

Tunnel-piled structure interaction: numerical simulation of hybrid centrifuge tests

Geyang Song^{a,*}, Alec M. Marshall^b

^a*Department of Engineering Science, University of Oxford, Parks Road, Oxford, OX1 3PJ, United Kingdom. Formally Faculty of Engineering, University of Nottingham, University Park, NG7 2RD Nottingham, United Kingdom.*

^b*Faculty of Engineering, University of Nottingham, University Park, NG7 2RD Nottingham, United Kingdom.*

Abstract

Tunnel excavation in urban areas causes ground movements that could damage existing nearby piled structures. Geotechnical centrifuge modelling has been widely used as a tool to study problems related to tunnelling activities and its interaction with existing infrastructure systems. Recent hybrid centrifuge tests using the Coupled Centrifuge-Numerical Modelling (CCNM) approach have provided high-quality experimental data of soil-piled structure interactions in dry sand, demonstrating the role of structure stiffness on head load transfer among piles and the subsequent impact on pile shaft resistance with tunnel volume loss. This paper extends the experimental data set with a finite element numerical analysis of the problem, providing additional insights into the complex interactions. An advanced hypoplastic constitutive model was adopted for the soil and, to enable appropriate comparison of numerical and experimental results, the conditions within the centrifuge tests

*Corresponding author

Email addresses: geyang.song@eng.ox.ac.uk (Geyang Song),
alec.marshall@nottingham.ac.uk (Alec M. Marshall)

were replicated numerically. Despite some discrepancies between numerical and experimental results, in particular related to limitations of the adopted soil-pile interface model, results from the numerical simulations are shown to broadly agree with the centrifuge test data. Numerical analysis results are used to explore the effect of tunnelling on pile settlements and the development of radial stresses around piles, as well as the stress paths at the soil-pile interface. These data provide additional insights to complement and extend current understanding of the complex soil-pile interactions taking place.

Keywords: Tunnelling, finite element analysis, pile, structure

1 **Highlights**

- 2 • Effect of tunnelling on piled structures.
- 3 • Numerical analysis is used to explore the pile settlement.
- 4 • Development of radial stress around piles with tunnelling.
- 5 • Stress path of soil element close to the pile with tunnelling.

6 1. Introduction

7 Piles are used to support a variety of infrastructure systems. Tunnel ex-
8 cavation in highly congested cities can often take place close to existing piled
9 foundations, with associated ground movements and stress relief affecting
10 the equilibrium state of the existing piles. This may cause pile settlements,
11 uneven settlement among pile groups, or pile distress beyond design specifi-
12 cations (Kaalberg et al., 2005; Selemetas, 2005; Jacobsz et al., 2004; Lee and
13 Chiang, 2007; Marshall and Mair, 2011; Ng et al., 2013, 2014; Williamson
14 et al., 2017a,b; Franza and Marshall, 2019; Franza et al., 2021a; Loganathan
15 et al., 2000; Wang et al., 2020; Franza et al., 2021a,b). These studies have
16 demonstrated the importance of understanding the influence of tunnel exca-
17 vation on pile resistance.

18 Geotechnical centrifuges have been widely used as a tool to investigate
19 tunnel-pile-structure interaction (TPSI) problems. In these studies, piles are
20 generally individually loaded or rigidly connected via a pile cap to investi-
21 gate the tunnel-pile-structure interaction problems (Loganathan et al. (2000);
22 Lee and Chiang (2007); Boonsiri and Takemura (2015); Wang et al. (2020)).
23 However, these methods neglect or overestimate the effect of structure stiff-
24 ness, which could affect the load transfer among the piles during tunnel
25 volume loss, and consequently change the shaft resistance along the piles.
26 Recent developments at the University of Nottingham Centre for Geome-
27 chanics (NCG) have incorporated a hybrid approach to modelling the tunnel-
28 building interactions using the so-called Coupled Centrifuge-Numerical Mod-
29 elling (CCNM) application (Idinyang et al., 2018a,b; Franza and Marshall,
30 2019), wherein the tunnel, soil, and piles are modelled in the centrifuge, a

31 connected building is simulated numerically, and data related to pile dis-
32 placements and loads are transferred in real-time between the centrifuge and
33 numerical domains. The approach accurately accounts for vertical pile head
34 load redistribution during tunnel volume loss (which depends on the char-
35 acteristics of the modelled building), updates the pile head loads applied in
36 the centrifuge as the test progresses, and provides a high-fidelity simulation
37 of the global tunnel-pile-structure interaction problem. [Song and Marshall](#)
38 [\(2020b\)](#) used the CCNM application to model the interaction between tun-
39 nel volume loss and piles connected to a five-storey steel frame structure and
40 demonstrated the significance of the structure effect on pile resistance.

41 Numerical models have also clearly made important contributions to de-
42 veloping our understanding of tunnel-pile and tunnel-pile-structure interac-
43 tions. Many numerical investigations have made use of available centrifuge
44 test data as a means of verifying the numerical models ([Hong et al., 2015](#);
45 [Ng et al., 2015](#); [Soomro et al., 2018](#); [Li and Zhang, 2020](#); [Cheng et al., 2007](#);
46 [Wang et al., 2020](#)). The numerical analyses typically adopt pressure or dis-
47 placement controlled methods to simulate the tunnel volume loss process. In
48 some instances, the mode of volume loss simulation is guided by the type of
49 model tunnel used in the centrifuge tests against which the numerical mod-
50 els are compared; a fluid-filled flexible membrane model tunnel is arguably
51 best suited to a pressure-controlled (or material softening ([Li and Zhang,](#)
52 [2020](#))) simulation, whereas a displacing rigid-boundary model tunnel is well
53 replicated by a displacement controlled simulation. There are studies which
54 have adopted simulations which go against the above logic that have success-
55 fully demonstrated agreement between numerical and centrifuge test results

56 (Cheng et al., 2007; Hong et al., 2015; Soomro et al., 2018; Wang et al., 2020).
57 The study conducted by Song and Marshall (2020a) investigated the impli-
58 cations of the use of the different model tunnel types using centrifuge and
59 numerical modelling data. In common with the centrifuge tests, numerical
60 models also typically assume either a free pile head or one where the pile is
61 rigidly connected to a pile cap; the effect of global structure stiffness on pile
62 loading and displacement is not considered. As a result, there is a lack of
63 detailed numerical simulation of tunnel-pile-structure interaction where the
64 effect of structure stiffness is included.

65 In this paper, an advanced hypoplastic constitutive model is employed
66 within the finite element analysis (FEA) software ABAQUS (Hibbitt, 2002)
67 to simulate the tunnel-pile-structure interaction centrifuge tests reported by
68 Song and Marshall (2020b), which used the CCNM application to account
69 for the effect of building stiffness on pile head load redistribution during
70 tunnel volume loss. The displacement controlled method was used in the
71 numerical simulations to replicate the deformed shape of the eccentric rigid
72 boundary mechanical (eRBM) model tunnel used in the centrifuge tests. A
73 comparison is made between the numerical and centrifuge test results, fo-
74 cusing on pile settlements and load transfer between piles, with limitations
75 of the adopted soil-pile interface model also discussed. Despite some dis-
76 crepancies between numerical and experimental results, sufficient confidence
77 was achieved in the adopted numerical simulation for the soil-structure in-
78 teraction analysis within dry sand. The numerical model is then used to
79 extend the understanding of the complex soil-pile interactions, investigating
80 elements that could not be easily measured experimentally, such as soil set-

81 elements and radial stress development around the piles, as well as the stress
82 paths at the soil-pile interface.

83 **2. Centrifuge modelling**

84 Two centrifuge tests are reported in this paper: (1) a tunnel-pile group in-
85 teraction (TPGI) test and (2) a tunnel-pile-structure interaction (TPSI) test.
86 These tests were previously reported in [Song and Marshall \(2020b\)](#); readers
87 can refer to that paper for a more in-depth description of the equipment and
88 test methodology.

89 The centrifuge tests were conducted on the NCG 2 m radius, 50 g-ton
90 geotechnical centrifuge at an acceleration of 80 times gravity. Figure 1 shows
91 the layout of the two centrifuge tests. In test TPGI, four piles were indi-
92 vidually loaded, and the pile head load did not change with tunnel volume
93 loss. In test TPSI, piles were virtually connected to a 5-storey steel frame
94 structure using the CCNM application ([Idinyang et al., 2018a,b](#); [Franza and](#)
95 [Marshall, 2019](#)) (more details provided later).

96 *2.1. Centrifuge model*

97 The centrifuge container has internal dimensions of 150 mm width, 700 mm
98 length, and a height of 400 mm. The model tunnel had an initial diameter of
99 $D_t=90\text{mm}$ and was buried with a cover distance $C=162\text{ mm}$, giving a cover
100 to diameter ratio of $C/D_t=1.8$.

101 An eccentric rigid boundary mechanical (eRBM) model tunnel ([Song](#)
102 [et al., 2018](#); [Song and Marshall, 2020a](#)) was used in the centrifuge tests to
103 simulate tunnel volume loss. The eRBM model tunnel consists of six tunnel
104 segments that represent the tunnel boundary. A bi-directional screw shaft

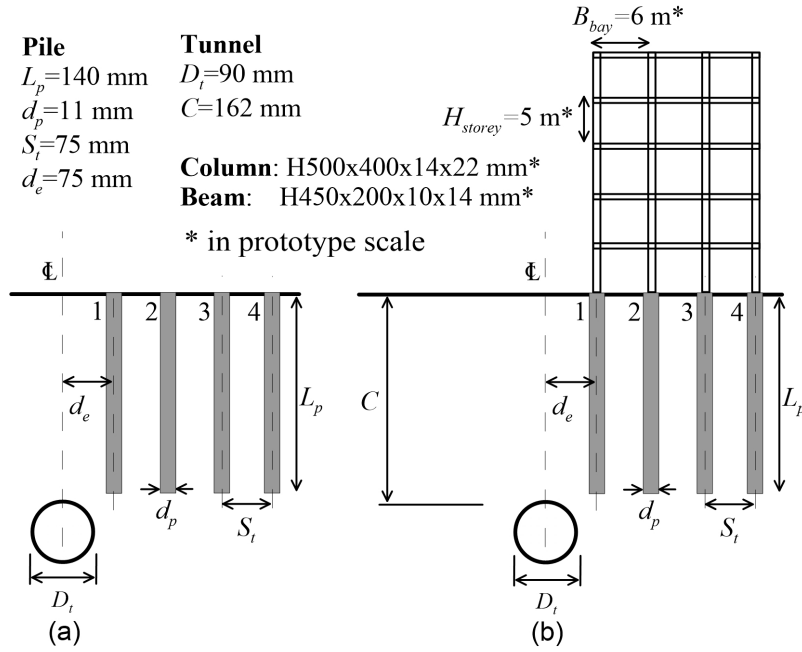


Figure 1: Test layout of the centrifuge tests (a) TPGI, and (b) TPSI

105 drives the six segments, which displace inwards at varying levels with rota-
 106 tion of the screw shaft to produce an eccentric profile of displacement around
 107 the tunnel boundary, with maximum displacement at the tunnel crown and
 108 zero displacement at the invert. A detailed description of the model tunnel
 109 configuration is provided in [Song and Marshall \(2020a\)](#).

110 In test TPGI, designated working loads were applied to each of the piles
 111 and maintained constant throughout the tunnel volume loss process using
 112 a load control system. In test TPSI, the same working loads were initially
 113 applied to the piles, after which the load control of the piles was passed over
 114 to the CCNM application, allowing the ABAQUS numerical simulation to
 115 adjust pile head loads during the tunnel volume loss process ([Franza and
 116 Marshall, 2019](#)). In both tests, tunnel volume loss was increased in small

117 increments of $\approx 0.1\%$; subsequent increments of volume loss were only allowed
118 after achieving a ‘stable state’ and acquiring all necessary data. This ‘stable
119 state’ is most relevant to the TPSI test where, for a given increment of
120 volume loss, pile head displacements are passed to the numerical model of the
121 connected structure through the real-time interface of the CCNM application
122 (Idinyang et al., 2018a), which calculates new pile head loads depending on
123 the magnitude of pile settlement and the characteristics of the building. The
124 adjusted pile head load is then passed back to the centrifuge through the
125 CCNM application, which may cause subsequent small changes in pile head
126 displacements, requiring another ‘loop’ of the CCNM process. This ‘loop’
127 is repeated until the ‘stable state’ is achieved, based on a requirement for
128 sufficiently small changes in pile head load and displacements.

129 A linear elastic five-storey steel frame structure was simulated in the
130 ABAQUS numerical model, with a Young’s modulus of $E = 210$ GPa and a
131 Poisson’s ratio of $\mu = 0.3$; the sizes of the columns and beams are given in
132 prototype scale in Figure 1. Based on Eurocode specifications (Gulvanessian
133 et al., 2009), the total prototype scale pile head load applied to the two inner
134 piles was 2364 kN, and 1630 kN for the two outer piles.

