1	Performance of steam ejector with nonequilibrium condensation for
2	multi-effect distillation with thermal vapour compression (MED-
3	TVC) seawater desalination system
4	Chuang Wen <sup>1</sup> , Hongbing Ding <sup>2</sup> , Yan Yang <sup>1, *</sup>
5	<sup>1</sup> Faculty of Engineering, University of Nottingham, Nottingham NG7 2RD,
6	United Kingdom
7	<sup>2</sup> Tianjin Key Laboratory of Process Measurement and Control, School of Electrical
8	and Information Engineering, Tianjin University, Tianjin 300072, China
9	*Corresponding author: Yan Yang, Email: yan.yang1@nottingham.ac.uk;
10	flyloveyang@gmail.com
11	Abstract: The single-phase and two-phase flow models are developed and compared
12	for the performance evaluation of a steam ejector for the multi-effect distillation with
13	thermal vapour compression (MED-TVC) seawater desalination system. The results
14	show that a single-phase flow model with ignoring the phase change predicts an
15	unphysical temperature of the steam in the supersonic flow with the minimum value of
16	approximately 122 K, which raises the query of the formation of the ice. The two-phase
17	wet steam model corrects the distribution of the flow parameter by predicting the heat
18	and mass transfer during the phase change. The steam achieves the first nonequilibrium
19	condensation process inside the primary nozzle and another four alternating
20	condensation and re-evaporation processes. The single-phase flow model under-
21	predicts the entropy loss coefficient by approximately 15% than the two-phase wet
22	steam model. The performance comparison is achieved against the single-phase model

23	to present the accuracy of the two-phase model for the steam ejector simulation. This
24	demonstrates that the nonequilibrium condensation is essential for the performance
25	analysis of steam ejectors for MED-TVC seawater desalination system.
26	Keywords: multi-effect distillation (MED); thermal vapour compression (TVC); steam

27 ejector; seawater desalination; nonequilibrium condensation; wet steam

28 **1. Introduction** 

The multi-effect distillation with thermal vapour compression (MED-TVC) 29 seawater desalination system provides a solution for freshwater production, which 30 31 achieves energy saving by upgrading the low-grade energy [1, 2]. The steam ejector, as the main part of the TVC unit, recovers the low-pressure steam from the last effect of 32 evaporators, which accomplish high efficient utilisation of the low-grade energy [3, 4]. 33 34 Thermodynamic and economic analysis has shown that the reduction of the exergy destruction in the TVC was cost-effective for the entire seawater desalination system 35 [5]. The MED-TVC seawater desalination system also contributes to environmental 36 37 protection by integrating renewable energy [6-8].

The studies on steam ejectors for MED-TVC seawater desalination system including the novel design [9], thermodynamic analysis [10] and optimisation studies [11]. Ghaebi and Abbaspour [12] integrated heat recovery steam generators to MED-TVC seawater desalination systems. The thermodynamic analysis illustrated that the novel design improved the exergy efficiency by 57.5%. Tang et al. [13] designed a new steam ejector with pressure regulation and the optimisation improved entrainment ratios by 11.77%. Tang et al. [14] also reported that the multi-optimisation of the entrainment

passage can lead to an improvement of the entrainment ratio of 28.75% for the newly 45 designed steam ejector for MED-TVC seawater desalination systems. Gu et al. [15] 46 proposed a steam ejector with a variable geometry by inserting a spindle inside the 47 primary nozzle and averaged entrainment ratios reached 1.39 compared to the normal 48 ejector of 0.69. Xue et al. [16] reported a novel design of two-stage vacuum ejectors 49 and the experimental test demonstrated that the new design provided the vacuum 50 pressure of about 5.3 kPa compared to normal ejectors of 18.6 kPa. Sadeghi et al. [17] 51 proposed a thermodynamic study and optimised power - ejector - desalination systems, 52 53 and their study illustrated that the decrease of the total exergy destruction resulted in high temperatures at the exit of the steam ejector to produce distilled water. 54

Park [18] optimised steam ejectors for the seawater desalination system by 55 56 introducing the swirling flow to the primary nozzle using computational fluid dynamics (CFD) modelling, which could obtain high entrainment ratios by changing the strength 57 of the swirling flow. Sharif [19] carried out the 2D axisymmetric and three-dimensional 58 59 (3D) simulation of a steam ejector and the comparison revealed that the axisymmetric simulation obtained similar results to 3D models considering the overall performance 60 of the steam ejector. Liu et al. [20] computationally investigated the influence of area 61 ratios on steam ejectors for MED-TVC seawater desalination systems and they found 62 63 that the entrainment ratio increased from 0.025 to 0.8. Khalid et al. [21] optimised the location of steam ejectors for MED-TVC seawater desalination systems and best unit 64 performances could be achieved by integrating the steam ejector at the middle effect 65 regardless of the number of effects. Wang et al. [22] performed the optimising study on 66

primary nozzles within steam ejectors for MED-TVC seawater desalination systems
using CFD modelling and they showed that the overall efficiency of the steam ejector
increased by 14.41%.

