Improving power quality efficient in demand response: aggregated heating, ventilation and
 air-conditioning systems

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47 Improving power quality efficient in demand response: aggregated heating, ventilation and

- 48 air-conditioning systems

51 ABSTRACT

This study aims to identify the role of aggregated heating, ventilation, and air conditioning (HVAC) loads based on system characteristics using the lazy state switching control mode focusing on the overall power consumption rather individual response speed. This study is attempted to provide secondary frequency regulation using aggregated HVAC loads with more stable operation with the lazy state switching control mode based on conditional switching of the HVAC unit's working state. The stability of power consumption improves power quality in smart grid design and operation. The aggregated HVAC must reach a stable condition before tracking the automatic generation control signal and fully developed smart grids complex structure. Still, HVAC slowed responses make inappropriate for faster demand response services. Unsuitable control algorithm leads to system instability and HVAC unit overuse. An extended command processing on the client side is proposed to deal with the adjusting command. The unique advantages of the proposed algorithm are three folds. (1) the control algorithm preserves its working state and has nothing conflicting with the lockout constraints for individual system units; (2) the control algorithm shows promising performance in smoothing the overall power consumption for the aggregated population; and (3) the control logic is fully compatible with other control algorithms. The proposed modeling and control strategy are validated against simulations of thousands of units, and the simulation result indicates that the proposed approach has promising performance in smoothing the power consumption of aggregate units' population.

72 Keywords: Renewable energy; Smart Grid; Demand response; Power quality; Heating,
 73 ventilation and air conditioning (HVAC); Lazy state switching.

