

Dynamic response of hybrid carbon fibre laminate beams under ballistic impact

Yuwu Zhang¹, Tao Liu^{1,2*}, Zeyuan Xu¹

¹Centre for Structural Engineering and Informatics

²Composites Research Group

Faculty of Engineering, University of Nottingham,

University Park, Nottingham, NG7 2RD, U.K.

Email: Tao.Liu@nottingham.ac.uk, Tel: + 44 (0)115 7484059

Abstract

This novel hybrid fibre composites combining stiff composites with soft composites are developed to improve the ballistic impact resistance of composite beams while maintaining good quasi-static loading bearing capacity. The ballistic impact performance of the hybrid beams have been investigated experimentally at a projectile velocity range of $50 \text{ ms}^{-1} \leq v_0 \leq 300 \text{ ms}^{-1}$, including ballistic limits, failure modes, energy absorption capacity and the interaction between stiff and soft composite parts. For each type of monolithic beams, i.e. stiff, soft and hybrid monolithic beams, three categories of failure modes have been identified: minor damage with rebound of projectile at the low impact velocities, fracture of beam at the medium impact velocities and perforation of beam at the high impact velocities. The critical velocity of hybrid monolithic beam was similar to that of the soft monolithic beam under the same failure mode, and higher than that of the stiff monolithic beam. For the sandwich beams with stiff, soft and hybrid face sheets, the failure modes were similar to those of the monolithic beams. Among the monolithic beams, the hybrid and soft monolithic beams exhibited better energy absorption capacity than the stiff monolithic beams. As for the sandwich beams, the hybrid-face sandwich beams absorbed more kinetic energy of projectile

25 than the soft-face sandwich beams at higher projectile velocity. The advantages of the stiff/soft
26 hybrid construction include: (i) at lower impact velocity, the soft composite part survived with
27 negligible damage under impact; (ii) due to the buffer effect of the soft part at the front face,
28 stress distribution within the stiff part of the hybrid monolithic beams is more uniform than
29 that of the stiff monolithic beams.

30 *Keywords:* Fibre composites, hybrid beams, ballistic impact, failure modes, energy absorption
31 capacity

32 **1. Introduction**

33 Fibre reinforced composites have been attractive in both military and civilian applications due
34 to their outstanding mechanical properties [1]. It has been demonstrated that the lightweight
35 structures made of fibre composites possess excellent performances to resist ballistic impact
36 when the composites laminate is in $[0^\circ/90^\circ]$ cross-ply lay-up [2, 3]. Cunniff [3] reported that
37 the ballistic limit of fibre composites are proportionally increasing with the Cunniff velocity
38 c^* of the fibre filament and can be defined as follow

$$39 \quad c^* = \left(\frac{\sigma_f \varepsilon_f}{2\rho_f} \sqrt{\frac{E_f}{\rho_f}} \right)^{1/3} \quad (1)$$

40 where σ_f and ε_f are the tensile strength and failure strain of fibres, respectively, while E_f
41 and ρ_f are the tensile Young's modulus and density of fibres, respectively. Thus, the Cunniff
42 velocity c^* is governed by two material properties, i.e. specific strain energy $\frac{\sigma_f \varepsilon_f}{2\rho_f}$ and

43 longitudinal wave speed $\sqrt{\frac{E_f}{\rho_f}}$ of fibres. This approach provides a guidance in development of

44 the fibre composites of high ballistic limit [4, 5]. However, it does not give any insight into the
45 effect of matrix on the ballistic impact response of fibre composites. Matrix has the functions
46 of bonding fibre reinforcements together and transferring stress between them [6]. It can also

47 protect fibres against abrasion as well as adverse environmental impacts. Though the matrix
48 itself is unable to dissipate a large amount of energy, it has an indirect effect on the energy
49 absorption of fibre composites via load transfer with the broken fibres. Lee et al. [7] argued
50 that, compared with soft matrix, stiff matrix resulted in less deformation degree of fibre
51 reinforcements and more significant stress concentration. In addition, the enhancement of
52 fibre/matrix bonding strength reduces ballistic impact resistance of fibre composites. Ruijter et
53 al. [8] analysed the effect of matrix stiffness, at the range of 10^{-4} to 4 GPa, on the ballistic
54 impact protection of Twaron[®] fabric composites via a series of experimental measurements.
55 They found that the ballistic limit of the composites strongly depended on the matrix stiffness,
56 and the highest ballistic limit was achieved when the matrix stiffness was at the range of 0.01
57 to 1 GPa. Beyond the stiffness of 1 GPa, the matrix restricted the deformation of fibres, while
58 the matrix was unable to provide enough adhesion to bond the fibres together if below the
59 stiffness of 0.01 GPa. Karthikeyan et al. [9] investigated the effect of shear strength on the
60 ballistic response of laminated composites, including cured and uncured carbon fibre
61 composites, and polyethylene fibre composites (Dyneema[®]) with two different matrices. They
62 reported that the Cunniff velocity failed to characterise the ballistic resistance of fibre
63 composites, and the ballistic limit of the composites increased with decrease of shear strength
64 of the matrix. The matrix with lower shear strength was able to relieve more stress gradient of
65 cross-ply laminates through interlaminar shearing [10], thus a wider range of membrane
66 stretching in each layer was achieved which ensured higher impact force resistance. It was
67 reported that the soft matrix laminates failed progressively by tensile rupture of fibres under
68 ballistic impact [5, 9].

69 Although the composites with soft matrix exhibit better ballistic performance than the ones
70 with stiff matrix, it has limited ability to resist the out-of-plane bending force as well as in-
71 plane compression owing to microbuckling of fibres. Ashby and Brechet [11] proposed that

72 the hybrid material, which was a combination of two or more materials, could superimpose the
73 properties of each material and be multifunctional. It has been demonstrated that the hybrid
74 composite laminates reinforced by two or more types of fibres can offer better ballistic
75 performance than the laminates reinforced by only one type of fibre [5, 12-16]. As reported by
76 Pandya et al. [12], the ballistic limit was increased by adding E-galss fibre layers to carbon
77 fibre composites compared to the pure carbon fibre composites with the same thickness.
78 Bandaru et al. [13] investigated the different combinations of the fibre reinforced composites,
79 namely, glass fibre, carbon fibre and Kevlar fibre composites. They found that the Kevlar
80 composite laminate hybridized with carbon fibre layer possessed the best ballistic resistance,
81 and the ballistic performance could be improved by increasing the toughness of composites.
82 O'Masta et al. [5] investigated the penetration behaviour of the hybrid laminate combined two
83 types of ultrahigh molecular weight polyethylene (UHMWPE) fibre composites both with soft
84 matrix (Dyneema[®]). They reported that the penetration resistance of the multi-layer laminates
85 might benefit from the optimized stacking sequence of layers, i.e. the layer with higher
86 compressive strength and lower impendence as front face, and the layer with higher tensile
87 strength as back face. The existing research on ballistic impact of hybrid fibre composites
88 mainly focuses on the effect of hybridization of different types of fibre reinforcements
89 embedded in single type of matrix, i.e. either stiff or soft matrix. With regards to certain
90 structures, the requirements for stiffness and ballistic resistance are equally important, e.g. the
91 shell of an airplane nose subject to bird collision and the hood of an automobile subject to
92 bullets as well as debris impact. Hence, it is imperative to develop hybrid composites which
93 can not only guarantee structural stiffness but also resist high-velocity ballistic impact.
94 However, limited ballistic impact tests have been reported on the fibre composites hybridizing
95 stiff composite and soft composite, which may benefit from good ballistic resistance from the
96 soft part and good quasi-static loading bearing capacity from the stiff part. As the failure modes

97 of these two types of fibre composites are different, the mechanism of the interaction between
98 these two composites has not been well established. Although Larsson et al. [15] gave an
99 insight into the ballistic performance of the hybrid composites which combined stiff carbon
100 fibre composites with soft polyethylene fibre composites, the failure modes as well as energy
101 absorption capacity of the hybrid material containing soft and stiff composites are still unclear.
102 Sandwich structures with fibre composite face sheets and honeycomb core are multi-functional
103 lightweight structures owing to the good bending resistance and energy absorption capacity
104 [17-19]. As the deformation are bending governed when they subject to soft impact, the fibre
105 composite sandwich structures exhibit better soft impact resistance than the monolithic ones
106 [20, 21]. However, Russell et al. [20] reported that the fibre composite beams failed
107 catastrophically at a lower projectile impulse than the steel sandwich beams owing to the lower
108 ductility of the fibre reinforced polymer composites. In addition, the ballistic impact resistance
109 of sandwich structures improves negligibly compared to that of monolithic structures with the
110 same areal mass. This is owing to the fact that the ballistic impact is a kind of localised impact
111 that doesn't lead to significant bending of structure. It is inspired that replacing a part of stiff
112 face sheets of sandwich structures with the soft composites may overcome these problems. The
113 sandwich structures with stiff/soft hybrid face sheets are expected to not only prevent
114 catastrophic failure of stiff face sheets under soft impact but also exhibit better resistance under
115 ballistic impact. To date, the ballistic performance of this type of stiff/soft hybrid sandwich
116 structure has not been investigated.

117 This paper experimentally investigates the ballistic impact response of a novel hybrid
118 composite beam with stiff composites and soft composites, including the failure modes, energy
119 absorption capacity, and the effect of the interaction between the stiff/soft composite parts on
120 the deformation of hybrid beams. In the following sections of the paper, the experimental
121 materials and manufacturing process are described in Section 2, and the mechanical properties

122 of the constituent materials are presented in Section 3. In Section 4 and Section 5, the ballistic
123 impact methodology and experimental results are then discussed, respectively.

124 **Scope and novelty of this study**

125 The paper aims to investigate the ballistic impact performance of the novel stiff/soft hybrid
126 fibre composite beams in comparison with those of stiff and soft monolithic beams. The novelty
127 of this study includes

- 128 • The ballistic impact response of the hybrid fibre composite beams combining stiff
129 composites and soft composites is experimentally measured at different impact
130 velocities. The advantages of the hybrid beams are identified by comparing with the
131 ballistic impact response of traditional monolithic beams from the aspects of ballistic
132 limits, failure modes and energy absorption capacity.
- 133 • Both the ballistic resistance of novel stiff/soft hybrid monolithic beams and sandwich
134 beams is investigated owing to the different bending stiffness and applications.
- 135 • The effect of time scales of wave propagation in stiff and soft composite parts on the
136 failure modes and ballistic limits of beams is reported.
- 137 • The effect of the interaction between the stiff/soft composite parts on the deformation
138 and failure mechanism of each part of hybrid beams is analysed.

139 **2. Materials and manufacturing**

140 *2.1. Materials*

141 The laminated composite sheets, used as the monolithic beams and face sheets of sandwich
142 beams, were reinforced by Pyrofil TR50S 15K carbon fibres (diameter is 7 μm). The thickness
143 of each unidirectional fibre layer was 0.1 mm. The slow IN2 epoxy infusion resin and EF80
144 flexible epoxy resin, both supplied by Easy Composites Ltd, were used as the matrix materials
145 for manufacturing different types of fibre composites. Both of them are two part (resin and
146 hardener) epoxy resin system. The IN2 epoxy resin with low mixed viscosity (200-450 mPa·s)

147 is able to infuse through fibre reinforcements quickly, and becomes hard and brittle after full
148 cure. Hence, it is suitable for manufacturing resin infusion composites. As for the EF80 flexible
149 epoxy resin, it exhibits higher mixed viscosity (500-1200 mPa·s) than the IN2 epoxy resin. In
150 addition, it has the capacity of maintaining flexibility after full cure, and is therefore suitable
151 for the applications where the flexibility of fibre reinforced composite parts are required.
152 Throughout the paper, the fibre composites with IN2 epoxy infusion resin are termed stiff
153 composites and the ones with EF80 flexible epoxy resin are termed soft composites.
154 Owing to the different bending stiffness and structural applications from those of monolithic
155 composite beams, the sandwich beams were also investigated in this study. The phenolic resin-
156 impregnated aramid paper honeycombs, commercially known as Nomex[®] honeycombs, were
157 employed as the cores of the sandwich beams in this study owing to its high ratio of
158 strength/stiffness to density [22-25]. The manufacturing process of the Nomex honeycombs is
159 summarized as follow: the Nomex aramid paper layers made from random fibres are stacked
160 on each other and adhered by the thermoset epoxy adhesive strips at intervals. The hexagonal
161 unit cells were formed by expanding the paper layers along the stacking direction. Finally, the
162 expanded geometry was impregnated into phenolic resin to be coated and obtain the specific
163 density of the honeycombs. The density and out-of-plane thickness of the Nomex honeycomb
164 core were $\rho_h = 54 \text{ kgm}^{-3}$ and $H = 10 \text{ mm}$, respectively. Figure 1 (a) shows the in-plane structure
165 of its hexagonal unit cell. The single-wall thickness of the unit cell geometry is $t_h = t_f + t_r$,
166 where t_f and t_r are the thicknesses of the single aramid paper layer and phenolic resin layer,
167 respectively. However, the wall thickness of the unit cell geometry along the stacking direction
168 is $2t_h$ due to the expansion process. The characteristic cell size of the honeycombs is defined
169 as $L_C = \sqrt{3}L_h = 4.8 \text{ mm}$, with L_h as the edge length of the hexagonal unit cell.

170 2.2. Manufacturing

171 In this study, both the stiff and soft fibre reinforced composite panels were manufactured using
172 a vacuum assisted resin transfer moulding (VA-RTM) system. The unidirectional dry fibre
173 layers were arranged in a $[0^\circ/90^\circ]_n$ lay-up inside a mild steel mould, i.e. orthogonally stacking,
174 as shown in Fig. 1 (b). The steel mould had one outlet port located at the centre and four inlet
175 ports located at the four corners, both of diameter 2.5 mm. Eight bolts at the edges of the mould
176 were tightened to provide sufficient seal. Degassing of resin and gas tightness checking of VA-
177 RTM system were conducted before resin injection. A vacuum pump connected with the outlet
178 port created a vacuum environment in the mould to infuse the resin through the dry fibre layers.
179 For soft matrix, the compressed air of pressure 8 bars within a catch-pot was imposed to
180 facilitate the infusion of liquid resin. The ratios of resin to hardener by weight were 100 : 30
181 and 100 : 145 for manufacturing stiff composite panels and soft composite panels, respectively.
182 The infused composite panels were then cured for 7 h at 65 °C. To reduce the flaws caused by
183 cutting dry fibre layers, approximately 10 mm was removed from each edge of the panels after
184 demoulding.

