

Modelling reveals post-transcriptional regulation of GA metabolism enzymes in response to drought and cold

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Abstract

The hormone gibberellin (GA) controls plant growth and regulates growth responses to environmental stress. In monocotyledonous leaves, GA controls growth by regulating division-zone size. We used a systems approach to investigate the establishment of the GA distribution in the maize leaf growth zone to understand how drought and cold alter leaf growth. By developing and parameterizing a multiscale computational model that includes cell movement, growth-induced dilution and metabolic activities, we revealed that the GA distribution is predominantly determined by variations in GA metabolism. Considering wild-type and UBI::GA20-OX-1 leaves, the model predicted the peak in GA concentration, which has been shown to determine division-zone size. Drought and cold modified enzyme transcript levels, although the model revealed that this did not explain the observed GA distributions. Instead, the model predicted that GA distributions are also mediated by post-transcriptional modifications increasing the activity of GA20oxidase in drought and of GA2oxidase in cold, which we confirmed by enzyme activity measurements. This work provides a new, mechanistic understanding of the GA metabolism in plant growth regulation.

Word count 171/250

Significance statement

Explanation of the significance of the research at a level understandable to an undergraduate-educated scientist outside their field of specialty:

Understanding why plant growth reduces in drought and cold is essential to understand how these conditions affect crop yields. Previous studies have shown that growth depends on the distribution of the hormone gibberellin (GA). By developing a computational model and comparing predictions with GA measurements, we show that the GA distribution is mainly created by spatial variations in GA synthesis and degradation. We reveal that although the synthesis and degradation enzyme transcripts are affected by drought and cold, this does not explain the GA distributions. Instead, we find that specific enzyme activities are increased to create the GA distributions that underlie the growth responses. Thus, we gain a fundamentally new understanding of plant growth inhibition by drought and cold.

119/120 words

Introduction

The hormone gibberellin (GA) controls plant growth and plays a key role in growth responses to environmental conditions (1, 2). This growth regulation is thought to be underpinned by the GA distribution; however, how the GA distribution is regulated is largely unknown. In roots and monocotyledonous leaves, the sizes of the division zone (DZ) and elongation zone (EZ) are key parameters that determine overall organ growth rates (3-6). The boundaries of these growth zones are dynamically controlled by hormone distributions (7), which depend on hormone metabolism, transport between cells, and dilution (due to cell growth). In *Arabidopsis* roots, for example, the DZ size has been shown to be regulated by GA synthesis (8-10), GA signaling (11), auxin transport (12, 13) and cross-talk between auxin and cytokinin (14-16).

Maize leaves provide an alternative organ for studying growth regulation, with the major advantage that they enable direct measurement of spatial distributions of hormone and transcript levels and enzyme activities along the growth zone (9, 17). In maize leaves, bioactive gibberellins, GA₁ and GA₄, show a distinct maximum within the DZ (9, 17). Kinematic and hormone analysis of wild-type leaves, *dwarf3* leaves (defective in GA synthesis), and UBI::GA20-OX-1 leaves (over-expressing a key GA20ox biosynthesis enzyme) demonstrated that the GA₁ distribution determines the length of the DZ (9) (similar to its function in the *Arabidopsis* root (8), although sensor observations suggest GA distribution differs (18)). Thus, the expression of GA metabolic enzymes plays a key role in creating the GA₁ distribution and controlling DZ size (9). These GA metabolic enzymes also mediate growth responses to cold (19, 20), salt (21), nutrients (10, 22), light (23) and water (24), and crosstalk between the growth-regulatory hormone pathways (25, 26), making them a key component of environmental growth responses.

Although metabolite and transcript measurements along the growth zone provide insights into how hormone levels are related to local cell division and expansion, they essentially produce static measurements, making it hard to infer the underlying dynamic processes. Understanding how molecular and cellular processes interact to establish, maintain and adjust the hormone distributions that control organ growth can be challenging, and theoretical models have proven invaluable in providing a mechanistic understanding (13, 14, 16, 27-29). Considering the GA dynamics within the *Arabidopsis* root, previous modelling demonstrated that cell elongation causes significant dilution in the EZ (28). Thus, in contrast to auxin distribution being primarily determined by carrier-mediated transport (12, 13), the GA distribution appears to be controlled by an entirely different mechanism.