The aforementioned CFD and thermodynamic analysis improved the 70 understanding of steam ejectors for MED-TVC seawater desalination systems ignoring 71 nonequilibrium condensation processes in steam ejectors. Fortunately, the importance 72 of the condensation phenomenon has been gradually realized in recent studies. Bonanos 73 [23] proposed a physical model of a steam ejector with assumptions of the one-74 75 dimensional and perfect gas model without considering the condensation process, and it was emphasized that the low temperatures due to the acceleration of the fluid may 76 lead to the condensation of the steam, thus invalidating the assumption of perfect gas 77 78 behaviour. Liu et al. [24] performed a thermodynamic analysis of steam ejectors for MED-TVC seawater desalination units, which investigated the impact of condensation 79 behaviours on steam ejectors based on the homogeneous equilibrium theory assuming 80 81 that the phase change occurred instantaneously when the steam reached the saturation state. Their study reported that the condensation is a pervasive phenomenon inside 82 steam ejectors. Tang et al. [25] carried out visualization experiments observing 83 condensation behaviours within steam ejectors for MED-TVC seawater desalination 84 systems. The experimental test demonstrated that massive condensing droplets were 85 observed with nonuniform distributions of the droplet size over the cross-area plane 86 within supersonic flows. These studies illustrate that nonequilibrium condensation 87 processes are significant for performance evaluations of steam ejectors for MED-TVC 88

89 seawater desalination systems.

The present study fills in the scientific gap including the development of the two-90 91 phase wet steam model for nonequilibrium condensation in supersonic flows, the comparison of single-phase flow and two-phase flow models for steam ejectors and the 92 performance evaluation of a steam ejector for MED-TVC seawater desalination 93 systems based on the two-phase flow model. Specifically, the nonequilibrium 94 condensation process is integrated to develop a mathematical model to evaluate 95 performances of steam ejectors for MED-TVC seawater desalination systems. The 96 97 assessments of the single-phase and two-phase flow models are carried out to describe the flow features within steam ejectors. The nonequilibrium condensation processes are 98 discussed inside steam ejectors for MED-TVC seawater desalination systems. 99

#### **2. MED-TVC seawater desalination system**

The MED-TVC seawater desalination system mainly consists of a seawater supply 101 unit, multi-evaporators, a steam ejector and a condenser, as shown in Fig. 1. Seawater 102 103 is fed in condensers with heat exchange between seawater and heating steam in the parallel tubes. During this pre-process in the condenser, a small quantity of the feed 104 seawater is used as cooling water, while the main part is sprayed into each effect of the 105 multi-evaporators, where the seawater is heated to evaporate into water vapour. The 106 produced steam then goes into the next effect of multi-evaporators working as heating 107 fluids inside the parallel horizontal tubes which will condense to distilled water due to 108 109 the heat exchange with the feed seawater. The remaining liquid of the feed seawater is processed as brine to be drained off from the system. These processes are repeated until 110

- the last effect of multi-evaporators, where the main part of produced steam is entrained
- into an ejector as a recycled steam system while the other part goes into the condenser
- 113 as the heating fluid to pre-heat the intake seawater.



Fig. 1 Schematic diagram of a typical MED-TVC seawater desalination system 115 The steam ejector is an important part of MED-TVC seawater desalination 116 systems. The motive primary flow expands in steam ejectors to entrain the low-pressure 117 steam from the last effect of multi-evaporators. The discharge flow of steam ejectors is 118 introduced into the first effect of the multi-evaporators as the heating fluid. This process 119 not only saves steam consumptions for high energy efficiencies but also allows low-120 pressure operating conditions to eliminate the possibility of fouling and scaling. Figure 121 2 illustrates the schematic diagram of steam ejectors, which mainly includes five parts, 122 namely, a primary nozzle, suction chamber, mixing section, constant section and a 123 diffuser [26]. The dimension of the steam ejector employed for numerical simulations 124 is described in detail in Table 1. 125



126

128

127 Fig. 2 Schematic diagram of a steam ejector for MED-TVC seawater desalination

systems
---------

129 Table 1 Dimension of the steam ejector for MED-TVC seawater desalination systems

Steam ejector dimension	Size (mm)
Inlet diameter of the primary nozzle	7.76
Throat diameter of the primary nozzle	1.76
Outlet diameter of the primary nozzle	7.00
Length of the converging part of the primary nozzle	28.70
Length of the diverging part of the primary nozzle	33.35
Inlet diameter of the mixing chamber	48.00
Length of the mixing chamber	130.00
Diameter of the constant section	19.00
Length of the constant section	95.00
Outlet diameter of the diffuser	40.00
Length of the diffuser	180.00

# 130 **3. Mathematical model**

Fundamental equations governing the flow features in a steam ejector are compressible Navier-Stokes equations [27-29]. Considering the complicated flow structure inside steam ejectors, including the supersonic flow, condensing flow, flow separation and shock waves, the shear stress transport (SST) k- $\omega$  turbulence model is employed for performance evaluations of steam ejectors for MED-TVC seawater desalination systems.

