Performance investigation and design optimization of a battery thermal management system with thermoelectric coolers and phase change materials

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Abstract: In this work, a novel battery thermal management system (BTMS) integrated with thermoelectric coolers (TECs) and phase change materials (PCMs) is developed to ensure the temperature working environment of batteries, where a fin framework is adopted to enhance the heat transfer. By establishing a transient thermal-electric-fluid multi-physics field numerical model, the thermal performance of the BTMS is thoroughly examined in two cases. The findings demonstrate that increasing the TEC input current, fin length, and thickness is beneficial for reducing the maximum temperature and PCM liquid fraction. Nevertheless, although the increase in fin length can lower the temperature difference, the influence of fin thickness and TEC input current on the temperature difference is tiny. Based on the numerical findings, the optimal fin length and thickness of 7 mm and 3 mm are obtained. In this situation, when the TEC input current is 3 A, the maximum temperature, temperature difference, and PCM liquid fraction in Case 1 are 315.10 K, 2.39 K, and 0.002, respectively, and those are respectively 318.24 K, 3.60 K, and 0.181 in Case 2. The configuration of Case 1 outperforms that of Case 2, due to the fewer TECs and greater distance from the battery pack to the TEC within Case 2. When experiencing a higher battery discharge rate, the TEC input current should also be correspondingly increased to ensure the temperature performance of the battery. The relative findings contribute to new insights into battery thermal management.

Keywords: thermoelectric; battery thermal management system; fin framework; numerical model; phase change material

Nomenclature		λ	thermal conductivity, W·m ⁻¹ ·K ⁻¹		
		γ	latent heat, $J \cdot kg^{-1}$		
Same to 1		E	turbulent dissipation rate, $m^2 \cdot s^{-3}$		
Symbols		ρ	density, kg⋅m ⁻³		
c_p	specific heat, J·kg ⁻¹ ·K ⁻¹	μ	dynamic viscosity, Pa·s		
$d_{ m h}$	hydraulic diameter, mm	β	liquid fraction		
\vec{E}	electric field density vector, V·m ⁻²	σ	electrical conductivity, S·m ⁻¹		
Н	enthalpy, J·kg ⁻¹	Subsarint			
h	sensible heat enthalpy, J·kg ⁻¹	Subscripts			
Δh	phase change enthalpy, J·kg ⁻¹	b	battery		
Ι	current, A	co	copper electrode		
Re	Reynolds number	1	liquid phase		
Ĵ	current density vector, A·m ⁻²	m	material		
k	turbulent kinetic energy, m ² ·s ⁻²	n	n-type thermoelectric leg		
L	fin length, mm	р	p-type thermoelectric leg		
Μ	fin thickness, mm	pcm	phase change material		
р	pressure, Pa	S	solid phase		
Q	heat generation power, W	Abbraviations			
Ś	source term	Abbreviations			
Т	temperature, K	BTMS	battery thermal management system		
и	coolant flow speed, m/s	CFD	computational fluid dynamics		
ν	mass flow rate, kg·s ⁻¹	EV	electric vehicle		
V	volume, mm ³	PCM	phase change material		
Greek symbols		PW	paraffin wax		
Greeksy		TEC	thermoelectric cooler		
α	Seebeck coefficient, $\mu V \cdot K^{-1}$				

1 1. Introduction

2 The vigorous promotion of electric vehicles (EVs), considered one of the key measures to reduce 3 CO₂ emissions, has received strong support from the international community (Singh et al., 2023). 4 Lithium-ion batteries, esteemed as the essential equipment in EV energy supply, have been highly 5 commended for their exceptional characteristics of excellent energy density and cycle life (Shan et al., 6 2023; Weng et al., 2022). Nevertheless, achieving the high efficiency of lithium-ion batteries involves 7 controlling their operating temperature within the range of 20-50°C and managing the overall 8 temperature differential of the battery pack to a value below 5°C (Lin and Zhou, 2023). Nonetheless, 9 in practical operation, the electrochemical reactions occurring within lithium-ion batteries give rise to 10 significant high-temperature issues (Subramanian et al., 2021). In the absence of effective cooling 11 measures, the possibility of thermal runaway in batteries exists, which can ultimately lead to the 12 spontaneous combustion of EVs (Liu et al., 2023). Hence, there is a pressing demand for the innovation 13 of an effective battery thermal management system (BTMS) to resolve the high-temperature concern 1 in lithium-ion batteries.

2 In the field of BTMS, liquid cooling, air cooling, thermoelectric cooler (TEC) cooling, heat pipe 3 cooling, and phase change material (PCM) cooling are the predominant technical methodologies 4 (Mousavi et al., 2023). Leveraging the high latent heat properties of PCMs, the PCM-based BTMS can 5 effectively govern the battery temperature while ensuring temperature uniformity without necessitating any additional energy consumption (Luo, J. et al., 2023). Nevertheless, the application 6 7 of PCMs in battery thermal management presents a formidable challenge due to their low thermal 8 conductivity and restricted latent heat. For this reason, many researchers have tried to improve the 9 thermal conductivity of PCMs (Ling et al., 2021; Subramanian et al., 2021). Li et al. (2014) conducted 10 a dedicated experiment to assess the effect of incorporating the porous metal foam into the pure PW-11 based PCM on the dissipation of battery heat; They found that the utilization of composite PCMs 12 contributes to further reducing the battery temperature. Talele and Zhao (2023) employed a numerical 13 simulation to investigate the impact of nano-enhanced PCMs, composed of pure PW-based PCMs and 14 alumina nanoparticles, on battery heat dissipation; It was revealed that the utilization of the nano-15 enhanced PCM facilitates battery heat conduction and temperature control. The mentioned research 16 offers an effective solution to improve the thermal conductivity of PCMs.