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Abbreviations \mathcal{E}_{l} an infinitesimal time delayAGCautomatic generation control f_{i}^{*} the probability for an HVAC unit to resi- a certain temperature segmentDRdemand responsea certain temperature segmentETPequivalent thermal parameter $\Delta m_{i}^{ont/off}$ the number of HVAC units in state i given momentHVACHeating, ventilation, and air conditioning LSSlazy state switching $\Delta m_{i}^{ont/off}$ the number of HVAC units in state i given momentTCLthermostatically controlled loadsPpower consumption (W) of single HVACPEVplug-in electric vehiclesPpower consumption (W) of single HVACIndicesiindex of state-space η power system's transmission efficiency I index of time ΔP instantaneous power increase $U_{c}(\mu_{e}, \delta_{e})$ represents a uniform distributionVariables and parameters χ_{a} inner air temperature (*F) of HVAC unit Δm χ_{m} inner air temperature (*F) of HVAC unit δ_{m} parameters deadband vector χ_{a} thermal conductance (Btu/hr.*F) of the building envelopeUc(**)Uniform distribution between values M_{m} thermal iconductance (Btu/hr.*F) of the inner air and inner solid mass μ_{ka} center value of floor area (ft ²) Q_{a} the heat flux (Btu/hr) into the inner air mass μ_{kk} center value of floor R-value (*F.ft ² .hr/Bt Q_{a} the heat flux (Btu/hr) to the inner air μ_{kk} center value of door R-value (*F.ft ² .hr/Bt <th colspan="2">Nomenclature</th> <th>S</th> <th>the working state of an HVAC unit</th>	Nomenclature		S	the working state of an HVAC unit
AGCautomatic generation control f_i^* the probability for an HVAC unit to residenceAGCautomatic generation control f_i^* the probability for an HVAC unit to residenceDRdemand responsea certain temperature segmentETPequivalent thermal parameter $\Delta m_i^{ont/off}$ the number of HVAC units in state iHVACHeating, ventilation, and air conditioningis in state i given momentLSlazy state switchingthe total number of HVAC units inTCLthermostatically controlled loads PV PEVplug-in electric vehicles p power consumption (W) of single HVACIndicesiindex of state-space η power consumption (W) of single HVAC i index of state-space η power system's transmission efficiency X_m inner mass temperature ("F) of HVAC unit ΔP x_m inner air temperature ("F) of HVAC unit Δp T_o outside air temperature ("F) of HVAC unit Δm U_a thermal conductance (Btu/hr.*F) of the building envelope U_{a} H_m thermal conductance (Btu/hr.*F) of the building envelope U_{a} H_m thermal mass (Btu/*F) of the inner air mass μ_{ac} Q_m heat flux (Btu/hr) into the inner air mass μ_{ac} Q_m heat flux (Btu/hr) to the inner solid mass μ_{ac} Q_m heat flux (Btu/hr) to the inner air mass μ_{ac} Q_m heat flux (Btu/hr) to the inner air mass μ_{ac} Q_m heat flux (Btu/hr) for the bui	A = =		\mathcal{E}_t	an infinitesimal time delay
Actautomatic generation control J'_{I} DRdemain responseETPequivalent thermal parameterHEMShome energy management systemHVACHeating, ventilation, and air conditioningLSSlazy state switchingTCLthermostatically controlled loadsPEVplug-in electric vehiclesiindex of state-spaceiindex of state-spacetindex of timeVariables and parameters x_a inner air temperature (*F) of HVAC unit x_a inner mass temperature (*F) of HVAC unit T_o outside air temperature (*F) of HVAC unit y_a thermal conductance (Btu/hr.*F) of the building envelope H_m thermal conductance (Btu/hr.*F) of the building envelope H_m thermal mass (Btu/*F) of the inner air and inner solid mass Q_m heat flux (Btu/hr) to the inner solid mass Q_m heat flux (Btu/hr) to the inner solid mass Q_m thermal mass (Btu/*F) of the building materials and furniture Q_{scr} thermal mass (Btu/*F) of the building materials and furniture Q_{scr} thermal mass (Btu/*F) of the building materials and furniture Q_{scr} thermal mass (Btu/*F) of the building materials and furniture Q_{scr} thermal mass (Btu/*F) of the building materials and furniture Q_{scr} thermal mass (Btu/*F) of the building materials and furniture Q_m thermal mass (Btu/*F) of the building materials and furniture Q_m thermal mass (Btu/*F	Abbreviations		f_{i}^{*}	the probability for an HVAC unit to reside in
$\begin{array}{cccccccccccccccccccccccccccccccccccc$		demand response	JI	a certain temperature segment
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	FTP	equivalent thermal parameter	⊾ on/o	
HVACHeating, ventilation, and air conditioning ISSgiven momentLSSlazy state switchingnthe total number of HVAC units in simulation testsPEVplug-in electric vehiclespower consumption (W) of single HVACPIVACindex of state-space η indicesiindex of state-spaceiindex of time ΔP Variables and parameters ΔP x_a inner air temperature (°F) of HVAC unit x_m inner mass temperature (°F) of HVAC unit T_o outside air temperature (°F) U_a thermal conductance (Btu/hr.°F) of the building envelope H_m thermal conductance (Btu/hr.°F) between the inner air and inner solid mass Q_m heat flux (Btu/hr) into the inner air mass Q_m H_m thermal mass (Btu/°F) of the building materials and furniture Q_{set} HVAC unit's temperature (°F) deadband A_f Q_{set} HVAC unit's temperature (°F) deadband A_{ramin} Q_{set} HVAC unit's temperature (°F) deadband A_{ramin} Q_{set} HVAC unit's temperature (°F) for a population A_{ramin} Q_{set} HVAC unit's temperature (°F) for a population A_{ramin}	HEMS	home energy management system	Δm_i	the number of HVAC units in state i at a
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$\begin{array}{cccc} PEV & plug-in electric vehicles & P & pluwer consumption(w) of single fivAc \\ P_{HVAC} & total power consumption(w) of single fivAc \\ P_{HVAC} & total power consumption(w) of single fivAc \\ aggregated loads & aggregated loads \\ f & power system's transmission efficiency \\ L & index of time & D^{P} & instantaneous power increase \\ U_{c}(\mu_{s},\delta_{s}) represents a & uniform & distribut \\ variables and parameters \\ x_{a} & inner air temperature(^{e}F) of HVAC unit \\ x_{m} & inner air temperature(^{e}F) of HVAC unit \\ T_{o} & outside air temperature(^{e}F) of HVAC unit \\ T_{a} & thermal conductance (Btu/hr.^{e}F) of the \\ building envelope \\ H_{m} & thermal conductance (Btu/hr.^{e}F) between \\ th einner air and inner solid mass \\ Q_{m} & heat flux (Btu/hr) int the inner air mass \\ Btu^{e}F) of the internal air \\ Q_{m} & heat flux (Btu/hr) to the inner solid mass \\ Q_{m} & heat flux (Btu/hr) to the inner solid mass \\ C_{a} & thermal mass (Btu^{e}F) of the building \\ materials and furiture \\ U_{set} & HVAC temperature (^{e}F) setpoint \\ \delta_{Af} & center value of floor area distribution \\ deadband of air exchange distribution \\ deadband of air exchange distribution \\ deadband of oir R-value (distribution \\ deadband of oor R-value distribution \\ deadban$	TCL	thermostatically controlled loads	D	simulation tests
Indicesaggregated loadsiindex of state-space η iindex of time ΔP index of time ΔP variables and parameterscentered by μ_s , and spans the distance x_a inner air temperature (°F) of HVAC unit x_m inner mass temperature (°F) U_a thermal conductance (Btu/hr.°F) of thebuilding envelopebuilding envelope H_m thermal conductance (Btu/hr.°F) betweenthe inner air and inner solid mass μ_{Af} Q_a the heat flux (Btu/hr) into the inner air mass Q_m heat flux (Btu/hr) to the inner solid mass C_m thermal mass (Btu/°F) of the building materials and furniture U_{set} HVAC temperature (°F) setpoint δ_{rm} center value of floor area distribution δ_{rd} deadband of floor area distribution δ_{rd} deadband of floor area distribution σ_{ramin} minimal air temperature (°F) for a population δ_{Rw} deadband of or or R-Value distribution	PEV	plug-in electric vehicles	r P _{HVAC}	total power consumption (W) of the
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	Indices			aggregated loads
tindex of time ΔP instantaneous power increaseVariables and parameters $c_c(\mu_*,\delta_*)$ represents a uniform distribution x_a inner air temperature (°F) of HVAC unitcentered by μ_* , and spans the distance x_m inner mass temperature (°F) δ_m u_a thermal conductance (Btu/hr.°F) of the building envelope $U_c(*,*)$ U_a thermal conductance (Btu/hr.°F) of the building envelope $Uc(*,*)$ H_m thermal conductance (Btu/hr.°F) between the inner air and inner solid mass μ_{Af} Q_a the heat flux (Btu/hr) into the inner air mass μ_{Ia} Q_m heat flux (Btu/hr) to the inner solid mass μ_{Rw} C_a thermal mass (Btu/°F) of the building materials and furniture μ_{Rd} U_{set} HVAC temperature (°F) setpoint δ_{Af} δ HVAC unit's temperature (°F) for a population of HVAC loads δ_{Rw} $deadband of roof R-Value distribution\delta_{Rw}$	i	index of state-space	η	power system's transmission efficiency