135 *2.2. Model piles and strain sensors*

136 The model piles were made from hollow aluminium tube with an outer
137 diameter of 10 mm and a thickness of 1 mm, giving an axial stiffness $EA =$
138 19.4×10^3 MN in prototype scale. In practice, a 0.8 m diameter concrete pile
139 has an axial stiffness $EA = (10 - 14) \times 10^3$ MN, which is slightly lower than
140 the model pile. Piles had sand grains (the same sand used for soil body)
141 bonded to the outer surface of the pile to create a fully rough interface. The

142 final pile diameter was $d_p=11$ mm.

143 Optical Fibre Bragg Grating (FBG) sensors were used to measure strains
144 at localised locations along the piles (Song et al., 2021), allowing calculation
145 of the distribution of pile shaft resistance. The FBG sensors were made from
146 a single-mode optical fibre. Two fibres, each containing three FBG sensors
147 (corresponding to strain measurement locations), were installed along op-
148 posing inner surfaces of the model piles, with measurement locations at 40,
149 85 and 130 mm below the ground surface. The model piles were calibrated
150 on a loading frame within a temperature-controlled room, providing a reli-
151 able linear relationship between FBG wavelength shift and applied load (i.e.
152 calibration factor).

153 *2.3. Model preparation and testing procedure*

154 Fine-grained silica sand commonly known as Leighton Buzzard Fraction
155 E sand was used for the tests. The sand has a typical average diameter
156 D_{50} of 0.14 mm, specific gravity G_s of 2.65, and was prepared by dry sand
157 pouring. The model preparation procedure can be briefly summarised as
158 follows. One end of the eRBM model tunnel was fixed within the back wall
159 of the strongbox, which was laid horizontally (the model tunnel oriented
160 upwards), and a temporary wall secured at the location corresponding to
161 the intended soil surface. The sand was poured in the direction of the tunnel
162 longitudinal axis to achieve a relative density (I_d) of 90%. After sand pouring,
163 the strongbox was rotated to its upright position and the temporary wall
164 removed (revealing the soil surface). The four piles were then pushed into
165 the sand at 1 g using a frame to ensure the piles were pushed vertically at the
166 designated location and to the required depth. The pile loading actuators

167 were then connected to the piles.

168 The centrifuge testing procedure can be briefly summarised as follows.
169 A constant 5 N vertical load (model scale) was applied to the piles and
170 maintained during centrifuge spin-up to 80 g (done to try to minimise relative
171 soil-pile displacements during the spin-up process). Three stabilisation cycles
172 were performed (going from 80 g to 10 g and back to 80 g; done to encourage
173 uniform stress conditions within the models and improve repeatability of
174 tests). After these cycles, the pile loading and volume loss processes, as
175 previously described, were performed.

176 3. Finite element simulation

177 Finite element models were developed to simulate the TPGI and TPSI
178 centrifuge tests using the user-defined hypoplastic constitutive model devel-
179 oped by [von Wolffersdorff \(1996\)](#) to model the soil.

180 3.1. Element mesh and boundary conditions

181 Figure 2 shows the finite element mesh for test TPSI. The intention of the
182 analysis was to simulate the centrifuge tests as closely as possible. Therefore,
183 the dimensions of the numerical model match exactly with the centrifuge test.
184 An eccentric displacement control method was used to simulate the eccentric
185 rigid boundary mechanical (eRBM) model tunnel used in the centrifuge tests
186 ([Song and Marshall, 2020a](#)). In this method, the rigid tunnel boundary is
187 divided into six segments and pre-defined radial displacements are imposed
188 for each segment to generate a non-uniform radial displacement around the
189 tunnel. Figure 2 shows the radial displacement of each segment at a tunnel
190 volume loss of $V_{l,t} = 3\%$. Solid elements (C3D8) were used to model the

191 soil, pile and rigid tunnel boundary. Beam elements (B31) were used to
 192 model the steel frame structure. The coefficient of lateral earth pressure was
 193 assumed to be $K_0 = 0.5$. A fixed boundary was used along the bottom of the
 194 mesh, vertical roller boundaries were used on the sides of the mesh, and no
 195 constraints were applied to the ground surface. Element size was determined
 196 using a procedure whereby a further decrease in element size had a negligible
 197 effect on soil settlement with tunnel volume loss (based on the greenfield
 198 tunnelling condition).

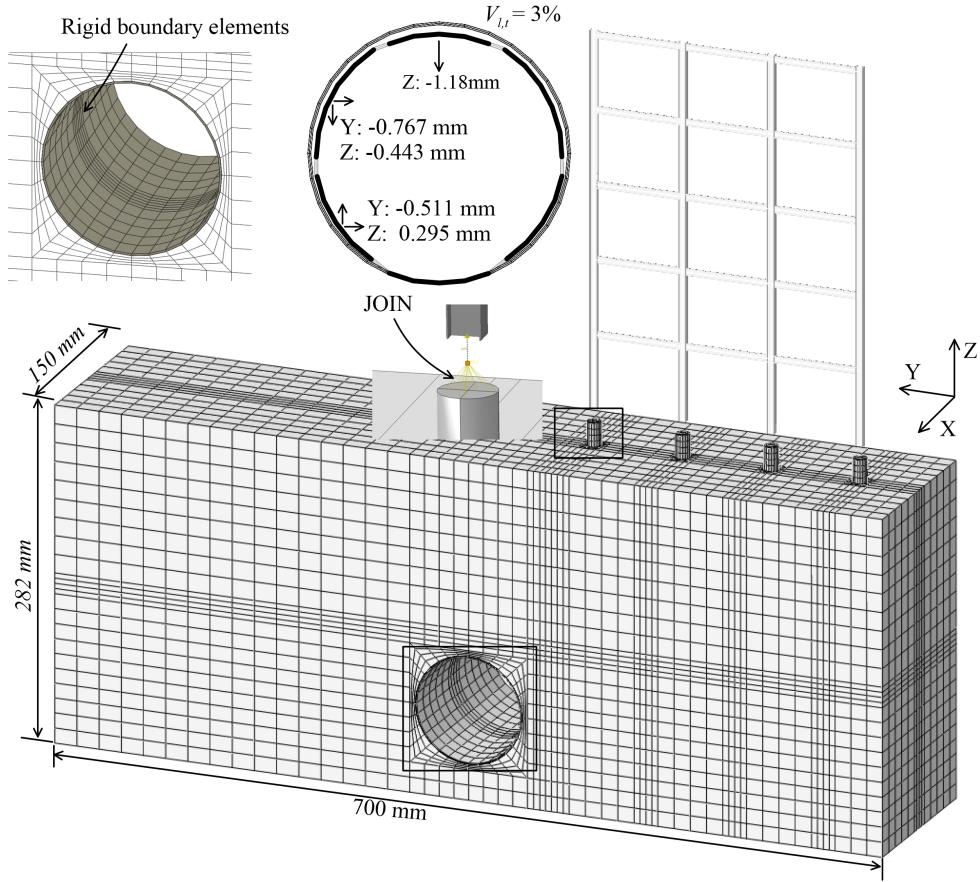


Figure 2: Finite element mesh for test TPSI

199 *3.2. Constitutive model and model parameters*

200 The basic hypoplastic model was adopted in this study, which consists the
201 following 8 parameters: critical state friction angle ϕ'_c , granular hardness h_s ,
202 fitting parameter n , minimum/maximum/critical void ratio at zero pressure
203 $e_{d0}/e_{i0}/e_{c0}$, and $\alpha; \beta$ which govern the stiffness of the soil. The hypoplastic
204 model parameters for Leighton Buzzard Fraction E sand were obtained and
205 calibrated using oedometer and triaxial tests data from [Song and Marshall](#)
206 [\(2020a\)](#). Note that parameters α and β calibrated by [Song and Marshall](#)
207 [\(2020a\)](#) were based on stress-strain data from two drained triaxial compres-
208 sion tests where the axial strain data was obtained from an external linear
209 variable differential transformer (LVDT). [Jardine et al. \(1984\)](#) indicated that
210 the use of external LVDTs provides insufficient accuracy for stiffness mea-
211 surement in the triaxial test. Therefore, for this paper, local LVDT data
212 from the two drained triaxial compression tests were used to re-calibrate the
213 parameters α and β . Figure 3 shows the stress-strain behaviour from the two
214 triaxial tests using both local and external LVDT data, as well as the finite
215 element simulation result using $\alpha=0.08$ and $\beta=1.5$. Note that, despite the
216 slight over-prediction of the peak deviator stress for the FEA, the simulation
217 replicates the soil stiffness within the small strain range (axial strain less
218 than 0.5%) very well, which is of primary concern for the numerical analysis
219 of tunnel construction processes ([Addenbrooke et al., 1997](#)). Table 1 sum-
220 marises the modified model parameters adopted in this study (after [Song](#)
221 [and Marshall \(2020a\)](#)).

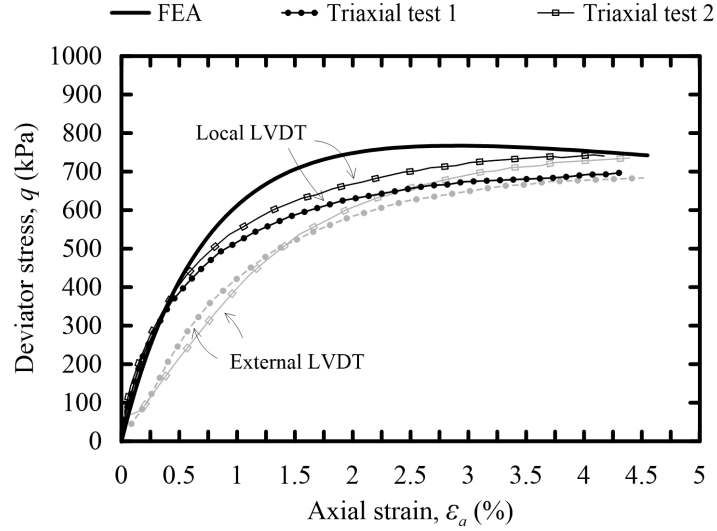


Figure 3: Triaxial test calibration

Table 1: Adopted hypoplastic model parameters for Leighton Buzzard Fraction E sand, after [Song and Marshall \(2020a\)](#)

Parameter	Value	Source
Critical state friction angle ϕ'_c	32°	Heap test
Granular hardness h_s	1969 MPa	Oedometer test
Exponent n	0.447	Oedometer test
Minimum void ratio at zero pressure e_{d0}	0.624	Herle and Gudehus (1999)
Critical void ratio at zero pressure e_{c0}	1.16	Oedometer test
Maximum void ratio at zero pressure e_{i0}	1.392	Herle and Gudehus (1999)
Exponent α	0.08	Triaxial test* $I_d = 90\%$
Exponent β	1.5	Triaxial test* $I_d = 90\%$

* Based on local LVDT measurements

222 *3.3. Numerical modelling procedure*

223 The numerical model is intended to simulate the conditions within the
224 centrifuge tests as closely as possible, for example, self-weight of the pile,
225 the effect of increasing gravity level from 1 g to 80 g, the tunnel volume
226 loss process, and the effect of the connected steel frame structure. Note
227 that the frame structure is weightless in the numerical model; the weight of
228 the structure as well as the working loads applied were calculated based on
229 Eurocodes (discussed previously) and imposed to the pile heads (total pile
230 head load).

231 For gravity increase (spin-up) simulation, it was found that replicating the
232 full 1 g to 80 g process caused instabilities within the numerical simulations
233 during the tunnel volume loss stage, preventing analysis of the full centrifuge
234 test. By replicating from 2 g to 80 g, the numerical analyses could simulate
235 the full experimental volume loss range (up to tunnel volume loss $V_{l,t} = 3\%$).
236 Results presented in this paper therefore relate to models that replicated the
237 2 g to 80 g process; [Song and Marshall \(2020a\)](#) indicated that the difference
238 in ground settlements at a given tunnel volume loss was negligible between
239 the ‘1-80 g’ and ‘2-80 g’ simulations.

240 The soil-pile interface for the finite element analyses was simulated us-
241 ing a Coulomb friction law, in which the friction coefficient was set to be
242 $\tan(\phi'_c)=0.62$ (matching the rough pile interface from the centrifuge tests
243 where sand was bonded to the exterior of the piles). An absolute elastic slip
244 distance (1.5 mm) was used to define the tangential behaviour of the soil-pile
245 interface, which is based on centrifuge pile jacking tests reported by [Song](#)
246 [and Marshall \(2020b\)](#).

247 To replicate the non-uniform radial displacement of the eRBM model
248 tunnel in the centrifuge (Song and Marshall, 2020a), a rigid boundary mesh
249 was implemented (see Figure 2) with a non-uniform displacement profile.
250 The interface between the soil and the rigid boundary was simulated using
251 a Coulomb friction law with the assumption that the soil-tunnel boundary
252 interface behaved in the same way as the pile-soil interface. In terms of
253 the steel frame structure simulation for test TPSI, the same model used in
254 the TPSI centrifuge test (with the CCNM application) was adopted in the
255 numerical simulation. Note that, in both centrifuge and FEA tests, only
256 vertical loads were transferred between the building frame and the piles,
257 neglecting the effect of lateral and rotational degrees of freedom; Franza and
258 Marshall (2019) demonstrated that the vertical degree of freedom has the
259 dominant role for this considered scenario.