17 Nonetheless, the introduction of high thermal conductivity materials undoubtedly lowers the latent 18 heat of PCMs. Once the PCM's latent heat is completely consumed, it may cause serious heat 19 accumulation problems within the battery pack, thereby increasing the risk of thermal runaway of the 20 battery. Meanwhile, the temperature difference across the battery pack rises rapidly. Hence, the 21 coupling of PCMs with air or liquid cooling-based BTMS has become a mainstream research direction 22 (Zhang et al., 2021; Zhang, Y. et al., 2022). Ranjbaran et al. (2023) numerically studied the effects of 23 cooling duct shape and inlet pressure on the thermal performance of a BTMS that incorporates PCMs 24 and air cooling; The results indicated that the system maintains effective control over the maximum 25 battery temperature and temperature difference, even under the demanding conditions. Yang et al. 26 (2023) employed a numerical simulation to investigate the performance of a BTMS that combines a 27 Z-shaped liquid cooling plate and PCM/foam aluminum; They found that this combination could efficiently reduce the energy consumption of the system while upholding proficient heat dissipation. 28 29 However, the integration of air or liquid cooling with PCMs still holds limitations. Air cooling is hard 30 to reach the internal region of PCMs, while liquid cooling technology is limited by its size, weight, 31 and substantial power usage (Babu Sanker and Baby, 2022). Therefore, it is necessary to find an 32 efficient cooling and environmentally friendly technology to combine with PCMs.

1 Thermoelectric cooling, as an emerging active battery thermal management technology, is leading 2 a new trend in the field of battery thermal management with unique advantages such as fast response, 3 no emissions, efficient cooling, precise temperature control, and flexible switching of dissipation or 4 preheating modes (Sait, 2022). Nevertheless, the operation of the TEC demands a continuous current 5 input, leading to significant power consumption in the TEC-based BTMS. Consequently, integrating the TEC-based active BTMS with the PCM-based passive BTMS presents a practical solution 6 7 (Siddique et al., 2018). Jiang et al. (2019) used a combination of experiments and numerical 8 simulations to study the performance of a BTMS integrating with copper foam composite PCMs and 9 TECs; Their outcomes demonstrated a substantial decrease in the maximum battery temperature and a 10 significant prolongation of lifespan in contrast to the natural air convection and liquid cooling method. 11 Liu et al. (2022) utilized a numerical simulation to analyze the effectiveness of a BTMS combining 12 PCMs and TECs; Their research revealed that as the TEC input current is increased, there is a substantial decrease in battery temperature, but this comes at the expense of declining temperature 13 uniformity and coefficient of performance. Song et al. (2018) designed a BTMS based on the TEC and 14 15 PCMs for prismatic batteries, and analyzed its thermal performance under different charging and 16 discharging rates by CFD simulations; Their results showed that the battery temperature could meet 17 the requirements for the majority of the time, both in the cooling and heating processes. However, the reported BTMS integrated with TECs and PCMs is limited by the low thermal conductivity of PCMs. 18 19 During the high-rate battery discharge process, the PCM experiences excessive melting, causing a 20 rapid rise in battery temperature and temperature difference, surpassing predefined limits. Meanwhile, 21 for the BTMS coupled with TECs and PCMs, the current performance investigation mainly relies on 22 the CFD (Computational Fluid Dynamics) simulation or heat transfer modeling, lacking systematic 23 analysis and failing to consider multi-physics coupling characteristics.

24 Accordingly, this work proposes a novel BTMS that combines PCMs and TECs, in which a fin 25 framework is introduced to enhance the heat transfer from the TEC to the battery and PCMs. The fin 26 framework structure enables the TEC to efficiently control the PCM melting and battery temperature. 27 In addition, the design of stacked structures has the potential for extensive expansion, which is 28 conducive to the widespread application of the system. Regarding the numerical modeling aspect, a 29 transient thermal-electric-fluid multi-physics field numerical model is developed to evaluate the 30 thermal performance of the proposed BTMS. On this basis, comprehensive performance investigations 31 and design optimizations for the BTMS are conducted, including exploring the effects of various 32 parameters on the BTMS thermal performance, i.e., structural configuration, fin length and thickness, 1 TEC input current, and discharge rate.



2 **2.** Geometric description of the novel BTMS

3 4

Fig. 1. Schematic diagram of the three-dimensional geometry of the BTMS.

5 Fig. 1 presents a schematic diagram of the geometric model for the novel BTMS proposed in this 6 work. The system comprises N identical cells, with a shared S-shaped liquid cooling plate positioned 7 between adjacent cells. Notably, both sides of the liquid cooling plate feature an identical distribution 8 of TECs. Building upon the mentioned design, the proposed novel BTMS incorporates a stacked 9 structure, endowing it with unlimited scalability and significantly boosting its suitability for diverse 10 practical scenarios. In order to present a visual depiction of the geometry of the BTMS, a representative 11 cell is selected for an elaborate description. The cell comprises the battery pack, the pure PW-based 12 PCM, the aluminum fin framework, the TEC, and the S-shaped liquid cooling plate. The aluminum fin 13 framework encompasses the outer framework, inner partitions, and fins, with dimensions (length \times 14 width \times height) of 178 mm \times 92 mm \times 90 mm and a thickness of 2 mm. The central cavity of the outer 15 framework is divided into four small rectangular cavities with equal sizes through horizontal and vertical partitions. Additionally, rectangular fins with uniform sizes are evenly distributed on both the 16 17 outer framework and inner partitions to enhance heat transfer efficiency. The four prismatic LiFeO4 18 batteries in the battery pack are ingeniously positioned at the central region of the four small cavities.

1 The space remaining between these small cavities and batteries is appropriately filled with pure PW-2 based PCMs. The same number and size of TECs are uniformly placed on both sides of the outer 3 framework. The TEC incorporates p/n-type thermoelectric legs, copper electrodes, and ceramic plates. 4 Upon supplying power to the TEC, the ceramic plate at one end undergoes heating and operates as the 5 heating side, while the ceramic plate at the other end concurrently cools down, functioning as the cooling side. The cooling end is tightly affixed to the outer framework, delivering a cooling source to 6 7 the battery pack and PCM, while the heating end is interconnected with the S-shaped liquid cooling 8 plate, through which the temperature of the heating end is reduced to enhance the cooling efficiency 9 of TECs. The S-shaped liquid cooling plate has a thickness of 10 mm, and the internal liquid flow channel has a diameter of 8 mm. Water is selected as the cooling medium within the flow channel. 10 11 Further geometric information can be referred to in Fig. 1.