185 Figure 1 (c) shows the sketch of a Nomex honeycomb core sandwich beam specimen used for
186 ballistic impact. Throughout this paper, the global coordinates are defined with the 3-axis
187 aligned with the out-of-plane direction of beams, and with the 1-axis and 2-axis representing
188 the in-plane directions of beams. Different types of face sheets used in sandwich beam
189 specimens are listed in Fig. 1 (b). All the face sheets and monolithic beams of total length
190 $L = 240$ mm and width $w = 40$ mm were cut from the cured laminated panels using a
191 diamond saw, and the Nomex honeycomb core was cut by a sharp blade to be the same
192 dimension as the laminated beams. The details of monolithic fibre composite beams (i.e. stiff
193 monolithic beam, soft monolithic beam and hybrid monolithic beam) and sandwich beams (i.e.
194 stiff-face sandwich beam, soft-face sandwich beam and hybrid-face sandwich beam) are
195 summarized in Table 1. According to this Table, the stiff and soft composite beams of different

196 thicknesses were used to assemble to form six types of beams with similar areal mass. n in the
197 $[0^\circ/90^\circ]_n$ lay-up architecture is determined to be 10, 5, 4 and 2, respectively, corresponding to
198 the panel thickness of $t=3.9$ mm, 1.9 mm, 1.6 mm and 0.8 mm, respectively. The thicknesses
199 of the stiff and soft monolithic beams were both $t=3.9$ mm, and the thickness of each face
200 sheet of the stiff-face and soft-face sandwich beams were both $t=1.6$ mm. For the hybrid
201 beams which comprised of stiff and soft composite parts with equal thickness, the thicknesses
202 of each composite part of the hybrid monolithic beam and hybrid-face sandwich beam were
203 $t=1.9$ mm and $t=0.8$ mm, respectively. Hence, the number of fibre layer in sandwich beams
204 was 4 less than that in monolithic beams. The fibre volume fractions and density of each
205 laminated composite part were approximately 50% and $\rho = 1380 \text{ kgm}^{-3}$, respectively.

206 Some additional steps were taken for assembling beams. The stiff and soft composite parts of
207 hybrid monolithic beams, and the face sheets of hybrid-face sandwich beams were glued
208 together, respectively, using the Loctite EA 9461[®] epoxy adhesive. The face sheets and
209 honeycomb cores of sandwich beams were glued together also using the Loctite EA 9461[®]
210 epoxy adhesive. In hybrid-face sandwich beams, the part contacted with the each side of the
211 Nomex honeycomb core was stiff part and soft part, respectively, as sketched in Table 1. In
212 addition, to ensure the ends of the sandwich beams can be end-clamped sufficiently, the Nomex
213 honeycomb core was filled with fast IN 2 epoxy resin, supplied by Easy Composites Ltd, over
214 the clamped portion of each length 40 mm. The assembled hybrid monolithic beams and
215 sandwich beams were then cured in the oven for 5 h at 60 °C with 25 KN transverse loading
216 applied on the beams to achieve better bonding. The areal mass of the epoxy adhesive per layer
217 was measured to be 0.14 kgm^{-2} , and all the assembled composite beams had similar areal mass
218 in the range of 5.12 - 5.40 kgm^{-2} .

219

220 3. Mechanical properties of the constituent materials

221 The quasi-static uniaxial tensile and compressive responses of the fibre reinforced composites,
222 and the quasi-static out-of-plane compressive response of Nomex honeycomb core were
223 measured using an Instron screw-driven testing machine at an applied nominal strain rate 10^{-3}
224 s^{-1} . There were five repeats for each type of test.

225 *3.1. Uniaxial tests on fibre reinforced composite sheet material*

226 The tension and compression tests on the stiff and soft fibre composite materials were
227 conducted using the methods described by the EN ISO 527-4 and ASTM D3410/B,
228 respectively. The aluminium tabs were adhered to the clamped ends of the rectangular
229 specimens for friction gripping during test. The uniaxial forces of the specimens were
230 determined by the load cell of the screw-driven testing machine, and the uniaxial strain of the
231 specimens were measured by a single Stingray F-146B Firewire camera video gauge. In tension,
232 the stiff and soft laminates both in $[0^\circ/90^\circ]$ and $\pm 45^\circ$ orientations were tested. However, only
233 the compressive response of the stiff laminate in $[0^\circ/90^\circ]$ orientation was measured as the
234 compressive response of the soft laminate in $[0^\circ/90^\circ]$ orientations was too weak to be measured
235 using the standard method. The specimens had a gauge length of 50 mm for tension test,
236 whereas had a gauge length of 12 mm for compression test in order to prevent Euler buckling.
237 Figure 2 (a) shows the measured nominal tensile and compressive stress versus strain relations
238 of the composite laminates in $[0^\circ/90^\circ]$ orientations. In the tension tests, the stiff and soft
239 composite laminates displayed **almost** identical linear elastic responses, with the tensile
240 strength of 535 MPa and elastic modulus of 34 GPa. It was observed that the stiff and soft
241 composite laminates had the same failure mechanism in tension, i.e. tensile fracture of fibre
242 reinforcements. In the compressive tests, the stiff composites displayed elastic-brittle response,
243 with the compressive strength was 221 MPa at nominal strain of 0.011.
244 In contrast, as the tensile response of the laminates in $\pm 45^\circ$ orientations was governed by the
245 shear of matrix, the laminates in this orientation were more ductile and had lower strengths

246 than those in $[0^\circ/90^\circ]$ orientations, see Fig. 2 (b). The stiff composites exhibit elastic-plastic
247 hardening response with the tensile strength of 187 MPa and nominal failure strain of 0.225.
248 However, the soft composites have significantly lower tensile strength and higher nominal
249 failure strain, which are 36 MPa and 0.36, respectively in $\pm 45^\circ$ orientations. The slight
250 hardening response of the soft composites after initial yield is governed by the fibre rotation
251 towards the tensile axis [9]. In addition, both the stiff and soft composites in $\pm 45^\circ$ orientations
252 failed with matrix cracking without fibre rupture.

253 *3.2. Out-of-plane compression tests on Nomex honeycomb core*

254 The quasi-static out-of-plane compression tests on the Nomex honeycomb core were conducted
255 using the same machine as that for testing the mechanical performance of fibre composite
256 laminates. The tested honeycomb core specimen had an in-plane dimension of length $L_L = 65$
257 mm and width $L_w = 65$ mm, with 175 unit cells. The transverse load F and deformation δ of
258 honeycomb core were measured by the load cell and two symmetrically installed Linear
259 Variable Differential Transformers (LVDT), respectively. The nominal compressive stress and
260 strain of the specimen were taken as $\sigma = F / A$ and $\varepsilon = \delta / H$, respectively, with
261 $A = 65 \times 65 \text{ mm}^2$ as the original cross-sectional area of the honeycomb core specimen. The
262 measured nominal compressive stress versus strain curve of the honeycomb core is plotted in
263 Fig. 2 (c). It indicates that the specimen shows a linear elastic mechanical behaviour before
264 achieving a peak compressive stress and has an abrupt softening after the peak stress, then
265 displays hardening followed by densification at a nominal compressive strain of $\varepsilon = 0.75$. The
266 compressive strength of the Nomex honeycomb core was measured to be $\sigma_s = 3.09 \text{ MPa}$.

267 **4. Ballistic impact test protocol**

268 Ballistic impact tests were conducted to investigate the failure modes and energy absorption
269 capacity of the monolithic and sandwich composite beams, and find out the advantages of the
270 hybrid beams. The sketch of the experimental setup developed by Turner et al. [26] is shown

271 in Fig. 3. A steel fixture with four M6 bolts at each end was used for fully clamping the beams.
272 The fixture was fully fixed to minimize shock and guarantee negligible energy of projectile
273 transmitted to the fixture. Both the fixture and beams were put into a transparent polycarbonate
274 cupboard to prevent projectile and debris of beams from flying out. The free span lengths of
275 the beams were 170 mm and the front faces of beams were positioned 200 mm from the muzzle
276 of the gas gun. The gas gun of barrel length 3.5 m, outer diameter 16 mm and internal diameter
277 13 mm was employed for accelerating a non-deforming steel spherical projectile of diameter
278 $d = 12.7$ mm and mass $M = 8.3$ g. The calibration test before measurement was conducted to
279 ensure the accelerated projectile impacted at the centre of the beams in all tests and no torsion
280 occurred in the beams during impact. Either compressed air or pressurised liquid nitrogen was
281 used to propel the projectile to various velocities in the range of $50 \text{ ms}^{-1} \leq v_0 \leq 300 \text{ ms}^{-1}$,
282 producing the initial kinetic energy of projectile in the range of $10.4 \text{ J} \leq E_{k_0} \leq 373.5 \text{ J}$. The
283 initial velocity of projectile was measured using two laser gates located at the open end of the
284 gas gun barrel and confirmed with a Phantom Mercury HS v 12.1 high speed camera. The high
285 speed camera was also used to capture the failure modes of beams and residual velocity of
286 projectile during ballistic impact. Typically, the frame rate and exposure time were 38,000 fps
287 and $10 \mu\text{s}$, respectively, and the resolution was 320×344 . The Dedolight Dedocool Standard 2-
288 light kit, which was able to concentrate an intense beam of light over a highly concentrated
289 area, was set outside the polycarbonate cupboard to meet the requirements of high speed
290 videography. In order to reflect more light into the high speed camera, a smooth aluminium
291 panel was placed at the other side of beams, opposite to the camera. In addition, the cross
292 sections of beams were painted to be white using marker pen for observing the deformation of
293 beams more clearly. It should be noted that we suppose the soft composite parts, which are in
294 hybrid monolithic and hybrid-face sandwich beams, act as a cushion that avoids the direct stiff

295 contact between non-deforming projectile and stiff composite part. Based on this assumption,
296 we set the projectile firstly impact the soft composites part of the hybrid beams.

297 **5. Results and discussion**

298 The experimental measurements for the six types of composite beams have been summarized
299 in Table 2, including the initial projectile velocity, residual projectile velocity, kinetic energy
300 of projectile transmitted to beams, and failure modes of beams.

301 *5.1. Impact responses of monolithic beams*

302 In this section, the responses of three types of monolithic composite beams under a series of
303 ballistic impact tests were investigated, and the failure modes of these beams at various
304 velocities are identified. The fracture mode discussed below is defined as the complete fracture
305 of beams, and the perforation mode as the beams perforated without complete fracture. The
306 critical velocity between two failure modes was calculated as the average value of the
307 maximum velocity that triggered the low-velocity failure mode and the minimum velocity that
308 triggered the high-velocity failure mode. Take the stiff monolithic beam for example, the
309 measured maximum velocity for rebound mode was 56 ms^{-1} , and the measured minimum
310 velocity for fracture mode was 67 ms^{-1} . Hence, the critical velocity between the rebound and
311 fracture modes of the stiff monolithic beam was 61.5 ms^{-1} .

312 *5.1.1. Stiff monolithic beam*

313 The back-face deflections of the stiff monolithic beams before failure as a function of time at
314 selected impact velocities are plotted in Fig. 4. The back-face deflections of beams are
315 measured through high speed photographs after ballistic impact. The montages of high-speed
316 photographic images for three different failure modes are shown in Fig. 5 and discussed below
317 Rebound ($v_0 \leq 61.5 \text{ ms}^{-1}$): The spherical projectile is rebounded by the deformed beam at
318 impact velocity of 56 ms^{-1} , as shown in Fig. 5 (a).

319 Three-point fracture ($61.5 \text{ ms}^{-1} < v_0 \leq 116.5 \text{ ms}^{-1}$): The beams fail with fibre fracture at three
320 positions in this range of impact velocity. Figure 5 (b) shows that the fracture in the middle
321 develops from the back face of the beam, thus the fracture mechanism is stretch governed. The
322 fracture at the clamped ends is also stretch governed, as indicated in the photograph of Fig. 4.
323 At impact velocity of 67 ms^{-1} , the fracture mainly focuses on the middle of the beam while a
324 part of fracture also occurs at the clamped ends (Fig. 4). At higher impact velocity of 100 ms^{-1} ,
325 the beam fully fractures at three points, i.e. middle and two clamped ends. The back-face
326 deflection of the beam before fracture decreases with the increase of impact velocity.

327 Perforation ($v_0 > 116.5 \text{ ms}^{-1}$): The beams fail with perforation when the initial impact velocity
328 of projectile reaches to the perforation limit. As reported by Karthikeyan et al. [9], the projectile
329 with high kinetic energy first comminutes the fibres at the impacted point, and then results in
330 the local bending of back face. The significant bending of the back face leads to the tensile
331 fracture of fibres (Fig. 5 (c)) and consequently the perforation of beam. The back face view of
332 the perforated beam is diamond-shape damage at the impact point, as shown in Fig. 5 (c). The
333 beams have been perforated before a large deflection achieves.

334 The failure modes and critical velocities of the stiff monolithic beams are similar to those of
335 the three-dimensional woven carbon fibre resin composites [26].

336 *5.1.2. Soft monolithic beam*

337 The back-face deflections of soft monolithic beams before failure as a function of time history
338 at selected impact velocities are plotted in Fig. 6, and the montages of high-speed photographic
339 images for three different failure modes are shown in Fig. 7. As the beam has a long response
340 history at low impact velocity of 72 ms^{-1} , the response history at this velocity (Fig. 6 (a)) is
341 separated from others at higher velocities (Fig. 6 (b)) for clarity. The ballistic behaviour is
342 described as follow

343 Rebound ($v_0 \leq 84 \text{ ms}^{-1}$): At the velocity of 72 ms^{-1} , the projectile is rebounded along with a
344 part of beam fracture in the width direction, as shown in Fig. 7 (a).

345 One-point fracture ($84 \text{ ms}^{-1} < v_0 \leq 232.5 \text{ ms}^{-1}$): In this range of applied projectile velocity, the
346 soft monolithic beam only fractures in the middle. This is different from the three-point fracture
347 mode of the stiff monolithic beam. As shown in Figs. 7 (b) and (c), the beam is first partly
348 perforated by the projectile and then fully fractures in the middle. Fibre fracture along with
349 matrix cracking develops from the back face of the beam due to the significant bending at the
350 impact point.