260 The finite element analysis procedure can be summarised as follows. An
261 initial soil stress profile was imposed on the soil elements, where the static
262 earth pressure coefficient was set to $K_0 = 0.5$ and the soil stresses calculated
263 for an acceleration field of 2 g. Then, a geostatic step was conducted to ensure
264 the soil displacements were reset to zero (the maximum soil displacement
265 after this geostatic step was found to be 2×10^{-5} mm). Soil elements inside
266 the tunnel were then removed and tunnel boundary elements were added
267 to the model, with the Coulomb friction law interface activated at the soil-
268 tunnel boundary interface. Soil elements at the pile locations were removed
269 and the model piles added, followed by the activation of the soil-pile interface
270 (Coulomb friction law). For the TPGI FEA test, a 5 N load was then applied
271 to the piles (as in the centrifuge test). For the TPSI FEA test, piles were first

272 loaded to 5 N, then the steel frame structure (which is weightless) was added
273 to the model. In the TPSI centrifuge test, a hinged joint was used between
274 the base of the columns and the pile heads, transferring only vertical loads
275 between the columns and piles. This simplification was adopted because
276 the real rotational stiffness at this connection is not known. [Franza and](#)
277 [Marshall \(2019\)](#) illustrated that the influence of this pile-structure connection
278 is minor for framed buildings with isolated pile heads, as is the case in this
279 study, hence the impact of this assumption is minimal. For the real-time
280 data interface ([Idinyang et al., 2018a](#)), only vertical pile displacements and
281 vertical pile head loads were shared between the geotechnical (centrifuge)
282 and structural (numerical) domains. In the TPSI FEA test, the four piles
283 were connected to the steel frame structure via a pin joint. This pin joint
284 connection was achieved using the ABAQUS connection type JOIN with a
285 restriction of displacements in the X and Y directions as well as the rotation
286 along the Y and Z axes (see [Figure 2](#) for the coordinate system). Therefore,
287 only vertical displacements and vertical forces were translated between the
288 piles and the structure. The base of the structure columns were free to rotate,
289 which depends on the global deformation of the structure (identical to the
290 TPSI centrifuge test).

291 Once the structure was connected to the piles via this pin joint, the gravity
292 level of the entire model was increased from 2 g to 80 g [within one step (252
293 increments) within ABAQUS], during which time the tunnel boundary was
294 fixed in terms of distortion (change in shape) and translation (rigid body
295 motion). Piles were then loaded to the designated working load (255 N
296 for exterior piles 1 and 4, and 370 N for interior piles 2 and 3). Finally,

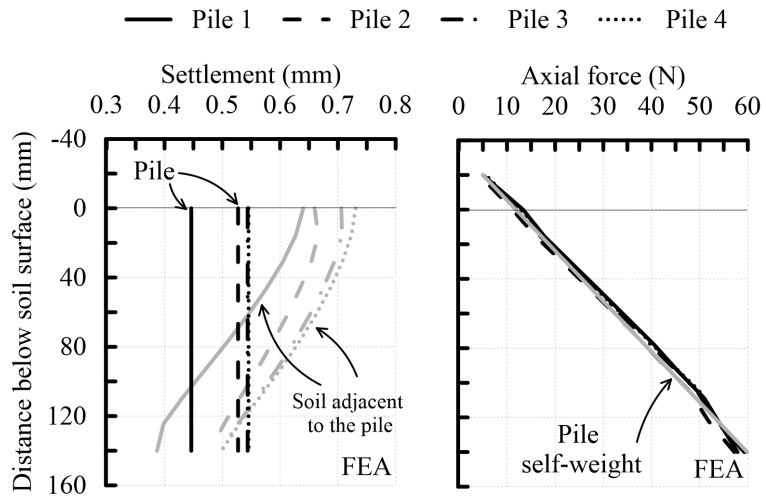
297 a non-uniform displacement profile (discussed above) was imposed on the
298 rigid boundary elements to simulate tunnel volume loss. For the TPGI FEA
299 test, pile head load was kept constant, whereas for the TPSI FEA test, pile
300 head load varied with tunnel volume loss as it was affected by the structure
301 stiffness.

302 4. Results

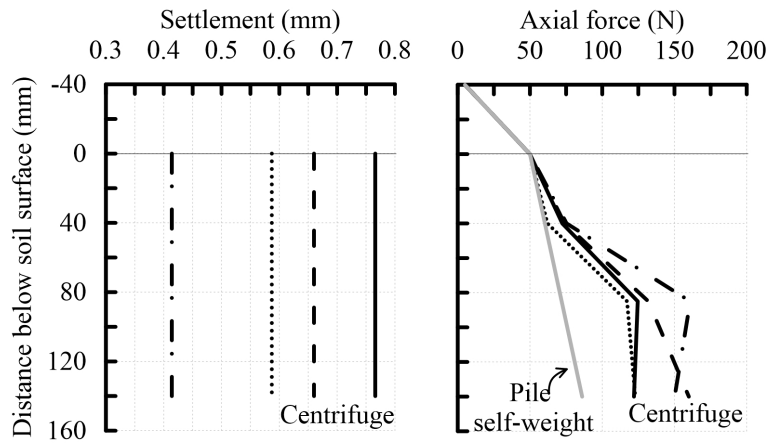
303 4.1. Spin-up effect on pile shaft resistance

304 For the centrifuge tests, a 5 N pile head load was maintained during cen-
305 trifuge spin-up (from 1 g to 80 g). The increase in self-weight of the soil
306 will cause relative displacements between the piles and the adjacent soil. To
307 better understand the spin-up effect, Figure 4 shows the pile settlement af-
308 ter gravity increase in the centrifuge and FEA TPGI tests. Both tests show
309 comparable pile settlement after spin-up, however the FEA pile settlement
310 increases with pile number (i.e. with distance from the tunnel, refer to Fig-
311 ure 1), a consequence of the fixed tunnel boundary, whereas Pile 1 (nearest
312 the tunnel) shows the largest settlement in the centrifuge test, indicating
313 that some movement of the model tunnel likely occurred during spin-up.
314 Figure 4 (a) also shows the soil settlement adjacent to the piles at their cen-
315 treline along the depth of piles for the FEA test which demonstrates that the
316 adjacent soil settlement was more than the pile settlement near the upper
317 portion of the piles but was similar in magnitude near the lower portion of
318 the piles (comparative centrifuge test data is not available), indicating that
319 the near-surface soil acts to drag down the piles.

320 Figure 4 also shows the axial force along the piles during spin-up for FEA



(a)



(b)

Figure 4: Displacement and axial force along the pile after spin-up: (a) finite element analysis, (b) centrifuge test

321 and centrifuge tests. The solid grey line represents the pile's self-weight at
322 80 g (the 5 N pile head load is included). Centrifuge test data show an in-
323 crease in axial force along the pile after spin-up (axial force along the pile
324 is greater than the pile self-weight), resulting from the drag-down forces ap-
325 plied by the soil to the pile shaft due to relative soil-pile movement. The pile
326 axial forces from the FEA match closely to the pile self-weight, indicating an
327 insignificant change in shaft resistance during spin-up. Shaft resistance mo-
328 bilisation is governed by (1) the magnitude of relative displacement between
329 the soil and pile, and (2) the magnitude of effective radial stress (σ'_r) around
330 the pile. In relation to (1), [Song and Marshall \(2020b\)](#) used a camera to mea-
331 sure the soil settlement (75mm away from the pile at the front transparent
332 wall of the centrifuge container) along the depth of the piles during centrifuge
333 spin-up. Results indicated a maximum relative soil-pile displacement in the
334 centrifuge test of around 1 mm, which is greater than the numerical simu-
335 lation result presented in Figure 4 (a) (maximum relative displacement of
336 around 0.2 mm).

337 In relation to (2), Figure 5 shows the average effective radial stress ($\sigma'_{r,ave}$)
338 along the depth of pile 1 after spin-up (2-80 g) in the TPSI FEA test.
339 The $\sigma'_{r,ave}$ value was calculated as the average effective radial stress around
340 the pile circumference. In addition, the static earth pressure is presented
341 ($\sigma'_{r,ave}/\sigma'_v=0.5$). FEA results show that the static earth pressure condition
342 remains valid along the pile, indicating that the shaft resistance mobilisation
343 was very limited. For the centrifuge test, due to the relatively larger move-
344 ment between the soil and piles, [Song and Marshall \(2020b\)](#) indicated that
345 the static earth pressure coefficient is no longer valid and, based on the radial

346 stress measurement data given by [Jacobsz \(2003\)](#), suggested that $\sigma'_{r,ave}/\sigma'_v$
 347 close to the pile after centrifuge spin-up was about 1.46 (see Figure 5). This
 348 difference in $\sigma'_{r,ave}$ between the FEA and centrifuge tests would significantly
 349 affect the axial force (mobilised shaft friction) along the pile during spin-up.

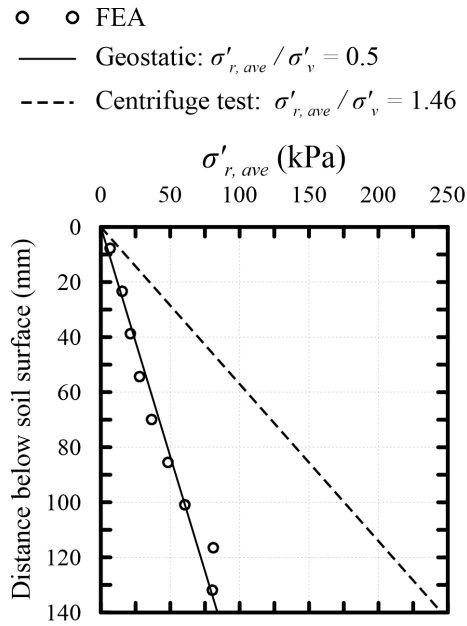


Figure 5: Average radial stress $\sigma'_{r,ave}$ after spin-up

350 4.2. Pile loading

351 After spin-up, piles were loaded to the designated working load (255 N
 352 for outer piles 1 and 4; 370 N for inner piles 2 and 3). Figure 6 shows the
 353 axial force along the piles before and after pile loading for test TPSI in both
 354 centrifuge and FEA tests.

355 For the centrifuge test, the pile end bearing load was not measured di-
 356 rectly; it was approximated by linearly extrapolating the data from the two

357 closest FBG measurement points (Figure 6 illustrates the locations of the two
 358 measurement points used in the extrapolation). All piles in both centrifuge
 359 and numerical tests show an increase in axial force along the entire pile length
 360 due to pile loading. For the piles in the centrifuge test, the increase in pile
 361 end bearing load is much smaller than the applied head load, indicating that
 362 the pile shaft resistance took most of the applied load. For the numerical
 363 simulation, the majority of the applied pile load was taken by the pile end
 bearing load.

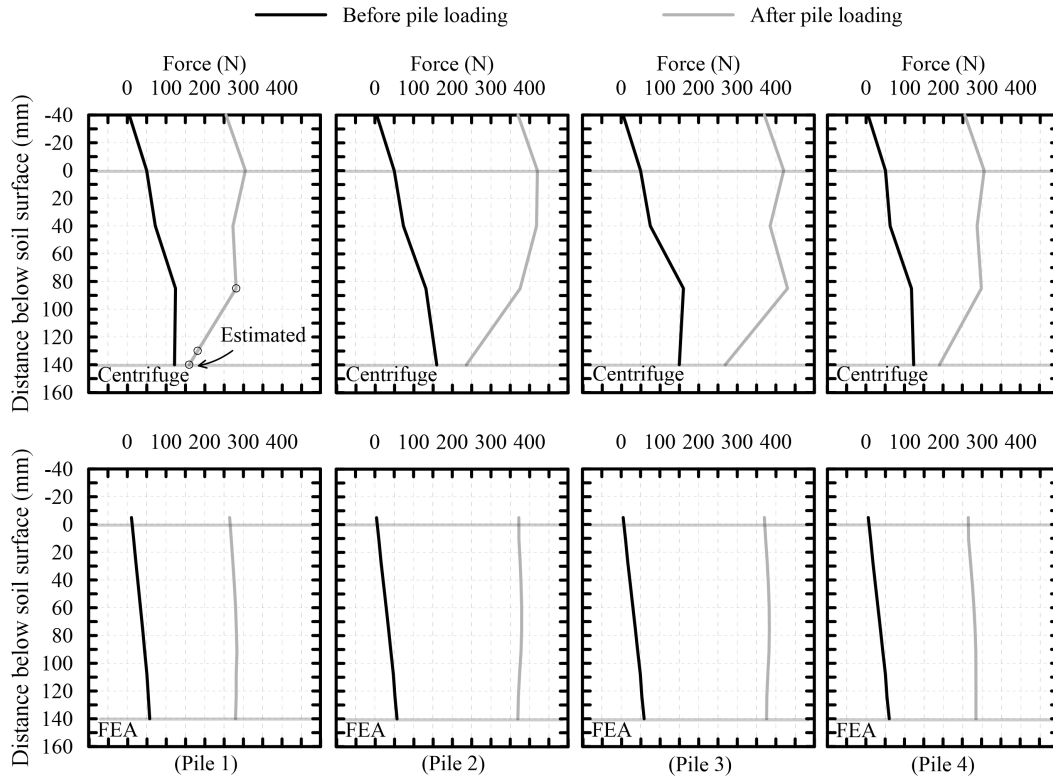


Figure 6: Pile axial force after pile loading for centrifuge and FEA test TPSI

364

365 To further understand the development of shaft resistance caused by pile

loading, Figure 7 shows the shaft resistance along the piles before and after pile loading in test TPSI. Note that, for the centrifuge tests, since there are only three measurement points along the depth of the piles, the shaft resistance between two measurement points is presented as a constant value (average shaft resistance between two measurement points), which results in some relatively large ‘jumps’ in shaft resistance in Figure 7. Prior to pile loading (after spin-up), negative pile shaft resistance developed along most (centrifuge) and all (FEA) of the lengths of the piles, indicating that the soil was pulling the pile downwards (as previously discussed). Note, however, the difference in magnitude between centrifuge and FEA results, with peak negative shaft resistance being about -40 kPa in the centrifuge test, compared to peak values of about -10 kPa from the FEA results. After pile loading, both centrifuge and numerical simulation results show an increase in shaft resistance which, for both centrifuge and FEA, occurs mainly near the base of the piles, where shaft friction changes from negative to positive. In the centrifuge, after pile loading, the full length of most piles (apart from the middle portion of piles 3) are noted to have positive shaft resistance, whereas for some of the piles in the FEA tests, the shear resistance in the upper portion of the piles remained negative (the pile head load was insufficient to cause a reversal of shear stress direction). The difference in magnitude of change in shaft resistance between centrifuge and FEA results is significant, with large increases of about 80 kPa taking place in the centrifuge (carrying most of the applied pile head load, as previously noted), compared to about 15 kPa for FEA (where most of the applied load was carried by the pile base load).