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$ \begin{array}{llllllllllllllllllllllllllllllllllll$	x_a	inner air temperature (°F) of HVAC unit	δ	
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	x_m	inner mass temperature (°F) of HVAC unit	Uniforn	parameters deadband vector n(*.*) Uniform distribution between two
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	T_o	outside air temperature (°F)		values
$\begin{array}{c} \mbox{building envelope} & \mbox{value with deadband of the second value} \\ H_m & \mbox{thermal conductance (Btu/hr.°F) between} & \mu_{Af} & \mbox{center value of floor area (ft2)} \\ \mbox{the inner air and inner solid mass} & \mu_{Ia} & \mbox{center value of air exchange (1/hr)} \\ Q_a & \mbox{the heat flux (Btu/hr) into the inner air mass} & \mu_{Rc} & \mbox{center value of roof R-value (°F.ft2.hr/Bt} \\ Q_m & \mbox{heat flux (Btu/hr) to the inner solid mass} & \mu_{Rw} & \mbox{center value of wall R-value (°F.ft2.hr/Bt} \\ C_a & \mbox{thermal mass (Btu/°F) of the internal air} & \mu_{Rf} & \mbox{center value of floor R-value (°F.ft2.hr/Bt} \\ C_m & \mbox{thermal mass (Btu/°F) of the building} \\ materials and furniture & & \\ U_{set} & \mbox{HVAC temperature (°F) setpoint} & & \\ \delta_{Af} & \mbox{deadband of floor area distribution} \\ \delta & \mbox{HVAC unit's temperature (°F) for a population} & \\ \delta_{Rw} & \mbox{deadband of wall R-Value distribution} \\ \end{tabular}$	U_a	thermal conductance (Btu/hr.°F) of the	Uc(* <i>,</i> *)	uniform distribution center by the first
$ \begin{array}{c} H_m & \mbox{thermal conductance (Btu/hr.°F) between} & \mu_{Af} & \mbox{center value of floor area (ft²)} \\ & \mbox{the inner air and inner solid mass} & \mu_{Ia} & \mbox{center value of air exchange (1/hr)} \\ Q_a & \mbox{the heat flux (Btu/hr) into the inner air mass} & \mu_{Rc} & \mbox{center value of roof R-value (°F.ft².hr/Bt} \\ Q_m & \mbox{heat flux (Btu/hr) to the inner solid mass} & \mu_{Rw} & \mbox{center value of wall R-value (°F.ft².hr/Bt} \\ C_a & \mbox{thermal mass (Btu/°F) of the internal air} & \mu_{Rf} & \mbox{center value of floor R-value (°F.ft².hr/Bt} \\ C_m & \mbox{thermal mass (Btu/°F) of the building} \\ materials and furniture & \mbox{Uset} & \mbox{HVAC temperature (°F) setpoint} & \delta_{Af} & \mbox{deadband of floor area distribution} \\ \delta & \mbox{HVAC unit's temperature (°F) for a population} & \delta_{Rc} & \mbox{deadband of wall R-Value distribution} \\ \sigma & \mbox{HVAC loads} & \delta_{Rw} & \mbox{deadband of wall R-Value distribution} \\ \end{array}$		building envelope		value with deadband of the second value
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$ \begin{array}{cccc} Q_a & \text{the heat flux (Btu/hr) into the inner air mass} \\ Q_m & \text{heat flux (Btu/hr) to the inner solid mass} \\ Q_m & \text{heat flux (Btu/hr) to the inner solid mass} \\ C_a & \text{thermal mass (Btu/°F) of the internal air} \\ C_m & \text{thermal mass (Btu/°F) of the building} \\ materials and furniture \\ U_{set} & \text{HVAC temperature (°F) setpoint} \\ \delta & \text{HVAC unit's temperature (°F) deadband} \\ \delta_{Ia} & \text{deadband of air exchange distribution} \\ \sigma & \text{HVAC loads} \\ \end{array} $	6	the inner air and inner solid mass	μ_{Ia}	center value of air exchange (1/hr)
$ \begin{array}{c} Q_m & \text{heat flux (Btu/hr) to the inner solid mass} \\ C_a & \text{thermal mass (Btu/°F) of the internal air} \\ C_m & \text{thermal mass (Btu/°F) of the building} \\ materials and furniture \\ U_{set} & \text{HVAC temperature (°F) setpoint} \\ \delta & \text{HVAC unit's temperature (°F) deadband} \\ T_{a,\min} & \mininimal air temperature (°F) for a population \\ of \text{HVAC loads} \\ \end{array} $ $ \begin{array}{c} \mu_{Rw} & \text{center value of wall R-value (°F, ft^2.hr/Bt} \\ \mu_{Rd} & \text{center value of door R-value (°F, ft^2.hr/Bt} \\ eadband of floor area distribution \\ deadband of air exchange distribution \\ deadband of air exchange distribution \\ deadband of wall R-Value distribution \\ deadband of wall R-Value distribution \\ \end{array} $	Q_a	the heat flux (Btu/hr) into the inner air mass	μ_{Rc}	center value of roof R-value (°F.ft ² .hr/Btu)
$ \begin{array}{ccc} C_{a} & \mbox{thermal mass (Btu/°F) of the internal air} \\ C_{m} & \mbox{thermal mass (Btu/°F) of the building} \\ materials and furniture \\ U_{set} & \mbox{HVAC temperature (°F) setpoint} \\ \delta & \mbox{HVAC unit's temperature (°F) deadband} \\ T_{a,\min} & \mbox{minimal air temperature (°F) for a population} \\ of \mbox{HVAC loads} \\ \end{array} $ $ \begin{array}{c} \mu_{Rf} & \mbox{center value of floor R-value (°F,ft^2,hr/Brilling) \\ \mu_{Rd} & \mbox{center value of door R-value (°F,ft^2,hr/Brilling) \\ \mu_{Rd} & \mbox{center value of floor area distribution} \\ \mu_{Rd} & \mbox{deadband of air exchange distribution} \\ \mu_{Rd} & \mbox{deadband of air exchange distribution} \\ \mu_{Rd} & \mbox{deadband of air exchange distribution} \\ \mu_{Rd} & \mbox{deadband of roof R-Value distribution} \\ \mu_{Rd} & \mbox{deadband of wall R-Value distribution} \\ \mu_{Rd} & \mbox{deadband distribution} \\ \mu_{Rd} & \mbox{deadband distribution} \\ \mu_{Rd} & \mbox{deadband distribution}$	Q_m	heat flux (Btu/hr) to the inner solid mass	μ_{Rw}	center value of wall R-value (°F.ft ² .hr/Btu)
$ \begin{array}{ccc} C_m & \text{thermal mass (Btu/°F) of the building} \\ materials and furniture & \mu_{Rd} & \text{center value of door R-value (°F.ft2.hr/B2} \\ U_{set} & \text{HVAC temperature (°F) setpoint} & \delta_{Af} & \text{deadband of floor area distribution} \\ \delta & \text{HVAC unit's temperature (°F) deadband} & \delta_{Ia} & \text{deadband of air exchange distribution} \\ T_{a,\min} & \min a ir temperature (°F) for a population & \delta_{Rc} & \text{deadband of roof R-Value distribution} \\ & \text{of HVAC loads} & \delta_{Rw} & \text{deadband of wall R-Value distribution} \\ \end{array} $	C_a	thermal mass (Btu/°F) of the internal air	μ_{Rf}	center value of floor R-value (°F.ft ² .hr/Btu)
$ \begin{array}{c} U_{set} \\ U_{set} \\ \delta \\ HVAC \ \text{temperature (°F) setpoint} \\ \delta \\ T_{a,\min} \\ \text{minimal air temperature (°F) for a population} \\ \delta \\ frac{1}{Bar} \\ \delta_{Rc} \\ \delta_{Rw} \\ \delta_{Rw} \\ \end{array} \begin{array}{c} \text{deadband of floor area distribution} \\ \text{deadband of air exchange distribution} \\ \text{deadband of roof R-Value distribution} \\ \delta_{Rw} \\ \delta_{$	C_m	thermal mass (Btu/°F) of the building	μ_{Rd}	center value of door R-value (°F.ft ² .hr/Btu)
$ \begin{array}{c} \delta \\ \delta \\ T_{a,\min} \end{array} \begin{array}{c} \text{HVAC unit's temperature (°F) deadband} \\ \delta_{Ia} \\ \delta_{Rc} \\ \delta_{Rc} \end{array} \begin{array}{c} \text{deadband of air exchange distribution} \\ \text{deadband of roof R-Value distribution} \\ \delta_{Rw} \\ \end{array} \end{array} $	IJ	HVAC temperature (°E) setpoint	$\delta_{A\!f}$	deadband of floor area distribution
$T_{a,\min}$ minimal air temperature (°F) for a population δ_{Rc} deadband of roof R-Value distributionof HVAC loads δ_{Rw} deadband of wall R-Value distribution	δ_{set}	HVAC unit's temperature (°F) deadband	δ_{Ia}	deadband of air exchange distribution
of HVAC loads $\delta_{\scriptscriptstyle Rw}$ deadband of wall R-Value distribution	$T_{a,\min}$	minimal air temperature (°F) for a population	δ_{Rc}	deadband of roof R-Value distribution
		of HVAC loads	δ_{Rw}	deadband of wall R-Value distribution
$T_{a, ext{max}}$ maximum air temperature (°F) for a $\delta_{R\!f}$ deadband of floor R-Value distribution	$T_{a,\max}$	maximum air temperature (°F) for a	$\delta_{R\!f}$	deadband of floor R-Value distribution
population of HVAC loads $\delta_{\it Rd}$ deadband of door R-Value distribution		population of HVAC loads	δ_{Rd}	deadband of door R-Value distribution
$T_{sp,i}$ temperature setpoint (°F) of HVAC unit i R_{on} ratio of "on" units in aggregated HVAC le	$T_{sp,i}$	temperature setpoint (°F) of HVAC unit $ i$	R _{on}	ratio of "on" units in aggregated HVAC loads
ΔT_{sp} the amount of temperature setpoint change	ΔT_{sp}	the amount of temperature setpoint change		