351 Perforation ($v_0 > 232.5 \text{ ms}^{-1}$): The beam is perforated without full fracture when the impact
352 velocity is high enough. The back-face deflection history of the beam for this failure mode is
353 not plotted in Fig. 6 as the deflection is negligible before perforation.

354 *5.1.3. Hybrid monolithic beam*

355 For the hybrid monolithic beam, the debonding occurs between the stiff and soft composite
356 parts during ballistic impact. The back-face deflections of both stiff part and soft part before
357 failure as a function of time are plotted in Fig. 8. As discussed in Section 4, the projectile
358 impacts the soft part firstly, then the stiff part in the back of the beam. The montages of high-
359 speed photographic images for three different failure modes are shown in Fig. 9

360 Rebound ($v_0 \leq 86 \text{ ms}^{-1}$): The projectile was rebounded by the beam under low velocity impact,
361 see Fig. 9 (a). Although the stiff composite part at the back face fractures, there is only slight
362 cracking at the impacted surface of the soft composite part, as the micro photographs shown in
363 Fig. 9 (a). The hybrid monolithic beam can therefore still resist load after impact. Under the
364 same impact velocity, however, the stiff and soft monolithic beams are fractured fully and
365 partly, respectively, as discussed in Sections 5.1.1 and 5.1.2.

366 One-point fracture ($86 \text{ ms}^{-1} < v_0 \leq 235 \text{ ms}^{-1}$): Both the stiff and soft parts failed with beam
367 fracture in the middle, and the debonding developed from the impact point to the clamped ends.
368 During the ballistic impact, the fibre fracture is observed at the back face of the stiff part, see
369 Fig. 9 (b).

370 Perforation ($v_0 \geq 235 \text{ ms}^{-1}$): When the impact velocity is high enough, the projectile perforates
371 the beam with a negligible deflection. As shown in Fig. 9 (c), the debonding is not observed
372 before perforation, but develops after that. It is concluded that the debonding is due to the wave
373 propagation rather than the different stiffness of the stiff part and soft part. Unlike the stiff
374 monolithic beam in Fig. 5 (c), the back face view of the perforated beam at the impact point is
375 circle-shape damage. This is due to the transition effect of soft composites at the front face,
376 which results in more uniform stress distribution of the stiff composite sheet around the
377 projectile.

378 *5.1.4. Discussion*

379 Figure 10 shows a comparison of critical velocities with respect to the failure modes of stiff,
380 soft and hybrid monolithic beams. The soft and hybrid monolithic beams have similar critical
381 velocities regarding to the same failure mode, and both higher than the stiff monolithic beams,
382 particularly for the failure mode of perforation.

383 The difference in critical velocities between the stiff and soft monolithic beams can be
384 explained as follow. The flexible and ductile EF80 epoxy matrix makes the soft monolithic
385 beam more deformable and less brittle than the stiff composite beam, which contributes to
386 longer interaction time between the projectile and composite beam. Hence, the plastic wave
387 can keep propagating in the soft monolithic beam for the failure mode of fracture, even though
388 the projectile has perforated the beam. With the increase of impact velocity, the interaction
389 time and wave propagation time become shorter, and the beam finally fails with perforation
390 when the perforation limit velocity reaches. Compared to the soft monolithic beam, the wave

391 propagation time in stiff monolithic beam is shorter due to the stiffer interaction, and the
392 projectile impacts on stiff monolithic beam is more likely to give rise to stress concentration.
393 Thus, the stiff monolithic beam can be perforated at lower impact velocity than the soft
394 monolithic beam. Throughout the impacts on stiff and soft monolithic beams, there is no
395 damage in terms of delamination observed in the plies.

396 Compared to the soft monolithic beam, the hybrid monolithic beam provides higher stiffness.
397 The debonding between the stiff and soft parts of the hybrid monolithic beam can always be
398 observed in the range of applied velocities, i.e. $72 \text{ ms}^{-1} < v_0 \leq 272 \text{ ms}^{-1}$. Due to the high
399 viscosity of the epoxy adhesive, the adhesive was unable to be degassed or vacuum infused,
400 which resulted in more imperfections introduced in the adhesive. Hence, the debonding
401 between the stiff and soft parts is easier to occur during impact. Based on the above analysis to
402 the perforation mode of hybrid monolithic beams, the development of debonding is mainly
403 governed by the wave propagation time in the beam, which is inversely scale with the initial
404 velocity of projectile. Hence, at low and medium velocities, the long interaction time between
405 the projectile and beam results in long wave propagation time and significant debonding (Fig.
406 9 (a) and (b)).

407 *5.2. Impact responses of sandwich beams*

408 The responses of sandwich beams with three types of face sheets, i.e. stiff face, soft face and
409 hybrid face, respectively, under ballistic impact are investigated. The montages of high-speed
410 photographic images at three impact velocity levels are shown in Fig. 11, Fig. 13 and Fig. 14.

411 At low impact velocity of approximately 73 ms^{-1} , the projectiles are rebounded by the stiff-
412 face and soft-face sandwich beams, as shown in Figs. 11 (a) and (b). However, the projectile
413 penetrates the front face sheet of the hybrid-face sandwich beam and reaches to the back face
414 sheet, leading to the debonding between back face sheet and honeycomb core, and finally
415 trapped into the beam (Fig. 11 (c)). This may due to the fact that the initial kinetic energy of

416 the projectile ($v_0 = 75 \text{ ms}^{-1}$) for hybrid-face sandwich beam is 7.8% higher than those of the
417 projectiles ($v_0 = 72 \text{ ms}^{-1}$) for stiff-face and soft-face sandwich beams. In addition, there is
418 debonding around the impact point occurred between front face sheet and honeycomb core of
419 the soft-face sandwich beam owing to the flexibility of soft composite sheet. As stated in
420 Section 2.2, though the number of fibre layer in sandwich beams is 4 less than that in monolithic
421 beams, all the sandwich beams are able to resist the projectiles and behave better than the stiff
422 and soft monolithic beams at this low velocity level. Figure 12 shows the back-face deflections
423 of monolithic and sandwich beams as a function of time at initial projectile velocity of
424 approximately 73 ms^{-1} . For clarity, only the deformation response of the soft composite part in
425 hybrid monolithic beam before the fracture of stiff composite part is plotted. It indicates that
426 the projectiles are rebounded by all the beams except for the stiff monolithic beam. The stiff
427 monolithic beam fails with fully fracture, and the maximum deflection is 31 mm that is
428 significantly higher than those (no more than 20 mm) of other beams. The sandwich beams
429 normally have smaller deflections than the monolithic beams due to the higher stiffness.

430 At medium impact velocity of around 105 ms^{-1} , the front face sheets of all sandwich beams are
431 perforated and the back face sheets fully fracture during impact, as shown in Fig. 13. The
432 debonding between back face sheet and honeycomb core is also observed in all sandwich
433 beams. Similar to the hybrid monolithic beam, the sheet-sheet debonding occurs in the back
434 face sheet of the hybrid-face sandwich beam, see Fig. 13 (c).

435 Figure 14 shows the montages of high-speed photographic images at higher impact velocity of
436 around 144 ms^{-1} . For the stiff-face sandwich beam, both the front face sheet and back face sheet
437 are perforated without full fracture. The explanation to this is identical to that to the stiff
438 monolithic beam, i.e. owing to the short interaction time between projectile and stiff
439 composites. For the soft-face as well as hybrid-face sandwich beams, the failure modes are
440 similar to those under the impact velocity of around 105 ms^{-1} .

441 5.3. Ballistic resistance of beams characterised by the initial-residual velocity relation of the
442 projectile.

443 Figure 15 shows the initial projectile velocity v_0 as a function of residual projectile velocity
444 v_r . Here, v_r is assumed to be 0 when the projectile is trapped into the beam. The ballistic
445 impact resistance of the beams can be reflected by the slopes and intercepts of the fitting lines,
446 i.e. higher slope and intercept correspond to better impact resistance of beams. This figure
447 indicates that the lowest intercept and slope of fitting lines are from the stiff monolithic beam
448 and stiff-face sandwich beam, respectively. In addition, the slopes of the stiff, soft and hybrid
449 monolithic beams are higher than those of the corresponding stiff-face, soft-face and hybrid-
450 face sandwich beams, respectively. This is because the number of fibre layer for monolithic
451 beams is more than that for sandwich beams in order to achieve identical areal mass, and carbon
452 fibre laminated composites play a far more significant role than the Nomex honeycomb core
453 in resisting ballistic impact.

454 5.4. Energy absorption capacity of beams

455 The kinetic energy of the projectile transmitted to the beams can be calculated as follow

456
$$\Delta E_{abs} = E_{k_0} - E_{k_r} = \frac{1}{2} M (v_0^2 - v_r^2) \quad (2)$$

457 where E_{k_0} and E_{k_r} are the initial and residual kinetic energy of projectile, respectively. ΔE_{abs}
458 is the energy transmitted from the projectile to fibre composite beams. This transmitted energy
459 converted to the kinetic energy of beams and energy absorbed by beams. Based on Fig. 15, the
460 kinetic energy of projectile transmitted to beams as a function of initial kinetic energy of
461 projectile is summarized in Fig. 16. The initial kinetic energy of projectile is in the range of
462 $13 \text{ J} \leq E_{k_0} \leq 307 \text{ J}$. Due to the different architectures, the monolithic and sandwich beams may
463 acquire different kinetic energy during the impact events. Assuming that the kinetic energy
464 acquired is identical for the beams with the same architecture, i.e. monolithic or sandwich,

465 during impact. As described in Section 4, the fixture for clamping beams was fully fixed, hence
466 the energy of projectile absorbed by the fixture can be neglected. Hence, the energy absorbed
467 by beams with the same architecture can be compared using the kinetic energy of projectile
468 transmitted to beams.

469 For the monolithic beams, the soft and hybrid monolithic beams have the best energy
470 absorption capacity, whereas the soft monolithic beam behaves better in energy absorption than
471 the hybrid monolithic beam when the initial projectile velocity is higher than 160 ms^{-1} , as
472 highlighted in Fig. 16. The stiff monolithic beam behaves worst in energy absorption. For the
473 sandwich beams, both the soft-face and hybrid-face sandwich beams exhibit better energy
474 absorption capacity than stiff-face sandwich beams. As discussed in Section 5.1.3, the buffer
475 of soft composite part resulted in more uniform and wider range of stress distribution in beams.
476 Hence, more energy of projectile can be absorbed by the face sheets and honeycomb core of
477 soft-face and hybrid-face sandwich beams than by those of stiff-face sandwich beams. As the
478 failure mode of the soft-face sandwich beams is same in the impact velocity range of
479 $107 \text{ ms}^{-1} < v_0 \leq 145 \text{ ms}^{-1}$, the energy absorption capacity of these beams reaches a plateau.
480 However, within this velocity range, the energy absorbed by hybrid-face sandwich beams still
481 increasing. The hybrid-face sandwich beam has better energy absorption capacity than soft-
482 face sandwich beam at impact velocity of 145 ms^{-1} . This may due to the interaction between
483 the soft and hard parts of hybrid face sheets. The other reason may be the debonding between
484 back face sheet and honeycomb core, which absorbs a part of kinetic energy of projectile.

485 Except for the soft-face and hybrid-face sandwich beams, the measured maximum initial
486 kinetic energy of projectile regarding to the mode of fracture is marked in Fig. 16 using an
487 upward dash arrow. This kinetic energy can be regarded as the critical value that results in the
488 transition of failure modes from fracture to perforation. It indicates that the energy absorption
489 capacity of these beams normally decreases during the transition of these two failure modes. It

490 can be explained as follow. Along the width direction of the beams, there are less fibres fracture
491 for the failure mode of perforation than those for the failure mode of fracture. As the energy
492 absorption capacity of composites is proportional to the failed fibres [7], the beams failed with
493 perforation therefore absorb less kinetic energy of projectile than the beams failed with fracture.
494 However, there is a slight increase for the energy absorbed by the stiff monolithic beam during
495 the transition of failure modes. This is due to the fact that the stiff monolithic beam failed with
496 perforation has wider range of fibre deformation and damage (e.g. fracture and comminution)
497 than that failed with fracture. It can be demonstrated by comparing the high-speed photographic
498 images in Figs. 6 (b) and (c), and also by Karthikeyan et al. [9]. This explanation is not suitable
499 for the stiff-sheet sandwich beams as the beam failed with fracture of back face sheet also has
500 significant fibre deformation and damage, as shown in Fig. 14 (a).

501 *5.5. The effect of epoxy adhesive*

502 Except for the failure of carbon fibre reinforcements, the epoxy adhesive also failed due to the
503 debonding between stiff and soft composite parts as well as face sheet and honeycomb core.
504 There are more debondings observed in hybrid monolithic and hybrid-face sandwich beams
505 than the other types of beams. In the present study, the tensile strength of the adhesive is 30
506 MPa [27], much lower than that of the carbon fibre. Russell et al. [20] numerically
507 demonstrated that no more than 5% of the initial kinetic energy of projectile is dissipated by
508 the delamination of fibre layers in the soft impact events. Kirthikeyan and Russel [10] reported
509 that the ballistic limit of the pre-delaminated fibre laminate was 10% higher than that of the
510 laminate with same areal mass but without pre-delamination. This was due to the benefit of
511 delamination that promoted an earlier transition from fibre fracture to stretching. The
512 debonding, between the stiff and soft composite parts of hybrid beams, governed by the low-
513 strength adhesive can also be regarded as 'pre-delamination'. Hence, the weak adhesive
514 interface may play an important role in indirectly dissipating impact energy of a projectile.