391 Overall, these results indicate that the FEA model did not fully capture
392 the load distribution within the piles during pile loading; the FEA results
393 show a bias for pile end-bearing resistance, whereas the centrifuge results
394 show greater load resistance along the pile shaft. This discrepancy is, in
395 part, a limitation of the adopted FEA soil-pile interface model (Coulomb
396 friction law, with an absolute elastic slip distance of 1.5 mm). The use of a
397 complex soil-pile interface model developed by [Stutz et al. \(2016\)](#) was also
398 attempted in this study, however its use alongside the adopted complex con-
399 stitute model for soil (required to get an accurate small-strain stress-strain
400 response) resulted in convergence issues at most values of tunnel volume
401 losses ($V_{l,t} > 0.5\%$). In addition, this discrepancy is also a consequence of
402 the FEA model results from the spin-up stage, where it was shown that the
403 lateral stresses acting on the piles in the centrifuge tests were likely consider-
404 ably larger than within the FEA simulations. Nevertheless, the subsequent
405 sections will explore how the FEA model results compare against centrifuge
406 test data during tunnel volume loss.

407 *4.3. Pile settlement due to tunnelling*

408 [Song and Marshall \(2020b\)](#) highlighted the importance of two main mech-
409 anisms governing changes in pile response to tunnelling: Mechanism T (for
410 tunnelling) relating to tunnelling induced ground movements, and Mecha-
411 nism S (for structure) relating to load transfer between pile heads due to
412 structure stiffness and deformation. The following discussion will also refer
413 to these mechanisms as a means of explaining some of the observed behaviour.

414 Figure 8 shows the normalised pile settlement (S_p/d_p ; positive settle-
415 ments are downwards) with tunnel volume loss for both centrifuge and FEA

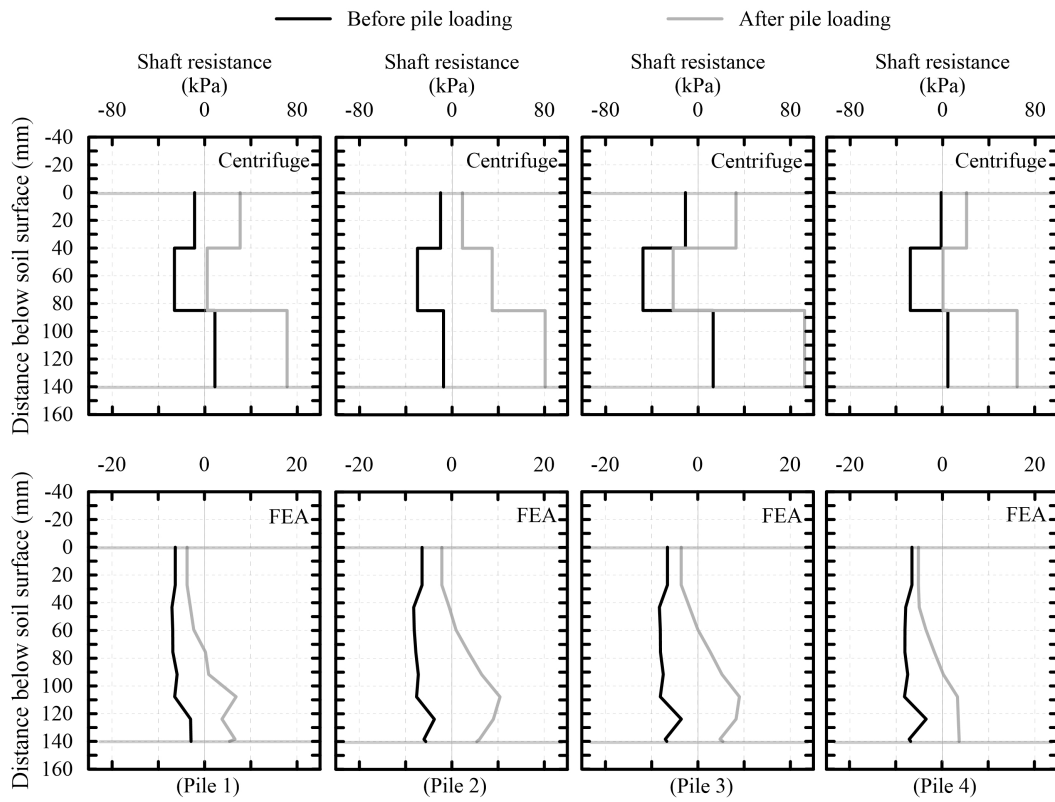


Figure 7: Shaft resistance along the pile after pile loading for centrifuge and FEA test TPSI

416 tests for piles 1 to 4; note that the normalised settlement scale is not consis-
417 tent across all piles. For test TPGI, a constant load was maintained during
418 the tunnel volume loss process, whereas the pile load varied in test TPSI
419 as a result of load redistribution from the (virtually) connected five-story
420 steel frame structure. In general, the difference between TPGI and TPSI
421 centrifuge test results for pile displacements is relatively small, indicating
422 that Mechanism S had a minor impact on pile settlements (for example,
423 at prototype scale, pile 2 settlement increased from about 10 mm for TPGI
424 to about 12 mm for TPSI at $V_{l,t} = 3\%$). This suggests that practical ap-
425 proaches for evaluating pile settlements caused by tunnelling (e.g. [Selemetas](#)
426 [\(2005\)](#); [Selemetas and Standing \(2017\)](#); [Devriendt and Williamson \(2011\)](#))
427 could conveniently overlook the effects of Mechanism S without significant
428 consequences (though pile-group effects may also be important, which are
429 not accounted for by [Devriendt and Williamson \(2011\)](#); analytical methods
430 such as [Franza et al. \(2021a\)](#) may provide a more robust approach for de-
431 sign). It should be noted, however, that the case considered here included a
432 relatively flexible framed building. For framed buildings, where it has been
433 shown that shear deformations dominate their response to tunnelling, [Xu](#)
434 [et al. \(2020\)](#) proposed a relative soil-building shear stiffness parameter κ ;
435 for this study, a value of $\kappa > 500$ was estimated, which is greater than all
436 cases considered within [Xu et al. \(2020\)](#) and indicates that the building used
437 in this study was relatively flexible (this is due mainly to the fact that the
438 [Xu et al. \(2020\)](#) buildings assumed plane-strain vertical walls running along
439 the direction of the tunnel, whereas individual columns were considered in
440 this study.) For less flexible structures, Mechanism S may have more of an

441 impact on pile settlements; more study is needed to consider a wider range
442 of relative soil-building stiffness cases.

443 The FEA settlements tend to over-predict centrifuge results for piles 1, 2
444 and 3 in both tests TPGI and TPSI. Both centrifuge and FEA results show
445 that the pile located closest to the tunnel (pile 1) settled most with tunnel
446 volume loss. In the centrifuge tests, the effect of the connected structure on
447 the pile 1 settlement response to volume loss was negligible (TPGI and TPSI
448 results being closely matched), whereas the FEA results for pile 1 show that,
449 at higher volume losses, the TPSI settlements become less than TPGI (due
450 to pile unloading from Mechanism S, as discussed in the next section). For
451 pile 2, both centrifuge tests (TPGI and TPSI) show similar pile settlement
452 initially ($V_{l,t}$ less than 1%) but diverge somewhat at higher volume losses,
453 with TPSI settlements being slightly larger than TPGI due to increased pile
454 head loads as volume loss increases (caused by load redistribution within
455 the building (Mechanism S), as discussed in the next section). A similar
456 observation is noted for the FEA results, though the difference in pile 2
457 settlement between TPSI and TPGI simulations is more significant than it
458 was in the centrifuge. The response of pile 3 is similar to that of pile 2,
459 with magnitudes of displacements being smaller. Finally, for pile 4 in the
460 centrifuge tests, at the end of tunnel volume loss ($V_{l,t} \approx 3\%$), test TPGI
461 shows greater settlement than test TPSI (indicating the TPSI pile head load
462 reduced during volume loss due to Mechanism S). For the FEA TPGI test,
463 the structure stiffness effect was sufficient to cause a negative (upwards)
464 displacement of pile 4 for tunnel volume loss $V_{l,t} > 1.5\%$ (note, however,
465 that the scale of pile 4 movements is very small; a 0.1% difference in S_p/d_p

466 corresponds to a prototype pile settlement of just under 1 mm).

467 In general, the FEA model provided satisfactory predictions of the pile
 468 settlements with tunnel volume loss; the magnitudes of settlements were
 469 clearly not a perfect match, however the trends in relation to associated
 470 mechanisms (i.e. pile loading/unloading during volume loss) were captured
 well.

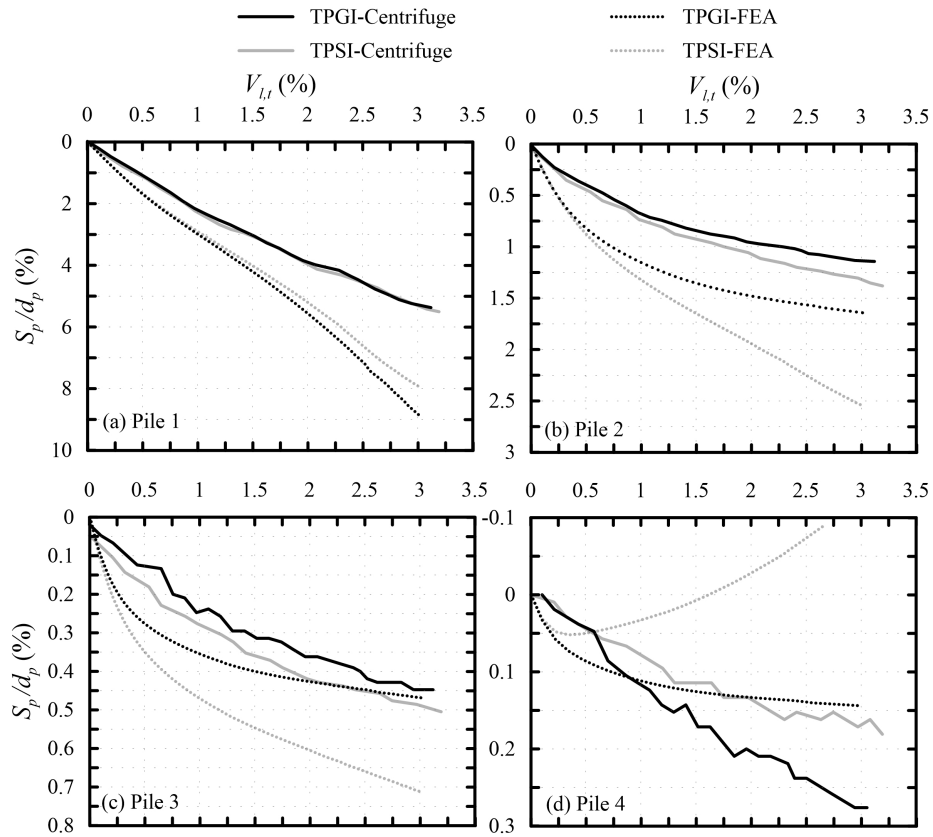


Figure 8: Normalised pile settlement (positive downwards) with tunnel volume loss for both centrifuge and FEA tests

471

472 4.4. *Pile head load transfer between piles*

473 Figure 9 shows the change in pile head with tunnel volume loss for both
474 centrifuge and FEA tests. Pile head loads remain constant for test TPPI,
475 hence the discussion below relates solely to test TPSI. The relative change of
476 pile head loads is noted to be very similar in the centrifuge and FEA tests,
477 which is a function of structural characteristics (consistent for both tests)
478 but also the magnitude of pile settlements (which differed, as illustrated in
479 Figure 8). Pile 1 shows a decrease in head load with tunnelling of about
480 50 N at $V_{l,t} = 3\%$ ($\approx 20\%$ reduction), which did not have a noticeable impact
481 on the centrifuge pile settlement (Figure 8), but did have a small effect on
482 the FEA settlements (with TPSI reducing compared to TPPI due to pile
483 unloading). The majority of the reduced pile head load from pile 1 was
484 transferred to the adjacent pile 2, which increased by about 65 N ($\approx 18\%$) at
485 $V_{l,t} = 3\%$ in both centrifuge and FEA tests. Pile 3 also showed an increase in
486 head load with tunnelling by approximately 11 N (3%) in the centrifuge and
487 19 N (5%) in the FEA test at $V_{l,t} = 3\%$. For pile 4, due to a global rotation
488 of the building, both centrifuge and FEA tests show a decrease in pile head
489 load with tunnelling of ≈ 30 N (12%) for the centrifuge and FEA tests. Note
490 that the net change in pile head load across the entire structure must equal
491 zero.

