the concrete on the local
477 buckling of the stainless steel outer tubes. This approach is also assessed herein in the
478 implementation of the design rules in EC4, AS 5100 and ACI 318, taking the local buckling
479 coefficient k as 10.67 in calculating the plate slenderness and hence the effective areas of the
480 outer tubes. It is worth noting that due account of the outward-only buckling mode has already
481 been taken in AISC 360 [23] and reflected in the cross-section noncompact slenderness limit
482 [44,45], which is derived by factoring the corresponding limit for hollow steel cross-sections,
483 $1.40(E/F_y)^{0.5}$, by a value of $(10.67/4)^{0.5}$; further explanation is provided in previous work by the
484 authors [10].

485

486 Quantitative comparisons of the compressive capacities predicted by the modified EC4, AS
487 5100 and ACI 318 (N_{code^*}) incorporating the higher buckling coefficient k of 10.67, and the
488 corresponding predictions from the unmodified design rules with $k=4$, with test and FE ultimate
489 strengths are reported in Table 6 for the slender CFDST cross-sections that fall outside the
490 respective codified noncompact slenderness limits. The mean ratios of N_u/N_{code^*} are all closer
491 to unity and less scattered than those for the case of $k=4$. The notably improved accuracy and
492 consistency is also evident in the graphical comparisons presented in Figs 13, 14 and 16,
493 respectively for the modified EC4, AS 5100 and ACI 318 predictions.

494

495 **5.3 Reliability analysis and discussion**

496 Statistical analyses were conducted to assess the reliability associated with the application of
497 the current and modified design rules to the examined CFDST cross-sections, according to the
498 procedures and requirements specified in EN 1990 [46]. In the present analyses, the mean to
499 nominal yield strength ratios $f_{y,mean}/f_{y,nom}$ were taken as 1.10 [47], 1.20 [47], and 1.16 [48], with
500 COVs of 0.030 [47], 0.045 [47] and 0.055 [48] for the lean duplex stainless steel, ferritic
501 stainless steel and the carbon steel, respectively. For the sandwiched concrete, the over-strength
502 ratio was determined from Eq. (15) [49],

$$503 \quad f_c = f_m - 1.64\delta \quad (15)$$

504 where f_m is the mean compressive concrete strength, and δ is the standard deviation, derived
505 from the measured COV values 0.019, 0.005 and 0.029 for C40, C80 and C120, respectively
506 [10]. The concrete over-strength ratios were therefore equal to 1.03, 1.01 and 1.05 for C40, C80
507 and C120, respectively, while the COV of the concrete strengths used in the reliability analysis
508 was conservatively taken as 0.180 [49] for all grades. The COVs of the geometric properties of
509 the stainless steel outer tube, concrete and carbon steel inner tube were taken as 0.05 [47], 0.01
510 [50] and 0.03 [48], respectively. Note that the partial factors for stainless steel, concrete and
511 carbon steel were taken as 1.10 [35], 1.50 [41] and 1.00 [51] in the assessment of the European
512 design provisions, while corresponding values of 1.11, 1.67 and 1.11 were used in the
513 assessment of the Australian design provisions, converted (inverted) from resistance factors of
514 0.9, 0.6 and 0.9 prescribed in AS 5100 [22] in the numerator rather than denominator. American
515 specifications consider the overall resistance factors, rather than individual partial factors in
516 composite design, with current recommended values in the numerator 0.75 and 0.65 for
517 concrete-filled tubular members, as specified in AISC 360 [23] and ACI 318 [24], respectively.
518 Therefore, the target partial safety factors for composite sections are equal to 1.0 for EC4 and

519 AS5100 design provisions since the individual target partial factors described above are already
520 included, and 1.33 and 1.54 for AISC 360 and ACI 318, respectively.

521

522 The key parameters and results from the Eurocode reliability analysis are summarised in Table
523 7, where $k_{d,n}$ is the design fractile factor, b is the average ratio of experimental and numerical
524 capacities to design model capacities [52], V_{δ} is the COV of the experimental and numerical
525 simulations relative to the resistance model, and γ_{MO} is the resulting partial safety factor for the
526 compressive strengths of the studied CFDST cross-sections. As can be seen from Table 7, the
527 required partial factors for the original and modified design rules are all close to or less than the
528 target values, and thus both the current and modified design rules are considered to satisfy the
529 reliability requirements of EN 1990 [46].

530

531 **6. Conclusions**

532 A comprehensive numerical modelling programme undertaken to examine the compressive
533 behaviour of CFDST cross-sections with lean duplex and ferritic stainless steel outer tubes is
534 reported in this paper. Finite element models have been established to replicate test results
535 reported in the literature, and utilised to acquire further FE data through parametric analyses.
536 The influence of key parameters on the ultimate response of the studied CFDST stub columns
537 was examined, including the local slendernesses of the outer and inner tubes, the concrete
538 strength and the stainless steel grade. The results of the parametric study generally revealed that
539 (i) the compactness of the stainless steel outer tube has a substantial influence on the ultimate
540 response of the CFDST cross-sections, while the local slenderness of the carbon steel inner tube
541 is less influential; (ii) the lower concrete grades can benefit to a greater extent from the
542 confinement offered by the outer tube; (iii) the use of lean duplex grade rather than ferritic
543 stainless steel for the outer tube results in superior CFDST compressive performance. Based on

544 the test and FE results, the applicability of the European Code EN 1994-1-1 (EC4) [21], the
545 Australian Standard AS 5100 [22] and the two American Specifications—AISC 360 [23] and
546 ACI 318 [24] for composite carbon steel members to the design of the studied CFDST cross-
547 sections was assessed. The assessment results generally indicated that the existing design rules
548 result in safe-sided, but unduly conservative (less so for the higher concrete grades) and rather
549 scattered capacity predictions.

550

551 Inaccuracies in the compressive resistance predictions stemmed principally from the lack of
552 consideration of strain hardening in the stainless steel outer tubes, insufficient allowance for
553 the restraining effect of the concrete against local buckling of the metal tubes and differences
554 in behaviour between high strength and normal strength concrete not being fully recognised.
555 Modifications to the current design provisions were therefore considered— a reduction factor
556 η to reflect the reduced relative effectiveness of using higher concrete grades and a higher
557 buckling coefficient k of 10.67 to consider the beneficial restraining effect of the concrete on
558 the local buckling of the stainless steel outer tubes. The modified design rules are shown to
559 yield greater accuracy and consistency, and their reliability was confirmed through statistical
560 analyses.