515 **6. Concluding remarks**

516 The ballistic responses of six types of carbon fibre composite beams, i.e. three monolithic
517 beams and three sandwich beams, have been investigated to identify the advantages of hybrid
518 beams. For each type of monolithic beam, there were three distinct failure modes identified:
519 minor damage with projectile rebound, fracture and perforation. The failure modes of fracture
520 and perforation were mainly governed by the fracture of fibre reinforcements, and the
521 development of these two damage modes depended on the wave propagation time in beams.
522 The hybrid and soft monolithic beam had similar critical velocities for each failure mode, and
523 both higher than the stiff monolithic beam. In addition, the hybrid monolithic beam had benefits
524 under low velocity impact as the failure only occurred in the stiff composite part of beam and
525 the soft part could still resisting loading. The back face damage mode of the hybrid monolithic
526 beam that failed with perforation was different from that of stiff monolithic beam ascribed to
527 the buffer effect of the soft composite part at the front face. For the stiff-sheet, soft-sheet and
528 hybrid-sheet sandwich beams, the failure modes were similar to those of the corresponding
529 monolithic beams, i.e. the projectiles were rebounded by or trapped into sandwich beams at
530 low impact velocity, and the back face sheet fully fractured and were perforated at medium and
531 high impact velocities, respectively.

532 The energy absorption capacity of the monolithic and sandwich beams have also been studied.
533 For the monolithic beams, the energy absorption capacity of the hybrid and soft monolithic
534 beams were better than that of the stiff monolithic beams, whereas the stiff monolithic and
535 stiff-face sandwich beams behaved worst. In addition, as more fibre reinforcements fractured,
536 the beams failed with fracture had better energy absorption capacity than those failed with
537 perforation. The hybrid-face sandwich beams exhibited better energy absorption capacity than
538 the soft-face sandwich beams at high impact velocity.

539 The weak adhesive interface between the stiff and soft composite parts in hybrid
540 monolithic/sandwich beams may have a positive effect on the energy absorption capacity of
541 beams. The strength and flexibility of adhesive may influence the development of debonding,
542 their effects on the ballistic impact resistance of hybrid laminated composites is a future topic.

543 **Acknowledgments**

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546 **Declaration of interest: none**

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Figure Captions

615 Figure 1. (a) The in-plane sketch of the Nomex honeycomb core unit cell in sandwich beam,
616 (b) the layer-up orientation of the fibre composite laminate and the types of face sheets. The
617 sketch of the assembled sandwich beam is shown in (c). The co-ordinate systems associated
618 with the beam and core are included in this figure. All dimensions are in mm.

619 Figure 2. Quasi-static stress-strain relationships of the stiff and soft fibre composites under
620 uniaxial compression and tension tests for (a) $0^\circ/90^\circ$ and (b) $\pm 45^\circ$ lay-up architecture. The
621 measured quasi-static out-of-plane compressive response of the Nomex honeycomb core of
622 density $\rho = 54 \text{ kg} \cdot \text{m}^{-3}$ is shown in (c).

623 Figure 3. Sketch of the experimental setup for ballistic impact on monolithic and sandwich
624 beams. All dimensions are in mm.

625 Figure 4. The time history of back face deflection of the stiff monolithic beams at selected
626 impact velocities. Time $t=0$ corresponds to the time instant when the projectile impacted on the
627 beams. The photographic image shows the part fracture of clamped end when the impact
628 velocity was 67 ms^{-1} .

629 Figure 5. Montage of the high speed photographs of the stiff monolithic beams under ballistic
630 impact. Three different failure modes of the beams are shown in this figure. The back face view
631 of the beam failed with perforation is also shown in (c).

632 Figure 6. The time history of back face deflection of the soft monolithic beams at (a) impact
633 velocities of 72 ms^{-1} and (b) higher impact velocities. Time $t=0$ corresponds to the time instant
634 when the projectile impacted on the beams.

635 Figure 7. Montage of the high speed photographs of the soft monolithic beams under ballistic
636 impact. Three different failure modes of the beams are shown in this figure.

637 Figure 8. The time history of back face deflections for stiff and soft parts in hybrid monolithic
638 beams at selected impact velocities. Time $t=0$ corresponds to the time instant when the
639 projectile impacted on the beams.

640 Figure 9. Montage of the high speed photographs of the hybrid monolithic beams under ballistic
641 impact. Three different damage modes of the beams are shown in this figure. (a) also shows
642 the micro damage of the stiff composites and soft composites after impact, and (c) also shows
643 the back face view of the beam failed with perforation at the impact point.

644 Figure 10. The ranges of impact velocity regarding to the different damage modes of the stiff,
645 soft and hybrid monolithic beams.

646 Figure 11. Montage of the high speed photographs of the (a) stiff-face, (b) soft-face and (c)
647 hybrid-face sandwich beams impacted by the spherical projectile at velocity around 73 ms^{-1} .
648 The two red curves in (c) represent the edges of back face sheet and honeycomb core, and the
649 front face view of hybrid-face sandwich beam at impact point are also shown in (c).

650 Figure 12. The time history of back face deflection for monolithic and sandwich beams at
651 impact velocity of around 73 ms^{-1} . It should be noted that the stiff monolithic beam and hybrid-
652 face sandwich beam are impacted at the velocity of 67 ms^{-1} and 75 ms^{-1} , respectively.

653 Figure 13. Montage of the high speed photographs of the (a) stiff-face, (b) soft-face and (c)
654 hybrid-face sandwich beams impacted by the projectile at velocity around 105 ms^{-1} .

655 Figure 14. Montage of the high speed photographs of the (a) stiff-face, (b) soft-face and (c)
656 hybrid-face sandwich beams impacted by the projectile at velocity around 144 ms^{-1} .

657 Figure 15. Initial projectile velocity V_0 as a function of residual projectile velocity V_r . The
658 projectile trapped in the hybrid-face sandwich beam has been highlighted in Fig. 11 (c). The
659 straight dash lines are reference lines. The impact direction of projectile is along 3-axis of the
660 coordinate system.

661 Figure 16. Kinetic energy of projectile transmitted to the beams as a function of initial kinetic
 662 energy of projectile.







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Table 1. Details of the monolithic and sandwich beams.

Composite sheets	Monolithic beams			Sandwich beams		
	Stiff	Soft	Hybrid	Stiff face sheet	Soft face sheet	Hybrid face sheet
Sketch of beams						
Number of sheet layers	20	20	10*2	8*2	8*2	4*4
Areal mass of laminates (kg/m ²)	5.38	5.38	5.30	4.30	4.30	4.30
Areal mass of honeycomb core (kg/m ²)	0	0	0	0.54	0.54	0.54
Areal mass of adhesive (kg/m ²)	0	0	0.14	0.28	0.28	0.56
Total areal mass of beams (kg/m ²)	5.38	5.38	5.44	5.12	5.12	5.40

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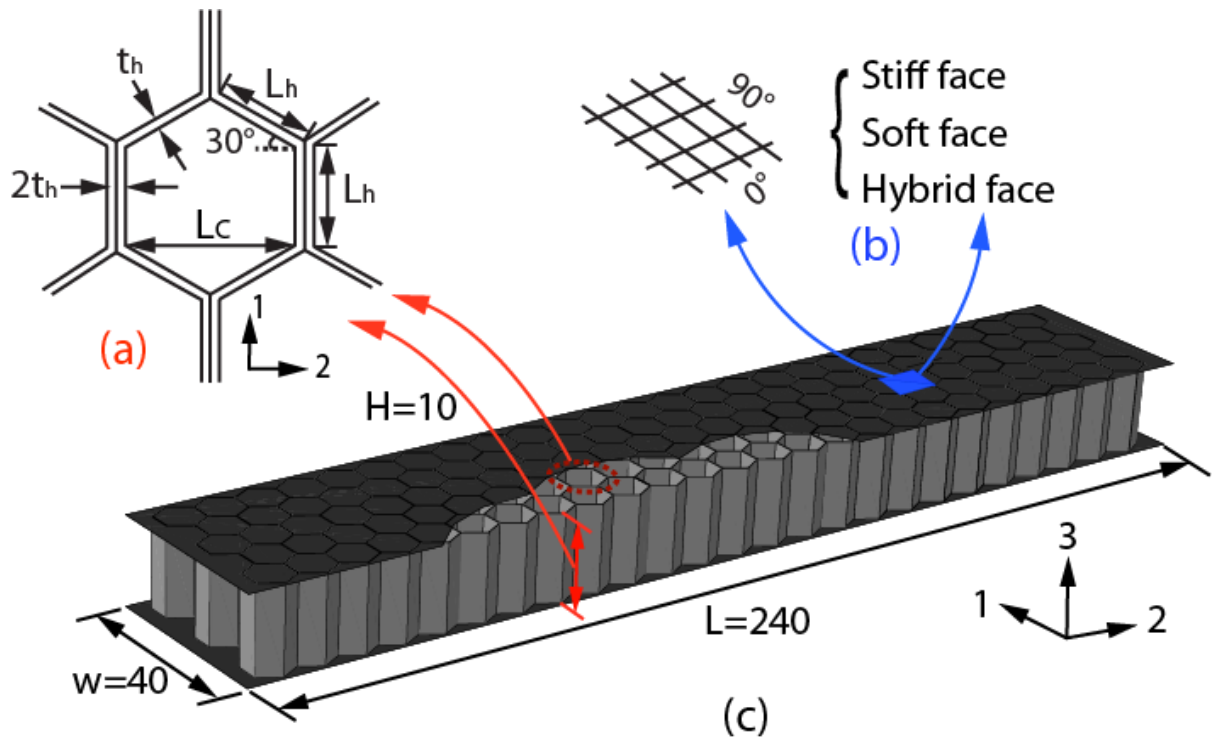
676 Table 2 A summary of the experimental measurements for six types of composite beams.

Beams	Initial velocity, v_0 (m/s)	Residual velocity, v_r (m/s)	Kinetic energy transmitted to beams, ΔE_{abs} (J)	Failure modes
Stiff monolithic beam	56	-16	11.95	Rebound
	67	-18	17.28	Three-point fracture
	100	69	21.74	Three-point fracture
	133	111	22.28	Perforation
	160	136	26.75	Perforation
Soft monolithic beam	72	-6	20.19	Rebound
	96	26	35.44	One-point fracture
	140	85	51.36	One-point fracture
	207	153	80.67	Three-point fracture
	258	220	75.37	Perforation
Hybrid monolithic beam	72	-8	21.25	Rebound
	100	40	34.86	One-point fracture
	145	86	56.56	One-point fracture
	198	153	65.55	One-point fracture
Stiff-face sandwich beam	272	246	55.90	Perforation
	72	-14	21.70	Rebound
	107	61	32.07	Back face fracture
	145	124	23.44	Back face perforation
Soft-face sandwich beam	72	-8	21.25	Rebound
	107	43	39.84	Back face fracture
	145	148	38.85	Back face fracture
Hybrid-face sandwich beam	75	0	23.34	Projectile trapped
	100	42	34.18	Back face fracture
	143	98	45.01	Back face fracture

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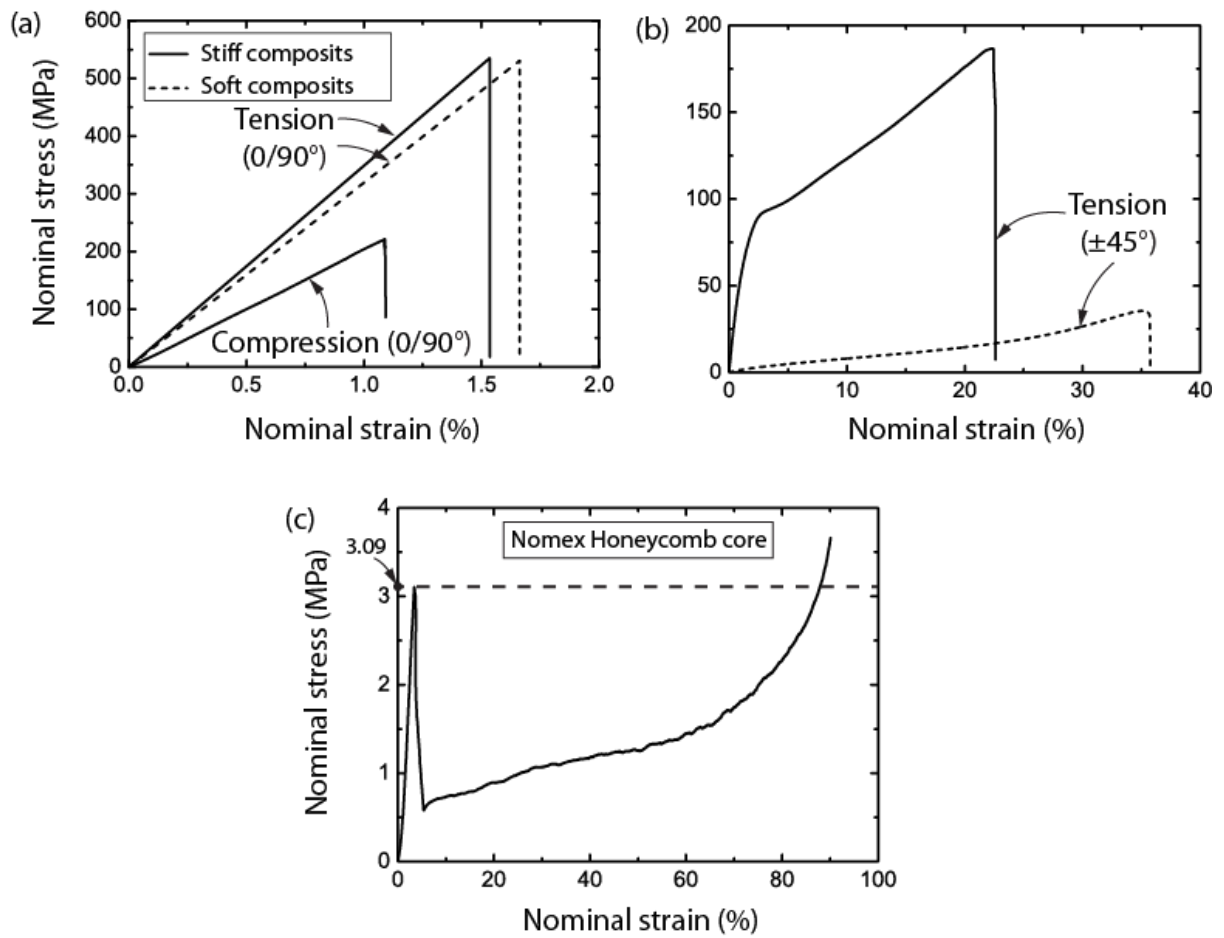
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Figure 1