137 
$$\frac{\partial \rho}{\partial t} + \frac{\partial (\rho u_j)}{\partial x_j} = -\Gamma$$
(1)

138 
$$\frac{\partial}{\partial t}(\rho u_i) + \frac{\partial}{\partial x_j}(\rho u_j u_i) = -\frac{\partial p}{\partial x_i} + \frac{\partial \tau_{ij}}{\partial x_j} - u_i \Gamma$$
(2)

139 
$$\frac{\partial}{\partial t}(\rho H) + \frac{\partial}{\partial x_{j}}(\rho u_{j}H + p) = -\frac{\partial}{\partial x_{j}}(\lambda_{eff}\frac{\partial T}{\partial x_{j}}) + \frac{\partial}{\partial x_{j}}(u_{i}\tau_{ij}) - h_{lv}\Gamma$$
(3)

140 
$$\frac{\partial}{\partial t}(\rho k) + \frac{\partial}{\partial x_i}(\rho k u_i) = \frac{\partial}{\partial x_j} \left( \Gamma_k \frac{\partial k}{\partial x_j} \right) + \overline{G}_k - Y_k + S_k$$
(4)

141 
$$\frac{\partial}{\partial t}(\rho\omega)\frac{\partial}{\partial x_{j}}(\rho\omega u_{j}) = \frac{\partial}{\partial x_{j}}\left(\Gamma_{\omega}\frac{\partial\omega}{\partial x_{j}}\right) + C_{\omega} - Y_{\omega} + D_{\omega} + S_{\omega}$$
(5)

142 Nonequilibrium condensation processes in steam ejectors are governed by two
 143 transport equations[30, 31];

# transport equations[30, 31]:

144 
$$\frac{\partial(\rho Y)}{\partial t} + \frac{\partial}{\partial x_j} \left(\rho Y u_j\right) = \Gamma$$
(6)

145 
$$\frac{\partial(\rho N)}{\partial t} + \frac{\partial}{\partial x_j} (\rho N u_j) = \rho J$$
(7)

<sup>146</sup> where  $\Gamma$  illustrates the condensation rate of the steam:

147 
$$\Gamma = \frac{4\pi r_c^3}{3} \rho_l J + 4\pi r^2 \rho_l N \frac{dr}{dt}$$
(8)

148 
$$J = \frac{q_c}{1+\phi} \frac{\rho_v^2}{\rho_l} \sqrt{\frac{2\sigma}{\pi m_v^3}} \exp\left(-\frac{4\pi\sigma}{3k_B T_v} r_c^2\right)$$
(9)

149 
$$\frac{dr}{dt} = \frac{\lambda_{\nu} \left(T_{s} - T_{\nu}\right)}{\rho_{l} h_{l\nu} r} \frac{\left(1 - r_{c}/r\right)}{\left(\frac{1}{1 + 2\beta \text{Kn}} + 3.78(1 - \nu)\frac{\text{Kn}}{\text{Pr}}\right)}$$
(10)

### 150 where *J* is the nucleation rate, and dr/dt is the droplet growth rate.

ANSYS FLUENT 19 [32] is utilized as a basic computational platform for conservation equations of Eqs. (1)-(5). The additional transport equations of Eqs. (6) -(7) and source terms of Eqs. (8) - (10) are integrated to ANSYS FLUENT by userdefined-scalar and user-defined-function interfaces [33]. The total pressure and total temperature boundary conditions are employed for the entrances and exit of the steamejector [34].

#### 157 4. Results and discussion

#### 158 4.1. CFD validation of nonequilibrium condensations in supersonic flows

The numerical validation of nonequilibrium condensations in supersonic flows is 159 carried out based on the case 252 of the Laval nozzle designed by Moses and Stein [35, 160 36], who performed the experimental measurement on the pressure distribution and the 161 droplet size of the wet steam flow. The supersonic flow condition is assigned to the exit 162 163 of the Laval nozzle. The computed pressure and droplet radius are compared against experimental data, as shown in Fig. 3. It can be observed that numerical results agree 164 well with experimental data. Specifically, the developed CFD modelling predicts the 165 166 onset of nonequilibrium condensations while calculates similar droplet radius compared to the values of experimental measurements. This demonstrates that the 167 developed CFD modelling accurately evaluates nonequilibrium condensations in 168 169 supersonic flows.