12

13 Fig. 2. Geometry of the system and arrangement of the TEC in different cases.

In addition, the above description demonstrates that the stacked-based system structure still holds in the case of mounting the TEC on the other two sides of the aluminum fin framework. The geometry of the system and the arrangement of TECs for different cases are illustrated in Fig. 2. In Case 1, there is a uniform distribution of TECs on both the front and rear exterior surfaces of the aluminum fin outer framework, comprising 6 TECs per exterior surface. In Case 2, the left and right exterior surfaces of the aluminum fin outer framework showcase a similar uniform arrangement, with 4 TECs affixed to each exterior surface. Notably, in Case 1, the length of the S-shaped liquid cooling plate is set at 178
mm, whereas in Case 2, it is adjusted to 92 mm, ensuring an exact match with the dimensions of the
outer framework. Table 1 presents the material parameters of the battery (Liu et al., 2022), aluminum,
water, and pure PW-based PCM (Zhang, F. et al., 2022). To access detailed information regarding the
dimensions and material parameters of the TEC components, kindly refer to Table 2 (Hu et al., 2023).
Table 1. Material parameters for battery (Liu et al., 2022) and other components (Zhang, F. et al., 2022).

		Specific heat	Density	Thermal conductivity	latent heat	Phase char	nge temperature
	Component	$(J \cdot kg^{-1} \cdot K^{-1})$	(kg·m ⁻³)	$(W \cdot m^{-1} \cdot K^{-1})$	$(J \cdot kg^{-1})$	(K)	
	Aluminum	900	2700	238	-	-	
	Battery	1150	1838.2	x, y: 15.3 z: 0.9	-	-	
	PCM	2000	800	0.2	255000	314.15-317	7.15
	Water	4200	998	0.6	-	-	
7	Table 2. Dimensions and material parameters of each component of the TEC (Hu et al., 2023).						
		Seebeck coef	ficient	Thermal conductivity	Electrical conductivity Size		Size
		$(\mu V{\cdot}K^{\text{-}1})$		$(W \cdot m^{-1} \cdot K^{-1})$	$(\mathbf{S} \cdot \mathbf{m}^{-1})$		(L×W×H mm ³)
	p-type legs	$-1.593 \times 10^{-9} T^2$ -7.062×10^{-5}	$+1.364 \times 10^{-6} T$	$\frac{1.071 \times 10^{-5} T^2 - 8.295 \times 10^{-3} T}{+2.625}$	$1.311T^2 - 1.3$ +4.023×10 ⁵	$364 \times 10^{3} T$	$1.4 \times 1.4 \times 1.6$
	n-type legs	$7.393 \times 10^{-11} T^2$ -8.494×10 ⁻⁵	$-2.500 \times 10^{-7} T$	$\frac{1.870 \times 10^{-5} T^2 - 1.447 \times 10^{-2} T}{+3.680}$	$0.657T^2 - 7.13$ +2.463×10 ⁵	$36 \times 10^2 T$	$1.4 \times 1.4 \times 1.6$
	copper electrodes	-		400	5.998×10^7		$3.8 \times 1.4 \times 0.4$
	ceramic plates	-		22	-		$40 \times 40 \times 0.8$

8 **3.** The transient thermal-electric-fluid multi-physical field numerical model

9 3.1 Model hypothesis

10 Before building a numerical model, some necessary model hypotheses need to be made explicit:

11 (i) The material characteristics of both the battery and PCM remain constant and unaffected by

12 temperature fluctuations (Li, B. et al., 2023).

13 (ii) The volume of PCMs is constant when they undergo the melting process.

(iii) Heat generation inside the battery occurs evenly and spreads out in all orientations (Liu et al.,2022).

16 (iv) Neglecting the effect of convective heat transfer after melting of the PCM (Cao et al., 2020).

17 (v) The effect of thermal radiation is not considered (Luo, D. et al., 2023d).

18 *3.2 Governing equations*

1 Within the numerical model for transient thermal-electric-fluid multi-physics, the governing 2 equations can be segregated into three components: solid domains other than the TEC, the TEC 3 domain, and the fluid domain.

4 3.2.1 Governing equations for solid domains other than the TEC

For this work, the prismatic LiFeO₄ battery is utilized, with dimensions of 70 mm × 27 mm × 90
mm (length × width × height) and a nominal capacity of 12 Ah (Wu et al., 2018). Heat generation
inside the battery can be controlled using the following energy conservation equation:

$$\frac{\partial}{\partial t}(\rho_{\rm b}c_{p,{\rm b}}T_{\rm b}) = \nabla \cdot (\lambda_{\rm b}\nabla T_{\rm b}) + \frac{Q_{\rm b}}{V_{\rm b}}$$
(1)

9 where *T*, *t*, ρ , λ , and c_p denote temperature, time, density, thermal conductivity, and specific heat, 10 respectively, the subscript b represents the battery, and V_b and Q_b are the volume and heat generation 11 power, respectively. The battery discharge rate can be quantified using the C-rate, which represents 12 the operating current relative to the nominal current. For instance, a discharge rate of 3 C indicates that 13 the battery operates with a current three times higher than its nominal current of 12 A. Table 3 presents 14 the heat generation power of the battery at various discharge rates, according to the reference value in 15 (Wu et al., 2018) and the method in (Heyhat et al., 2020).