In this study, we gain a mechanistic understanding of how GA distributions are controlled. We develop a multiscale model of GA dynamics within the maize leaf growth zone, by combining a detailed model of the GA metabolism within each cell with cellular growth dynamics. Focusing on the maize leaf enables us to compare model predictions to spatial metabolite and enzyme data (which is not feasible in smaller species such as *Arabidopsis* (17)), revealing that bioactive GA distribution is predominantly determined by spatial variations in metabolism.

We apply the new model to investigate how drought and cold affect the GA distribution, to understand how these stresses alter leaf growth. Mild drought reduces maize leaf growth by reducing DZ size, bioactive GA levels and the transcript levels of the GA20oxidase biosynthesis enzymes (30). The model reveals that GA20oxidase activity is increased to counteract the reduction in GA20oxidase transcripts, suggesting that the lower bioactive GA levels and growth response is mediated instead by increased transcription of the GA2ox catabolic enzymes.

The role of GA in the response to cold, which inhibits cell division rates but not DZ size (31), is still unclear. Measurements revealed a substantial reduction in the GA2oxidase transcripts, suggesting that cold reduces GA degradation. However, the model revealed that GA2oxidase activity is increased to counteract the reduced transcript levels and maintain bioactive GA concentrations at control levels. Thus, the model reveals new insights into drought and cold responses, suggesting modulation of specific oxidation rates determines bioactive GA distributions that underpin growth regulation.

Results

Model description

To understand how GA distribution is regulated, we constructed a cell-based model that describes GA biosynthesis, degradation and dilution (due to cell growth) within the maize leaf growth zone (Fig. 1a,b). The model exploits the simple linear leaf geometry and represents the leaf as a single file of cells. Based on stable leaf elongation rate (LER) during the first 5 days after emergence (31), we consider leaf growth to be in steady state. The model integrates cell growth and division rates from experimental measurements (32) (Fig. 1c-f). Cell length decreases slightly close to the base of the leaf before increasing with distance along the growth zone (Fig. 1c). Velocity is zero at the base of the leaf and increases with distance along the growth zone (Fig. 1d). Using these data, we calculated the relative elongation rates (RER) (Fig. 1e), which follows a roughly bell-shaped curve, and the cell division rates (Fig. 1f), which show a bell-shaped curve spanning the

DZ. The model also integrates the increase in the leaf's cross-sectional area along the growth zone to accommodate increases in cell volume when simulating dilution (33). Consistent with approximate doubling of both width and thickness of the leaf (33), volumetric quantifications showed that leaf cross section increases more than 5-fold across the growth zone (Fig. 1g). With these growth dynamics (Fig. 1c-f), the maize leaf growth zone is represented by a file of ca.1400 cells, with ~700 cells in the DZ and ~700 cells in the EZ. These growth dynamics are used to simulate dividing and growing cells (see Supplementary Information text (SI)).

In the model, we incorporated the sub-cellular structure of the cells. Within the DZ, cells predominantly contain nucleus and cytoplasm; we assumed that the nuclear volume is constant and equal to 50% of the cell volume at the most basal position (noting that nuclear volume stays constant in virtual absence of endoreduplication in maize leaves (31)), and thus, cell growth in the DZ occurs due to cytoplasmic expansion. Within the EZ, growth occurs primarily by rapidly increasing vacuolar volume. Based on cell length and cross-sectional area distributions (Fig. 1c,g), we calculated that cell volume increases approximately 12-fold over the EZ, which, under the assumption of vacuolar expansion (with no increase in nucleus or cytoplasm volume), results in around 92% of the cells' volume being vacuole when they enter the mature zone. This value agrees with previous suggestions that the vacuole takes up 90% – 95% of the cell volume (34).

GA biosynthesis involves a series of oxidation steps, converting the precursor, geranylgeranyldiphosphate (GGPP), to the bioactive GA₄ and GA₁ (35, 36). GA biosynthesis has been shown to be predominantly regulated at the later steps of this pathway (37) whereby GA₅₃ and GA₁₂ are converted to bioactive GAs (35, 36). Focusing on the pathway that leads to the more prevalent bioactive GA in maize, GA₁ (9) (Fig. 1b), we simulated GA biosynthesis and degradation within each cell: GA₅₃ undergoes a series of oxidation steps mediated by GA20ox to produce GA₂₀, which is converted to the bioactive GA₁ by GA3ox (35). GA2oxidases degrade the bioactive GA₁ and precursor GA₂₀ to GA₈ and GA₂₉, respectively, which are in turn converted by the GA2oxidase to their catabolite forms (35). We represented these reactions by a system of ordinary differential equations (ODEs) for the metabolite, enzyme and complex concentrations: each step was modelled using the law of mass action by assuming the GA metabolite first binding to the enzyme with a reversible reaction, and the resulting complex then dissociating into the next GA metabolite in the pathway and the enzyme (38). We assumed that enzymes are translated at a rate proportional to the transcript level.