492 These results demonstrate the importance of considering Mechanism S
493 when evaluating pile loading within tunnel-piled structure interaction prob-
494 lems, even for the relatively flexible building considered in this study (more
495 rigid structures will have a greater effect on pile head load redistribution,
496 as demonstrated by [Franza et al. \(2021b\)](#)). Mechanism S is currently not

497 considered within standard tunnel design risk assessments (e.g. Mair et al.
 498 (1996); Schoor et al. (2021)), though recent work by Franza et al. (2021b)
 499 has provided a rational approach for incorporating building stiffness within
 500 a computationally efficient two-stage model for soil-pile-structure interaction
 analysis.

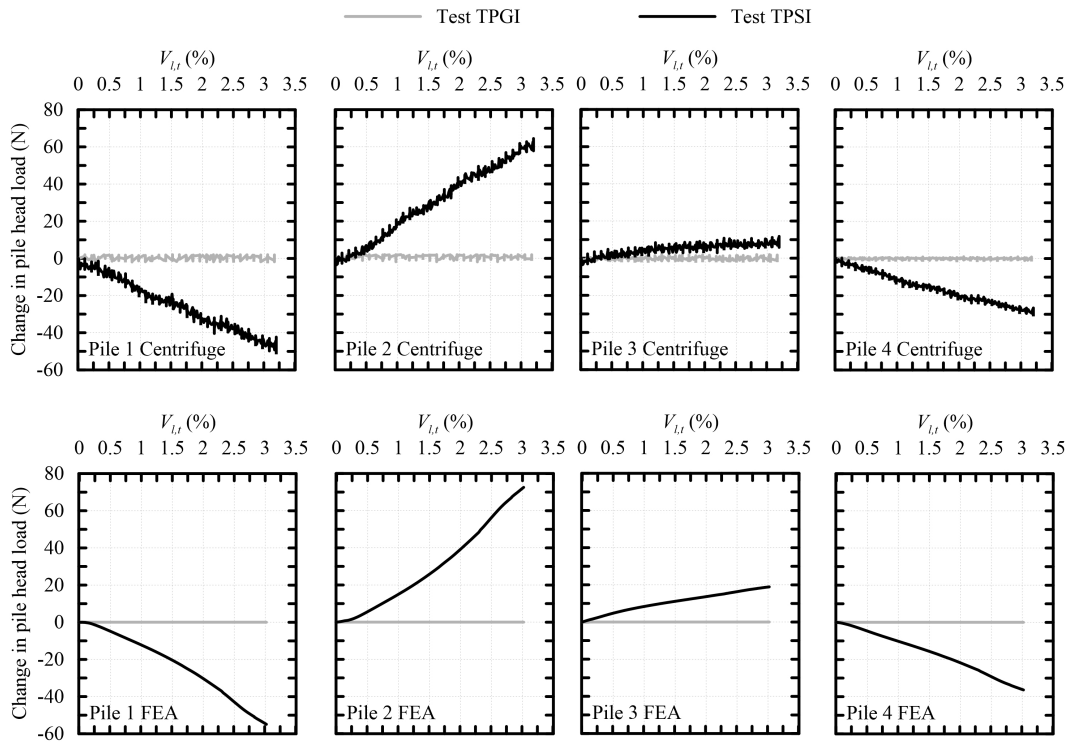


Figure 9: Pile head load with tunnel volume loss for both centrifuge and FEA tests

501

502 In general, despite the fact that the FEA test over-estimated pile set-
 503 tlement, the load transfer mechanism between piles agrees well between the
 504 FEA and centrifuge tests. The change in pile head load is related to the
 505 structure deformation, which is illustrated in Figure S1 in the supplemental
 506 data, showing pile settlements and the deformed structure for the centrifuge

507 and FEA tests at a tunnel volume loss of $V_{l,t} = 3\%$. Figure S1 illustrates
508 that that the degree of structure deformation in the FEA test was greater
509 than in the centrifuge test.

510 *4.5. Force distribution along piles with tunnelling*

511 To illustrate the effect of Mechanisms T and S on the force distribution
512 along the piles, Figure 10 plots the axial force along the depth of the piles
513 prior to and after tunnel volume loss ($V_{l,t} \approx 3\%$) for tests TPGI and TPSI in
514 both centrifuge and FEA tests. For pile 1 in test TPGI (constant pile head
515 load), both centrifuge and FEA tests show that pile end-bearing force reduces
516 with tunnelling, with additional shaft resistance being mobilised (to maintain
517 equilibrium) with pile settlement (see Figure 8). The FEA TPGI test results
518 for piles 2-4 show little to no effect of tunnel volume loss. For the centrifuge
519 TPGI results, piles 2 and 3 show little change after volume loss (pile 2 shows
520 a small increase in end-bearing load), however the data indicate that the end-
521 bearing load in pile 4 reduced as a result of tunnel volume loss. As discussed
522 in Song and Marshall (2020b), the reason for the reduction in end-bearing
523 load in pile 4 is not clear, but may be due to some pile-pile interactions or
524 boundary effects. In general, for test TPGI, as the structural stiffness effect
525 (mechanism S) is not considered and the axial force distribution along the
526 piles is only affected by tunnelling (mechanism T), both centrifuge and FEA
527 tests show that the pile located closest to the tunnel experienced the most
528 significant change in axial force. For piles located further away from the
529 tunnel, the effect of tunnelling on pile axial force is not significant.

530 For test TPSI, due to mechanism S, pile 1 head load decreased by ap-
531 proximately 45 N and 55 N (17% and 22%) at $V_{l,t} \approx 3\%$ in the centrifuge

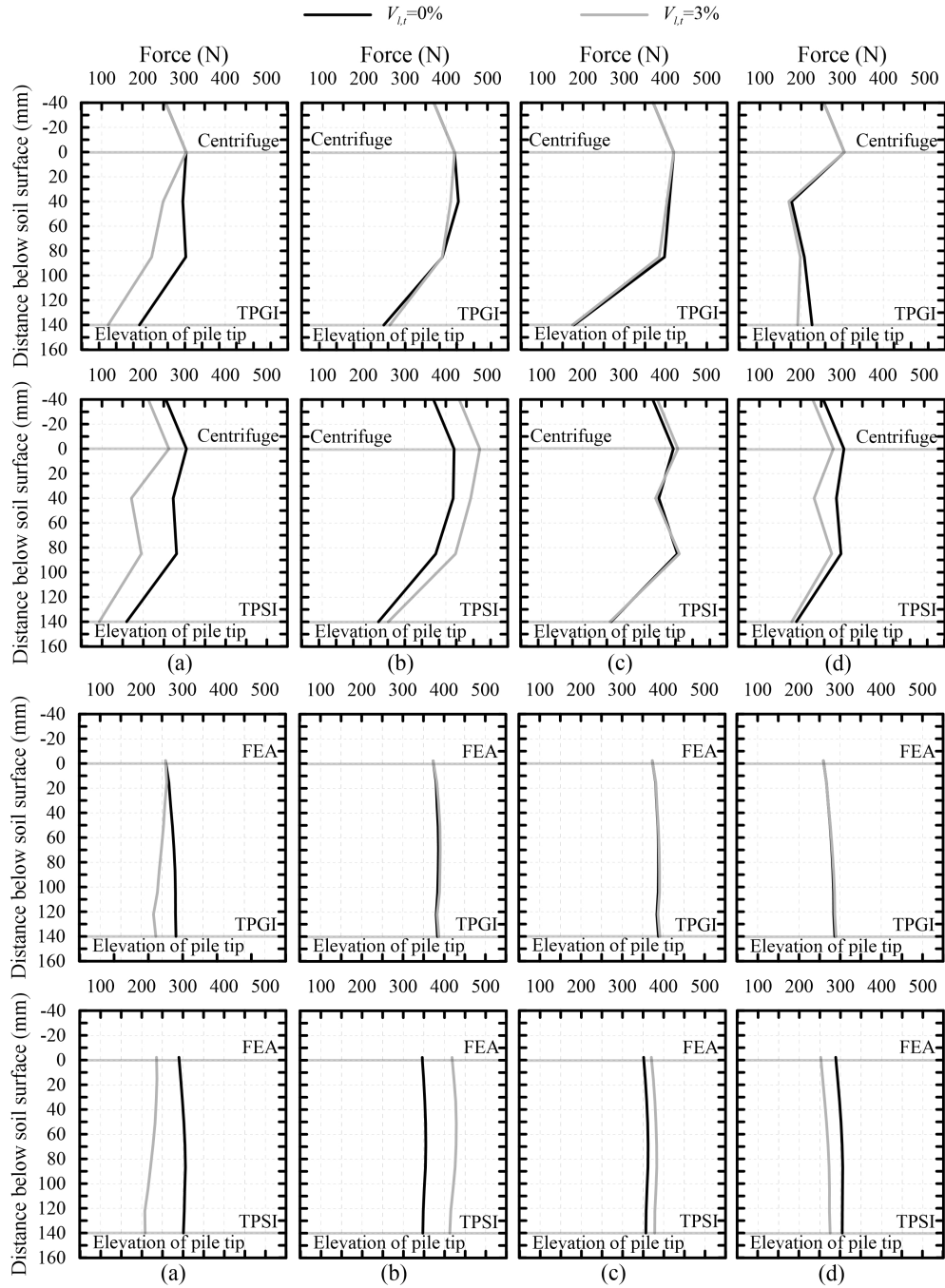


Figure 10: Pile axial load at $V_{l,t} = 0$ and 3% for both centrifuge and FEA tests: (a) pile 1, (b) pile 2, (c) pile 3, (d) pile 4

532 and FEA tests, respectively. Despite the decrease in pile head load, the pile
533 end-bearing load also decreased as a result of tunnel volume loss, by a mag-
534 nitude similar to pile 1 in test TPGI. In both centrifuge and FEA tests, the
535 magnitude of decrease of the end-bearing force is greater than the decrease
536 in pile head load, indicating that the pile shaft resistance increased. For pile
537 2 in test TPSI, due to mechanism S, head load increased in both centrifuge
538 and FEA tests by about 65 N (18% increase); in the centrifuge, this added
539 load was distributed to the pile tip (24 N; 37% of added load) and shaft (41 N;
540 63% of added load), whereas for the FEA, almost all of the added load was
541 taken by the pile tip. For pile 3 in test TPSI, centrifuge test results show
542 minimal change in pile axial force profile with tunnel volume loss, whereas
543 FEA results show a small increase in pile head load and end-bearing load
544 (load transferred to pile tip, as was the case for pile 2). For pile 4, both tests
545 show a decrease in pile head load (mechanism S); FEA results show that
546 the decreased pile head load was transferred to pile tip, whereas centrifuge
547 results show a decrease in both shaft resistance and end-bearing load. In
548 general, the magnitude of changes in axial forces along the piles from the
549 numerical simulation and centrifuge tests broadly agree, and the trends of
550 changes with tunnel volume loss agree well.

551 *4.6. Relative pile-soil settlements with tunnelling*

552 Axial force distributions along the piles presented in Figure 10 demon-
553 strate that the shaft resistance along the piles changes with tunnel volume
554 loss. The mobilisation of shaft resistance is caused by relative settlement
555 between the soil (S_v) and pile (S_p). For centrifuge tests TPGI and TPSI,
556 this relative settlement can be approximated using soil settlements (S_v) ob-

557 tained (using image analysis techniques) at the the front acrylic wall of the
558 centrifuge container at locations corresponding to the piles. However, this
559 approximate approach can not fully represent the soil settlements around the
560 pile circumference. The results of the numerical simulations, which provide
561 detailed results of soil settlements around the piles, can be used to investigate
562 the relative pile-soil settlements during tunnelling.