16 Table 3. Heat generation power of batteries under different discharge rates (Wu et al., 2018; Heyhat et al., 2020).

Discharge rate (C)	3	4	5
Heat generation power (W)	12.96	17.28	21.60

The heat conduction mechanism within the PCM can be modeled using the enthalpy method, and
its corresponding governing equation is expressed as follows (Zhang et al., 2023):

19
$$\rho_{\rm pcm} \frac{\partial H_{\rm pcm}}{\partial t} = \lambda_{\rm pcm} \nabla^2 T_{\rm pcm}$$
(2)

$$H_{\rm pcm} = h + \Delta h \tag{3}$$

21
$$h = \int_{T_0}^{T_{\text{pcm}}} c_{p,\text{pcm}} dT_{\text{pcm}}$$
(4)

22

8

$$\Delta h = \beta \gamma \tag{5}$$

where H_{pcm} , h, Δh , and γ are the enthalpy, sensible heat enthalpy, phase change enthalpy, and latent heat of the PCM, respectively, the subscript pcm represents the pure PW-based PCM, and the specific value of the liquid fraction β of the PCM can be defined using the following segmental function (Peng et al., 2022):

$$\beta = \begin{cases} 0T_{\rm pcm} < T_{\rm s} \\ \frac{T_{\rm pcm} - T_{\rm s}}{T_{\rm l} - T_{\rm s}} T_{\rm l} < T_{\rm pcm} < T_{\rm s} \\ 1T_{\rm pcm} > T_{\rm l} \end{cases}$$
(6)

where T_s and T_l are the initial melting temperature and complete melting temperature of the PCM, respectively.

C

The energy conservation equation for the solid aluminum portion of the fin framework and the Sshaped liquid cooling plate can be characterized by:

6

12

18

$$\frac{\partial}{\partial t}(\rho c_p T) = \nabla \cdot (\lambda \nabla T) \tag{7}$$

7 3.2.2 Governing equations of the TEC domain

8 The governing equation of the TEC domain can be split into two parts: the heat conduction domain 9 and the electric field domain. Within the heat conduction domain, ceramic plates, copper electrodes, 10 and p/n type thermoelectric legs are subject to the following energy conservation equations (Luo, D. 11 et al., 2023c):

$$\frac{\partial}{\partial t}(\rho_{\rm m}c_{p,{\rm m}}T_{\rm m}) = \nabla \cdot (\lambda_{\rm m}\nabla T_{\rm m}) + S_{\rm m}^{\rm T}$$
(8)

where \dot{S} is the energy source term, and the subscript m denotes the material of each component of the thermoelectric cooler. As the electric current flows through both the p/n-type thermoelectric leg and the copper conductor, it results in the generation of Joule heat. Simultaneously, Peltier heat and Thomson heat are also produced within the p/n-type thermoelectric leg (Tang et al., 2023). The specific expression for \dot{S}_m is as follows (Luo, D. et al., 2023c):

$$S_{\rm m}^{\Box} = \begin{cases} \sigma_{\rm p}^{-1}(T)\vec{J}^{2} - T_{\rm p}\vec{J}^{-1} \cdot \nabla \alpha_{\rm p}(T) - \frac{\partial \alpha_{\rm p}(T)}{\partial T}T\vec{J} \cdot \nabla T_{\rm p}; & \text{p-type thermoelectric leg (9-1)} \\ \sigma_{\rm n}^{-1}(T)\vec{J}^{2} - T_{\rm n}\vec{J}^{-1} \cdot \nabla \alpha_{\rm n}(T) - \frac{\partial \alpha_{\rm n}(T)}{\partial T}T\vec{J} \cdot \nabla T_{\rm n}; & \text{n-type thermoelectric leg (9-2)} \\ \sigma_{\rm co}^{-1}(T)\vec{J}^{2}; & \text{copper electrode (9-3)} \\ 0; & \text{ceramic (9-4)} \end{cases}$$
(9)

19 where \vec{J} , σ^{-1} , and α denote the current density vector, electrical resistivity, and Seebeck coefficient, 20 respectively. The subscripts co, p, and n represent the copper electrode, p-type thermoelectric leg, and 21 n-type thermoelectric leg, respectively. For p/n type thermoelectric legs, the terms in Eqs (9-1) and (9-22 2) from left to right represent Joule heat, Peltier heat, and Thomson heat, respectively (Luo, D. et al., 1 2023a).

The electric field conservation equations are used for characterizing p-type thermoelectric legs, ntype thermoelectric legs, and copper electrodes of the TEC within the electric field domain (Luo, D. et al., 2023d):

_

$$\vec{E} = -\nabla\phi + \alpha_{\text{p,n}}(T)\nabla T \tag{10}$$

6

5

$$\vec{J} = \sigma_{\rm m} \vec{E} \tag{11}$$

$$\nabla \cdot \vec{J} = 0 \tag{12}$$

8 where \vec{E} and ϕ denotes the electric field vector density and the electric potential, respectively.

9 3.2.3 Governing equations of the fluid domain

Utilizing the following transient computational fluid dynamics equations to characterize the fluid
domain of the cooling medium inside the S-shaped liquid cooling plate (Luo, D. et al., 2023b):

12
$$\frac{\partial}{\partial t} \left(\rho c_p T \right) + \nabla \cdot \left(\rho c_p \vec{v} T \right) = \nabla \left(\lambda \nabla T \right)$$
(13)

13
$$\frac{\partial}{\partial t}(\vec{\rho v}) + \nabla \cdot \left(\vec{\rho v v}\right) = -\nabla p + \nabla \cdot \left(\mu \nabla \vec{v}\right)$$
(14)

14
$$\frac{\partial \rho}{\partial t} + \nabla \cdot \left(\rho \vec{v} \right) = 0 \tag{15}$$

15 where μ , *p*, and \vec{v} denote the dynamic viscosity, pressure, and velocity vectors, respectively. Eqs. (13)-16 (15) represent the energy conservation, momentum conservation, and mass conservation equations for 17 the transient state, respectively. The determination of the specific flow pattern of the coolant depends 18 on the Reynolds number, which can be determined using the following equation:

$$Re = \frac{u \times d_{\rm h}}{\mu} \tag{16}$$

where *u* and d_h are the coolant flow speed and the hydraulic diameter of the channel, respectively. The coolant flow rate is fixed as 0.01 kg/s herein, resulting in a calculated Reynolds number of 3360, which surpasses 2300. Consequently, the simulations in this work adopt the realizable *k*- ε turbulence model (Li, M. et al., 2023), which transport equations include:

24
$$\rho \frac{\partial k}{\partial t} + \rho (\vec{v} \cdot \nabla) k = \nabla \cdot \left[\left(\mu + \frac{\mu_{\rm T}}{\sigma_{\rm k}} \right) \nabla k \right] + p_{\rm k} - \rho \varepsilon$$
(17)

$$\rho \frac{\partial \varepsilon}{\partial t} + \rho(\vec{v} \cdot \nabla)\varepsilon = \nabla \cdot \left[\left(\mu + \frac{\mu_{\rm T}}{\sigma_{\varepsilon}} \right) \nabla \varepsilon \right] + C_1 \rho S \varepsilon - C_{\varepsilon 2} \frac{\rho \varepsilon^2}{k + \sqrt{v_1 \varepsilon}}$$
(18)

2 with

$$C_{1} = max \frac{1}{4} 0.43, \frac{\eta}{5+\eta} \frac{\mu}{5}, \eta = \frac{Sk}{\varepsilon}$$
(19)

3

1

$$\mu_{\rm T} = \rho C_{\mu} \frac{k^2}{\varepsilon}, C_{\mu} = \frac{1}{A_0 + A_{\rm s} \frac{k}{\varepsilon} U^*}$$
(20)

5 where *k*, p_k , and ε are the turbulence kinetic energy, shear production of turbulence kinetic energy, and 6 turbulence kinetic energy dissipation rate, respectively, and the values of the model constants $C_{\varepsilon 2}$, σ_k , 7 σ_{ε} , and A_0 are 1.9, 1.0, 1.2 and 4.0, respectively. The specific parameters information can be found in 8 Ref. (Fu et al., 2016).

9 Eqs (1)-(20) mentioned above are basic governing equations of the transient thermal-electric-fluid 10 multi-physical field. Commonly used numerical computational methods for solving these differential 11 equations include the finite volume, finite element, and finite difference methods (Luo, D. et al., 2023c). 12 In this work, the backward difference method is used for the discretization of the time variable, and 13 the finite element method is chosen for discretizing the space variables.

14 *3.3 Boundary conditions of the numerical model*

15 Based on the commercial software COMSOL, numerical simulations of the aforementioned 16 transient thermal-electric-fluid multi-physical field numerical model are performed. The simulation 17 starts at 0 s with a time step of 0.5 s, and the initial temperature is set as 303.15 K, corresponding to 18 the ambient temperature. A discharge time of 270 min is selected in this work, to explore whether the 19 battery temperature, temperature difference, and PCM melting exceed the limits when the system 20 reaches a stable state after multiple charging and discharging cycles. For the TEC, the copper electrode 21 located at the current inflow end is specified as the terminal, with the copper electrode at the current 22 outflow end designated as the ground. For the S-shaped liquid cooling plate, set inlet boundary 23 conditions on the surface where the cooling medium enters, with a mass flow rate set at 0.01 kg/s and 24 an inlet temperature of 303.15 K. Meanwhile, the outlet surface of the cooling medium is treated with 25 a standard atmospheric pressure as the outlet boundary condition. Assign heat loss boundary conditions 26 to the surfaces of the BTMS exposed to the external environment, with a natural convection heat transfer coefficient specified as 5 W·m⁻²·K⁻¹. 27

1 3.4 Grid independence examination

2 Finer grid size is helpful to enhance calculation precision but is accompanied by a notable increase 3 in computational time. Therefore, conducting a grid independence examination is essential to strike 4 the optimal balance between accuracy and computational efficiency. The grid independence analysis 5 conducted in this work is based on Case 1, utilizing four grid numbers with a gradual increase: 491575, 6 861504, 1648287, and 2436493. Before initiating the grid independence examination, it is essential to 7 set the simulation conditions, comprising a battery discharge rate of 3 C, a TEC operating current of 3 8 A, and fin length and thickness of 5 mm and 2 mm, respectively. The variation of the maximum 9 temperature with time for different grid numbers is showcased in Fig. 3(a). When the grid number hits 10 1648287, the results demonstrate that the maximum temperature closely approximates that of 2436493 grids, with negligible deviation. Therefore, to achieve a compromise between computational precision 11 12 and time consumption, a grid number of 1648287 is chosen in this work. Fig. 3(b) gives specific grid 13 details of the BTMS at this chosen grid number.





16 *3.5 Experimental validation*

14

17 To verify the accuracy of the developed transient thermal-electric-fluid multi-physics field 18 numerical model, experimental data from previously published literature is compared with the model 19 results in this work. Firstly, a three-dimensional geometric model of the BTMS in Ref. (Jiang et al., 2019) is established, which integrates TECs and PCMs. Then, a finite element model for the BTMS is 20 built and its performance is predicted by the transient thermal-electric-fluid multi-physics field 21 22 numerical model. During numerical simulations, the boundary conditions are consistent with the 23 experimental conditions in Ref. (Jiang et al., 2019), to avoid deviations in the results caused by other 24 factors. Fig. 4 illustrates a comparison of the maximum temperature between the experimental data in published literature and the simulation results in this work. It can be observed that the simulation results are in good agreement with the experimental data, with an average deviation of about 0.92 K within 7200 s. This tiny deviation indicates that the transient thermal-electric-fluid multi-physics field numerical model can be used to precisely evaluate the thermal performance of the BTMS, which further highlights the reasonability and credibility of the following results.



6

7 Fig. 4. Comparison of the maximum temperature between numerical results and experimental results.

8 **4. Results and discussion**

9 This work assesses the thermal performance of the BTMS by considering key indicators such as the 10 maximum temperature and temperature difference of the battery pack and the liquid fraction of the 11 PCM. Specifically, the maximum temperature is defined as the maximum temperature on the surface 12 of all batteries, and the maximum temperature difference is derived from the difference between the 13 maximum and minimum temperatures among different batteries. Also, the liquid fraction of the PCM 14 is calculated by Eq. (6).