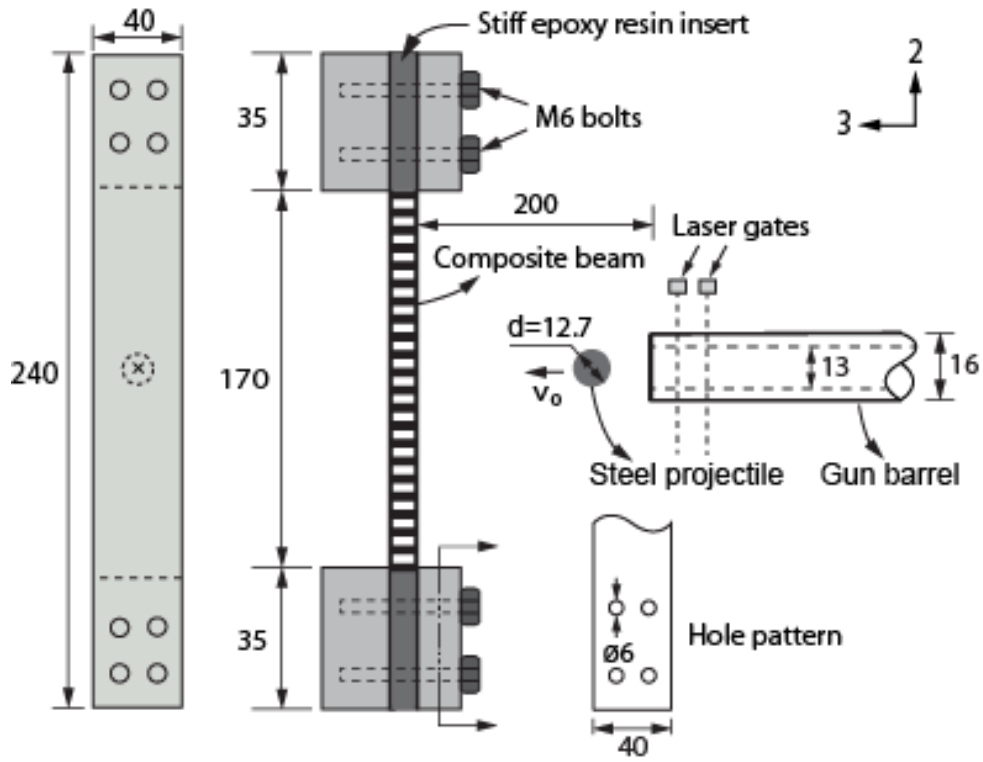


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Figure 2

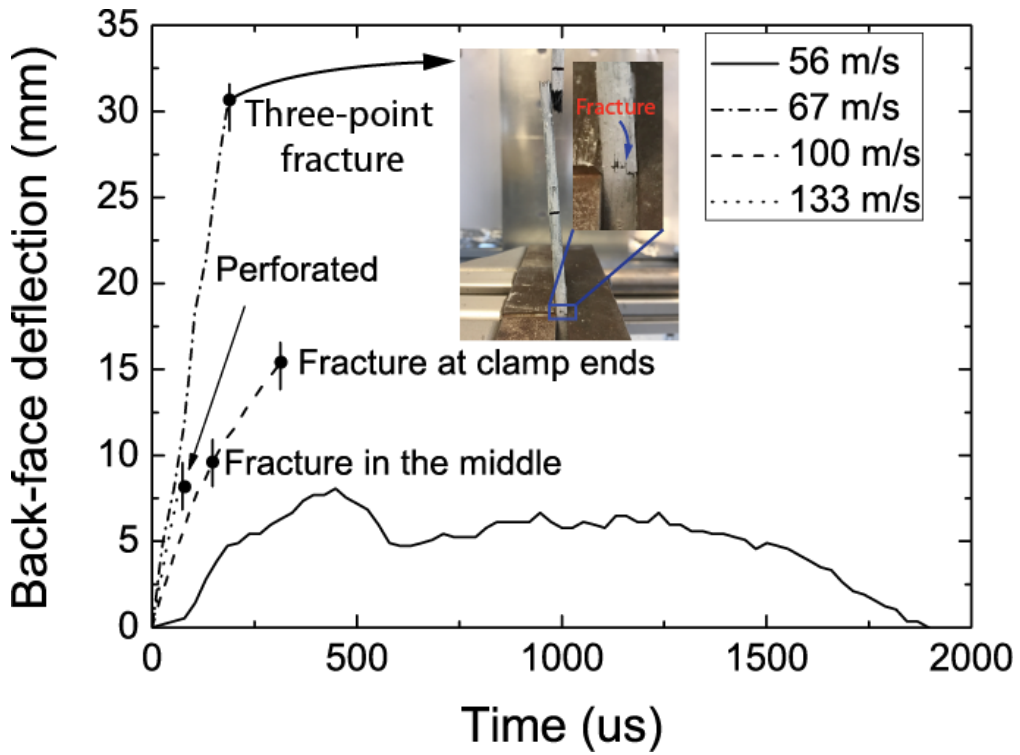


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Figure 3

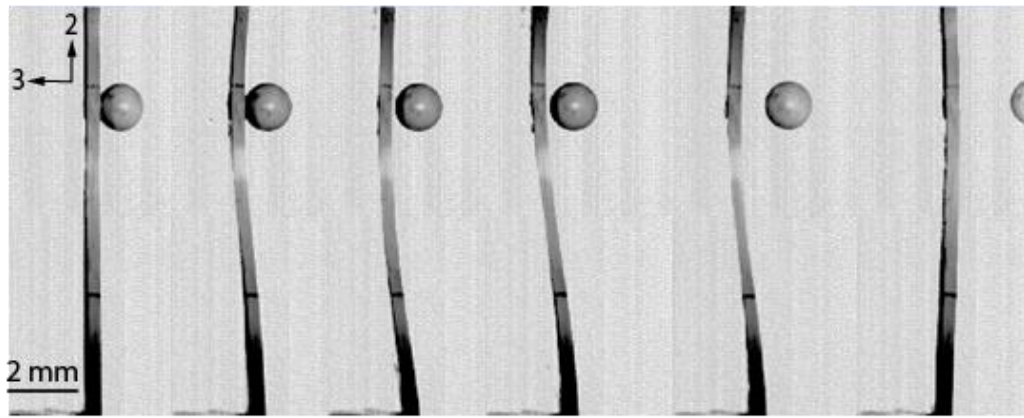


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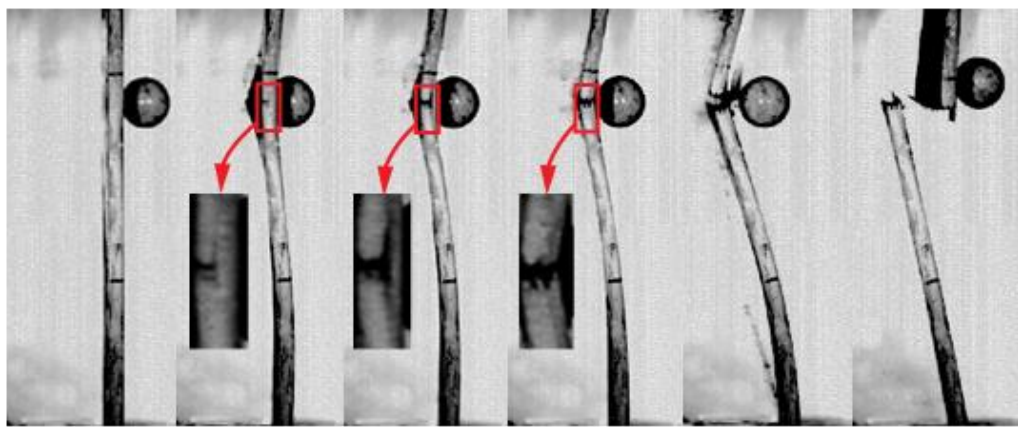
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Figure 4



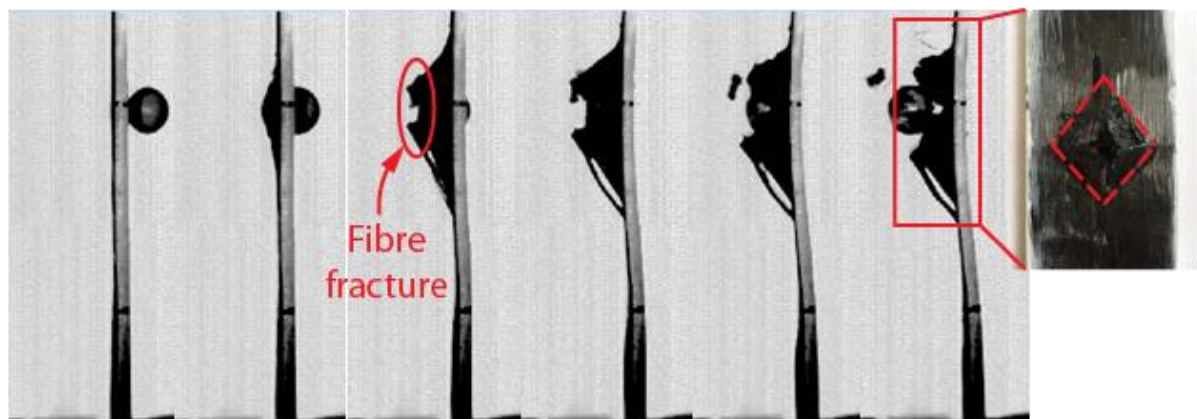
0 μs 184 μs 342 μs 447 μs 1105 μs 2100 μs

(a) 56 ms^{-1} _Rebound



0 μs 132 μs 158 μs 210 μs 579 μs 2816 μs

(b) 67 ms^{-1} _Three-point fracture



0 μs 26 μs 79 μs 105 μs 132 μs 184 μs

(c) 133 ms^{-1} _Perforation

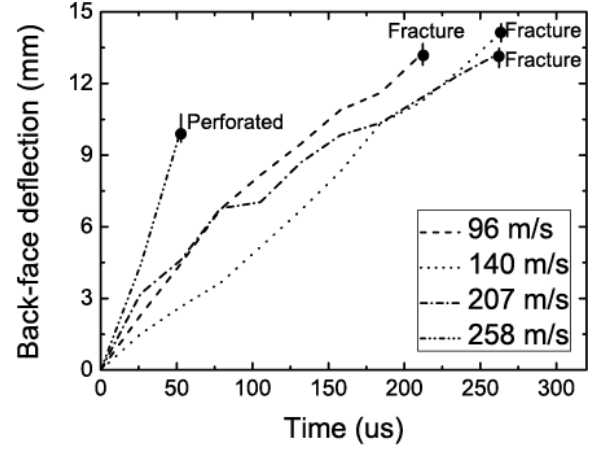
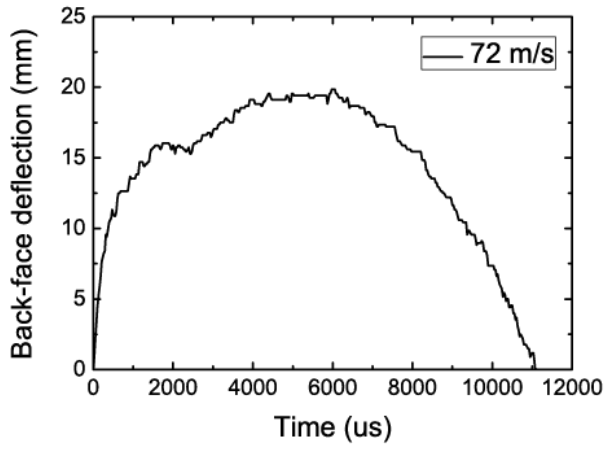
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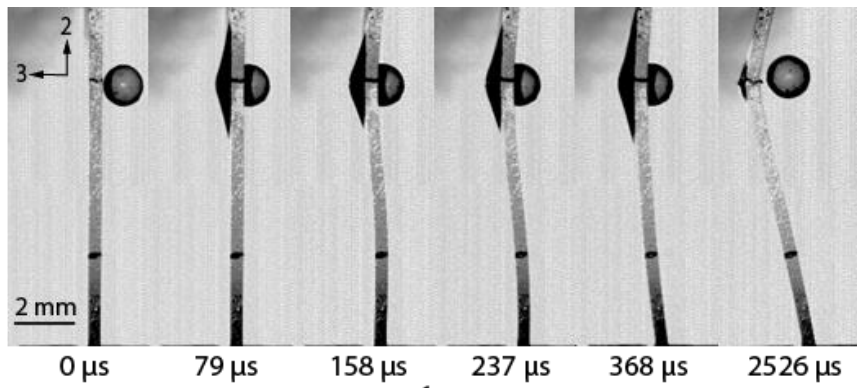
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Figure 5

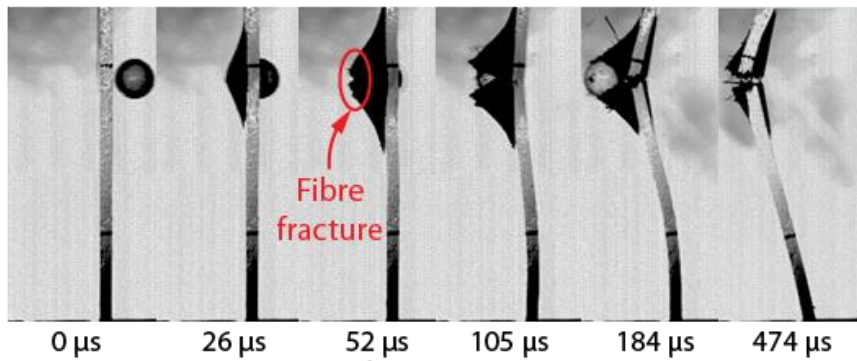


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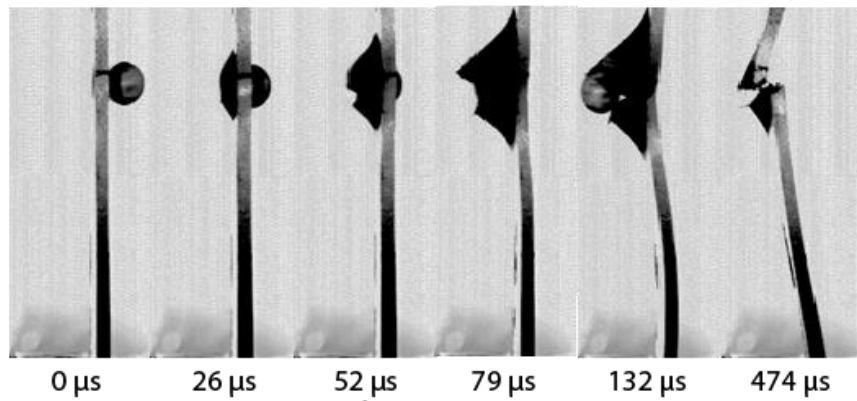
Figure 6