563 Figure 11 presents the numerical results for settlement of piles (S_p) and
564 the surrounding soil (S_v), along the circumference of the piles, at a tunnel
565 volume loss of $V_{l,t} = 3\%$ for the TPGI and TPSI tests. Three soil depths are
566 shown: the soil surface, 63 mm and 125 mm below the soil surface (upper,
567 middle, and lower rows of plots in Figure 11); theses three depths are used
568 to represent settlements in the upper, middle and lower portions of the piles,
569 respectively. The size of the circle represents the magnitude of the settlement,
570 with labels indicating the scale of settlement. As the piles are relatively rigid,
571 pile settlement is constant with depth, whereas soil settlement varies with
572 depth.

573 For pile 1 (closest to the tunnel), both TPGI and TPSI tests show that the
574 pile settlement is greater than the surrounding soil. Also, pile 1 settlement
575 in test TPGI is greater than TPSI, resulting from the reduction of pile head
576 load in test TPSI, whereas soil settlements for the two tests is very similar.
577 The soil settlement around pile 1 is not uniform; all three depths show that
578 the soil closest to the tunnel (0°) settled more than the soil on the opposite
579 side (180°), with the disparity increasing with depth. The magnitude of
580 soil settlement (size of the circle) increases with depth, indicating lower soil-
581 pile relative settlements at greater depth. In general, the pile 1 settlement

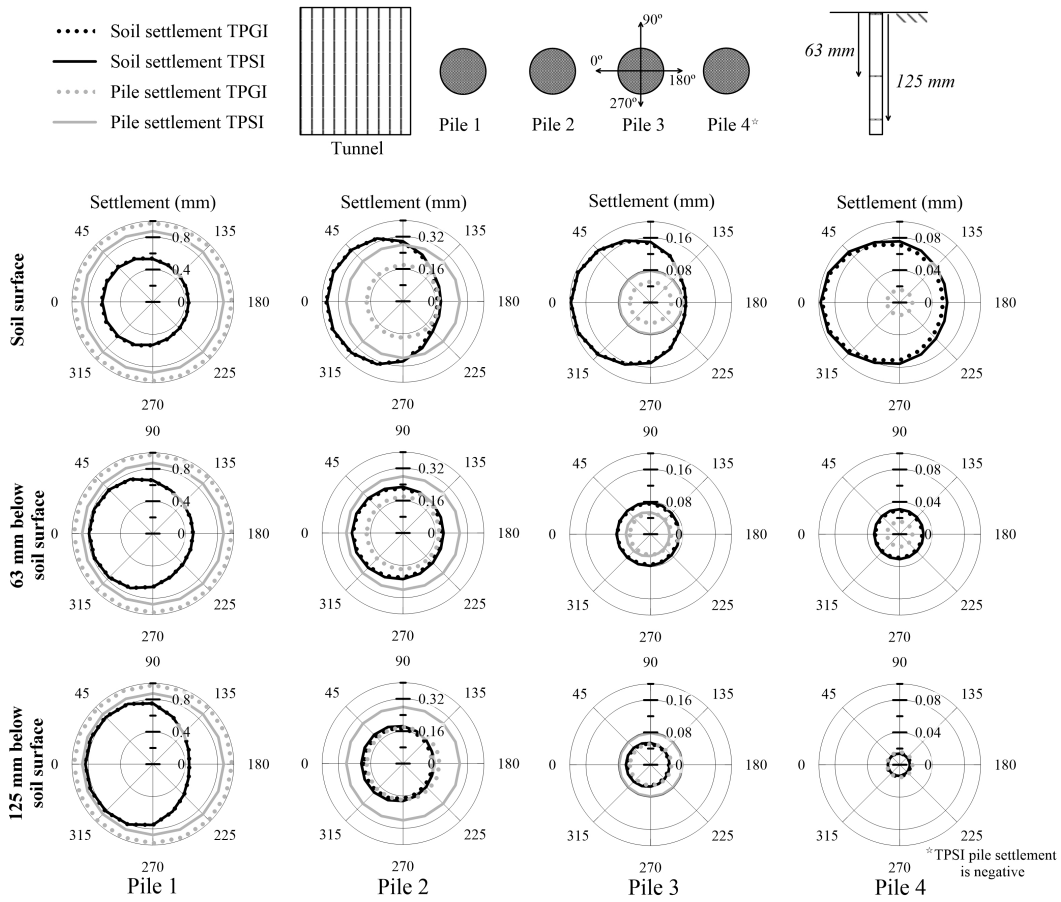


Figure 11: Pile and soil settlement at a tunnel volume loss of $V_{l,t} = 3\%$ for TPGI and TPSI FEA tests

582 is greater than that of the surrounding soil, indicating an increase in shaft
583 friction along the pile with tunnel volume loss. Referring back to Figure 10,
584 for pile 1 in both centrifuge and FEA tests, the decrease in pile end-bearing
585 load was greater than the decrease in pile head load, indicating an overall
586 increase in shaft resistance along the depth of the pile.

587 In contrast to pile 1, the non-uniformity of soil settlements for piles 2-4 is
588 greatest at the soil surface, with settlements around the pile becoming more
589 uniform at greater depths. Pile 2 settlement in test TPSI is greater than in
590 test TPGI because of the increase in pile head load (due to mechanism S;
591 as discussed in the previous subsection, the decreased pile 1 head load was
592 transferred to the adjacent piles 2 and 3, see Figure 10). Note that the
593 increase in pile head load for pile 2 in test TPSI was more significant than the
594 increase in pile end-bearing load; see Figure 10(b). To balance the added pile
595 head load, additional pile settlement is required to mobilise resistance; for test
596 TPSI, the tunnelling induced soil settlement was less than pile 2 settlement
597 in the middle and lower portions of the pile, resulting in a mobilisation of
598 increased shaft resistance in this region.

599 For piles 3 and 4, Figure 11 shows that the pile settlement was less than
600 the surrounding soil at all three depths. The differences in soil settlement
601 between TPGI and TPSI tests for all four piles is insignificant. For pile 4
602 (farthest away from the tunnel), tunnelling induced soil settlement around
603 the pile is minimal (mechanism T) and similar in magnitude for both TPGI
604 and TPSI tests. Nevertheless, due to the effect of structural stiffness (due
605 to mechanism S causing a decrease in pile head load), pile 4 experienced an
606 upwards (negative) displacement at $V_{l,t} = 3\%$ (refer to Figure 8(d)), hence the

607 pile's settlement is not shown in Figure 11. Note that this upwards movement
608 was not observed in the TPSI centrifuge test, though pile 4 settlement was
609 less in the TPSI test than the TPGI test, showing a consistent trend between
610 centrifuge and numerical results.

611 4.7. Radial stresses around piles

612 The numerical analysis results also provide detailed information about
613 the soil stress conditions around the piles and how it is affected by tunnel
614 volume loss, which is not available from the centrifuge tests. This information
615 enables a better understanding of how and why pile load distribution changes
616 during tunnelling. Figure 12 shows the radial stress (σ'_r) around the pile
617 circumference before and after tunnel volume loss ($V_{l,t} = 3\%$) for the TPSI
618 and TPGI FEA tests. The radial stress around the pile is plotted at three
619 depths: 8, 70 and 117 mm below the soil surface. As the radial stress around
620 the pile is two dimensional, the average radial stress around the pile at a given
621 depth can be represented by the size of the 'regions' shown in Figure 12 (this
622 aspect will be discussed further in the next subsection), whereas a shift of the
623 centre of the region indicates a stress offset in a particular area of the pile
624 circumference.

625 Prior to tunnel volume loss ($V_{l,t} = 0\%$), the piles were loaded to the
626 designated working load and the radial stress σ'_r is seen to increase with
627 depth. At this stage, the radial stress is generally uniformly distributed
628 around the pile circumference (the exception to this is near the soil surface,
629 where radial stresses are very low and, at the right side of the pile (farthest
630 from the tunnel), tend to zero; the stresses in this area were affected by
631 the spin-up procedure, where the pile was fixed in place, but the soil moved

632 slightly away from the tunnel).

633 At $V_{l,t} = 3\%$, for pile 1 (located closest to the tunnel), the radial stress
634 at the lower portion of the pile (117 mm below soil surface) shows a slightly
635 smaller stress region compared to $V_{l,t} = 0\%$ in both TPSI and TPGI tests,
636 indicating that the average radial stress decreased slightly with tunnel vol-
637 ume loss. At the middle and upper portions (70 and 8 mm below soil surface)
638 of pile 1, the size of the stress region is largest at $V_{l,t} = 3\%$ in both tests,
639 indicating an increase of average radial stress. The centres of the regions at
640 $V_{l,t} = 3\%$ for the upper portion of pile 1 are shifted to the right (away from
641 the tunnel), indicating a bias of stress on the far-side of the pile, caused by
642 horizontal movements of the soil towards the tunnel. With tunnel volume
643 loss, test TPGI shows a greater increase in average radial stress at the upper
644 portion of pile 1 than in test TPSI. The detailed stress paths (average ra-
645 dial stress versus shaft resistance around piles) will be discussed in the next
646 subsection.

647 For pile 2 in both TPGI and TPSI tests, Figure 12 shows that the size of
648 the radial stress regions at all depths is not significantly affected by tunnel
649 volume loss (there is a small overall reduction), but the locations of the
650 centres of the regions is affected, indicating a shift in the bias of stress around
651 the pile. At the middle and upper portions of pile 2, after tunnel volume loss,
652 the bias of radial stress moves to the right (far) side of the pile; as for pile
653 1, this was caused by horizontal soil movements towards the tunnel. The
654 magnitude of the bias change in test TPGI is greater than TPSI. At the
655 lower portion of pile 2, the bias in stress is shifted to the left (closest to the
656 tunnel). As the base of pile 2 is relatively fixed (tunnelling induced ground

657 movements at the base of pile 2 are minimal), this region acts to resist the
658 lateral movement of the pile (which is being driven to the left by the soil
659 pressures at the upper and middle portions of the pile).

660 The changes in radial stresses around piles 3 and 4 show similar trends
661 as pile 2, with little change to the average radial stress, a bias of stress to
662 the right of the piles in the middle and upper portions, and a bias of stress
663 to the left of the piles at the lower portion.

664 In terms of comparison between TPGI and TPSI tests, the magnitude of
665 change in radial stress with tunnelling at the lower and middle portions of
666 the piles is not significant. However, at the upper portion of piles, test TPGI
667 shows a greater shift in the bias of radial stress distribution than the piles
668 in test TPSI. This indicates that the structure stiffness (Mechanism S) pre-
669 dominately affects the development of radial stresses only within the upper
670 portions of the piles; this will be further discussed in the following subsection.

671 *4.8. Computed stress paths at the soil-pile interface*

672 As described in the above subsection, the average radial stress along
673 the middle and upper portions of pile 1 increased with tunnel volume loss,
674 whereas for pile 2 there was minimal change. To further understand the
675 shearing mechanism along the piles, Figure 13 shows the average radial stress
676 versus shaft resistance at the middle portion (70 mm below soil surface) of
677 piles 1 and 2 in the TPGI and TPSI FEA tests. The average radial stress
678 ($\sigma'_{r,ave}$) was calculated as the average value of the radial stress around the
679 pile; the shaft resistance (τ_{ave}) was calculated based on the pile axial forces
680 at that depth of the pile.

681 Results are provided from the entire FEA test process, which includes

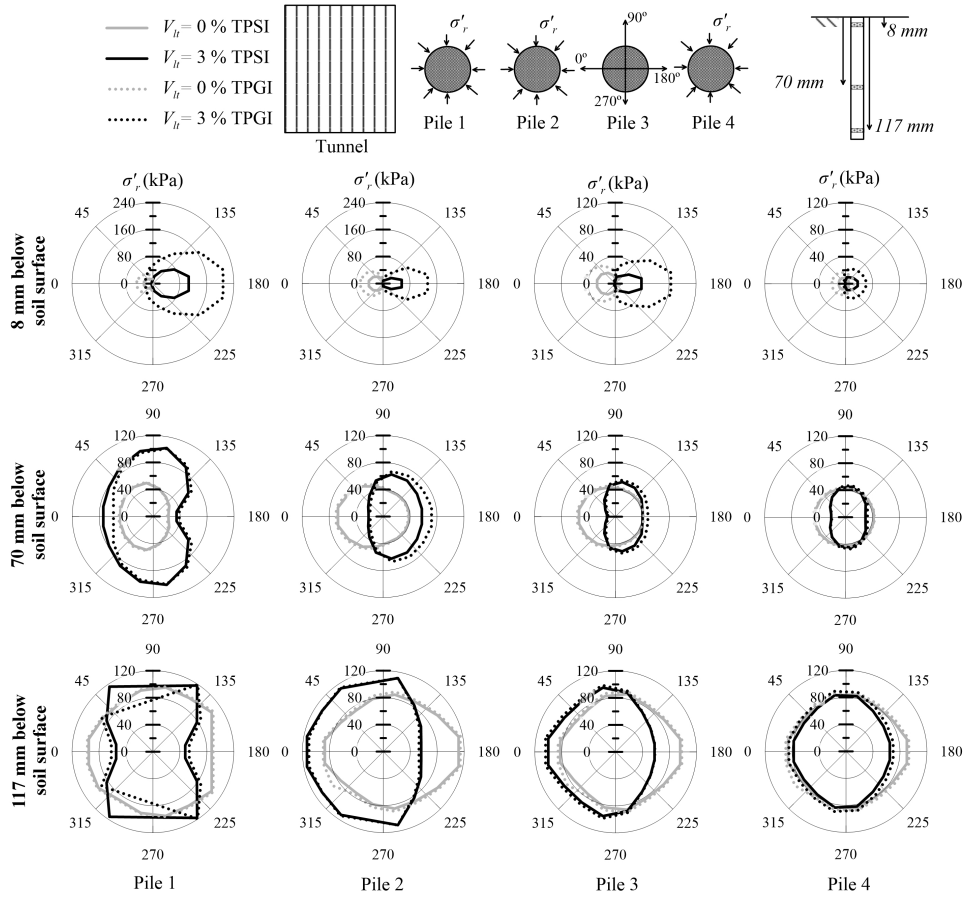


Figure 12: Radial stress around piles before and after tunnel volume loss ($V_{l,t} = 3\%$) for TPGI and TPSI FEA tests