15 4.1 Overall description of the BTMS simulation results

The temperature distribution of the complete BTMS and the battery pack, as well as the liquid fraction distribution of the PCM for both cases, are shown in Fig. 5. The simulation conditions used herein are the same as those used in the grid independence examination. Fig. 5(a) illustrates the overall temperature distribution contour of the BTMS. In Case 1, the system displays a lower overall temperature than in Case 2. Additionally, in Case 2, both the fin framework and the PCM in the middle part indicate substantially higher temperatures compared to Case 1. Fig. 5(b) exhibits the temperature

1 distribution contour of the battery pack in both cases. Observably, Case 2 indicates a larger high-2 temperature area and less temperature uniformity. The difference between Case 1 and Case 2 can be 3 attributed to the variation in the TEC arrangement. In Case 1, six TECs are placed on both the front 4 and rear of the fin framework, with a shorter distance between TECs on each side. As a result, this 5 configuration enhances the cooling efficiency of the battery and PCM. Fig. 5(c) illustrates the liquid fraction contour of the PCM in both cases. Specifically, in Case 1, only the PCM in direct contact with 6 7 the battery is melted, while in Case 2, a larger part of the PCM located in the central region has 8 undergone melting. This difference can be attributed to the higher heat accumulation in the central 9 region of the PCM in Case 2. Additionally, the temperature distribution contour of batteries depicted in Fig. 5(b) showcases that the maximum temperature in Case 2 is already higher than the limitation 10 11 of 323.15 K based on the given initial conditions. Thus, further optimization of the proposed BTMS is 12 required in subsequent investigations.



13

Fig. 5. Numerical results of the BTMS. (a) Temperature distribution contours of the complete BTMS; (b) Temperature
 distribution contours of the battery pack; (c) Liquid fraction distribution contours of PCMs.

16 4.2 Effect of fin length

The heat transfer efficiency among the TEC, PCM, and battery is mainly contingent on the dimensions of the fin framework, especially the fin length and thickness. In this work, the fin length is first optimized. Once the optimal fin length is determined, we proceed to optimize the fin thickness. Considering that the thickness of the PCM is 8 mm, various fin lengths (1 mm, 3 mm, 5 mm, 7 mm)
not exceeding 8 mm are selected for optimizations while maintaining the discharge rate, TEC input
current, and fin thickness constant at 3 C, 3 A, and 2 mm, respectively.

4 Figs 6(a) and 6(b) display variations in maximum temperature and temperature difference, 5 respectively. It is clear that for both cases, an increase in fin length leads to a decrease in both the maximum temperature and temperature difference of batteries. Specifically, as the fin length increases 6 7 from 1 mm to 7 mm, the maximum temperature decreases from 334.35 K to 315.85 K for Case 1, along 8 with a reduction in the temperature difference from 4.14 K to 2.39 K. Correspondingly, in Case 2, the 9 maximum temperature decreases from 335.99 K to 318.65 K, and the temperature difference decreases from 4.60 K to 3.42 K. The primary cause is that elongating the fin length diminishes the distance 10 between the fin framework and battery pack, concurrently augmenting the contact area between the 11 aluminum fin framework and PCM. Consequently, this enhances the heat transfer among the TEC, 12 PCM, and battery. 13







According to Fig. 6(b), it is worth noting that for fin lengths less than 7 mm, the maximum battery 16 17 temperature difference exhibits distinct phases of rapid increase, stabilization, followed by a rapid increase, and eventual leveling off. However, with a fin length of 7 mm, the temperature difference 18 experiences a rapid increase and then stabilization. The primary cause is that with a fin length below 19 20 7 mm, during the initial phase of battery discharge, the maximum temperature remains below the 21 melting point of PCMs, resulting in a rapid increase in the maximum temperature and temperature 22 difference. However, when the maximum temperature reaches the melting point, the rate of increase 23 in the temperature difference slows down. With the discharge proceeding, the PCM begins melting, 24 resulting in a reduction in its ability to control temperature and a rapid increase in the temperature

difference between batteries. As the PCM melts further, both the maximum temperature and temperature difference tend to stabilize. Nevertheless, with a fin length of 7 mm, it becomes evident that the PCM remains largely unmelted, resulting in the temperature difference going through a mere rapid increase phase followed by stabilization.

Fig. 7 shows the battery pack temperature distribution contours at 270 min. It is evident that increasing the fin length can effectively lower the maximum battery temperature and high-temperature range in both Case 1 and Case 2. Additionally, the battery surface temperature closer to the TEC shows a more pronounced decrease with the increase in fin length.



9

10 Fig. 7. Contours of the battery pack temperature distribution under different fin lengths at 270 min.

11 The liquid fraction of PCMs under different fin lengths is showcased in Fig. 8(a). It is evident that 12 during the initial phase of battery discharge, the PCM does not undergo melting. However, as the 13 discharge time progresses, there is a rapid rise in the liquid fraction, which subsequently reaches a 14 steady level. Combined with Fig. 6(a), it is observable that as the discharge commences, the maximum 15 battery temperature remains under the melting point of PCMs, thus, the PCM does not melt. Once the 16 maximum temperature attains the melting point of PCMs, the PCM undergoes melting, resulting in a 17 rapid rise of its liquid fraction. Eventually, as the discharge progresses, the PCM liquid fraction stabilizes. Increasing the fin length results in a decrease in the liquid fraction of PCMs in both cases. 18 19 When the fin length is extended from 1 mm to 7 mm, the liquid fraction of PCMs decreases by 0.636

for Case 1 and by 0.523 for Case 2. The liquid fraction distribution contour of PCMs at 270 min is showcased in Fig. 8(b). At a fin length of 1 mm, the PCM adjacent to the battery pack undergoes complete melting in both cases, with Case 2 exhibiting additional melting in the middle portion of the PCM compared to Case 1. With an increase in fin length to 7 mm, the PCM melting does not occur in

5 Case 1, but in Case 2, the region directly touching the battery starts to melt.





9 In summary, the greater the fin length, the better the thermal performance of the BTMS. Considering
10 the geometric limitation, the optimal fin length of 7 mm is suggested.