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- 103

104 1. Introduction

105 Future smart grid, power quality has gained particular importance due to increase number of sensitive loads and faces new challenges (Bidram and Davoudi 2012). Especially, variable 106 renewable energy generation and unstable load demand are both sources of uncertainties in 107 108 the grid (Eksin et al. 2015). At the supply side, renewables, such as solar and wind energy, 109 are established as mainstream sources of energy (Ismail et al. 2019). Renewables have undergone rapid growth globally and supply 40% of the world's energy. They are expected 110 111 to play a major role in the future power generation by 2040 (Cai and Braun 2019; Sedady 112 and Beheshtinia, 2019). However, the integration of large-scale renewable energy affects the power system in many ways. The intermittent nature of renewable energy presents 113 significant challenges on system security and operation, when a larger proportion of 114 115 renewable energy sources are integrated in, e.g., more than 20% (Pourmousavi et al., 2014; Zhu et al., 2015). If the penetration of renewables is around 50% or more, the traditional 116 117 automatic generation control (AGC) is incapable to maintain the frequency within acceptable limits (Malik and Ravishankar 2018). The power grid needs new resources for frequency 118 reserves to provide high quality power supply. 119

120 As a cost-effective balancing resource, demand response (DR) is supposed to provide 121 balancing service, which used to be provided by conventional generation units (Jin et al., 122 2018; Müller and Jansen 2019). Prior studies presented various types of candidate loads for DR, including thermostatically controlled loads (TCL) and plug-in electric vehicles (Antti et al., 123 2019; Hamidreza et al., 2019). Among these, heating, ventilation, and air conditioning 124 (HVAC) account for 50% of total building energy consumption (Ma et al. 2019). The HVAC 125 126 systems are becoming more and more popular, driven by economic growth and the desire 127 for a better life. It is estimated that power consumption of HVAC systems will increase 33 128 times by the end of this century (Ma et al., 2019). The systems have larger heat capacity and 129 longer cyclic time, and they are more susceptible to outer climatic conditions (Giwa et al., 2019; Vakiloroaya, 2014). The heat capacity of buildings act as a battery; the energy 130 increases when the HVAC unit is on (charging) and decreases when the unit is off 131 132 (discharging). The elasticity of HVAC power consumption is utilized to reduce the user's 133 energy cost and provides DR services such as peak shaving and ancillary services (Ji et al., 134 2014; Lu, 2012; Nguyen and Le, 2014). The HVAC systems potential for DR needs to be 135 evaluated.

Several methods for modeling and control of aggregated HVAC systems have been 136 proposed, including direct load control and indirect load control. For instance, Wang et al. 137 138 (2014) developed highly accurate modeling and control strategies based on the control center for large population of HVAC loads, wherein the HVAC loads execute commands from 139 140 the control center unconditionally. These control modes act quickly, but some limitations exist: (1) The lockout constraint has little effect on normal operations but drastically affects 141 the collective response for a large number of HVAC aggregated together because it needs to 142 143 interrupt their normal operations frequently; (2) Most control algorithms have to choose 144 between computing accuracy and system performance. The models with first-order equivalent thermal parameter (ETP) model show better performance but larger computing 145 error. Models based on the second-order ETP have been extensively studied nowadays; they 146

show relatively high computing accuracy but put a heavy calculation burden on the control center with lower performance (Bashash and Fathy, 2013; Zhang et al., 2013); (3) The control algorithms may face serious power flickers and fluctuations due to synchronized state switching of multiple HVAC units when adjusting their thermostat setpoints, with the peak power when all units are "on" and the minimum power when all units are "off". To suppress the power variation, the algorithm becomes more complex. (4) The control algorithms increase the frequency of unit's on/off switching.

Zheng and Cai (2014) found that the number of on/off cycles was about 0-3 cycles per 154 hour without DR control and increased to about 1-20 cycles per hour using various DR 155 control algorithms. These issues considerably increased the operation cost of DR control 156 157 algorithms. Li et al. (2017) proposed the lazy state switching (LSS) control concept for 158 aggregated HVAC loads. This study aims to improve the control algorithm and provide 159 secondary frequency regulation services in a fully developed smart grid environment by controlling a large number of HVAC loads. The main contributions are summarized as 160 follows. 161

- This study ensures safe and stable operations of users' HVAC systems, to protect users' load, and to preserve system stability, reducing the frequency of unit's on/off switching. This works well with the lockout effect and to minimize users' electricity bills as well as to smoothen the total demand curve, and make the DR control more acceptable to users.
- This study proposes the idea of homogeneity control to realize controlling the
 parameters' distribution interval. One can test the aggregated system performance of
 different homogeneities to verify the adaptability of the control methods.
- The proposed control algorithm is fully compatible with other control algorithms, and
 integrates into the same DR systems with other control algorithms, which enables a DR
 system to have multiple control modes at the same time.
- 4. The proposed modeling and control method is validated using GridLAB-D, which is capable of simultaneously simulating thousands of unique buildings using the second order ETP model (GridLAB-D 2012). Simulation results show that the proposed control algorithm effectively eliminate power flicker and power fluctuation and quickly restore the system to a steady state after the control center broadcasts commands to adjust the HVAC setpoint.
- The rest of this study is organized as follows. Section 2 briefly reviews related literatures. Section 3 discusses the characteristics of HVAC units. Section 4 develops the temperature distribution model for aggregated populations of HVAC units. The improved LSS control mode is developed in Section 5. The experiment results and discussions are explained in Section 6. Finally, conclusions and future studies are presented in Section 7.
- 183

184 **2. Literature Review**

The structure of a smart grid is highly complicated with high penetration of renewable 185 generation, contains lots of nonlinear or sensitive loads, and requires power supply with 186 higher quality and stability (Pourmousavi et al., 2014; Sedady and Beheshtinia, 2019). 187 Although numerous studies have focused on aggregate HVAC to smoothen the fluctuations 188 189 of renewable generation, the power quality problems caused by the DR system itself have 190 been overlooked. The system voltage and frequency seriously affected by the variation in 191 load demand (Kabache et al. 2014). The switching of high-power loads imposes a considerable impact on the power grid and produces the same effect when switching large 192 193 amount of loads at the same time (Zhang et al., 2013). Power fluctuations may cause various problems, including voltage flicker and frequency deviation, incurring poor power supply for
consumers, which causes lights to flicker and may damage useful electronic equipment
(Abdul et al., 2014). This is a potential problem in aggregated DR systems, especially in HVAC
load-based systems.