561

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566

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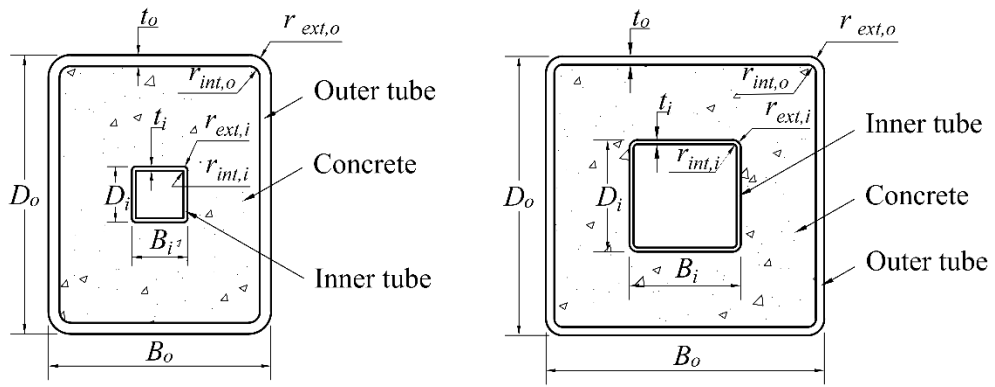
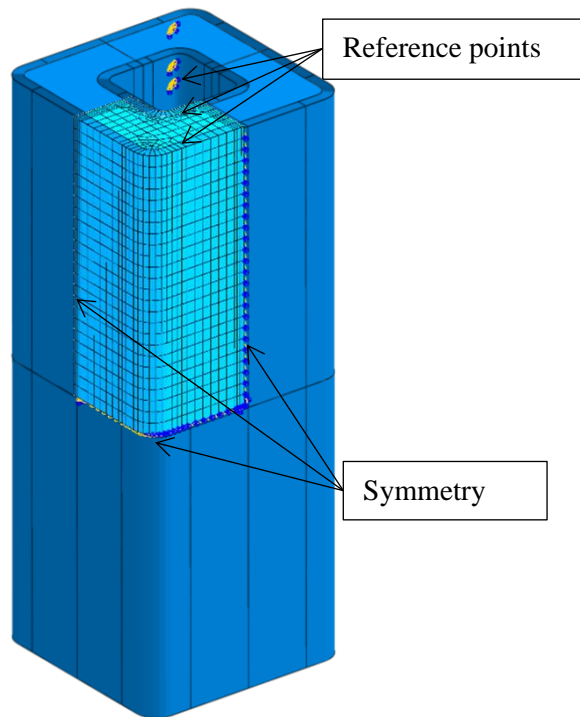


Fig. 1. Definition of symbols for CFDST specimens.

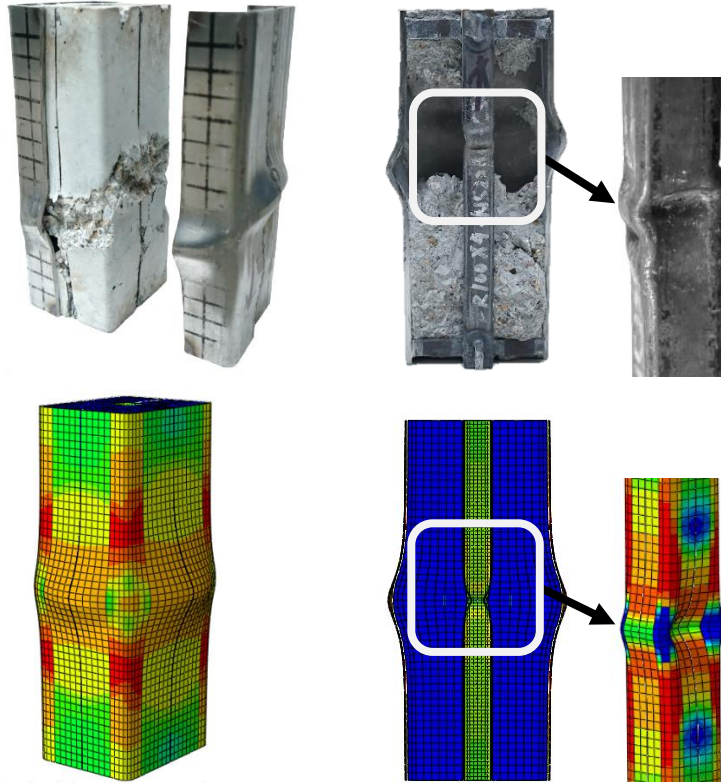


(a) Test setup.

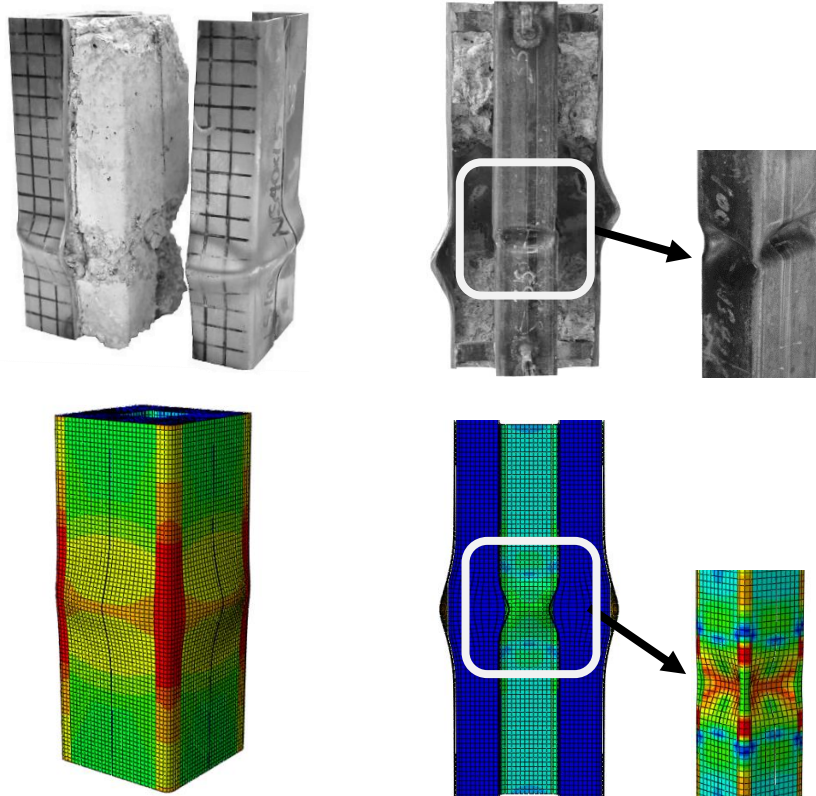


(b) FE model in ABAQUS.

Fig. 2. CFDST stub column (a) test setup and (b) FE model in ABAQUS.



(a) Outward local buckling of outer tube. (b) Inward and outward local buckling of inner tube.



(c) Outward local buckling of outer tube. (d) Inward local buckling of inner tube.

Fig. 3. Experimental and numerical failure modes of stub columns (FR100×4-NS20×1.5-C40 (a, b) LS100×3-NS40×1.5-C40 (c, d)).