The reactions involved in the GA metabolism pathway downstream of GA₅₃ occur in the cytoplasm (35, 36), and we assumed that the enzymes and complexes are only present in this compartment.

Data in Arabidopsis suggest that GA metabolites are also present in the nucleus and the vacuole (39). In absence of analogous data in maize, we assumed this to be similar in maize, hence within the model assuming equal metabolite concentrations throughout the cell.

Prescribing the growth dynamics and distributions of the GA_{53} concentration and GA20ox, GA3ox and GA2ox transcript levels, the cell-based model can be simulated to predict the distributions of the downstream metabolites, enzymes and complexes. The spatial distributions of the GA_{53} concentration and GA20ox, GA3ox and GA2ox transcript levels are upstream inputs, each of which are represented by a sum of b-spline functions (40) with coefficients that are estimated using the experimental data as part of the model fitting (see SI).

To summarize, we have developed a cell-based model that describes GA metabolism and dilution within the Maize leaf growth zone; the key assumptions behind this cell-based model (described above) are compiled in Table S1.

Derivation of a reduced model

The cell-based model comprises 17 ODEs for each cell in the growth zone, which for 1400 cells, results in a system of 25200 ODEs, which can be simulated until they reach a steady state. For a given parameter set, the cell-based model took several hours to run to predict the steady-state distributions, making detailed parameter surveys impractical. To estimate model parameter values that enable the model to reproduce the experimental data, we needed to derive a reduced model to reduce the simulation time. We derived a continuum description of the cell-based model, considering quantities in terms of distance from the leaf base. We further reduced the model by assuming that the ratio between the enzyme concentrations and metabolite concentrations are small (an approximation typically taken when modelling enzyme reactions (41), and shown previously to be appropriate for GA20ox-mediated oxidation (42)). The resulting reduced model comprised a system of 6 ODEs in terms of distance from the leaf base for the concentrations of GA_{44} , GA_{19} , GA_{20} , GA_1 , GA_{29} and GA_8 (highlighted with green stars in Fig. 1b), which depend on 8 oxidation rate constants (one associated with each oxidation step, which encompasses the translation rate, binding rates and enzyme activity), the 4 input functions (representing the spatial distributions of GA_{53} concentration and GA20ox, GA3ox and GA2ox transcript levels; pink stars in Fig. 1b) and the prescribed growth dynamics.

To aid clarity, we provide a summary of the model assumptions underlying the reduced model in Supplementary Table S1. As described below, using the reduced model, we were able to estimate

the reduced model parameters for a given experimental dataset and therefore all model results presented in Figures 2-5 are created by simulating the reduced model.

GA₁ distribution is predominantly determined by spatial variations in metabolism

To test whether the reduced model could represent our observations, we initially parameterized the reduced model using published experimental measurements of metabolite and transcript levels within 12 leaf segments along the maize leaf growth zone, fitting the reduced model parameters independently to data from B104 (9) and B73 inbred lines (30). Prior to fitting, we converted the metabolite measurements (in ng/gDW) (Figs. S4, S5), to nM concentrations (Figs. S6 and S7; SI). After the conversion, the spatial metabolite distribution profiles are globally similar to the original data but can differ in detail; for example, in the nM concentration profile, the peak GA₁ is slightly closer to the leaf base than in the corresponding GA₁ measurements (Fig. S8). Based on these data, we estimated parameters by minimising a weighted sum of squares criterion (detailed in Supplementary text, section 2.3.4). With the estimated parameters, the reduced model showed a reasonable agreement with the experimental measurements (Figs. 2b-k, S10) and faithfully reproduced the peak in cytoplasmic GA₁ level within the DZ (Fig. 2i).