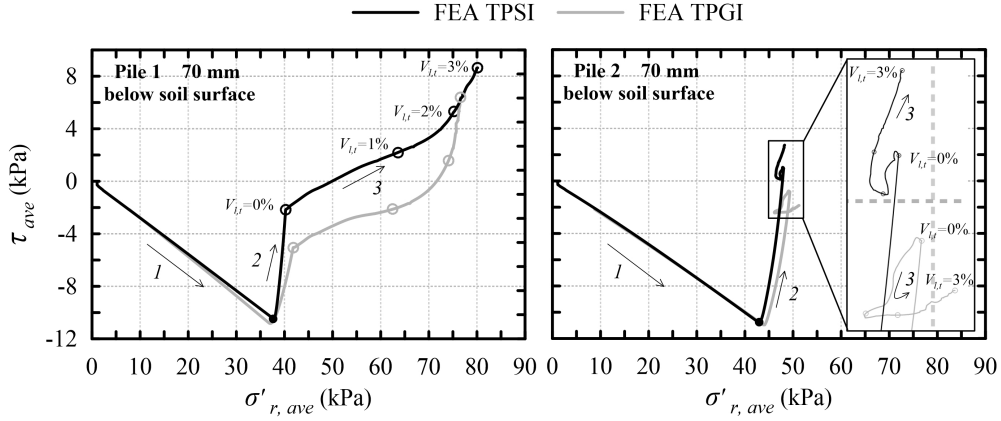


Figure 13: Stress path of the soil elements close to piles 1 and 2 in TPGI and TPSI FEA tests

682 three stages: (1) spin-up, (2) pile loading, and (3) tunnel volume loss. In
 683 stage (1), with the increase in gravity (self-weight of the soil), the average
 684 radial stress ($\sigma'_{r,ave}$) at the middle portion of the piles increased. As discussed
 685 in Section 5.1, the soil around the piles settled more than the piles and tended
 686 to pull the piles downwards, which caused negative shaft resistance along the
 687 piles. During spin-up (stage 1), the stress paths between the TPGI and TPSI
 688 tests are very similar.

689 Piles were then loaded to the designated working load (stage 2), during
 690 which time the average radial stress around both piles increased; pile 2 shows
 691 a greater increase because a higher working load was applied (370 N for pile
 692 2 and 255 N for pile 1). In addition, due to the pile loading, shear resistance
 693 increased in both piles. After pile loading, pile 2 shows an increase in shaft
 694 resistance, and test TPSI shows positive shaft resistance after pile loading
 695 (open circle with $V_{l,t} = 0\%$), whereas shaft resistance in pile 1 remains neg-
 696 ative (the applied head load being insufficient to cause the reversal of shaft

697 resistance, as discussed in Section 5.2). Note that the differences between
698 TPSI and TPGI results during pile loading (stage 2), which are most notice-
699 able for pile 1, are due to the influence of structure stiffness in test TPSI (the
700 structure was included in the FEA model at the start of stage 1).

701 During tunnel volume loss (stage 3), despite that fact that pile 1 head load
702 decreased in test TPSI (due to Mechanism S), both TPGI and TPSI tests
703 show an increase in average radial stress and shaft resistance with tunnelling.
704 Referring back to Figure 11, it was shown that the pile settlement at the
705 middle portion of the pile was greater than the surrounding soil after tunnel
706 volume loss; this relative displacement would cause shearing and potentially
707 dilation of the surrounding soil, which would increase the radial stress and
708 shaft resistance, consistent with the centrifuge results reported by [Song and
709 Marshall \(2020b\)](#). Other mechanisms, such as arching around the tunnel
710 ([Franza et al., 2019](#); [Iglesia et al., 2014](#)), would also act to increase radial
711 stresses in this region. For pile 2 in both TPGI and TPSI tests, the stress
712 paths in Figure 13 indicate a complex response to tunnel volume loss. The
713 average radial stress initially shows a decrease with tunnelling (up to $V_{l,t} \approx$
714 1%), and then starts to increase, though the magnitude of changes in shaft
715 resistance and average radial stress are relatively small. At the end of tunnel
716 volume loss ($V_{l,t} = 3\%$), pile 2 in test TPSI shows a greater increase in shaft
717 resistance than test TPGI; this occurred because of the increased pile 2 head
718 load in test TPSI due to Mechanism S.

719 To summarise, the soil-pile interface shearing mechanism during tunnel
720 volume loss is largely affected by the relative distance between the pile and
721 the tunnel. For the pile closest to the tunnel, axial forces along the pile from

722 both centrifuge and numerical tests indicate a decrease in pile end-bearing
723 load with tunnelling, causing the pile to settle relative to the surrounding
724 soil and resulting in increased shaft resistance along the upper and middle
725 portions of the pile. Numerical results from tests TPGI and TPSI suggest
726 that the increase in shaft resistance is less affected by the structure stiffness
727 (Mechanism S). For pile 2 in test TPSI, both centrifuge and numerical tests
728 showed an increase in pile head load due to mechanism S. Based on the
729 axial force distribution along pile 2 (presented in Figure 10), both FEA and
730 centrifuge tests show that most of the increased pile head load was translated
731 to the pile base, indicating that shaft resistance was not significantly affected
732 by tunnelling. For piles further away from the tunnel, the effect of tunnelling
733 on axial force distribution along the piles was insignificant, with little change
734 to shaft resistance.

735 5. Conclusions

736 This paper used results from hybrid centrifuge tests and numerical simu-
737 lations to study the complex interaction between tunnelling induced ground
738 displacements and a piled structure. Two cases are presented in the pa-
739 per: a tunnel-pile group interaction (TPGI) in which pile head load remains
740 constant, and a tunnel-piled structure interaction (TPSI) where piles were
741 connected (virtually within the hybrid centrifuge test) to a five-storey steel
742 frame. Both cases considered a row of four piles running transverse to the
743 tunnel direction, with pile tips located just above the depth of the tunnel
744 crown, and with the nearest pile located to the side of the tunnel. An ad-
745 vanced hypoplastic constitutive model was used for numerical simulations of

746 the centrifuge tests, providing results that were consistent with the mecha-
747 nisms observed from centrifuge test results. The numerical simulations en-
748 abled an in-depth analysis of the response of piles to tunnelling and the role
749 that a connected structure plays (i.e. contrasting the TPGI and TPSI cases).
750 The following conclusions can be made from the work:

- 751 • During spin-up, both numerical and centrifuge tests showed an increase
752 in axial force along the piles; at the upper portion of the piles, the soil
753 settled more than the piles, with negative shaft friction developing and
754 pulling the piles downwards. The magnitude of the negative shaft resis-
755 tance in the numerical simulations was much smaller than the centrifuge
756 tests.
- 757 • During pile loading, numerical simulations showed that the majority of
758 added pile head load was taken by the pile end-bearing load, whereas
759 centrifuge results indicated that most of the increased pile head load
760 was taken by the shaft resistance.
- 761 • The discrepancies between numerical and centrifuge results during spin-
762 up and pile loading were related to the accuracy of the adopted FEA
763 interface element and the difference in radial stresses developing around
764 the piles; it was shown that the lateral stresses acting on the piles
765 in the centrifuge were likely considerably larger than within the FEA
766 simulations, which is due to the limitation of the adopted FEA soil-pile
767 interface model (Coulomb friction law).
- 768 • Pile settlements in the numerical simulations were greater than those
769 measured in the centrifuge tests in general, however the numerical re-

770 sults provided a good prediction of the difference in pile settlement
771 between the TPGI and TPSI tests. For the TPSI case, the numerical
772 simulation over-predicted the change in pile head load.

773 • Results demonstrated the effect of two important mechanisms affecting
774 pile head load, the axial force distribution along piles, and pile settle-
775 ment: Mechanism T related to tunnelling induced ground displace-
776 ments, and Mechanism S related to the structure stiffness. Mechanism
777 T is typically considered within tunnel design risk assessments, whereas
778 Mechanism S, which was shown to have a significant effect on pile head
779 loads, is generally disregarded.

780 • The amount of load redistribution due to structural stiffness (Mecha-
781 nism S) in the centrifuge and numerical models agreed well. The head
782 load of the pile closest to the tunnel reduced by about 20% at a tunnel
783 volume loss of 3%, whereas the head load of the adjacent pile increased
784 by about 18% (the building considered in this study was relatively flex-
785 ible in shear; more rigid buildings will have a greater effect on pile head
786 load redistribution). This level of load redistribution may be important
787 when considering foundations with low safety factors (for pile loading)
788 or where piles are susceptible to damage from tensile stresses ([Franza
789 et al., 2021a,b](#)).

790 • Numerical simulations showed that the soil settlement around the pile
791 circumference was not uniform with tunnelling; the near-side (relative
792 to the tunnel) soil settles more than the far-side. In addition, both
793 centrifuge and numerical tests showed that Mechanism S had an effect

794 on soil and pile settlements, consequently affecting the shaft resistance
795 development (though centrifuge test results indicated that the effect of
796 Mechanism S on pile displacements may not be significant for practical
797 considerations; more study including a wider parametric study is
798 needed here).

799 • Numerical results were used to demonstrate how tunnelling affects the
800 radial stress profile around piles. The changes to radial stresses around
801 the piles were dominated by the effect of tunnelling induced ground
802 displacements, causing a general pattern of increased stresses on the
803 far-side of the piles along the middle to upper portions of the piles,
804 caused by the movement of soil in this region. This was accompanied
805 by an increase in radial stresses on the near-sides of the piles along
806 the bottom portion as a way of achieving horizontal equilibrium. The
807 exception to this was the pile closest the tunnel, where, near the pile
808 tip, a general reduction of radial stress was observed due to the stress
809 relaxation caused by tunnelling.

810 • The computed stress paths at the soil-pile interface from the numerical
811 simulations suggested that, for the pile located closest to the tunnel,
812 with pile settlement, shaft resistance and average radial stress increase
813 with tunnelling along the middle and upper portions of the pile. The
814 stress paths along other piles (further away from the tunnel), though
815 complex, showed relatively small changes in radial stress and shaft
816 resistance.

817 The current study focused on evaluating the consequence of tunnel ex-

818 cavation on an adjacent piled structure in sand. Future research is needed
819 to better understand the effect of soil, foundation, building, and geometric
820 parameters, in addition to consideration of how protective measures could
821 be incorporated, such as the use of protective walls between the tunnel and
822 foundation.

823 **6. NOTATION**

B_{bay}	The spacing of bay
C	Depth of cover above the tunnel
C_u	Coefficient of uniformity
d_e	Distance between the pile and tunnel (Pile 1)
d_p	Diameter of the pile
D_t	Diameter of the tunnel (d_t)
D_{50}	Average size of the soil particle
e_{max}	Maximum void ratio
e_{min}	Minimum void ratio
e_{c0}	Critical void ratio at zero pressure
e_{d0}	Minimum void ratio at zero pressure
e_{i0}	Maximum void ratio at zero pressure
824 e_{p0}	Initial void ratio of compression test at zero pressure
e_{max}	Maximum void ratio
E	Young's modulus
EA	Axial stiffness
EI	Flexural rigidity
G_s	Specific gravity
H_{storey}	Height of the building storey in prototype scale
h_s	Granular hardness
I_d	Relative density
K_0	Static earth pressure coefficient
L_p	Pile length, measured from ground surface to pile tip
n	Controls curve fitting parameter
S_p	Pile settlement

	S_t	Spacing between piles
	S_v	Soil settlement; vertical displacement
	$V_{l,t}$	Tunnel volume loss, in %
	α	Governs the peak friction angle of the soil
	β	Governs the soil stiffness
825	σ'_v	Vertical effective stress
	σ'_r	Radial effective stress
	$\sigma'_{r,ave}$	average radial effective stress
	τ_{av}	Average shaft resistance
	ϕ'_c	Critical state friction angle
	ν	Poisson's ratio

826 7. Supplemental data

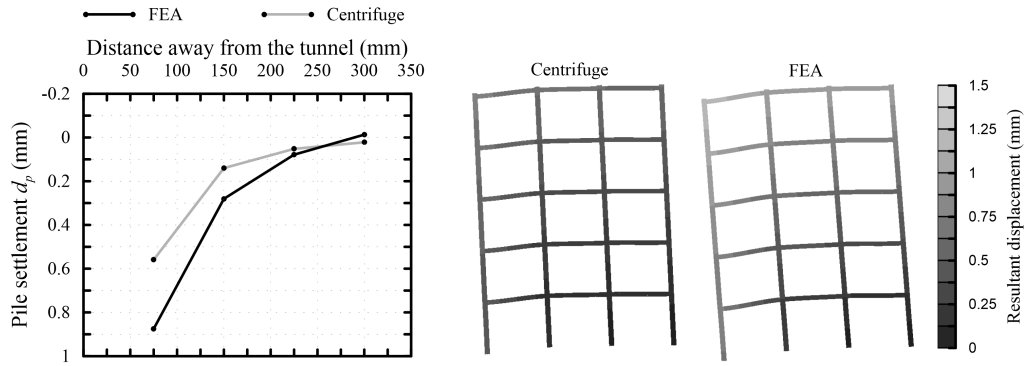


Figure S1: Deformed shape at a tunnel volume loss of $V_{l,t} = 3\%$ for test TPSI

827 **References**

828 Addenbrooke, T., Potts, D., Puzrin, A., 1997. The influence of pre-failure soil
829 stiffness on the numerical analysis of tunnel construction. *Géotechnique*
830 47, 693–712.