Prior studies have focused on DR systems to provide ancillary service, which is an 198 199 important electric service, and the system is used by residential, commercial, or industrial 200 users (Cui and Zhou 2018; Ma et al. 2017). The system realizes the communication between grid utilities and customers, guides users to schedule power consumption to save energy, 201 reduces costs, and helps grid operation (Muhammad et al., 2019; Ma et al., 2017). As a 202 203 representative TCL, HVAC units are studied extensively in the literature. Some studies have 204 regulated HVAC units by turning them on or off directly at the customer premises. Lu et al. 205 (2005) presented a state-queuing model and a temperature priority list strategy to control 206 on/off states of HVAC units. Vanouni and Lu (2015) presented a centralized control method 207 to provide continuous regulation services. Zhou et al. (2017) proposed a novel two-level 208 scheduling method to minimize the power imbalance cost. Hao et al. (2015) modeled the 209 aggregated HVAC as a stochastic energy storage battery and proposed a priority-stack-based control to control the power consumption to follow AGC signals and reduce the tracking 210 211 errors by the on/off states directly. However, direct HVAC regulation does not consider the temperature setpoint and the deadband, and the tracking error is very large when large 212 number of loads toggle their working state simultaneously (Ma et al. 2017). 213

214 Adjusting the HVAC setpoint is a control method for the regulation of HVAC units (Yin et al., 2016). It is the key to study the load temperature dynamics for aggregated systems of 215 216 thousands of HVAC units (Adhikari et al., 2018). Lu and Chassin (2004) proposed a 217 state-queuing mode of setpoint adjusting based on price response and analyzed the 218 degeneracy of states followed by a damping process. The control center or the operator needs to adjust the system on a timely basis, so it is hard for the system to reach a stable 219 220 state. It was concluded that the aggregated system cannot respond to AGC signals before 221 achieving a stable condition (Bashash and Fathy, 2013). To improve stability, Bashash and Fathy (2013) developed Lyapunov-stable sliding mode controller based on a Monte Carlo 222 223 model for real-time management of thermostatic air conditioning loads, assuming that 224 communication is accessible and loads quickly respond, without considering the 225 synchronized operation of multiple loads and their impacts on the power system. However, 226 sliding mode control is well known for its chattering effect.

227 Zhang et al. (2013) analyzed the inner air and mass temperature and proposed a 2D 228 temperature evolution model. They then developed a highly accurate aggregated model. At the same time, the increased communication data require high-speed communication 229 230 equipment and quick response HVAC units. Tindemans et al. (2015) developed a heuristic algorithm based on setpoint adjusting for decentralized implementation. Setpoint 231 adjustment enlarges the energy storage capacity, but it often causes large chattering effects 232 and tracking errors (Ma et al., 2017; Gowa et al., 2019). The reason is that all HVAC units 233 234 change their setpoint instantaneously when they receive control signals, resulting in many 235 loads changing their working state simultaneously.

Communication latency is another important part of the total response time. In future smart grids, each HVAC unit may be under the control of a different home energy management system (HEMS). The DR client does not communicate with the DR server directly, and the HEMS communicates with the DR server on behalf of the HVAC unit (Yan et al., 2017). The network traffic and transmission speed are limited. From the perspective of load characteristics, a typical residential HVAC system switches 0–3 times per hour without
DR control (Zheng and Cai 2014). Its long working cycle, slow response, and potentially
higher frequency on/off cycling make them inappropriate for fast DR service (Beil et al.,
2016).

Achieving users' engagement for DR system is required from the viewpoint of system 245 implementation (Parrish et al. 2019). The utility and system operator may expect customers 246 to implement home automation, enroll in some DR systems, and respond predictably to DR 247 signals (Ghanem and Mander 2014). However, consumer participation in DR may not follow 248 these expectations. It is supposed that DR participation is voluntary rather than compulsory 249 through regulation (Parrish et al., 2019). The potential uncertainties and risks require 250 251 decision-making whether to engage or not to conduct a cost-benefit analysis to be 252 considered (Jordehi, 2019). The cost of DR includes the initial investment involving the 253 technology's cost and preparation of a response schedule. Possible risks include discomfort cost, rescheduling and on-site generation cost, and unexpected operations imposed on a 254 255 load. At present, the DR penetration level is small; for example, it is only 6% in the U.S. (Wei 256 et al., 2016). The users benefit more systematically when a DR system is designed to improve user engagement. It is important to protect their load from overuse in addition to the limited 257 reduction in consumer bills. The risk of unexpected operations to the load is likely to 258 259 dissuade many customers from DR participation.

In summary, advanced DR system designs maintain power quality and grid stability while properly taking advantage of the HVAC units' operation characteristics, completely considering the users' interests and the risks imposed on the loads. This study aims to provide secondary frequency control with a large number of HVAC units, which has fewer requirements on communication network, has higher stability of whole power consumption, and tends to protect user loads at the same time.

266

267 3. HVAC Unit Dynamic Model

The characteristics of a single HVAC unit form the basis to develop an aggregated load control model. Containing numerous variables and constraints, an HVAC system is a complex, nonlinear, and discrete system (Khasawneh 2014). HVAC systems have a large heat capacity and long cyclic time, and they are more susceptible to outer climatic conditions (Vakiloroaya 2014). The dynamics of inner air temperature is studied based on the second order ETP model (GridLAB-D 2012). The compressor time delay constraint is also discussed, which is important in aggregated load control modeling.