Fig. 3 CFD validation of nonequilibrium condensations in the supersonic flow

#### 172 **4.2. CFD validation of steam ejectors**

Based on the successful validation of nonequilibrium condensations in the Moses and 173 Stein's Laval nozzle [35, 36], the developed mathematical model is further validated 174 for the steam ejector using experiment data reported by Sriveerakul et al. [37]. The 175 operating conditions include the temperature of the primary flow, Tp=130 °C, the 176 temperature of the suction flow,  $T_S = 5$  °C, and the back pressure of discharge flow,  $P_b$ 177 = 3000 Pa. The numerical and experimental results are described in Fig. 4. The 178 computed pressure agrees well with experimental data in the diffuser while the 179 180 numerical results are larger than experimental values in the constant section, which is attributed to the difficulty of calibrating the absolute pressure transducer near absolute 181 zero levels [37, 38]. Thus, it is concluded that the developed nonequilibrium 182 183 condensation model can be accurately used to evaluate a steam ejector for the MED-TVC seawater desalination system. 184



185

186 Fig. 4 CFD validation of a steam ejector for the MED-TVC seawater desalination

system

#### 188 **4.3. Effect of single-phase and two-phase flow models**

This section focuses on flow behaviours in a primary nozzle of steam ejectors for 189 MED-TVC seawater desalination systems, which provides an opportunity to show local 190 details on formations and developments of nonequilibrium condensation processes in 191 supersonic flows. The quadrilateral mesh is generated for the primary nozzle, as shown 192 in Fig. 5. Three different grids are employed for analysis of mesh independence on 193 computational results with 16000, 42000 and 88000 cells, respectively. The flow 194 structure is employed to show the impact of grid densities on the supersonic flow. The 195 196 Mach numbers and nucleation rates in the primary nozzle are illustrated in Figs. 6 - 7. As shown in the contours & profiles of Mach numbers, the difference is observed inside 197 the divergent part where the Mach number decreases because of heat and mass transfer 198 199 of phase change processes within supersonic flows. Likewise, when looking into the detailed distribution of contours and profiles of nucleation rates, the coarse mesh 200 calculates condensation parameters slightly different from the other two meshes. The 201 coarse mesh predicts the peak nucleation rate of  $4.52 \times 10^{25}$  m<sup>-3</sup> s<sup>-1</sup>, while medium and 202 fine meshes calculate the maximum value of  $1.53 \times 10^{26}$  m<sup>-3</sup> s<sup>-1</sup> and  $1.94 \times 10^{26}$  m<sup>-3</sup> s<sup>-1</sup>, 203 respectively. Thus, the medium mesh of 42000 quadrilateral cells is utilized to carry 204 out the computations of nonequilibrium condensations within the primary nozzle based 205 on computational accuracies and costs. 206





Fig. 5 Computational grid of the primary nozzle inside a steam ejector for the MED-



TVC seawater desalination system





Fig. 6 Effect of grid density on the Mach number in the primary nozzle of a steam

212

ejector



213

Fig. 7 Effect of grid density on the nucleation rate in the primary nozzle of a steam

215

#### ejector

Steam flow reaches supersonic flows in the primary nozzle, where the rapid 216 expansion correspondingly induces a sharp decrease of the static pressures and 217 218 temperatures. The steam flow goes over the saturated-vapour line and reaches the supersaturated state inside diverging parts of primary nozzles. The extreme 219 nonequilibrium state will lead to the occurrence of steam condensation, which is 220 expected to influence the flow behaviour in supersonic flows. After the grid 221 independence test, the single-phase and two-phase flow models are developed for 222 analysing nonequilibrium condensing processes inside supersonic flows within primary 223 nozzles. 224

Figures 8-10 illustrate the flow of the steam in the primary nozzle with and without considering nonequilibrium condensations, including static pressures, static temperatures and Mach numbers. It is observed that the single-phase flow represents dry steam behaviour without considering the phase change. Under the assumption of

dry gas flow, the steam pressure and temperature continuously decrease within primary 229 nozzles. For the two-phase steam flow involving the condensation process, the steam 230 231 expands further to go across the saturated-vapour line, which is far from the equilibrium state to induce condensation nuclei. The latent heat release during phase changes heats 232 the vapour phase and correspondingly results in a jump of the static pressure and static 233 temperature. This means that the steam condensation weakens the expansion 234 characteristics of supersonic flows within primary nozzles. For example, the Mach 235 numbers at the nozzle exit predicted by single- and two-phase flow models reach 3.92 236 237 and 2.84, respectively. The single-phase flow model overpredicts Mach numbers by 38% compared to the two-phase flow model. 238

Even worse, the single-phase flow model predicts an unphysical decline of the 239 static temperature of the steam in the supersonic flow. In this primary nozzle, the single-240 phase flow model predicts a static temperature of about 122 K at the nozzle exit, which 241 may raise the query of the formation of the ice in such a low temperature. The pressure-242 243 temperature profiles of the water are shown in Fig. 11. It depicts that the pressuretemperature profile calculated by the single-phase flow model crosses the melting line 244 and goes further to the solid region to generate the ice in such conditions. On the 245 contrary, the pressure-temperature crosses the saturation line and stays in the liquid 246 region due to the contribution of the phase change in supersonic flows. This 247 demonstrates that nonequilibrium condensation processes play a significant role in 248 249 performance evaluations of steam ejectors for MED-TVC seawater desalination systems. 250