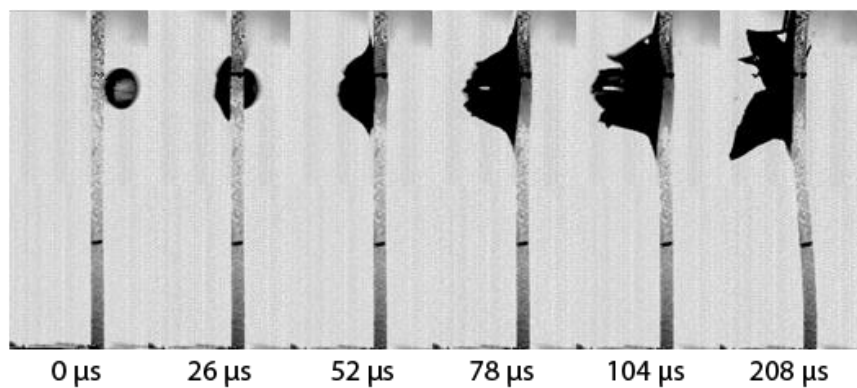
(a) 72 ms^{-1} _Rebound



(b) 140 ms^{-1} _One-point fracture



(c) 207 ms^{-1} _One-point fracture



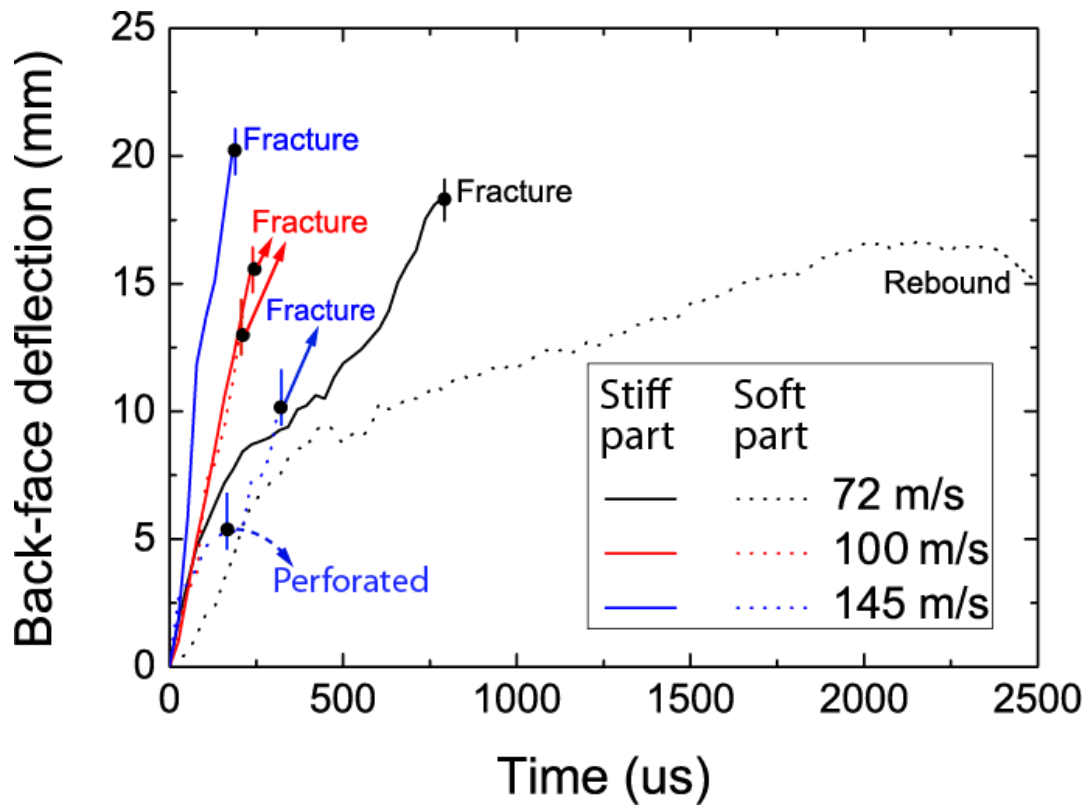
(d) 258 ms^{-1} _Perforation

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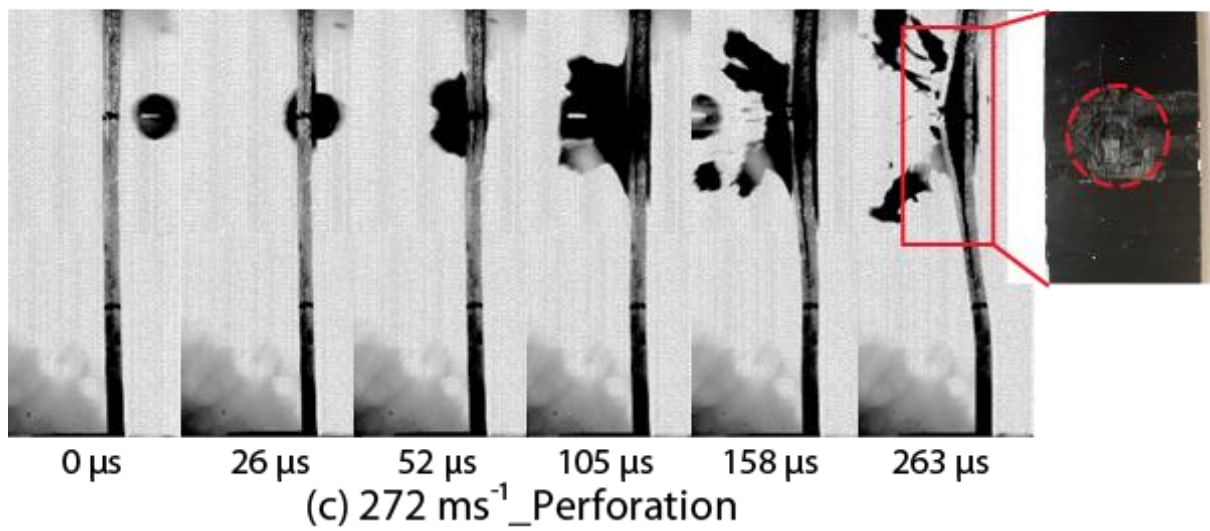
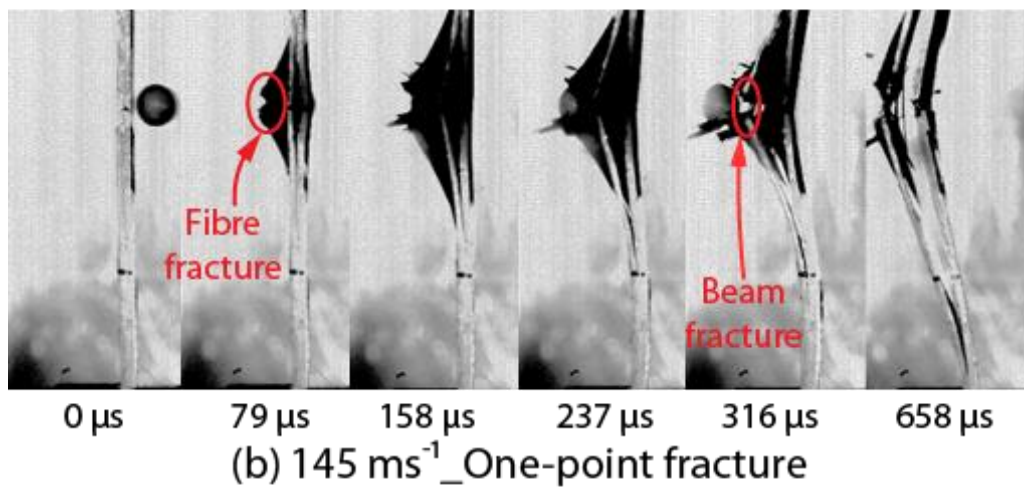
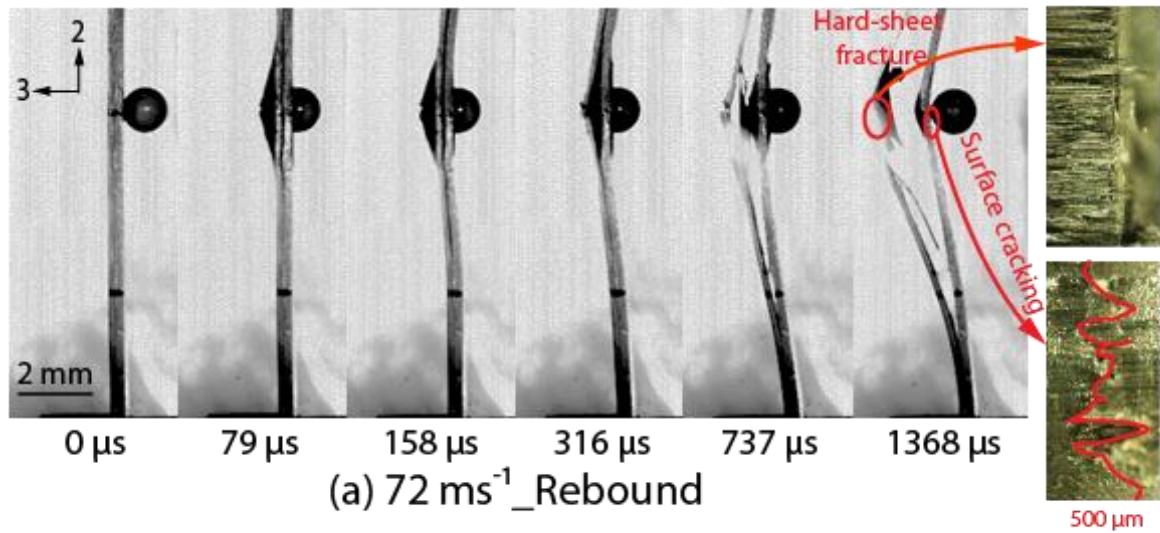
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Figure 7