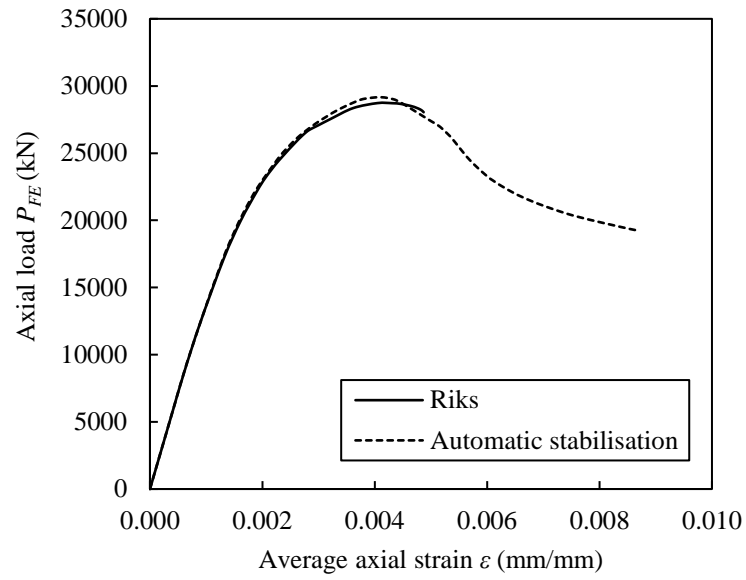


Fig. 4. Comparison of typical load–deformation responses generated from Riks and automatic stabilisation schemes.

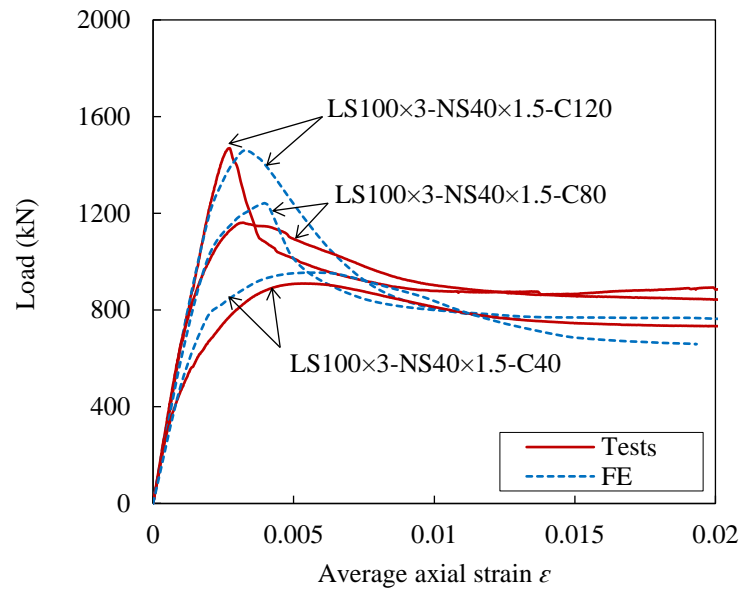


Fig. 5. Comparisons of test and FE load–average axial strain curves.

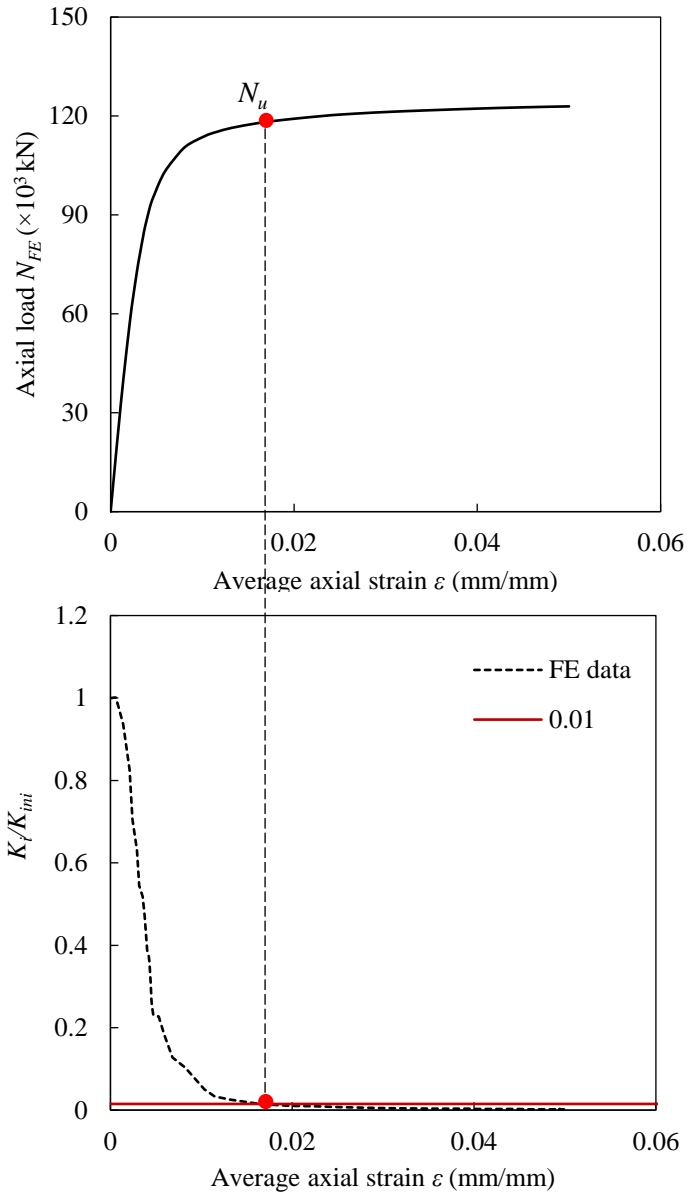


Fig. 6. Definition of ultimate axial compressive resistance when peak load was not attained in FE simulation.