251

Fig. 8 Impact of condensing flow on static pressures within primary nozzles of steam ejectors: contours of single- (a) and two-phase (b) flow models, and profiles at the central axis of single- and two-phase flow models (c)



256

Fig. 9 Impact of condensing flow on Mach numbers within primary nozzles of steam ejectors: contours of single- (a) and two-phase (b) flow models, and profiles at the central axis of single- and two-phase flow models (c)





Fig. 10 Impact of condensing flow on static temperatures within primary nozzles of steam ejectors: contours of single- (a) and two-phase (b) flow models, and profiles at the central axis of single- and two-phase flow models (c)





266

Fig. 11 Steam pressure-temperature profiles



The quadrilateral structured mesh is generated for steam ejectors for MED-TVC 269 270 seawater desalination systems, as shown in Fig. 12. The impact of gird densities on computational results of steam ejectors is carried out based on three quadrilateral 271 structured meshes including 39000, 73000 and 168000 cells, respectively. Table 2 272 describes the boundary conditions of steam ejectors for MED-TVC seawater 273 desalination systems. The high-pressure steam from the inlet of the primary nozzle is 274 assigned to 270 kPa and 463.15 k, which will expand in the steam ejector to entrain the 275 low-pressure steam from the suction chamber. The low-pressure steam from the last 276 277 effect of the MED unit will be recirculated to the suction chamber of the steam ejector to improve the low-grade heat stream with the total pressure of 1.6 kPa and total 278

279	temperature of 287.20 K. The steam with the total pressure and total temperature of
280	3.0kPa and 297.25 K is discharged from the exit of the ejector to the first effect of the
281	MED unit. Fig. 13 represents the impact of mesh independence on flow behaviours in
282	steam ejectors including static pressures, nucleation rates and entrainment ratios. It can
283	be seen that the results based on the coarse mesh are a little bit far from the ones from
284	medium and fine grids. Specifically, the coarse mesh predicts the maximum nucleation
285	rate of about 4.53 $\times$ 10^{22} m^{-3} s^{-1}, while the medium and fine meshes compute the
286	maximum value of $4.47\times10^{26}$ m^-3 s^-1 and $4.78\times10^{26}$ m^-3 s^-1, respectively. Consequently,
287	the medium mesh is used to evaluate the performances of steam ejectors for MED-TVC
288	seawater desalination systems.

Table 2 Boundary condition of steam ejectors for MED-TVC seawater desalination

290	90 systems				
	Boundary conditions	Inlet of primary nozzle	Inlet of suction chamber	Exit of steam ejector	
	Total pressure	270 kPa	1.6 kPa	3.0 kPa	
	Total temperature	463.15 K	287.20 K	297.25 K	







Fig. 13 Impact of the grid density on the steam ejector for the MED-TVC seawater

desalination system

299	Figure 14 illustrates flow structures in steam ejectors for MED-TVC seawater
300	desalination systems including Mach numbers, degrees of subcooling and nucleation
301	rates, respectively. The steam achieves supersonic flows inside the divergent section of
302	primary nozzles, which reaches extremely nonequilibrium state downstream the nozzle
303	throat with a maximum degree of subcooling of about 43 K. This induces the first
304	nucleation and condensation process of the steam with a peak nucleation rate of 4.47 $\times$
305	$10^{26}$ m <sup>-3</sup> s <sup>-1</sup> . The steam still maintains the supersonic flow downstream the condensation
306	region, where the degree of subcooling stays at approximately 12 K till the exit plane
307	of the primary nozzle.

The steam undergoes a further expansion-compression process to develop the 308 under-expanded supersonic flow inside mixing and constant sections, which induces 309 310 the intense change of the degree of subcooling. It can be observed that there are four expansion-compression processes of the steam in mixing and constant sections. The 311 degree of subcooling increases to a peak value of about 38 K and then decreases sharply 312 to the minimum value of -49 K during the first expansion-compression process, which 313 leads to a condensation and re-evaporation process of the steam. Specifically, this 314 further nucleation and condensation process contributes to the maximum liquid fraction 315 of 0.19, which then declines to the trough level of 0.12 due to the re-evaporation process. 316 This alternating condensation and re-evaporation processes occur during the four 317 expansion-compression processes of the steam in mixing and constant sections of steam 318 ejectors for MED-TVC seawater desalination systems. 319