275 Residential HVAC units belong to different users and are controlled individually by 276 simple hysteresis controllers. Prior studies described the thermodynamics of an HVAC unit 277 (Zhang et al., 2013). This study adopted the popular ETP model to describe the dynamics of 278 air and mass temperature using two coupled first-ordered ODE (GridLAB-D 2012).

$$\begin{cases} \frac{dx_a}{dt} = \frac{1}{C_a} \left[-(U_a + H_m)x_a + H_m x_M + U_a T_o + Q_a \right] \\ \frac{dx_m}{dt} = \frac{1}{C_m} \left[H_m x_a - H_m x_m + Q_m \right] \end{cases}$$

280

For a given HVAC system with known initial conditions, the solution trajectory for x_a is uniquely determined. Figure 1 shows typical coupled air and mass temperature trajectories with setpoint $U_{set} = 75^{\circ}\text{F}$, deadband $\delta = 2^{\circ}\text{F}$, and initial outside air temperature $T_o = 90^{\circ}\text{F}$. t_1 indicates the time when the unit's setpoint is raised by 1 °F. The air

(1)

285 temperature trajectory is different for each working cycle, especially when the thermostat setpoint is changed. The green dashed lines indicate the time period when the unit remains 286 off, ignoring the switching on signals due to the lockout effect. 287

288



289 290

Figure 1 Characteristics of a single HVAC unit

291

292 The lockout effect is an important protection function to ensure the compressor remains 293 off for certain amount of time, e.g. 5 min. During this period, the high pressure in the 294 compressor chamber is released. It may cause physical damage if the compressor restarts early under pressure (Zhang et al., 2013). The lockout effect does not affect normal 295 operations. However, it can seriously impact the aggregated load response during DR control. 296 Zhang et al., 2013 introduced another state vector for the locked population, thus increasing 297 the complexity of the algorithm. However, it is difficult to obtain the real-time status of all 298 HVAC loads because of communication latency. 299

300

4. Temperature Distribution Model for Aggregate HVAC Units 301

302 The basic principle of aggregate system analysis is to study the time-course evolution of 303 population instead of characterizing all individual HVAC units. Modeling and controlling of a large population of HVAC units is a challenging task for at least two reasons. First, it takes a 304 305 long time, from minutes to hours, for the aggregated system to reach a sable state, but the outdoor temperature keeps changing, pushing the control center to send out control 306 commands from time to time. The commands toggle some units' working state immediately. 307 308 The aggregated system runs under an unstable state most of the time. Second, most of the control algorithms tend to change the HVAC unit's on/off state from time to time to result in 309 reduction of the unit's lifetime and fluctuations of overall power consumption. Zheng and 310 Cai (2014) evaluated this impact and found that the number of on/off cycles increased from 311 approximately 0–3 times per hour at normal to approximately 5–20 times per hour under DR 312 313 control. All these significantly increase the operating cost.

314

315 4.1 Temperature Distribution Based on State-space

Based on the physical model of individual load discussed in Section 3, this section first 316 discusses the temperature distribution of HVAC loads for a large population (subsection 4.1). 317 Based on the distribution model, we analyzed the aggregated dynamics when adjusting the 318 population's setpoints (subsection 4.2) and the aggregated impact to the power system 319 320 (subsection 4.3).

Let $[T_{a,\min}, T_{a,\max}]$ denote the inner air temperature range at a certain thermostat 321 setpoint. One can discretize this temperature range evenly into n small segments of 322

uniform width, resulting in a 2n state-space model in Figure 2. At each segment, the unit takes some time from entering to leaving; the difference in time at different temperature segments shows the characteristics of the dynamic process.



326 327

328

Figure 2 HVAC unit state-space transition model

The probabilities for an HVAC unit to reside in each of the 2n states form the basis to study the distribution of the aggregated loads. When an HVAC unit runs at a steady state scenario, the inner air temperature evolves across the states. Temperature distribution statistics were analyzed based on the simulation tests. A total of 2000 sets of physical parameters are generated, which are randomly distributed around their nominal values with a certain amount of variance, as described in Table 1. Each of them represents the real condition in one house.

336 In this simulation test, this study sets the outdoor temperature $T_o = 90$ °F, which remained unchanged, and set all the units' cooling setpoint at $T_{sp} = 75^{\circ}F$. When the population runs for 337 338 enough time, the aggregated system reaches a steady state, and the power consumption becomes relatively stable. This study discredited the deadband into 10 segments uniformly 339 340 and obtained 20 different states to study the temperature distribution within the 341 temperature deadband. At any time, some of the loads reside in the ON states, moving 342 toward the lower limit of the temperature, while some others reside in the OFF states, moving toward the upper limit. The objective of this subsection is to statistically analyze the 343 344 number of units in each state and calculate the proportion of them in all units. The 345 proportion of the units in segment *i* is calculated as follows. 216

$$f_i^* = \frac{\Delta m_i^{on/off}}{n}$$

(2)

where $\Delta m_i^{on/off}$ is the number of units of state on/off residing in the segment *i* at a given moment and *n* is the total number of HVAC units, which is 2000 in this test case. Figure 3 shows the units' temperature distribution over the states. It shows that the loads are not uniformly distributed. For the "on" group, it becomes more dense as the temperature reduces that means the speed of temperature evolution reduces near the lower limit, as shown in Figure 3 a). It is the reverse distribution for the "off" group, as presented in Figure 3 b).



Figure 3 Probability Distribution of HVAC Units over ON/OFF states

362

The number of units staying in a specific state is estimated. The total power consumption 363 is estimated by adding the number of units in all "on" states. We assume that all the units' 364 power P and energy efficiency η are equal when their state is "on". The total power 365 366 demand is then determined by the number of units in the "on" state at any time.

(3)

367
$$P_{HVAC}(t) = \frac{P}{\eta} \sum_{i=1}^{n} \Delta m_i$$

368

369 4.2 System Evolution in Response to Control Commands

This study analyzed the dynamic process when adjusting units' setpoints using the 370 371 temperature distribution model described in Section 4.1 and assumed that all HVAC units are working under the cooling mode. The basic principle of controlling the aggregate system 372 373 is to adjust the population's thermostat setpoint, thus regulating the overall power 374 consumption. The first case begins from the steady state described in subsection 4.1; the central controller sends a control command to raise the population thermostat setpoint by 375 0.4 °F; all HVAC units respond to control commands immediately. We redefine the states in 376 the same pattern centered by the new setpoint, and then there are some "out-of-regime" 377 378 states.

379 Figure 4 showed the system states in the temperature distribution model. The white block implies "out-of-regime" states. For the "off" state, the temperature of the "out-of-regime" 380 states is lower than the new low limit. Therefore, the HVAC units take more time to increase 381

their temperatures to the new upper limit. However, for the "on" states, the HVAC units in the "out-of-regime" states need to switch their state immediately. The instantaneous increase in power of the entire system is expressed as follows.

$$\Delta P = -\frac{P}{\eta} (m_1^{on} + m_2^{on})$$
(4)

386

385

Figure 5 showed the instantaneous probability distribution when the central controller sends out a command to decrease the population's thermostat setpoint by 0.4 °F. For the "on" states, the HVAC units of "out-of-regime" states need to work longer. The "off" states need to switch "on" immediately. The amount of instantaneous power increased is expressed as follows.