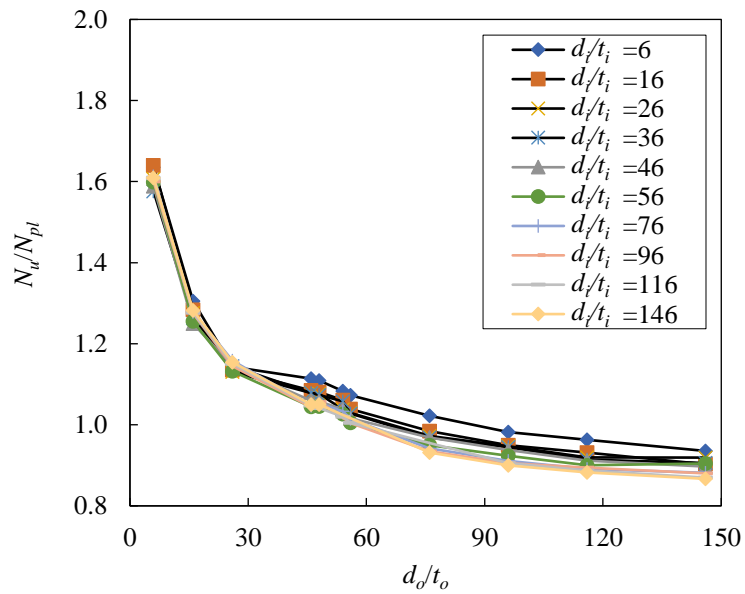
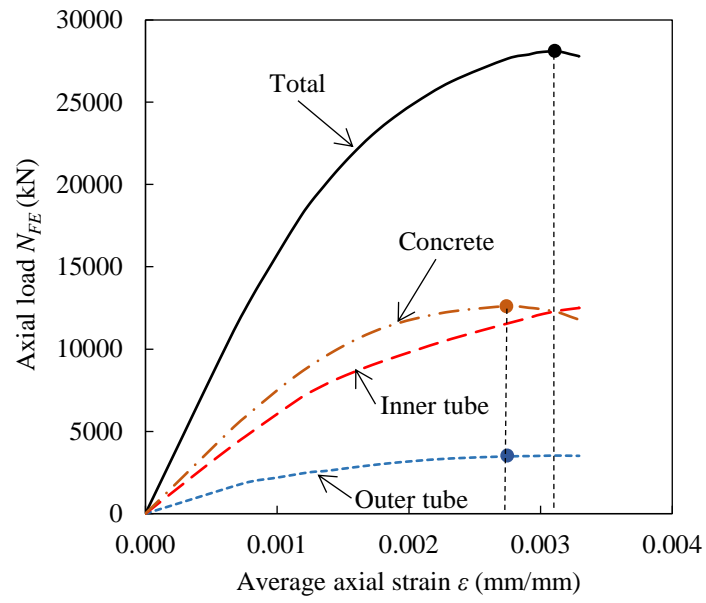
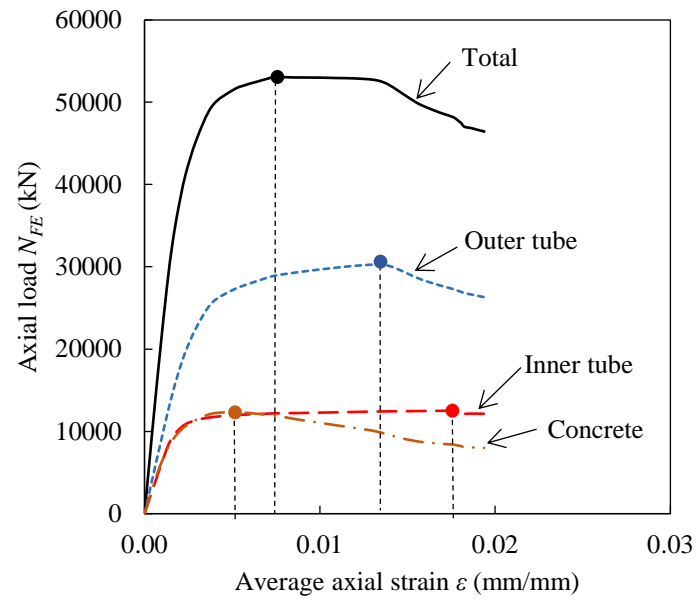


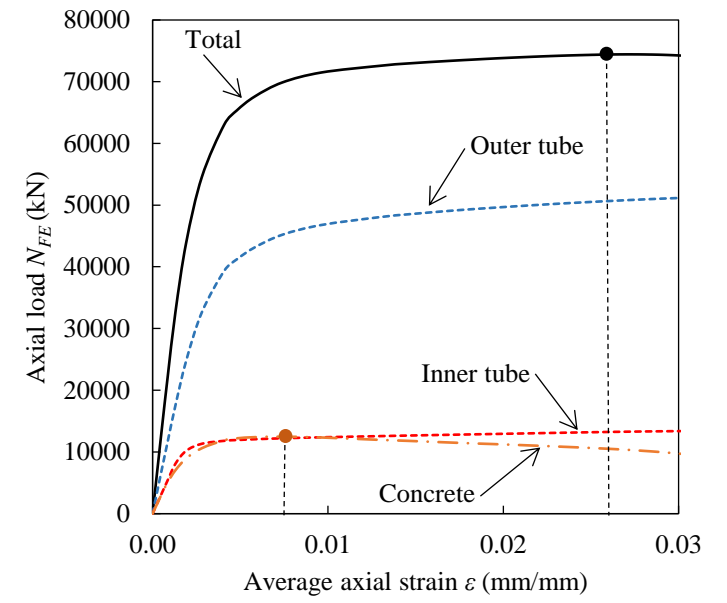
Fig. 7. Influence of outer tube slenderness on normalised resistance of studied CFDST cross-sections.



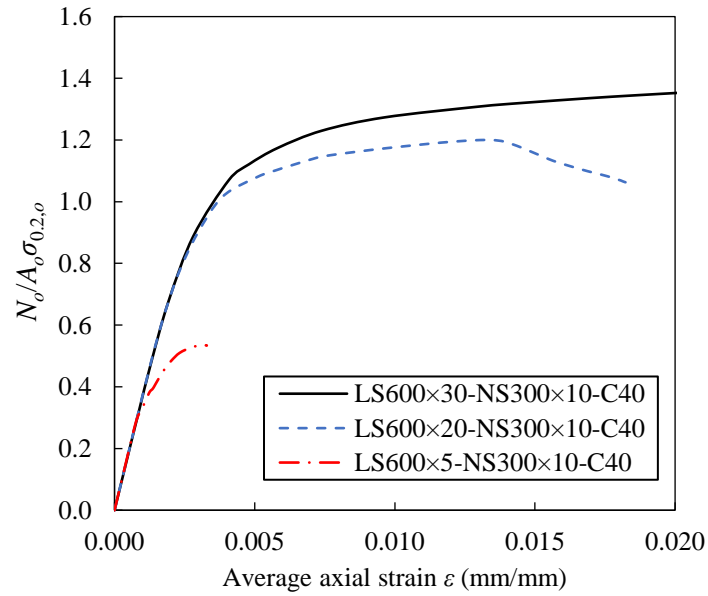
(a) Specimen LS600×5-NS300×10-C40.