831 Boonsiri, I., Takemura, J., 2015. Observation of ground movement with
832 existing pile groups due to tunneling in sand using centrifuge modelling.
833 *Geotechnical and Geological Engineering* 33, 621–640.

834 Cheng, C.Y., Dasari, G.R., Chow, Y.K., Leung, C.F., 2007. Finite ele-
835 ment analysis of tunnel–soil–pile interaction using displacement controlled
836 model. *Tunnelling and Underground Space Technology* 22, 450–466.

837 Devriendt, M., Williamson, M., 2011. Validation of methods for assessing
838 tunnelling-induced settlements on piles. *Ground Eng* , 25–30.

839 Franza, A., Marshall, A.M., 2019. Centrifuge and real-time hybrid test-
840 ing of tunnelling beneath piles and piled buildings. *ASCE Journal of*
841 *Geotechnical and Geoenvironmental Engineering* 145, 04018110. doi:[10.](https://doi.org/10.1061/(ASCE)GT.1943-5606.0002003)
842 [1061/\(ASCE\)GT.1943-5606.0002003](https://doi.org/10.1061/(ASCE)GT.1943-5606.0002003).

843 Franza, A., Marshall, A.M., Jimenez, R., 2021a. Nonlinear soil-pile interac-
844 tion induced by ground settlements: pile displacements and internal forces.
845 *Géotechnique* 71, 239–248.

846 Franza, A., Marshall, A.M., Zhou, B., 2019. Greenfield tunnelling in sands:
847 the effects of soil density and relative depth. *Geotechnique* 69, 297–307.
848 doi:[10.1680/jgeot.17.p.091](https://doi.org/10.1680/jgeot.17.p.091).

- 849 Franza, A., Zheng, C., Marshall, A.M., Jimenez, R., 2021b. Investigation
850 of soil-pile-structure interaction induced by vertical loads and tun-
851 nelling. *Computers and Geotechnics* In press. doi:[10.1016/j.compgeo.](https://doi.org/10.1016/j.compgeo.2021.104386)
852 [2021.104386](https://doi.org/10.1016/j.compgeo.2021.104386).
- 853 Gulvanessian, H., Formichi, P., Calgaro, J.A., 2009. *Designers' Guide to*
854 *Eurocode 1: Actions on Buildings: EN1991-1-1 and-1-3 TO-1-7*. Thomas
855 Telford Ltd.
- 856 Herle, I., Gudehus, G., 1999. Determination of parameters of a hypoplas-
857 tic constitutive model from properties of grain assemblies. *Mechanics of*
858 *Cohesive-frictional Materials* 4, 461–486.
- 859 Hibbitt, K., 2002. *ABAQUS/Explicit User's Manual: Version 6.3*. Hibbit,
860 Karlson & Sorensen.
- 861 Hong, Y., Soomro, M.A., Ng, C., 2015. Settlement and load transfer mech-
862 anism of pile group due to side-by-side twin tunnelling. *Computers and*
863 *Geotechnics* 64, 105–119.
- 864 Idinyang, S., Franza, A., Heron, C., Marshall, A.M., 2018a. Real-time data
865 coupling for hybrid testing in a geotechnical centrifuge. *International Jour-*
866 *nal of Physical Modelling in Geotechnics* doi:[doi.org/10.1680/jphmg.](https://doi.org/10.1680/jphmg.17.00063)
867 [17.00063](https://doi.org/10.1680/jphmg.17.00063).
- 868 Idinyang, S., Franza, A., Heron, C., Marshall, A.M., 2018b. Real-time data
869 coupling for hybrid testing in a geotechnical centrifuge. *International Jour-*
870 *nal of Physical Modelling in Geotechnics* , 1–13.

- 871 Iglesia, G.R., Einstein, H.H., Whitman, R.V., 2014. Investigation of Soil
872 Arching with Centrifuge Tests. *Journal of Geotechnical and Geoenviron-*
873 *mental Engineering* 140, 04013005. doi:[10.1061/\(asce\)gt.1943-5606.](https://doi.org/10.1061/(asce)gt.1943-5606.0000998)
874 [0000998](https://doi.org/10.1061/(asce)gt.1943-5606.0000998).
- 875 Jacobsz, S.W., 2003. The effects of tunnelling on piled foundations. Ph.D.
876 thesis. University of Cambridge.
- 877 Jacobsz, S.W., Standing, J.R., Mair, R.J., Hagiwara, T., Sugiyama, T., 2004.
878 Centrifuge modelling of tunnelling near driven piles. *Soils and Foundations*
879 44, 49–56.
- 880 Jardine, R.J., Symes, M.J., Burland, J.B., 1984. The measurement of soil
881 stiffness in the triaxial apparatus. *Géotechnique* 34, 323–340. doi:[10.](https://doi.org/10.1680/geot.1984.34.3.323)
882 [1680/geot.1984.34.3.323](https://doi.org/10.1680/geot.1984.34.3.323).
- 883 Kaalberg, F.J., Teunissen, E.A.H., Van Tol, A.F., Bosch, J.W., 2005. Dutch
884 research on the impact of shield tunnelling on pile foundations, in: Klaas
885 Jan Bakker, Adam Bezuijen, W.B.E.K. (Ed.), *Proceedings of the 5th Inter-*
886 *national Symposium on Geotechnical Aspects of Underground Construc-*
887 *tion in Soft Ground*, Taylor & Francis Group. pp. 123–131.
- 888 Lee, C.J., Chiang, K.H., 2007. Responses of single piles to tunneling-
889 induced soil movements in sandy ground. *Canadian Geotechnical*
890 *Journal* 44, 1224–1241. URL: <https://doi.org/10.1139/T07-050>,
891 [arXiv:https://doi.org/10.1139/T07-050](https://doi.org/10.1139/T07-050).
- 892 Li, Y., Zhang, W., 2020. Investigation on passive pile responses subject to

- 893 adjacent tunnelling in anisotropic clay. *Computers and Geotechnics* 127.
894 doi:[10.1016/j.compgeo.2020.103782](https://doi.org/10.1016/j.compgeo.2020.103782).
- 895 Loganathan, N., Poulos, H.G., Stewart, D.P., 2000. Centrifuge model testing
896 of tunnelling-induced ground and pile deformations. *Geotechnique* 50, 283–
897 294.
- 898 Mair, R.J., Taylor, R.N., Burland, J.B., 1996. Prediction of ground move-
899 ments and assessment of risk of building damage due to bored tunnelling,
900 in: Mair, R.J., Taylor, R.N. (Eds.), *Geotechnical Aspects of Underground*
901 *Construction in soft ground*, Balkema, London. pp. 713–718.
- 902 Marshall, A.M., Mair, R.J., 2011. Tunneling beneath driven or jacked end-
903 bearing piles in sand. *Canadian Geotechnical Journal* 48, 1757–1771.
- 904 Ng, C.W.W., Hong, Y., Soomro, M., 2015. Effects of piggyback twin tun-
905 nelling on a pile group: 3d centrifuge tests and numerical modelling.
906 *Géotechnique* 65, 38–51.
- 907 Ng, C.W.W., Lu, H., Peng, S.Y., 2013. Three-dimensional centrifuge mod-
908 elling of the effects of twin tunnelling on an existing pile. *Tunnelling and*
909 *Underground Space Technology* 35, 189–199.
- 910 Ng, C.W.W., Soomro, M.A., Hong, Y., 2014. Three-dimensional centrifuge
911 modelling of pile group responses to side-by-side twin tunnelling. *Tun-*
912 *nelling and underground space technology* 43, 350–361.
- 913 Schoor, J., R, W., Yin, K., Stephenson, V., 2021. Assessing the impacts of
914 construction-induced ground movement on framed buildings, C796. Tech-
915 nical Report. CIRIA. London, UK.

916 Selemetas, D., 2005. The response of full-scale piles and piled structures to
917 tunnelling. Ph.D. thesis. University of Cambridge.

918 Selemetas, D., Standing, J.R., 2017. Response of full-scale piles to EPBM
919 tunnelling in London Clay. *Geotechnique* .

920 Song, G., Marshall, A.M., 2020a. Centrifuge modelling of tunnelling induced
921 ground displacements : pressure and displacement control tunnels. *Tun-*
922 *nelling and Underground Space Technology* 103, 103461. doi:[10.1016/j.](https://doi.org/10.1016/j.tust.2020.103461)
923 [tust.2020.103461](https://doi.org/10.1016/j.tust.2020.103461).

924 Song, G., Marshall, A.M., 2020b. A centrifuge study on the influence of
925 tunnel excavation on piles in sand. *ASCE Journal of the Geotechnical and*
926 *Geoenvironmental Engineering* 146, 04020129.

927 Song, G., Marshall, A.M., Heron, C., 2018. A mechanical displacement con-
928 trol model tunnel for simulating eccentric ground loss in the centrifuge,
929 in: *9th International Conference of Physical Modelling in Geotechnics:*
930 *ICPMG*.

931 Song, G., Xu, J., Heron, C.M., Marshall, A.M., Correia, R., Korposh, S.,
932 2021. The application of FBGs for centrifuge testing: pile axial loads and
933 wall bending moments. *International Journal of Physical Modelling in*
934 *Geotechnics* In press, 1–33. URL: [https://doi.org/10.1680/jphmg.20.](https://doi.org/10.1680/jphmg.20.00078)
935 [00078](https://doi.org/10.1680/jphmg.20.00078), doi:[10.1680/jphmg.20.00078](https://doi.org/10.1680/jphmg.20.00078).

936 Soomro, M.A., Ng, C.W.W., Memon, N., Bhanbhro, R., 2018. Lateral be-
937 haviour of a pile group due to side-by-side twin tunnelling in dry sand:

- 938 3d centrifuge tests and numerical modelling. *Computers and Geotechnics*
939 101, 48–64.
- 940 Stutz, H., Mašín, D., Wuttke, F., 2016. Enhancement of a hypoplastic model
941 for granular soil–structure interface behaviour. *Acta Geotechnica* 11, 1249–
942 1261.
- 943 Wang, H., Leung, C.F., Yu, J., Huang, M., 2020. Axial response of short
944 pile due to tunnelling-induced soil movement in soft clay. *International*
945 *Journal of Physical Modelling in Geotechnics* 20, 71–82. URL: <https://doi.org/10.1680/jphmg.18.00045>, doi:10.1680/jphmg.18.00045.
946
- 947 Williamson, M.G., Mair, R.J., Devriendt, M.D., Elshafie, M.Z.E.B., 2017a.
948 Open-face tunnelling effects on non-displacement piles in clay – part 1 :
949 centrifuge modelling techniques. *Géotechnique* 67, 983–1000. doi:10.1680/
950 [jgeot.SIP17.P.120](https://doi.org/10.1680/jgeot.SIP17.P.120).
- 951 Williamson, M.G., Mair, R.J., Devriendt, M.D., Elshafie, M.Z.E.B., 2017b.
952 Open-face tunnelling effects on non-displacement piles in clay – part 2 :
953 tunnelling beneath loaded piles and analytical modelling. *Géotechnique*
954 67, 1001–1019. doi:10.1680/jgeot.SIP17.P.120.
- 955 von Wolfersdorff, P.A., 1996. A hypoplastic relation for granular materials
956 with a predefined limit state surface. *Mechanics of Cohesive-frictional*
957 *Materials* 1, 251–271.
- 958 Xu, J., Franza, A., Marshall, A.M., 2020. Response of framed buildings on
959 raft foundations to tunneling. *Journal of Geotechnical and Geenviron-*

960 mental Engineering 146, 04020120. doi:[10.1061/\(ASCE\)GT.1943-5606.](https://doi.org/10.1061/(ASCE)GT.1943-5606.0002376)
961 [0002376](https://doi.org/10.1061/(ASCE)GT.1943-5606.0002376).