320 By combining nonequilibrium condensations in the primary nozzle and four

condensation and re-evaporation processes in mixing and constant sections of steam 321 ejectors, it is observed that the peak values of degree of subcooling are gradually 322 decreasing, while their trough levels are increasing. For instance, the first to fifth peak 323 values of the degree of subcooling are 43 K, 38 K, 26K, 21 K, 19K, and the first to 324 fourth trough levels are -49 K, -8 K, -6 K, -1 K, respectively. This correspondingly 325 decreases the peak value of the nucleation rate of  $4.47 \times 10^{26}$  m<sup>-3</sup> s<sup>-1</sup>,  $1.22 \times 10^{21}$  m<sup>-3</sup> s<sup>-1</sup> 326  $^1,~3.85\times10^{16}~m^{-3}~s^{-1},~4.26\times10^{10}~m^{-3}~s^{-1}$  and  $1.23\times10^9~m^{-3}~s^{-1}$  for the first to fifth 327 condensation processes, which finally changes the first to the fourth peak value of the 328 liquid fraction of 0.19, 0.16, 0.143, 0.141, respectively. The degree of subcooling of the 329 steam remains above zero downstream the fourth expansion-compression flow in the 330 constant section of steam ejectors, which makes the liquid fraction stay at around 0.14 331 332 in this region.



Fig. 14 Flow structures in the steam ejector for the MED-TVC seawater desalination
system: contours of Mach numbers (a), contours of degrees of subcooling (b),

contours of nucleation rates (c), contours of liquid fractions (d), and profiles of Mach 336 numbers, degrees of subcooling, nucleation rates and liquid fractions at central lines 337 (e) 338 The flow structures represent the typical gas-liquid two-phase flows inside the 339 divergent part of primary nozzles, mixing and constant sections of steam ejectors for 340 MED-TVC seawater desalination systems, which are expected to affect energy losses 341 within steam ejectors. The entropy loss coefficient is employed here to evaluate the loss 342 of steam ejectors for MED-TVC seawater desalination systems. The entropy loss 343 coefficient is a function of the enthalpy, entropy and temperature, which is defined as 344 [39]: 345

346 
$$\eta = \frac{h_{in} - h_{out}}{h_{in} - h_{out} + T_{v,out}(s_{out} - s_{in})}$$
(11)

where  $\eta$  is the entropy loss coefficient,  $h_{in}$  and  $h_{out}$  are the enthalpies at ejector inlet and outlet,  $s_{in}$  and  $s_{out}$  are the entropy at ejector inlet and outlet,  $T_{v,out}$  is the steam temperature at an ejector outlet.

Table 3 describes the thermodynamic parameters and entropy loss coefficient of 350 steam ejectors for MED-TVC seawater desalination systems based on single- and two-351 phase flow models, including the enthalpy, entropy and temperature of the steam at the 352 inlet and out of steam ejectors. It can be found that the single-phase flow model ignoring 353 phase change processes computes larger enthalpy, entropy and temperature than the 354 two-phase flow model at ejector outlets. Subsequently, the single-phase flow model 355 calculates the entropy loss coefficient of 0.084 while the wet steam model predicts a 356 higher value of 0.097. That is, the dry gas model under-predicts the entropy loss 357

358	coefficient by approximately 15% compared to the two-phase flow model. It
359	demonstrates that nonequilibrium condensations play a vital role in performance
360	analyses of steam ejectors for MED-TVC seawater desalination systems.
361	
362	Table 3 Entropy loss coefficient and thermodynamic parameters of steam ejectors for

363 MED-TVC seawater desalination systems based on single- and two-phase flow

2	C A	
-	<b>h</b> /I	
_	$\mathbf{v}$	

	models						
	$h_{in}$	Sin	hout	Sout	$T_{v,out}$	η	Error
	(J/kg)	(J/(kg.K))	(J/kg)	(J/(kg.K))	(K)	(-)	(%)
Dry gas	751761.15	147.59	686752.18	2056.06	368.96	0.084	15%
Wet steam	751761.65	147.59	677778.21	2031.61	364.23	0.097	-

365

## **5.** Conclusions

Performance analyses of a steam ejector are carried out for MED-TVC seawater 367 desalination systems considering nonequilibrium condensation behaviours. The single-368 phase flow model with ignoring phase change processes predicts an unphysical 369 temperature of the steam in the supersonic flow with the minimum value of 370 approximately 122 K in the primary nozzle. The two-phase flow model predicts that 371 372 the steam expands further and departs from equilibrium states to induce the occurrence of the nonequilibrium condensation in supersonic flows. The flow structures in steam 373 ejectors for MED-TVC systems illustrates that the steam reaches extremely 374 375 nonequilibrium states in the steam ejector to induce the nucleation and condensation processes in the primary nozzle, mixing and constant sections. The liquid fraction stays 376 at around 0.14 in the constant section of the steam ejector due to the nonequilibrium 377

condensation. The single-phase flow model under-predicts the entropy loss coefficient
by approximately 15% compared to a two-phase flow model. This demonstrates that
nonequilibrium condensations play a crucial role in performance analyses of steam
ejectors for MED-TVC seawater desalination systems

382 Acknowledgements

This project has received funding from the European Union's Horizon 2020 research and innovation programme under the Marie Sklodowska-Curie grant agreement No 792876 and the National Natural Science Foundation of China under Grant 51876143.