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Figure 8



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Figure 9

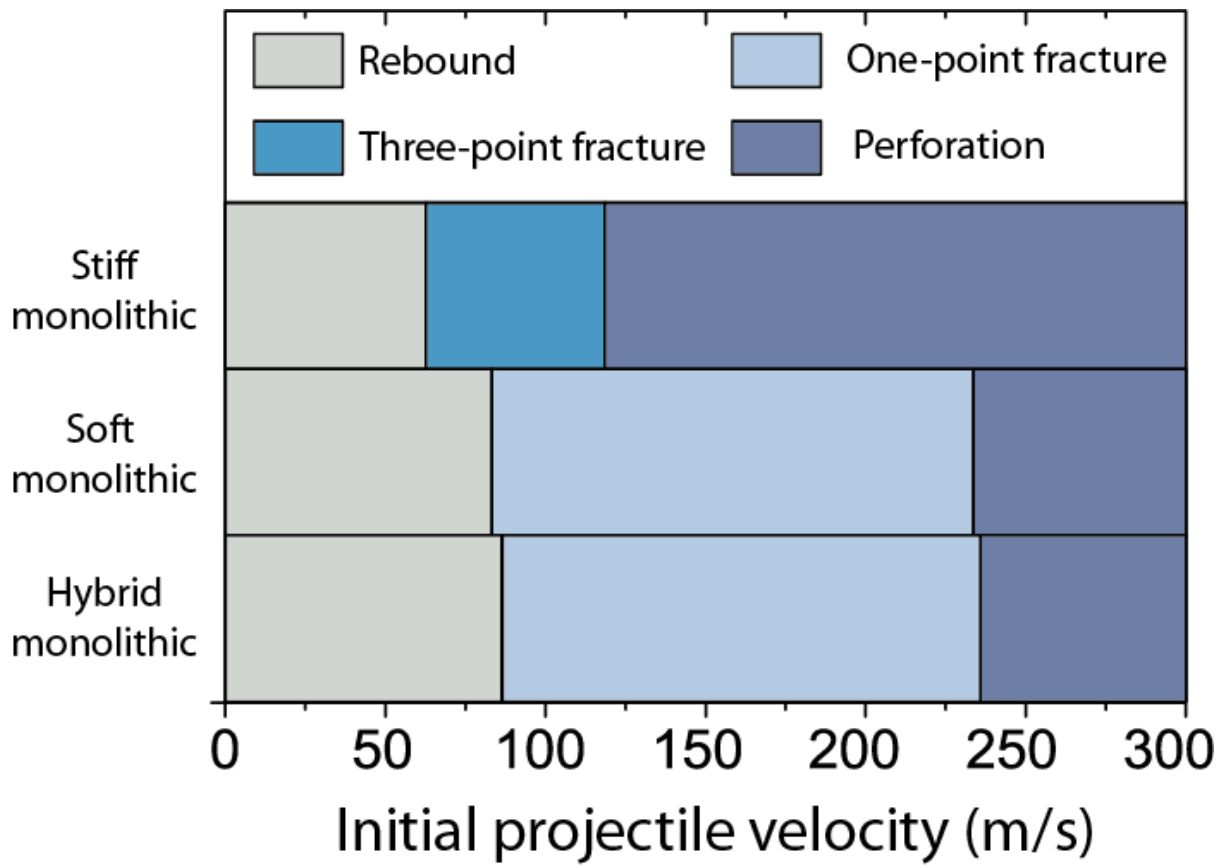
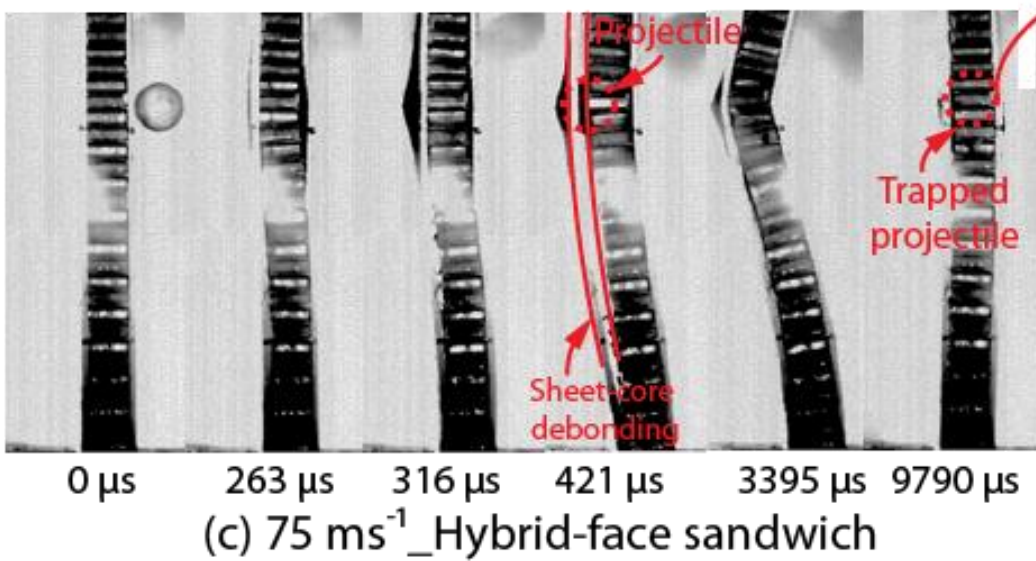
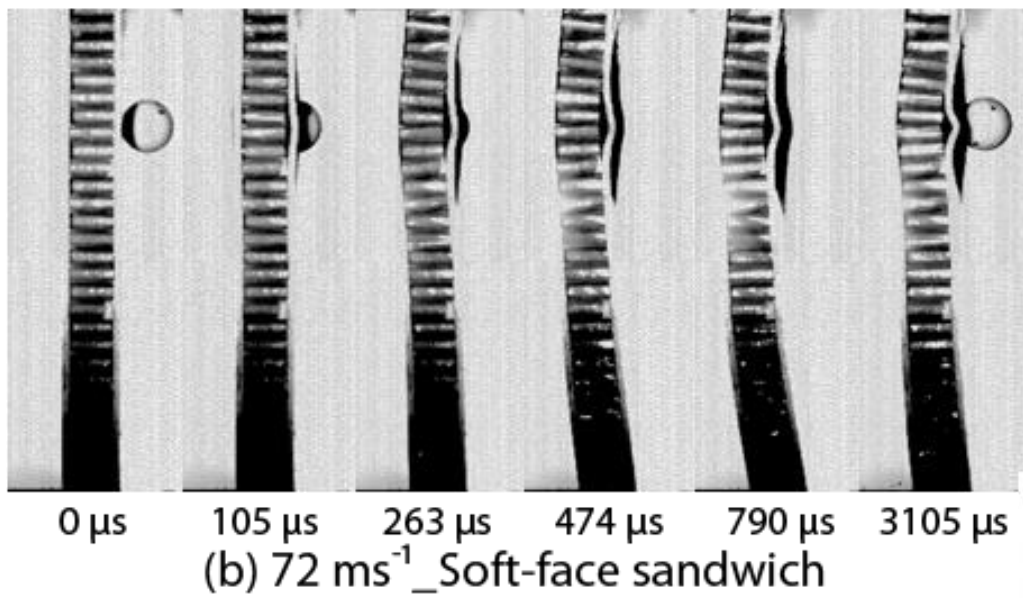
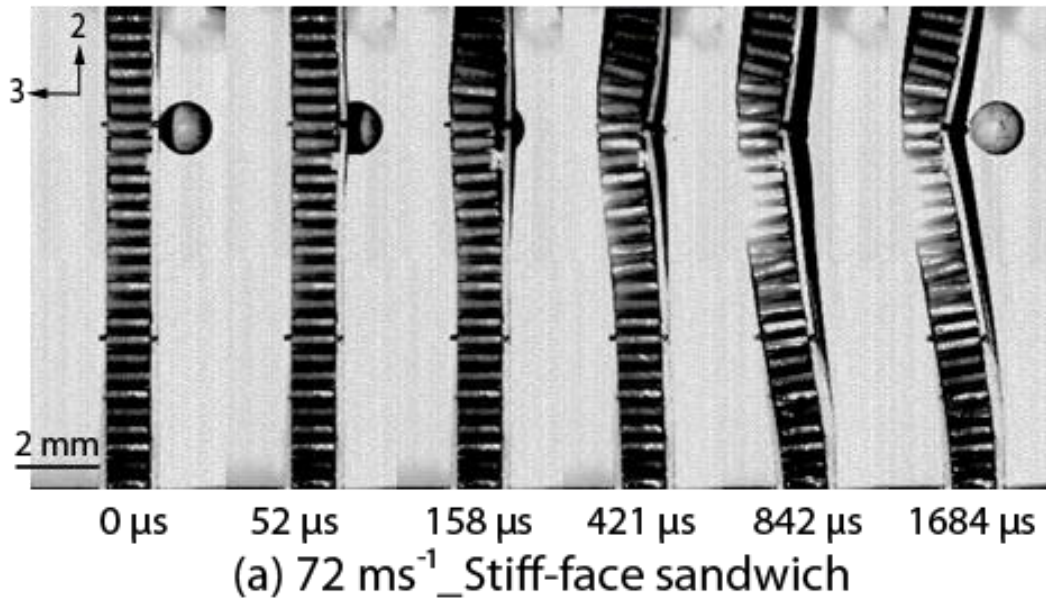


Figure 10

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Figure 11

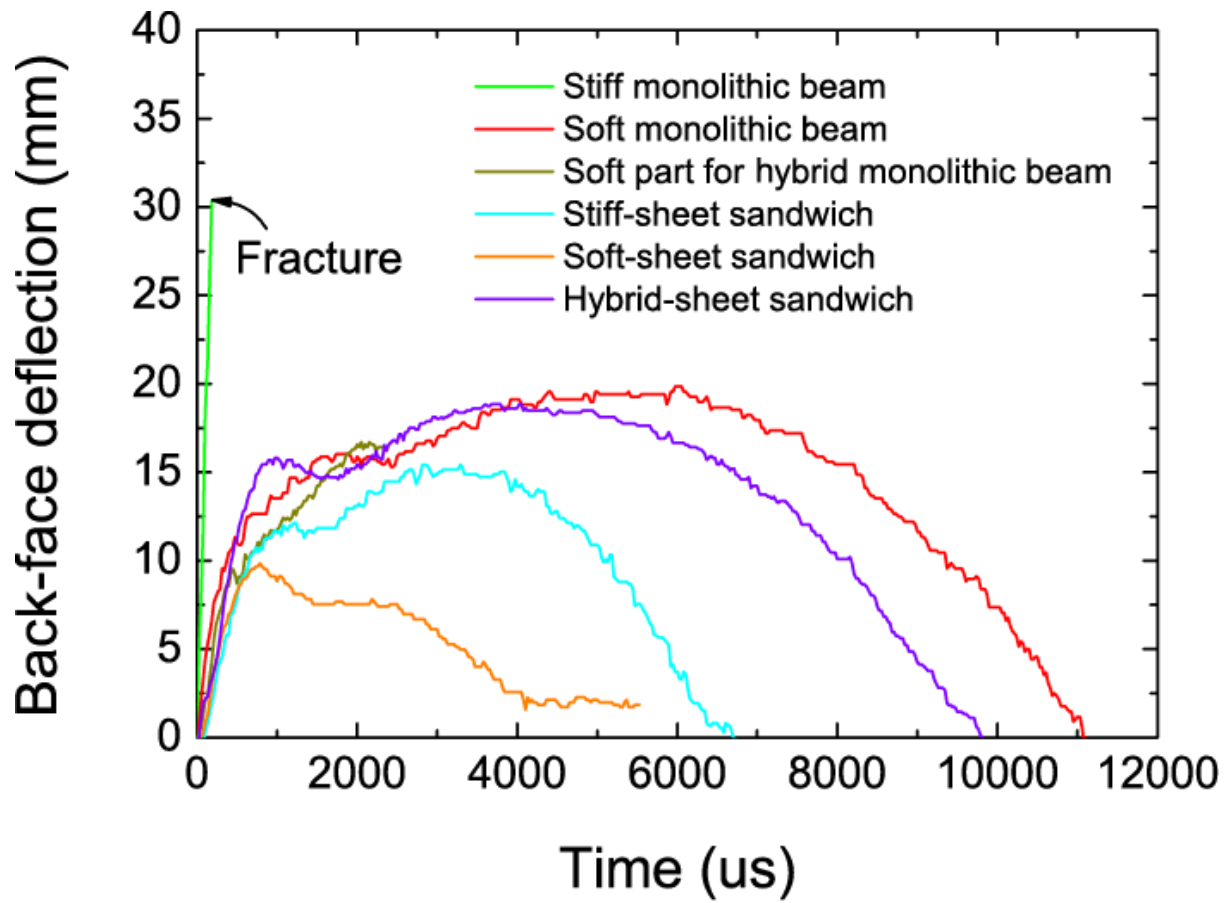


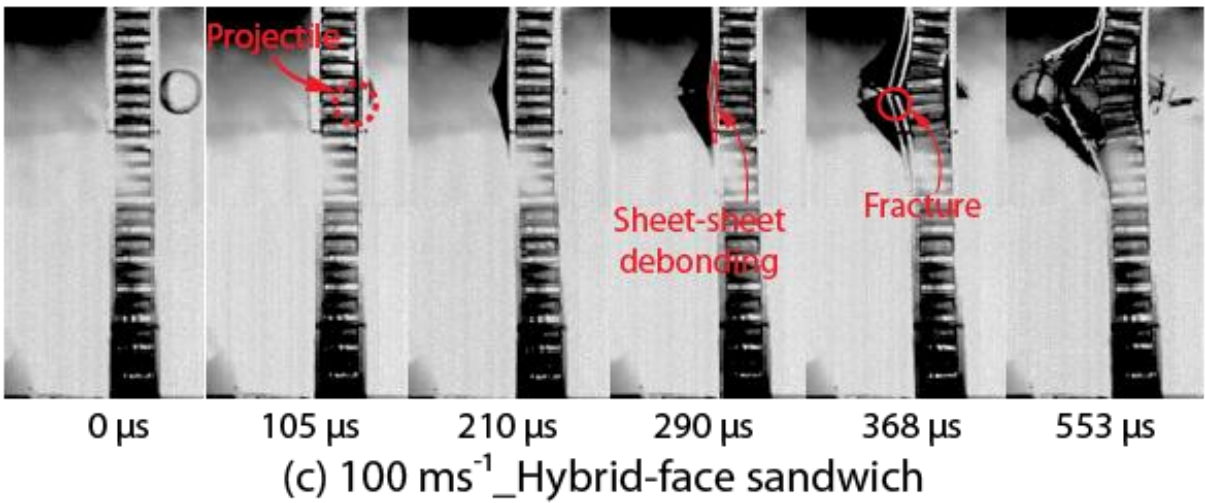
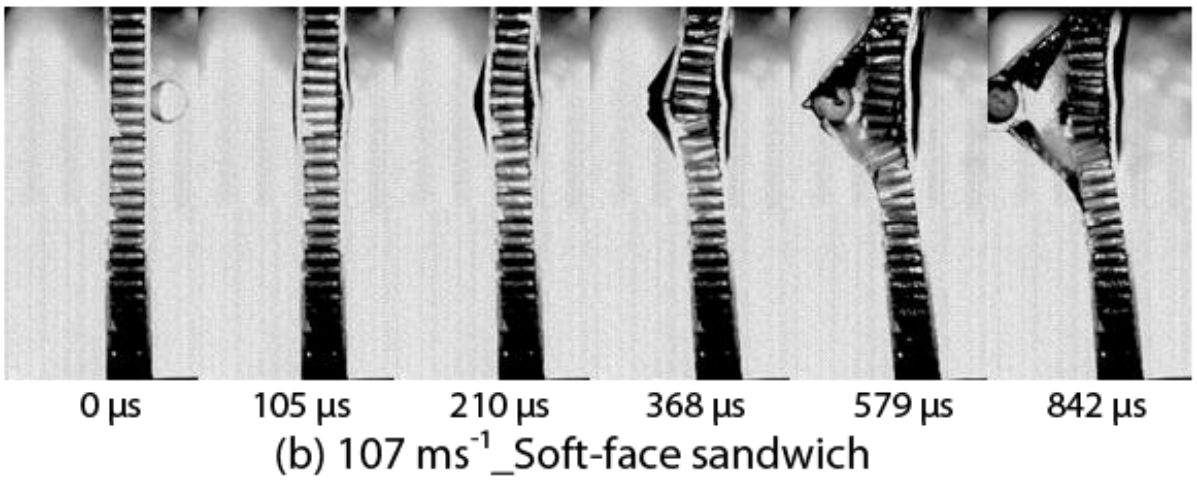
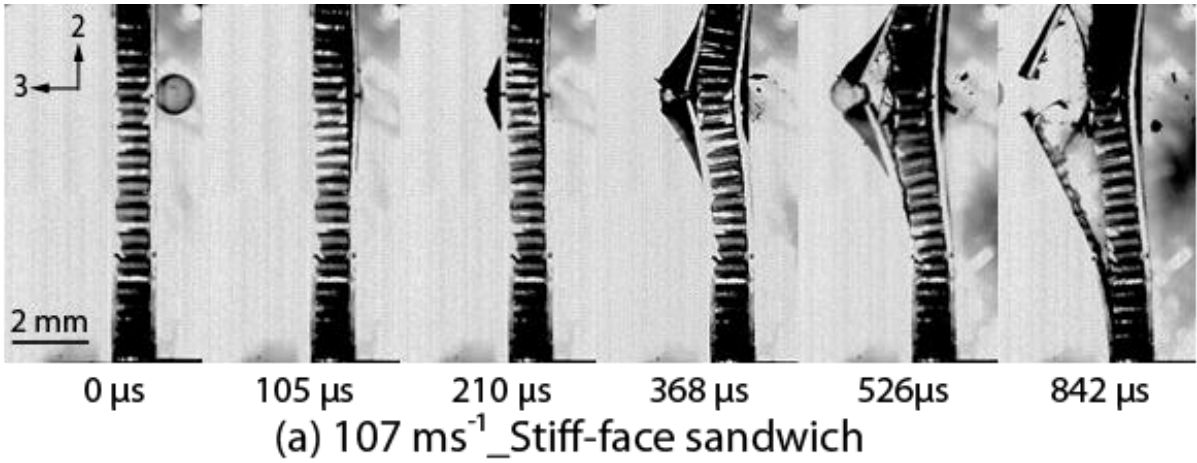
Figure 12