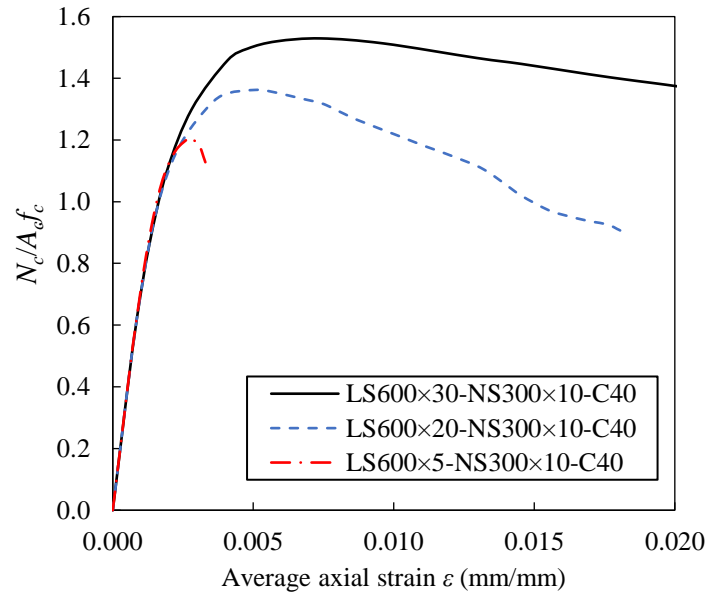
(b) Specimen LS600×20-NS300×10-C40.



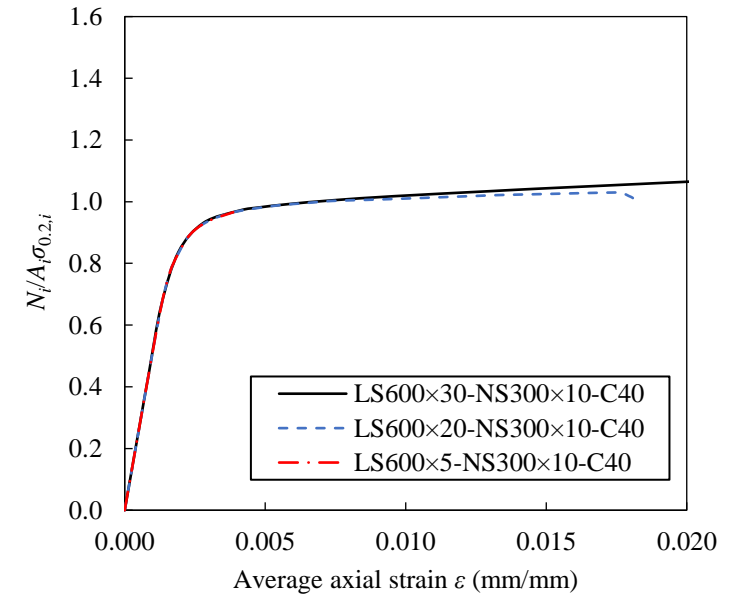
(c) Specimen LS600×30-NS300×10-C40.



(d) Performance of outer tubes.



(e) Performance of concrete.



(f) Performance of inner tubes.

Fig. 8. Comparisons of CFDST specimens with varying outer tube local slendernesses.

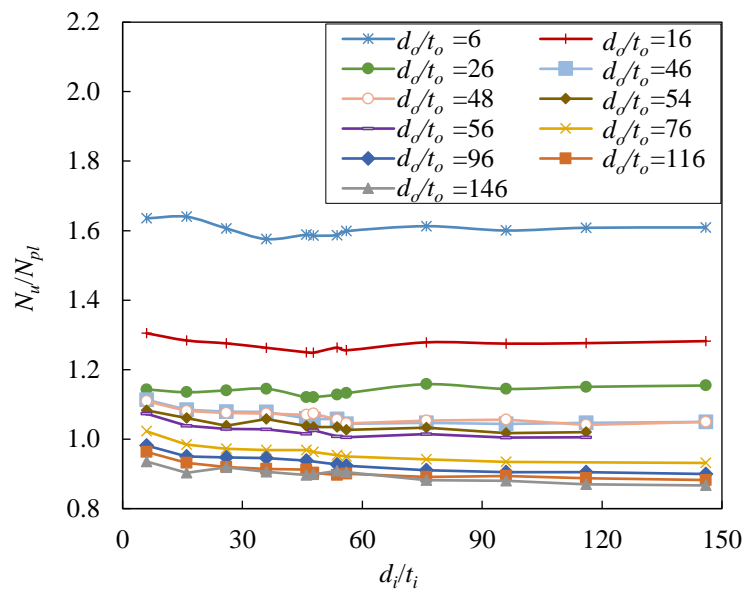


Fig. 9. Influence of inner tube slenderness on normalised load-carrying capacity of studied CFDST sections.