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is increased

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Figure 5. Instantaneous probability distribution of the system after decreases the thermostat
 setpoint

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412 **4.3 Power Fluctuation**

The overall power consumption shows an immediate spike, followed by a damping oscillation process. A major contributor that affects the aggregate transient process is the diversity of the parameters of HVAC units. The highly homogeneous load populations often arouse strong oscillations, whereas a well-diversified load population undergoes a damping process with quick attenuation. In the literature, these observations are made mostly based on first-order thermostatically controlled load models; the second order ETP model of HVAC units also yields a similar behavior.

420 The oscillation process is validated against realistic simulations using GridLAB-D with 421 thermostat setback programs, under different homogeneity of aggregate populations. In these two test cases, all the HVAC units participate in the same setback program where the 422 set points are simultaneously shifted up from 75 °F to 76 °F at t=1(h) and released at 423 t = 4 (h). The homogeneity of the population is controlled by reducing the parameters' 424 425 distribution interval around their nominal values. The default distribution intervals are 426 described in Table 1 (Adopted from Zhang et al. 2013). The quantified homogeneity of 0.2 δ_m is shown in Table 2. Detailed information about these parameters is provided in (GridLAB-D 427 428 2012).

429

Table 1. Default parameter values/distribution of the building used in GridLAB-D simulations(Adopted from Zhang et al. 2013)

Distribution	Value	Value
$U_c(\mu_{Af},\delta_{Af})$ Uniform distribution of floor area	U _c (2250,1500)	Uniform(1500,3000)
$U_c(\mu_{la}, \delta_{la})$ Uniform distribution of air exchange	U _c (0.625,0.75)	Uniform(0.25,1)
$U_c(\mu_{Rc}, \delta_{Rc})$ Uniform distribution of roof R-value	U _c (30,20)	Uniform(20, 40)
$U_{a}(\mu_{Pu}, \delta_{Pu})$ Uniform distribution of wall R-value	U _c (20,20)	Uniform(10,30)
$U_c(\mu_{Rf}, \delta_{Rf})$ Uniform distribution of floor R-value	$U_{c}(22.5,25)$	Uniform(10,35)
$U_{c}(\mu_{Rd}, \delta_{Rd})$ Uniform distribution of door R-value	Uc(3,4)	01110111(1,5)

433 Table 2. Parameters values/distribution of homogeneity 0.2 δ_m

Distribution	Value	Value
$U_c(\mu_{Af}, 0.2\delta_{Af})$ Uniform distribution of floor area	U _c (2250,300)	Uniform(2100,2400)
$U_c(\mu_{la}, 0.2\delta_{la})$ Uniform distribution of air exchange	U _c (0.625,0.15)	Uniform(0.55,0.7)
$U_c(\mu_{Rc}, 0.2\delta_{Rc})$ Uniform distribution of roof R-value	U _c (30,4)	Uniform(28, 32)
$U_c(\mu_{Rw}, 0.2\delta_{Rw})$ Uniform distribution of wall R-value	U _c (20,4)	Uniform(18,22)
$U_c(\mu_{Rf}, 0.2\delta_{Rf})$ Uniform distribution of floor R-value	$U_c(22.5,5)$ $U_c(3,0.8)$	Uniform(20,25) Uniform(2.6,3.4)
$U_c(\mu_{Rd}, 0.2\delta_{Rd})$ Uniform distribution of door R-value		

434

Here, $U_c(\mu_*, \delta_*)$ represents the uniform distribution centered by μ_* and spans the distance δ_* . For a uniform distribution in the range $[V_*^-, V_*^+]$:

437

$$\mu_* = (V_*^- + V_*^+)/2$$

$$\delta_* = V_*^+ - V_*^-$$
(6)

(7)

To simplify the notation, we collect the parameters' distribution distance to form a parameter deadband vector as follows.

440

$$\boldsymbol{\delta}_{m} = \begin{bmatrix} \boldsymbol{\delta}_{Af}, \boldsymbol{\delta}_{Ia}, \boldsymbol{\delta}_{Rc}, \boldsymbol{\delta}_{Rw}, \boldsymbol{\delta}_{Rv}, \boldsymbol{\delta}_{Rd} \end{bmatrix}^{T}$$

For the uniformly distributed parameters, keeping their center values unchanged, the load
homogeneity is controlled by adjusting the parameters' distribution interval.

443

Figure 6-a) shows the percentage of "On" units of the population whose parameter distribution interval is $0.2 \delta_m$. In another simulation test, the parameter distribution intervals are deceased to $0.1 \delta_m$. The percentage of "On" units is shown in Figure 6 b).





451

454

Figure 6. Aggregated response of 1F setback program of different population homogeneities

455

5. Improved LSS Model 456

This study aims to improve the LSS mode as a new control method (Li et al. 2017). The key 457 idea to maintain stability of power consumption is to preserve the diversity of temperature 458 distribution of the aggregate population. This involves changing the way that HVAC loads 459 respond to control commands. In practice, the LSS control mode can not eliminate load 460 oscillations completely after a control action to preserve the diversity in the temperature 461 distribution and reach a new steady state quickly instead of oscillating. Another 462 distinguishing characteristic is that the LSS mode reduces the frequency of the HVAC unit's 463 464 on/off switching.

465

466 5.1 Designing of HVAC Units for Improved LSS Control

The units are not distributed uniformly among different temperature segments. There are 467 468 more units in the segments near the limit where their working states are changed. This means that a small adjustment of the setpoint will cause many units to change their working 469 470 states and cause serious power fluctuations.

471 The LSS method does not require any units to toggle any HVAC unit's working state immediately and tends to extend the units' working state as long as possible. Units of 472 473 different working states act differently when the control center broadcasts a command to 474 adjust the populations' thermostat setpoint. For example, when it needs to adjust load 475 setpoint to a lower value, all "ON" state HVAC units execute the command immediately and maintain their "ON" state until the new lower limit T_{-}^{new} ; but all the "OFF" units do not 476 477 execute the command. They just keep the command till the temperature reaches the upper limit T_{+}^{old} , and they execute the command to change their setpoint only after they change 478 their working state to "ON". The flowchart of the DR system with the LSS is shown in Figure 479 7. 480



497 other control methods, the LSS control requires each HVAC unit to be equipped with a smart

498 controller embedded in the HVAC unit or HEMS. Figure 7 b) indicates the logic process of the499 smart controller handling the control command, which contains two working threads.

500 When a command is received, the receiver thread pass it to the preprocessor. The 501 preprocessor reads the shared memory, searches whether there exists a saved command, 502 and merges them together. For example, if there exists a command to increase the setpoint 503 by 1 °F, and the new command is to decrease the setpoint by 0.4 °F; then the merged 504 command is to increase the setpoint by 0.6 °F. Then, the preprocessor saves the merged 505 command to the memory.