11 4.3 Effect of fin thickness

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Apart from the fin length, the fin thickness is another crucial factor influencing the thermal performance of the BTMS. Investigations are conducted with fin thickness ranging from 1 mm to 4 mm, while maintaining the fin length, TEC input current, and discharge rate remain constant at 7 mm, A, and 3 C, respectively.

Figs 9(a) and 9(b) illustrate the variation of maximum temperature and temperature difference under 16 17 different fin thicknesses. Increasing the fin thickness increases the heat transfer area among the fin and 18 PCM, decreasing the maximum battery temperature for both cases. Specifically, when the fin thickness 19 is increased from 1 mm to 4 mm, the maximum temperature decreases from 316.69 K to 314.50 K for 20 Case 1 and from 319.30 K to 317.67 K for Case 2. However, the temperature difference experiences a 21 slight uptick as the fin thickness increases. Specifically, as the fin thickness increases from 1 mm to 4 22 mm, the temperature difference rises from 2.31 K to 2.39 K in Case 1 and from 3.37 K to 3.62 K in 23 Case 2. Combined with Fig. 6, it can be concluded that compared to the fin thickness, the increase in 24 heat transfer area resulting from adjustments in fin length is more responsive to heat transfer

- 1 enhancement of the fin framework. Besides, it is worth noting that for all configurations, Case 1
- 2 consistently demonstrates lower maximum temperatures and temperature differences than Case 2.



3 4

Fig. 9. Effect of fin thickness. (a) Maximum temperature; (b) Temperature difference.







Fig. 10 gives the battery pack temperature distribution contours at 270 min. With the increase in fin thickness, the high-temperature range of the battery pack is immensely relieved, and the battery pack exhibits a greater temperature uniformity. Case 2 enables a higher temperature and a larger hightemperature range in the battery pack compared to Case 1. This variance can be attributed to the fewer 1 TECs and greater distance from the battery pack to the TEC within Case 2.

2 The liquid fraction of PCMs under different fin thicknesses is illustrated in Fig. 11(a). As the 3 thickness of the fin increases, there is a decrease in the liquid fraction of the PCM. In Case 1, when 4 discharging up to 270 min with a fin thickness of 1 mm, the liquid fraction of PCMs is 0.039, while 5 the PCM remains largely solidified when the fin thickness is increased to 3 mm and above. Besides, 6 the liquid fraction of PCMs in Case 2 is quite greater than that in Case 1, due to the fewer TECs and 7 greater distance from the battery pack to the TEC. Fig. 11(b) illustrates the liquid fraction contours of 8 PCMs at 270 min. With an increase in fin thickness, the melting region of the PCM gradually 9 diminishes. In Case 1, only a small amount of PCMs near the battery area undergoes melting, while in 10 Case 2, a significant portion is melted. Apparently, Case 1 exhibits a better thermal performance than





12

Fig. 11. Liquid fraction of PCMs at different fin thicknesses. (a) The change of liquid fraction of PCMs during battery
 discharge; (b) Liquid fraction distribution contours of PCMs at 270 min.

Based on the above analysis, the temperature difference of batteries at the fin thickness of 4 mm is slightly higher than that at the fin thickness of 3 mm. Although the increase of fin thickness can further reduce the maximum temperature and alleviate the melting of PCMs, it will deteriorate the temperature difference and increase the system weight as well. Consequently, the optimal fin thickness of 3 mm is suggested.

20 4.4 Effect of the TEC input current

An extremely high current input can lead to a substantial increase in power consumption, while insufficient current inputs may fail to effectively regulate the temperature of the battery pack. Therefore, it is vital to investigate the effect of TEC input current on thermal performance. Herein, four different TEC input currents (2 A, 3 A, 4 A, and 5 A) are employed to perform studies while keeping the fin length at 7 mm, fin thickness at 3 mm, and battery discharge rate at 3 C. Furthermore, with an increase in the input current, the temperature difference between the two ends of the TEC also experiences an increase, and the increased temperature differential deteriorates the cooling efficiency of the TEC. Consequently, an S-shaped liquid cooling plate is employed on the hot side of the TEC to lower its temperature difference.

6 Fig. 12(a) showcases the maximum battery temperature variation for different TEC input currents. 7 Increasing the TEC input current leads to a higher cooling power, thus lowering the maximum 8 temperature for both cases. The maximum temperature exhibits a significant reduction when the TEC 9 input current is increased from 2 A to 5 A, with Case 1 experiencing a drop from 317.88 K to 309.66 K and Case 2 showing a decrease from 321.47 K to 311.38 K. Furthermore, at the same TEC input 10 current, the maximum temperatures of Case 1 are consistently lower than those of Case 2. 11 Significantly, even at the TEC input current of 2 A, the maximum temperature does not exceed 323.15 12 K for either case. The variation in temperature difference under different TEC input currents is 13 showcased in Fig. 12(b). Due to the rapid response of the TEC, during the initial discharge phases, 14 15 raising the TEC input current leads to a temperature difference increase. However, as time passes, the 16 temperature difference alteration becomes smooth. At 270 min, when the TEC input current is raised 17 from 2 A to 5 A, the temperature difference decreases from 3.65 K to 3.51 K for Case 1 and from 2.46 18 K to 2.19 K for Case 2. It is concluded that variations in current primarily impact the maximum temperature, with a limited effect on the temperature difference. Details of the battery surface 19 20 temperature distribution when the battery pack is discharged for 270 min can be found in Fig. 13.



Fig. 12. Effect of the TEC input current. (a) Maximum temperature; (b) Temperature difference.

21

The variation of PCM liquid fraction concerning different TEC input currents is depicted in Fig.
14(a). An increase in the TEC input current results in a decrease in the PCM liquid fraction. When the

- TEC input current reaches 3 A or higher in Case 1 and 4 A or higher in Case 2, the PCM does not undergo melting. At the TEC input current of 2 A, the PCM liquid fraction is 0.147 for Case 1 and 0.685 for Case 2, while they respectively decrease to 0.002 and 0.181 at the TEC input current of 3 A. Details of the liquid fraction contour of PCMs when the battery is discharged to 270 min are shown in Fig. 14(b). At a constant TEC input current of 2 A, in Case 1, only the PCM region close to the battery pack undergoes melting, whereas in Case 2, the PCM melts except for the area near the TEC. As the
- 7 TEC input current rises, the extent of PCM melting progressively diminishes.