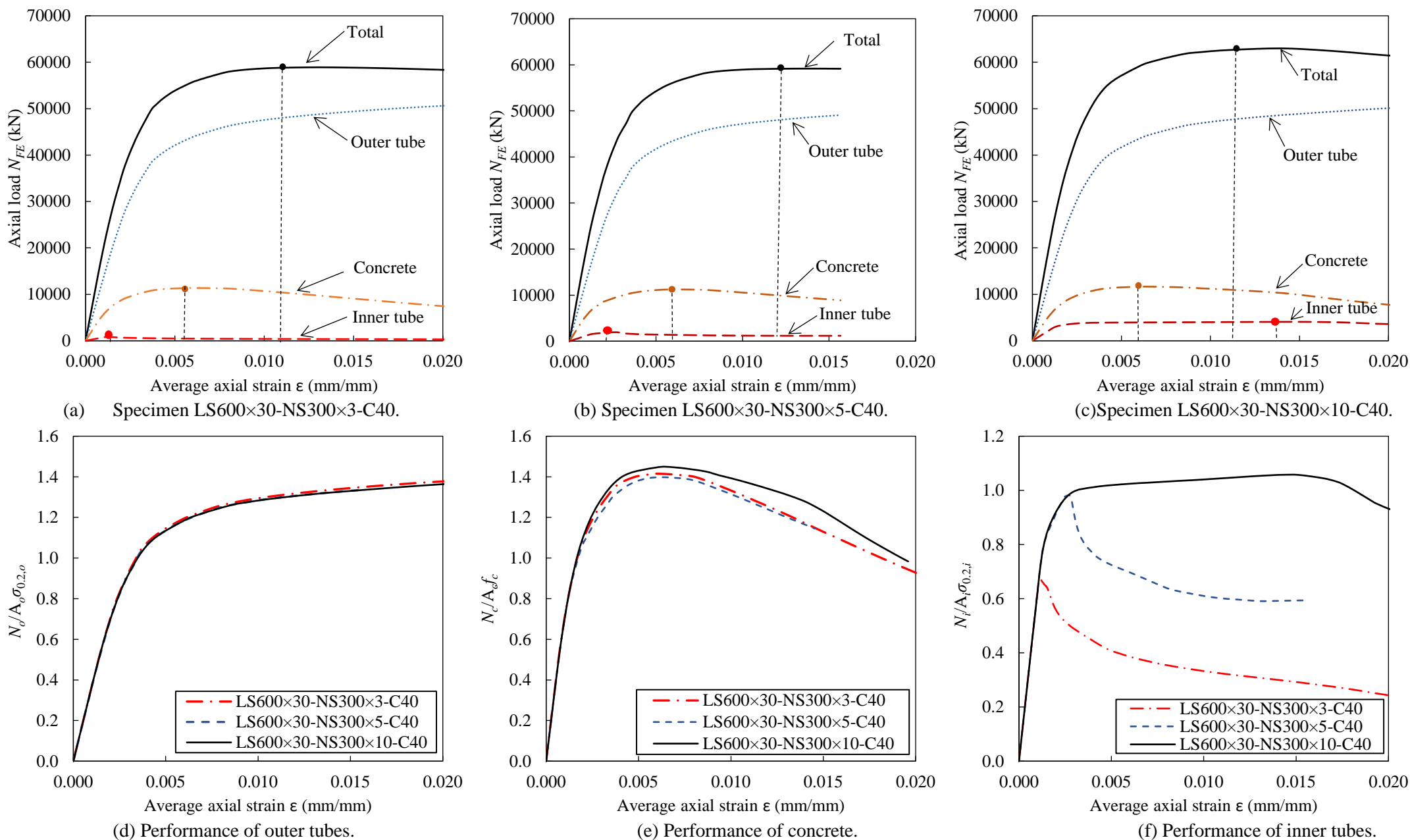


Fig. 10. Comparisons of CFDST specimens with varying inner tube local slendernesses.

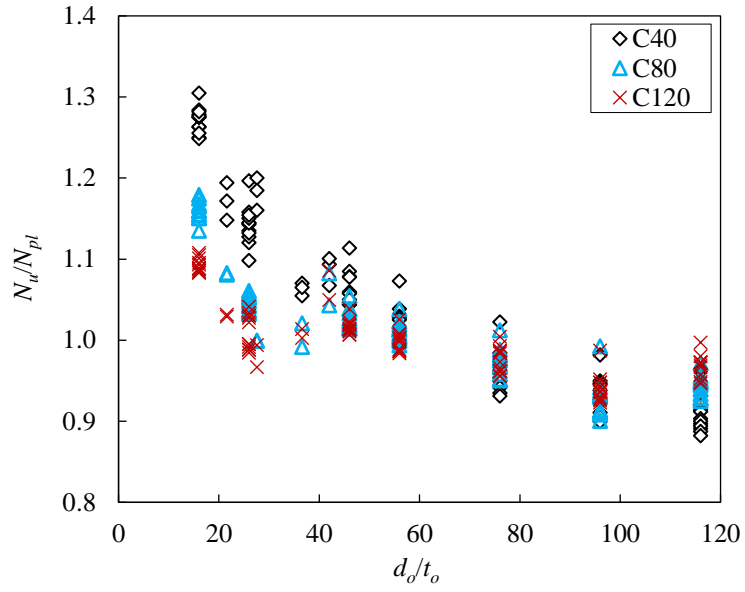
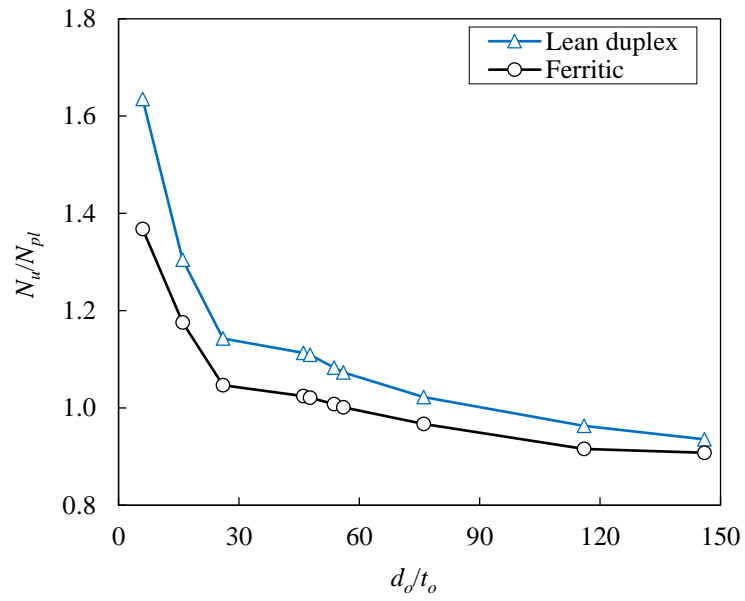
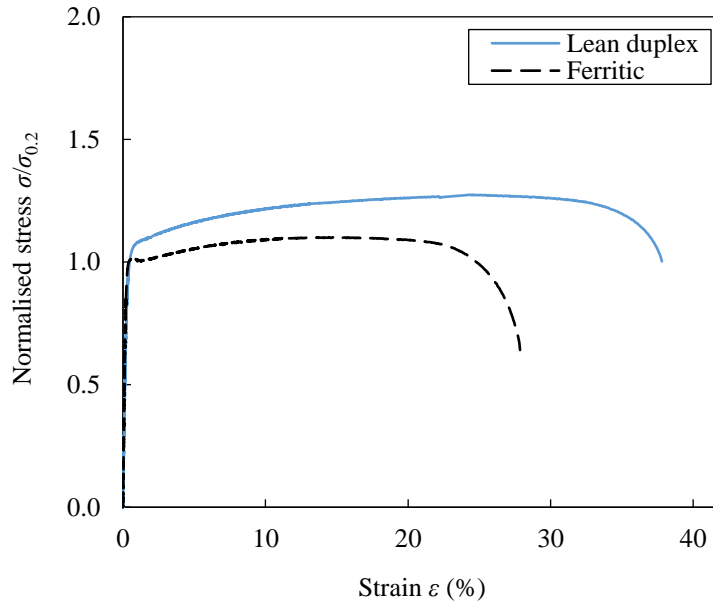


Fig. 11. Influence of concrete grade on normalised load-carrying capacity of studied CFDST sections.



(a) Comparisons of CFDST specimens of two different stainless steel grades.



(b) Normalised material properties of lean duplex and ferritic stainless steel.

Fig. 12. Influence of stainless steel grade on normalised load-carrying capacity of studied CFDST sections.

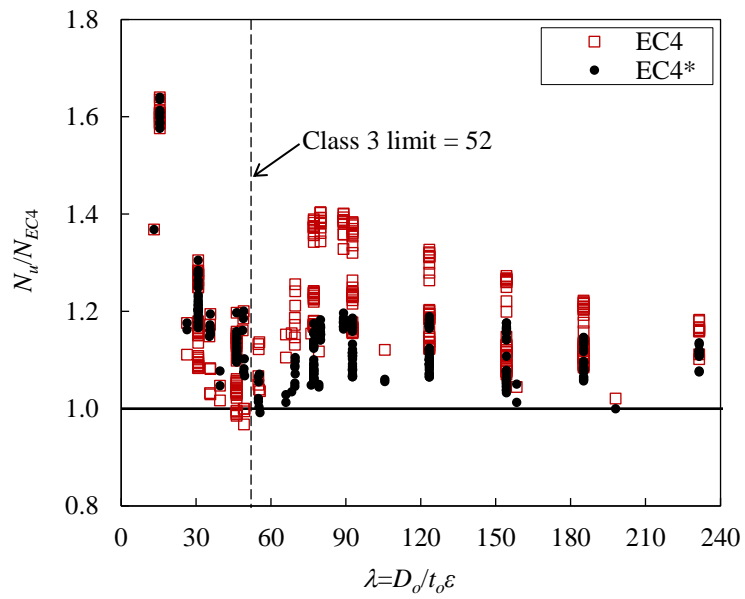


Fig. 13. Comparisons of test and FE results with strength predictions from EC4.