The worker thread reads the shared memory periodically to check the command type and executes it in different ways according to the command type. If the command is a lazy one, the thread will do a condition test. The worker thread executes the command after the conditions are met. It then transfers the return code to the preprocessor to handle the saved command. The command cannot be executed until the condition is satisfied. The HVAC unit condition switch is expressed as follows.

512
$$T_{sp,i}(t) = \begin{cases} T_{sp,i}(t-\varepsilon_t) & S(t-\varepsilon_t) = 0\\ & \& \Delta T_{sp}(t-\varepsilon_t) \cdot [T_{sp,i}(t-\varepsilon_t) - T_o] < 0\\ & T_{sp,i}(t-\varepsilon_t) + \Delta T_{sp}(t-\varepsilon_t) & S(t-\varepsilon_t) = 1\\ & \& \Delta T_{sp}(t-\varepsilon_t) \cdot [T_{sp,i}(t-\varepsilon_t) - T_o] > 0 \end{cases}$$
(8)

513

514 5.2 Improved Response Mode of Individual HVAC units

This study begins from the steady state with $U_{set} = 75^{\circ}\text{F}$, $\delta = 2^{\circ}\text{F}$, $T_o = 90^{\circ}\text{F}$ to examine the effects of the individual and aggregate dynamics of HVAC under LSS control mode when adjusting the setpoint. The setpoint is reduced by 1 °F. Figure 8 a) shows the inner air temperature trajectories of ten samples with instantaneous switching in other control modes. Figure 8 b) shows air temperature trajectories under the LSS mode of ten samples. 520



521 522



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527 528

Figure 8. Temperature trajectories of ten samples

In the case of instantaneous switching, all the loads adjust their on/off states according to the new setpoint immediately after receiving the control command. There is a serious impact on the diversity of the aggregated loads after the control actions. However, under LSS control, some loads satisfying the switching condition execute the command and keep working till the new temperature limit is reached; others keep their working state until they reach the older temperature limits.

535

536 **5.3 Preservation of Diversity in HVAC unit Air Temperature**

537 This subsection discusses the load temperature distribution dynamics when adjusting the 538 system thermostat setpoint. The key to maintain a stable power consumption is to maintain 539 the diversity of the aggregate population of HVAC units. To illustrate the improvement of LSS 540 control mode, we examine the load diversity changes when adjusting the system setpoint. 541

Previous studies have attempted to improve the aggregate control. Their main drawback is that they tried to control all units instantly and tried to avoid the lockout constraints based on a large operational cost. Figure 9 shows the system state evolution process when the system is controlled to increase the setpoint under the LSS control mode.



547 548 549

a) Temperature distribution under the initial setpoint



- 550 551
- b) Temperature distribution after receiving the adjusting command
- 552



c) Temperature distribution in the middle of the transition process



556 557

d) Temperature distribution at the end of the transition process

Figure 9. Density evolution of the process when shifting up the population's setpoint

558 559 560

561 6. Discussions

Two high homogeneity scenarios are studied to evaluate the proposed control method to illustrate the adaptability and performance of the proposed control method. The stability of the aggregated loads is illustrated by varying the percentage of "ON" units. The proposed aggregate model provides a robust control mechanism for large populations of HVAC units. We use the same setback program that shifts the population's thermostat setpoint by 1 °F higher at t = 2 h and changes it back at t = 5 h. Figure 10 shows the dynamic process of 2000 HVAC units of different homogeneities.

569 Under the LSS control mode, the aggregate HVAC system's response curve follows the red 570 line in Figure 10. This study notes the following observations:

571 1. The initial spike is weaker and a little late, which comes with a climbing process. The

- 572 power flickers and fluctuations disappeared, which is inevitable under instantaneous 573 switching control methods.
- 574 2. There was almost no succeeding fluctuation under the proposed control mode.
- 575 3. The proposed model tends to maintain the working states of the HVAC units and 576 protects the unit from overuse.
- 577 4. The frequency of HVAC units' on/off switching would be lower than normal operation 578 because HVAC units are controlled to prolong their work cycle from time to time.
- 579
- 580





a) Unit parameter distribution interval is 0.2 δ_m of the default intervals

583



584 585

- b) Unit parameter distribution interval is 0.1 δ_m of the default intervals
- Figure 10. Aggregate responses under setback program with different parameter distribution
 intervals
- 588
- The stability of the aggregated system can not only improve power quality but also improve the ability to respond to signals. The aggregated loads cannot track AGC signals until the system achieves a stable condition. A good performance in the stability of power consumption shows the potential of the proposed model to improve power quality in the control of aggregate HVAC systems.

However, this study is subject to a number of uncertainties. (1) The weather conditions are associated with considerable uncertainties. Various parameters and evolution speeds have a direct impact on HVAC units in a complicated way. The time scale beneath which HVAC systems work are comparable significantly to weather conditions; therefore, to control and adjust the aggregate system, this study considers the trends of weather variations; and (2) the first spike with a large amplitude and long duration time still exists, and other resources are required to balance the power variation. The amplitude and interval of system regulation are limited by the compensation capability of other resources. Third, there are unavoidable uncertainties including users' preferences and unexpected operations.

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604 **7. Conclusion**

This study improved the LSS control mode to provide secondary frequency regulation in a fully developed smart grid environment, which fully adapted to the slow response and operation constraints of HVAC systems. The LSS mode shows promising performance in maintaining the diversity of inner air temperature distribution of units in the aggregate system. It is essential for an aggregated system to restore stability after control actions and get ready quickly to track the next AGC signals. Traditional control methods tend to monitor the system status in real time, which is always accompanied by a high operation cost.

In contrast to traditional control methods, the LSS control mode has a minor requirement 612 613 for real-time monitoring of HVAC' working states and does not require any unit to interrupt its working state. This study tends to extend some units' work cycles, which preserves the 614 615 population's state diversity during the adjustment. For individual HVAC units, the LSS mode 616 can reduce the frequency of the unit's on/off switching, which protects them from overuse. The power consumption is quickly restored to a stable state, thus making it easy for the 617 618 utilities to improve DR applications based on HVAC systems. Integrated with other resources, the aggregate HVAC system adjusts the overall power consumption within limits and 619 620 improves the efficiency and controllability of the whole system.

Future study is required to adapt the proposed control method to a changing ambient temperature and to develop adaptive control algorithms for the control center. Others should focus on integrating the LSS mode with other control algorithms to achieve better results. This study may provide valuable and useful ideas for researchers and industrialists working to develop better control methods. It is hoped that these novel methods will help improve the renewable usage and power quality in future smart grids.

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