8 9







11 Fig. 14. Liquid fraction of the PCM at different TEC input currents. (a) The change of liquid fraction of the PCM during

1 battery discharge; (b) Liquid fraction distribution contours of the PCM at 270 min.

To summarize, the thermal performance of the system is effectively improved with the increase of the TEC input current. However, when the TEC input current reaches 3 A, the thermal performance of the system already meets the requirements well, and as the current further increases, the performance improvement decreases, accompanied by an increase in energy consumption. For this reason, the optimal TEC input current value of 3 A is suggested.

7 *4.5 Effect of battery discharge rate*

8 To comprehensively explore the exceptional performance of the BTMS, this section extends the 9 battery discharge rate. Employing the previously mentioned optimal structure, the TEC input current 10 is increased to 5 A to evaluate the system's performance at extreme battery discharge rates of 4 C and 11 5 C.



12

Fig. 15. Effect of different battery discharge rates. (a) Maximum temperature; (b) Temperature difference; (c) The liquid
fraction of PCMs; (d) Contours of the battery pack temperature distribution at 270 min; (e) Liquid fraction distribution
contours of PCMs at 270 min.

Figs 15(a), (b), and (c) display the maximum temperature, temperature difference, and PCM liquid fraction with discharge time for different discharge rates, respectively. The increase in the battery discharge rate leads to increased values for maximum temperature, temperature difference, and PCM

1 liquid fraction in both cases. Under a discharge rate of 4 C, Case 1 exhibits a maximum temperature 2 of 316.39 K, a temperature difference of 3.08 K, and a PCM liquid fraction of 0.018. Meanwhile, for 3 Case 2, these values are 319.75 K, 3.94 K, and 0.246, respectively. Upon elevating the discharge rate 4 to 5 C, Case 1 exhibits values of 323.01 K for maximum temperature, 4.72 K for temperature 5 difference, and 0.496 for the liquid fraction of PCMs. Meanwhile, for Case 2, these values are 328.89 K, 6.11 K, and 0.829. More about the temperature distribution contours of batteries when discharged 6 7 for up to 270 min can be found in Fig. 15(d). It can be found that the area of the high-temperature 8 region in Case 2 is significantly higher than that in Case 1 in the same situation. Fig. 15(e) shows the 9 liquid fraction contour of PCMs at 270 min. In Case 1, with a discharge rate of 4 C, it is evident that the PCM remains largely unmelted. However, when the discharge rate is elevated to 5 C, the portion 10 11 of the PCM situated far from the TEC begins to melt. In Case 2, with a discharge rate of 4 C, the PCM 12 in direct proximity to the battery pack has melted, whereas as the discharge rate is further raised to 5 C, all PCMs reach a state of melting. 13

From the above description, it is evident that at a discharge rate of 4 C, both cases successfully keep the maximum temperature below 323.15 K and the temperature difference below 5 K. Moreover, the melting of the PCM is effectively controlled. In the event of a battery discharge rate of 5 C, Case 2 slightly exceeds the temperature limit with regards to maximum temperature and temperature difference, while Case 1 stays within the desired range. It is noteworthy that sustained discharge at a high rate of 5 C is not frequently encountered in everyday usage. Therefore, both cases showcase outstanding performance even at this elevated discharge rate.

21 **5.** Conclusions

22 In this work, a BTMS integrated with TECs and PCMs is developed to ensure the temperature 23 working environment of batteries. The system applies a stacked design, which can be extended to 24 achieve wider applications. Meanwhile, in response to the challenge of a rapid increase in battery 25 temperature and temperature difference due to excessive PCM melting after long charging and 26 discharging cycles, a novel fin framework is employed to enhance the heat transfer among the TEC, 27 battery, and PCM. To obtain the optimal fin parameters and analyze the thermal performance of the 28 BTMS, a transient thermal-electric-fluid multi-physical field numerical model is established. The key 29 findings are outlined below:

(1) The configuration in Case 1 is more favorable compared to the one in Case 2, due to the fewer
 TECs and greater distance from the battery pack to the TEC within Case 2. Under the optimal fin

parameters, both cases are able to adhere to the battery temperature requirements, except for Case 2
wherein the maximum temperature and temperature difference exceed the limit values at an ultrahigh
discharge rate of 5 C.

4 (2) Compared to fin thickness, fin length has a more significant impact on the system thermal 5 performance. The maximum temperature, temperature difference, and PCM liquid fraction decrease 6 with an increase in both fin length and thickness, with a tiny influence of temperature difference by 7 the fin thickness. The optimal fin framework with the fin length of 7 mm and fin thickness of 3 mm 8 enables the BTMS to effectively control the melting of PCM and the battery temperature even for a 9 stable state after long charging and discharging cycles.

(3) Increasing the TEC input current will result in a decrease in the maximum temperature and PCM
liquid fraction, with minimal impact on the temperature difference. At a 3 C discharge rate, the optimal
TEC input current of 3 A is obtained, with the maximum temperature, temperature difference, and
PCM liquid fraction of 315.10 K, 2.39 K, and 0.002, respectively for Case 1, and 318.24 K, 3.60 K,
and 0.181, respectively for Case 2.

(4) When the battery discharge rate increases, the TEC input current should also increase
accordingly to ensure the battery's temperature performance. At a high discharge rate of 5 C, the BTMS
configuration in Case 1 can maintain the optimal battery operating temperature environment with a
TEC input current of 5 A, while the maximum temperature and temperature difference in Case 2 exceed
the limits.

(5) In future studies, we will further optimize the parameters of the TEC to improve the thermal
 performance of the BTMS. In addition, we will comprehensively consider the thermal performance
 and overall energy consumption of the BTMS, and explore a control strategy to achieve dynamic
 temperature regulation under actual conditions.

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