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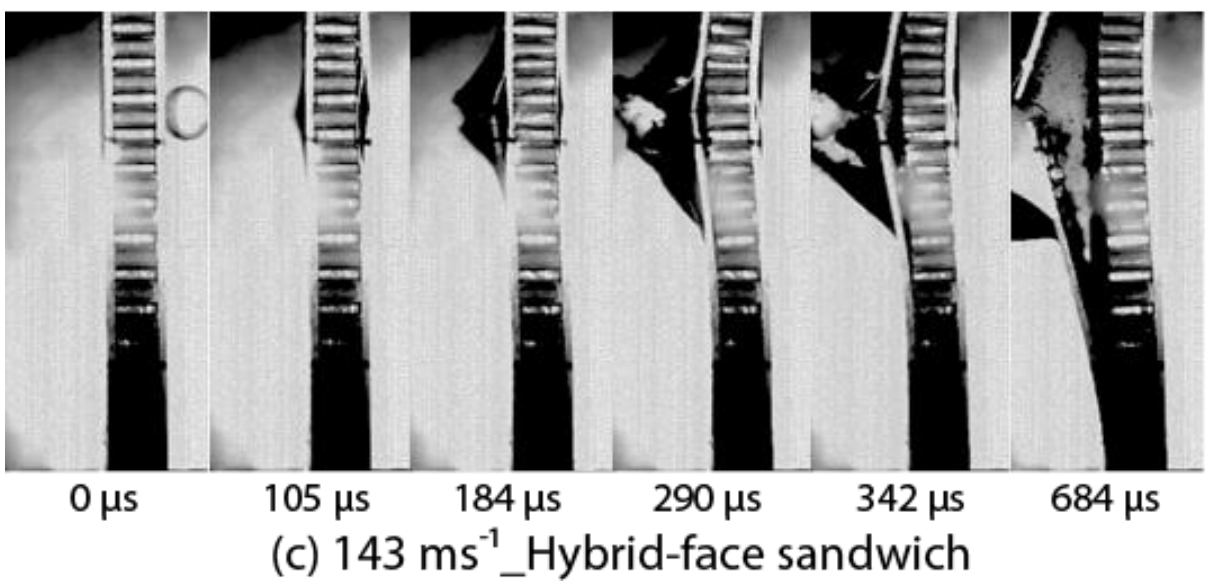
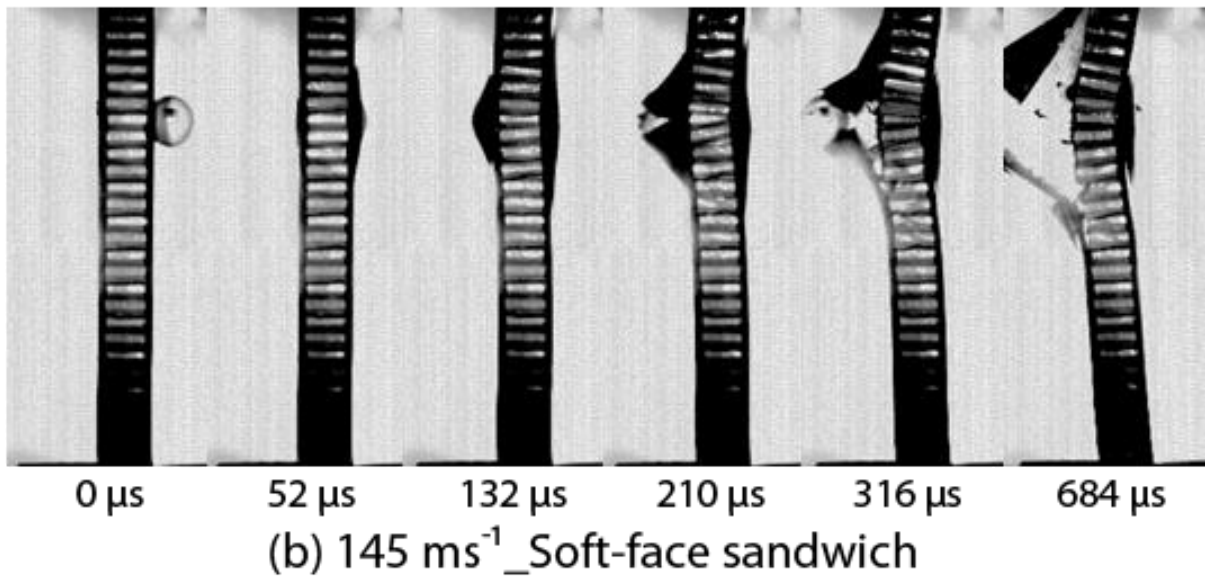
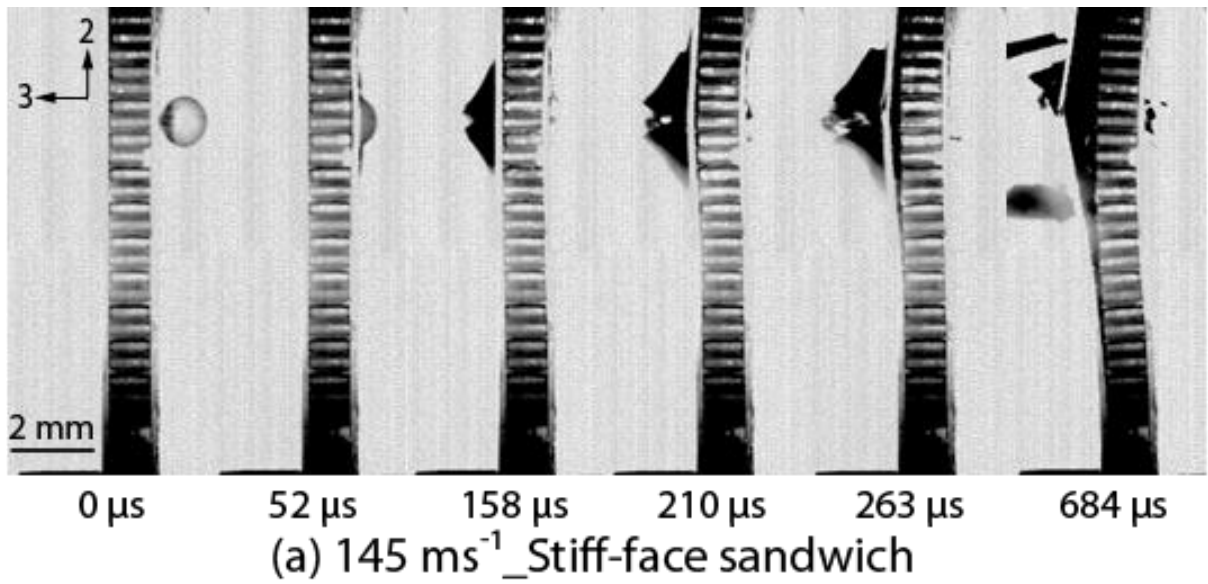
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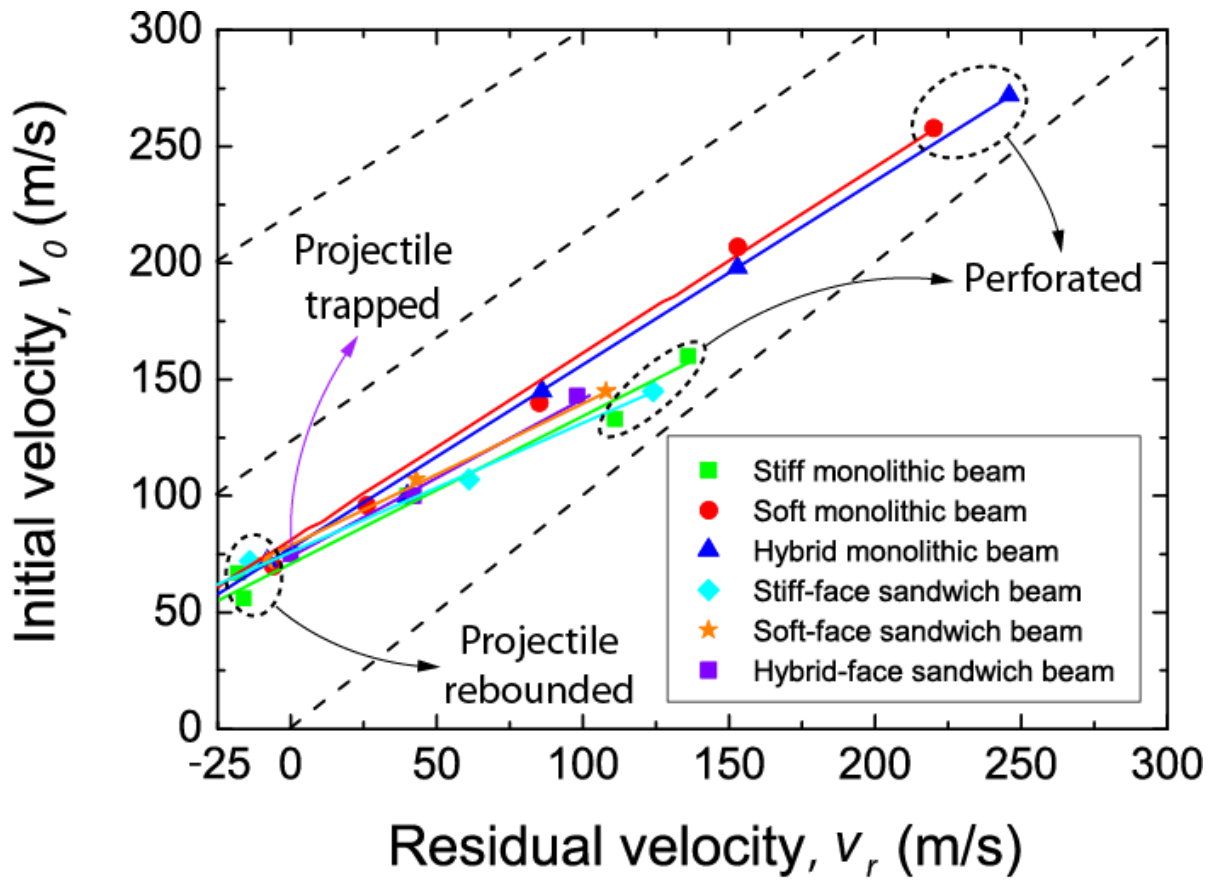
Figure 13



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Figure 14

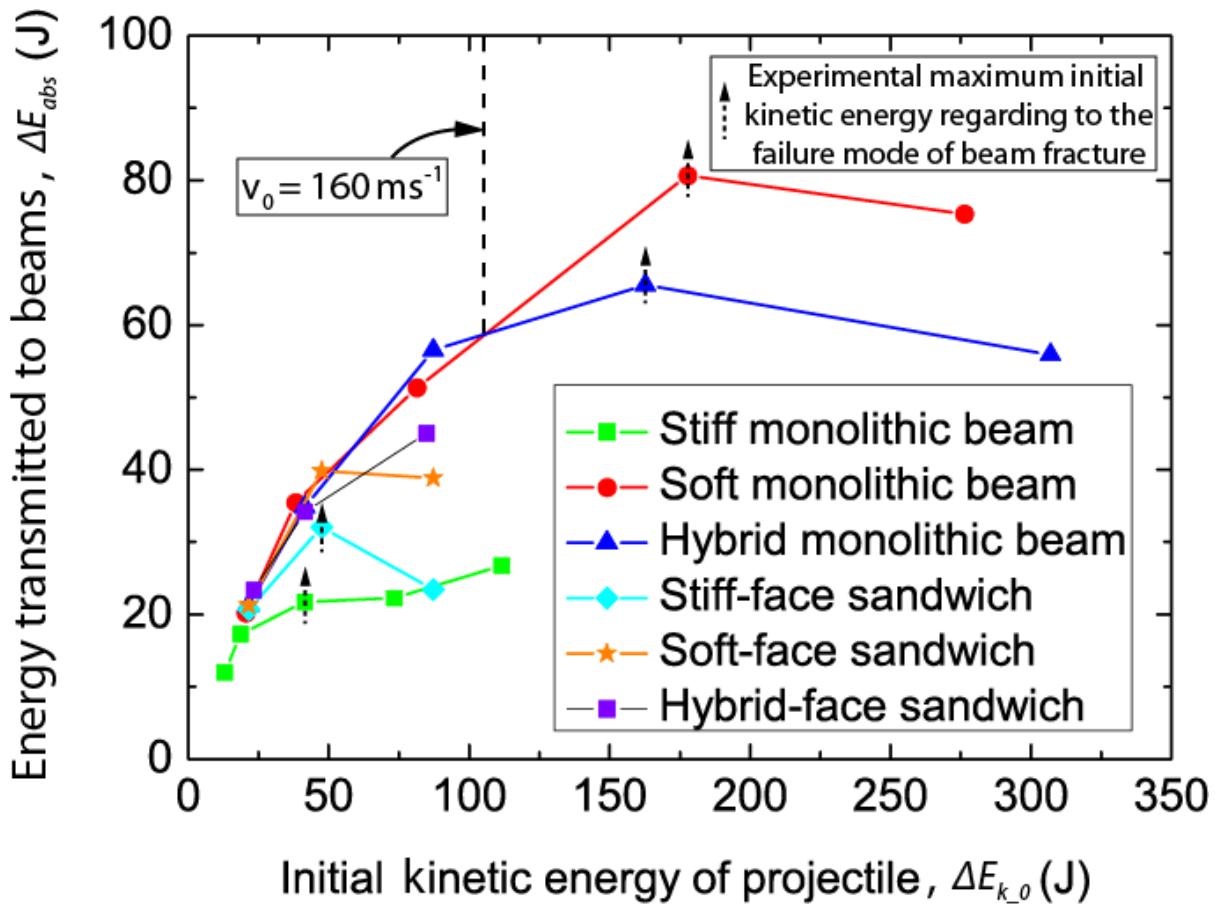


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Figure 15



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Figure 16