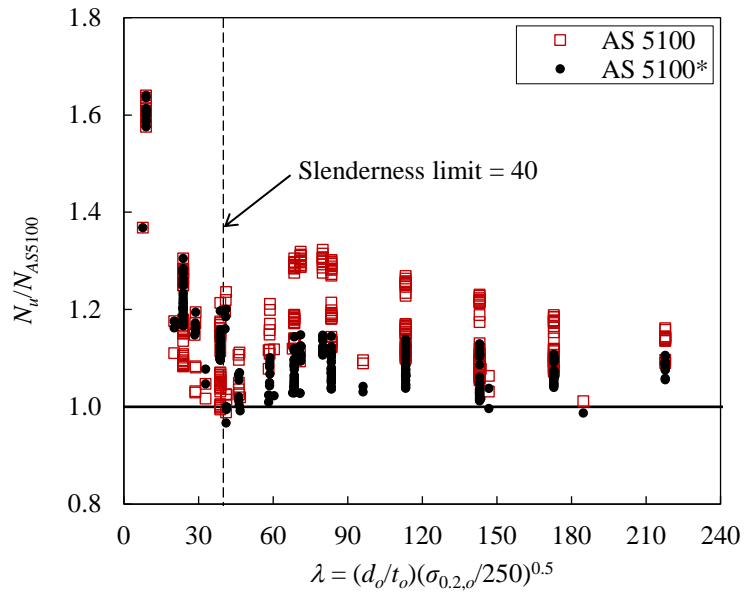


Fig. 14. Comparisons of test and FE results with strength predictions from AS 5100.

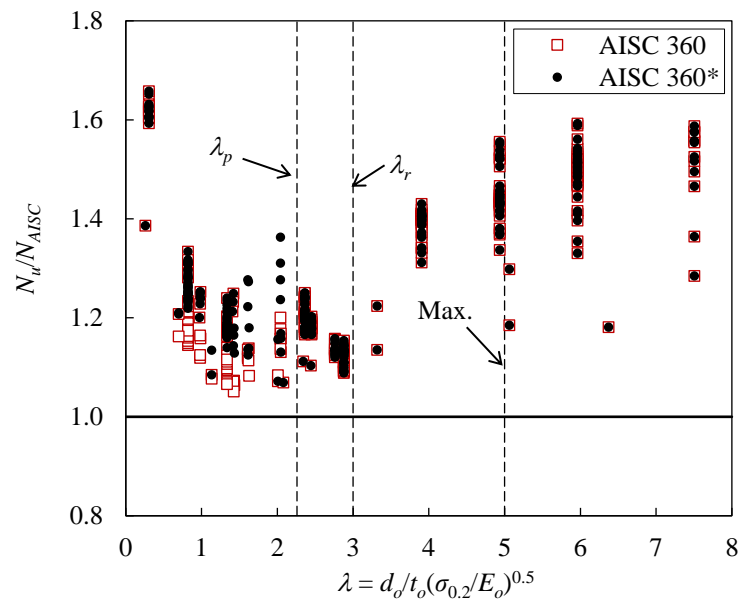


Fig. 15. Comparisons of test and FE results with strength predictions from AISC 360.

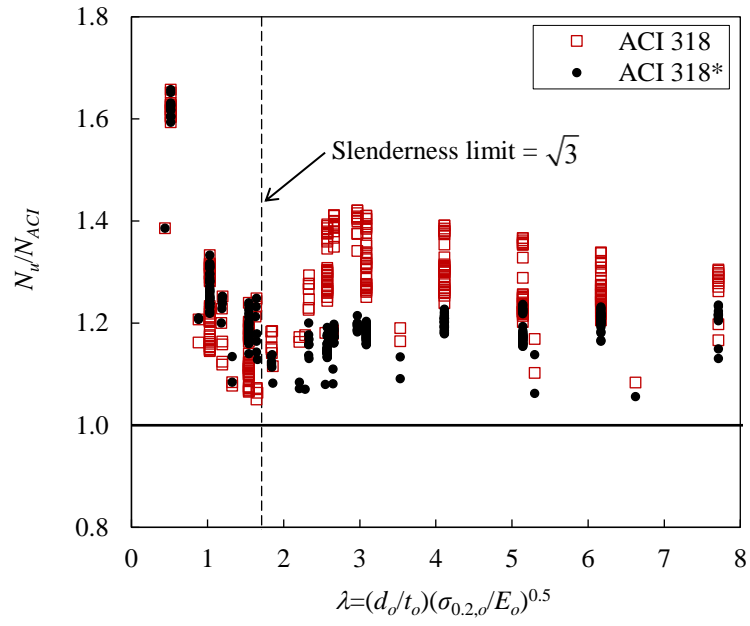


Fig. 16. Comparisons of test and FE results with strength predictions from ACI 318.

Table 1. Summary of experimental results on CFDST stub columns [10] and FE validation.