#### 387 **References**

[1] Y. Tang, Z. Liu, Y. Li, C. Shi, Combined auxiliary entrainment and structure
 optimization for performance improvement of steam ejector with consideration of

back pressure variation, Energy Conversion and Management, 166 (2018) 163-173.

391 [2] L. Guimard, A. Cipollina, B. Ortega-Delgado, G. Micale, F. Couenne, P. Bandelier,

- C. Jallut, New considerations for modelling a MED-TVC plant under dynamic
  conditions, Desalination, 452 (2019) 94-113.
- [3] Y. Tang, Z. Liu, C. Shi, Y. Li, A novel steam ejector with pressure regulation to
  dredge the blocked entrained flow for performance improvement in MED-TVC
  desalination system, Energy Conversion and Management, 172 (2018) 237-247.
- [4] D. Strušnik, M. Marčič, M. Golob, A. Hribernik, M. Živić, J. Avsec, Energy
  efficiency analysis of steam ejector and electric vacuum pump for a turbine
  condenser air extraction system based on supervised machine learning modelling,

- 400 Applied Energy, 173 (2016) 386-405.
- 401 [5] M.L. Elsayed, O. Mesalhy, R.H. Mohammed, L.C. Chow, Exergy and thermo402 economic analysis for MED-TVC desalination systems, Desalination, 447 (2018)
  403 29-42.
- 404 [6] A. Razmi, M. Soltani, M. Tayefeh, M. Torabi, M. Dusseault, Thermodynamic
  405 analysis of compressed air energy storage (CAES) hybridized with a multi-effect
  406 desalination (MED) system, Energy Conversion and Management, 199 (2019)
  407 112047.
- 408 [7] B. Ghorbani, M. Miansari, S. Zendehboudi, M.-H. Hamedi, Exergetic and economic
  409 evaluation of carbon dioxide liquefaction process in a hybridized system of water
  410 desalination, power generation, and liquefied natural gas regasification, Energy
  411 Conversion and Management, 205 (2020) 112374.
- [8] K. Mohammadi, M. Saghafifar, K. Ellingwood, K. Powell, Hybrid concentrated
  solar power (CSP)-desalination systems: A review, Desalination, 468 (2019)
  114083.
- [9] Y. Tang, Z. Liu, Y. Li, C. Shi, H. Wu, Performance improvement of steam ejectors
  under designed parameters with auxiliary entrainment and structure optimization
  for high energy efficiency, Energy Conversion and Management, 153 (2017) 1221.
- [10] I.B. Askari, M. Ameri, Techno economic feasibility analysis of Linear Fresnel solar
  field as thermal source of the MED/TVC desalination system, Desalination, 394
  (2016) 1-17.

- [11] C. Wang, L. Wang, X. Wang, H. Zhao, Design and numerical investigation of an
  adaptive nozzle exit position ejector in multi-effect distillation desalination system,
  Energy, 140 (2017) 673-681.
- 425 [12] H. Ghaebi, G. Abbaspour, Thermoeconomic analysis of an integrated multi-effect
- 426 desalination thermal vapor compression (MED-TVC) system with a trigeneration
- 427 system using triple-pressure HRSG, Heat and Mass Transfer, 54 (2018) 1337-1357.
- 428 [13] Y. Tang, Z. Liu, C. Shi, Y. Li, A novel steam ejector with pressure regulation to
- 429 optimize the entrained flow passage for performance improvement in MED-TVC
- 430 desalination system, Energy, 158 (2018) 305-316.
- 431 [14] Y. Tang, Z. Liu, Y. Li, C. Shi, C. Lv, A combined pressure regulation technology
- with multi-optimization of the entrainment passage for performance improvement
  of the steam ejector in MED-TVC desalination system, Energy, 175 (2019) 46-57.
- 434 [15] W. Gu, X. Wang, L. Wang, X. Yin, H. Liu, Performance investigation of an auto-
- 435 tuning area ratio ejector for MED-TVC desalination system, Applied Thermal
  436 Engineering, 155 (2019) 470-479.
- [16] H. Xue, L. Wang, L. Jia, C. Xie, Q. Lv, Design and investigation of a two-stage
  vacuum ejector for MED-TVC system, Applied Thermal Engineering, 167 (2020)
  114713.
- [17] M. Sadeghi, M. Yari, S.M.S. Mahmoudi, M. Jafari, Thermodynamic analysis and
  optimization of a novel combined power and ejector refrigeration cycle –
  Desalination system, Applied Energy, 208 (2017) 239-251.
- 443 [18] I.S. Park, Numerical investigation of entraining performance and operational

- robustness of thermal vapor compressor having swirled motive steam inflow,
  Desalination, 257 (2010) 206-211.
- [19] N. Sharifi, Axisymmetric and three dimensional flow modeling within thermal
  vapor compressors, Heat and Mass Transfer, 49 (2013) 1489-1501.
- 448 [20] J. Liu, L. Wang, L. Jia, X. Wang, The influence of the area ratio on ejector
- efficiencies in the MED-TVC desalination system, Desalination, 413 (2017) 168175.
- 451 [21] K.A. Khalid, M.A. Antar, A. Khalifa, O.A. Hamed, Allocation of thermal vapor
- 452 compressor in multi effect desalination systems with different feed configurations,
- 453 Desalination, 426 (2018) 164-173.
- [22] K. Wang, L. Wang, L. Jia, W. Cai, R. Gao, Optimization design of steam ejector
  primary nozzle for MED-TVC desalination system, Desalination, 471 (2019)
  114070.
- 457 [23] A.M. Bonanos, Physical modeling of thermo-compressor for desalination
  458 applications, Desalination, 412 (2017) 13-19.
- [24] J. Liu, L. Wang, L. Jia, H. Xue, Thermodynamic analysis of the steam ejector for
  desalination applications, Applied Thermal Engineering, 159 (2019) 113883.
- 461 [25] Y. Tang, Z. Liu, Y. Li, H. Wu, X. Zhang, N. Yang, Visualization experimental study
- of the condensing flow regime in the transonic mixing process of desalinationoriented steam ejector, Energy Conversion and Management, 197 (2019) 111849.
- 464 [26] C. Wen, B. Rogie, M.R. Kærn, E. Rothuizen, A first study of the potential of
  465 integrating an ejector in hydrogen fuelling stations for fuelling high pressure

- 466 hydrogen vehicles, Applied Energy, 260 (2020) 113958.
- 467 [27] C. Wen, N. Karvounis, J.H. Walther, H. Ding, Y. Yang, Non-equilibrium
- 468 condensation of water vapour in supersonic flows with shock waves, International
- 469 Journal of Heat and Mass Transfer, 149 (2020) 119109.
- 470 [28] H. Ding, Y. Li, E. Lakzian, C. Wen, C. Wang, Entropy generation and exergy
- destruction in condensing steam flow through turbine blade with surface roughness,
- Energy Conversion and Management, 196 (2019) 1089-1104.
- 473 [29] C. Wen, N. Karvounis, J.H. Walther, Y. Yan, Y. Feng, Y. Yang, An efficient
- 474 approach to separate CO2 using supersonic flows for carbon capture and storage,
- 475 Applied energy, 238 (2019) 311-319.
- [30] A. Kantrowitz, Nucleation in very rapid vapor expansions, The Journal of chemical
  physics, 19 (1951) 1097-1100.
- 478 [31] J. Young, The spontaneous condensation of steam in supersonic nozzle, Physico
- 479 Chemical Hydrodynamics, 3 (1982) 57-82.
- 480 [32] ANSYS Fluent Theory Guide, ANSYS Inc., USA, (2017).
- [33] Y. Yang, J.H. Walther, Y. Yan, C. Wen, CFD modeling of condensation process of
  water vapor in supersonic flows, Applied Thermal Engineering, 115 (2017) 13571362.
- [34] Y. Yang, X. Zhu, Y. Yan, H. Ding, C. Wen, Performance of supersonic steam
  ejectors considering the nonequilibrium condensation phenomenon for efficient
  energy utilisation, Applied Energy, 242 (2019) 157-167.
- 487 [35] C.A. Moses, G.D. Stein, On the growth of steam droplets formed in a Laval nozzle

- using both static pressure and light scattering measurements, Journal of Fluids
  Engineering, 100 (1978) 311-322.
- 490 [36] J. Starzmann, F.R. Hughes, S. Schuster, A.J. White, J. Halama, V. Hric, M.
- 491 Kolovratník, H. Lee, L. Sova, M. Št'astný, M. Grübel, M. Schatz, D.M. Vogt, Y.
- 492 Patel, G. Patel, T. Turunen-Saaresti, V. Gribin, V. Tishchenko, I. Gavrilov, C. Kim,
- 493 J. Baek, X. Wu, J. Yang, S. Dykas, W. Wróblewski, S. Yamamoto, Z. Feng, L. Li,
- 494 Results of the International Wet Steam Modeling Project, Proceedings of the
- 495 Institution of Mechanical Engineers, Part A: Journal of Power and Energy, 232
- 496 (2018) 550-570.
- [37] T. Sriveerakul, S. Aphornratana, K. Chunnanond, Performance prediction of steam
  ejector using computational fluid dynamics: Part 1. Validation of the CFD results,
  International Journal of Thermal Sciences, 46 (2007) 812-822.
- 500 [38] T. Sriveerakul, S. Aphornratana, K. Chunnanond, Performance prediction of steam
- ejector using computational fluid dynamics: Part 2. Flow structure of a steam
  ejector influenced by operating pressures and geometries, International Journal of
  Thermal Sciences, 46 (2007) 823-833.
- [39] S. Dykas, M. Majkut, K. Smołka, M. Strozik, Study of the wet steam flow in the
  blade tip rotor linear blade cascade, International Journal of Heat and Mass
  Transfer, 120 (2018) 9-17.