Specimen	D_o/t_o	D_i/t_i	$\sigma_{0.2,o}$ (MPa)	$\sigma_{0.2,i}$ (MPa)	f_c (MPa)	N_{exp} (kN)	N_{FE} (kN)	N_{FE}/N_{exp}
LR150×3-NS20×2.5-C40	48.6	7.7	475	468	41.8	1223	1313	1.07
LR150×3-NS20×2.5-C40R	48.6	7.7	475	468	41.8	1255	1313	1.05
LR150×3-NS20×2.5-C80	48.5	7.7	475	468	81.6	1681	1645	0.98
LR150×3-NS20×2.5-C120	48.4	7.7	475	468	115.9	1996	1963	0.98
LR150×3-NS20×1.5-C40	48.6	12.9	475	357	41.8	1216	1267	1.04
LR150×3-NS20×1.5-C80	48.5	13.2	475	357	81.6	1577	1594	1.01
LR150×3-NS20×1.5-C120	48.5	13.3	475	357	115.9	2019	1928	0.95
LS100×3-NS40×4-C40	31.8	10.4	556	404	41.8	1420	1354	0.95
LS100×3-NS40×4-C40R	31.7	10.4	556	404	41.8	1401	1354	0.97
LS100×3-NS40×4-C80	32.1	10.3	556	404	81.6	1464	1561	1.07
LS100×3-NS40×4-C120	31.9	10.4	556	404	115.9	1706	1774	1.04
LS100×3-NS40×1.5-C40	31.6	28.4	556	324	41.8	1209	1193	0.99
LS100×3-NS40×1.5-C80	31.8	28.1	556	324	81.6	1323	1401	1.06
LS100×3-NS40×1.5-C120	31.8	28.1	556	324	115.9	1516	1621	1.07
FR120×3-NS20×2.5-C40	41.9	7.7	401	468	41.8	910	954	1.05
FR120×3-NS20×2.5-C80	42.1	7.5	401	468	81.6	1161	1242	1.07
FR120×3-NS20×2.5-C120	41.7	7.7	401	468	115.9	1469	1460	0.99
FR120×3-NS20×1.5-C40	41.7	13.3	401	357	41.8	856	892	1.04
FR120×3-NS20×1.5-C40R	41.6	13.2	401	357	41.8	864	892	1.03
FR120×3-NS20×1.5-C80	41.7	13.1	401	357	81.6	1155	1196	1.04
FR120×3-NS20×1.5-C120	41.8	13.2	401	357	115.9	1409	1427	1.01
FR100×4-NS20×2.5-C40	26.1	13.1	439	468	41.8	1030	1036	1.01
FR100×4-NS20×2.5-C80	26.4	13.4	439	468	81.6	1235	1248	1.01
FR100×4-NS20×2.5-C120	26.4	13.4	439	468	115.9	1398	1427	1.02
FR100×4-NS20×1.5-C40	26.4	13.4	439	357	41.8	1015	990	0.98
FR100×4-NS20×1.5-C40R	26.3	13.1	439	357	41.8	999	990	0.99
FR100×4-NS20×1.5-C80	26.4	13.5	439	357	81.6	1191	1201	1.01
FR100×4-NS20×1.5-C120	26.3	13.1	439	357	115.9	1359	1386	1.02
Mean								1.02
COV								0.035
Max.								1.06
Min.								0.95

Table 2. Ranges of variation of parameters for the parametric study.

d_o/t_o	d_i/t_i	$\sigma_{0.2,o}$ (MPa)	$\sigma_{0.2,i}$ (MPa)	f_c (MPa)
6, 16, 26, 46, 48, 54, 56 76, 96, 116, 146	6, 16, 26, 36, 46 56, 76, 96, 116, 146	401, 556	404	40, 80, 120

Table 3. Code limits on cross-sectional slendernesses and material strengths.

Design codes	Limitations of cross-sectional slenderness		$\sigma_{0.2}$ (MPa)	f_c (MPa)
	Original	Normalised slenderness limits		
EN 1994-1-1	$D_o/t_o \leq 52 \sqrt{\frac{235}{\sigma_{0.2,o}} \frac{E_o}{210000}}$	$(D_o/t_o) \sqrt{\frac{210000}{E_o} \frac{\sigma_{0.2,o}}{235}} \leq 52$	235–460	20–50
AS 5100	$\lambda_e = \frac{d_o}{t_o} \sqrt{\frac{\sigma_{0.2,o}}{250}} \leq 40$	$\frac{d_o}{t_o} \sqrt{\frac{\sigma_{0.2,o}}{250}} \leq 40$	230–400	25–65
AISC 360	$\lambda_p = \frac{d_o}{t_o} \leq 2.26 \sqrt{\frac{E_o}{\sigma_{0.2,o}}}$	$\frac{d_o}{t_o} \sqrt{\frac{\sigma_{0.2,o}}{E_o}} \leq 2.26$	≤ 525	21–70
ACI 318	$t_o \geq D_o \sqrt{\frac{\sigma_{0.2,o}}{3E_o}}$	$(D_o/t_o) \sqrt{\frac{\sigma_{0.2,o}}{E_o}} \leq \sqrt{3}$	≤ 345	≥ 17.2

Table 4. Overall comparison of test and FE axial compressive strengths with predicted strengths.

No. of tests: 28	N_u/N_{EC4}	N_u/N_{EC4*}	N_u/N_{AS5100}	$N_u/N_{AS5100*}$	N_u/N_{AISC}	N_u/N_{AISC*}	N_u/N_{ACI}	N_u/N_{ACI*}
No. of FE modelling: 311								
Mean	1.20	1.14	1.17	1.12	1.27	1.29	1.27	1.21
COV	0.108	0.093	0.100	0.100	0.131	0.121	0.086	0.076

Table 5. Comparison of Test and FE strengths with design predictions for specimens falling within their respective codified slenderness limits.

f_c (MPa)		Ratio of test-to-predicted strengths							
		N_u/N_{EC4}	N_u/N_{EC4*}	N_u/N_{AS5100}	$N_u/N_{AS5100*}$	N_u/N_{AISC}	N_u/N_{AISC*}	N_u/N_{ACI}	N_u/N_{ACI*}
40	Mean	1.20	1.20	1.20	1.20	1.24	1.24	1.24	1.24
	COV	0.060	0.060	0.060	0.060	0.054	0.054	0.055	0.055
80	Mean	1.09	1.15	1.09	1.15	1.15	1.21	1.15	1.21
	COV	0.055	0.047	0.055	0.047	0.049	0.040	0.049	0.040
120	Mean	1.04	1.15	1.04	1.15	1.12	1.22	1.12	1.22
	COV	0.044	0.032	0.044	0.032	0.040	0.025	0.040	0.025

Table 6. Comparison of test and FE axial compressive strengths with design predictions for specimens exceeding their respective codified slenderness limits.

Parameters	Ratio of test-to-predicted strengths						
	N_u/N_{EC4}	N_u/N_{EC4*}	N_u/N_{AS5100}	$N_u/N_{AS5100*}$	N_u/N_{ACI}	N_u/N_{ACI*}	
Mean	1.21	1.10	1.17	1.07	1.29	1.18	
COV	0.083	0.042	0.069	0.036	0.053	0.029	

Table 7. Reliability analysis results calculated according to EN 1990 [46].

Design code	Sample type	Sample number	$k_{d,n}$	b	V_δ	Required value of γ_{MO}	Target value of γ_{MO}
EC4	Test+FE	28+311	3.119	1.20	0.111	1.00	1.00
EC4*	Test+FE	28+311	3.119	1.14	0.088	0.99	1.00
AS 5100	Test+FE	28+311	3.119	1.17	0.100	0.94	1.00
AS 5100*	Test+FE	28+311	3.119	1.12	0.095	0.98	1.00
AISC 360	Test+FE	28+311	3.119	1.27	0.114	1.15	1.33
AISC 360*	Test+FE	28+311	3.119	1.29	0.106	1.11	1.33
ACI 318	Test+FE	28+311	3.119	1.27	0.092	1.09	1.54
ACI 318*	Test+FE	28+311	3.119	1.21	0.073	1.10	1.54