Using the reduced model enabled us to estimate the model parameters (i.e. the rate constants in the metabolism network); thus, we were able, for the first time, to assess the relative impact of individual cellular and subcellular processes on the established GA₁ distribution. Removing either the presence of dilution (Fig. 3a) or the presence of cell movement (Fig. 3b), or the presence of both dilution and cell movement (Fig. 3c), had little effect on the predicted GA distributions. Similar results were obtained for B104 (Fig. S10). The influence of dilution and cell movement on the GA distribution depends on the magnitudes of the rate constants – with the estimated rate constants, the metabolism network quickly reaches an equilibrium within each cell so that dilution and cell movement are slower processes that have little effect on the predicted GA concentrations (see Fig S11, which shows how dilution and cell movement have an effect on the GA₁ distribution if the rate constants are smaller). We conclude that dilution and cell movement have only minor effects on the GA distributions, and that the GA₁ distribution is predominantly determined by the spatial variations in metabolism.

The estimated parameters provide insights into the mechanisms that determine the distributions of the GA metabolites, and differences between the B73 and B104. The parameter estimates obtained (Table S2) suggests that for B73 the GA₂ox-mediated degradation rate of the precursor GA₂₀ is small, but that there is a faster GA₃ox-mediated conversion of GA₂₀ to the bioactive GA₁,

which explains the low GA_{20} concentrations observed. In contrast, for B104, the degradation of GA_{20} is fast, whereas the conversion of GA_{20} to GA_1 is slower. To test this model prediction experimentally, we therefore directly compared the rates of GA2ox and GA3ox in the growth zone of B73 and B104 leaves. In agreement with the model prediction, these data revealed that in B73, GA3ox enzyme activity (producing GA_1) is consistently higher than GA2ox activity (producing GA_{29} ; Fig. 3d). Moreover, as predicted by the model, in B104 the inverse situation occurs (Fig. 3e).

As one may expect, doubling the GA20ox-mediated oxidation rates increases the predicted GA_1 concentrations (Figs. 3f, S12), whereas doubling the GA2ox rates decreases the predicted GA_1 concentrations (Figs. 3f, S13) although the qualitative features of the GA_1 distribution remain the same. Varying the oxidation rate associated with the GA3ox-mediated step had little effect on the GA_1 predictions (Figs. 3f, S14; doubling the GA3ox oxidation rate increases the rate at which GA_{20} is converted to GA_1 , however, this also decreases the GA_{20} concentrations: at quasi-steady state these processes cancel each other out, resulting in little effect on the GA_1 distribution).

The reduced model also enabled us to investigate the importance of the spatial distributions of the GA_{53} metabolite and enzyme transcript levels. With constant GA_{53} , the predicted GA_1 formed only a small peak in the DZ and increased as cells left the growth zone (Figs. 3g, S15), whereas with constant enzyme levels, the GA_1 peak in the DZ was less pronounced (Figs. 3h, S16). We conclude that the spatial variations in both GA_{53} and enzyme transcription are essential to create the GA_1 distribution that underpins the growth regulation.

Activity of the heterologous GA20ox is higher than the native enzyme

We next set out to test if the reduced model is able to explain the effect of experimental perturbations on GA metabolism, distribution and leaf growth. We first studied the effects of over-expressing the AtGA20-oxidase1 biosynthesis enzyme (UBI::GA20-OX-1), which enhances bioactive GA levels and growth in both Arabidopsis (43, 44) and maize by increasing DZ size (9) (Fig. 4a). To investigate how over-expressing AtGA20-oxidase1 affects the metabolism dynamics, we simulated the UBI::GA20-OX-1 dynamics by including an additional enzyme, AtGA20ox, in the reduced model and incorporating terms representing the rate at which the AtGA20ox enzyme mediates the three oxidation steps: GA_{53} to GA_{44} , GA_{44} to GA_{19} , and GA_{19} to GA_{20} . Initially, we assumed that for each of these steps the native and heterologous GA20oxidase enzyme transcripts mediate the same rate of metabolite oxidation, and tried to fit the reduced model to metabolite and transcript data from wild-type and UBI::GA20-OX-1 (9). With this assumption, we

found that the reduced model could not recapitulate the spatial distributions of transcript and metabolite levels observed experimentally (Fig. S17); the reduced model suggests that for the downstream GAs to be higher in UBI::GA20-OX-1 requires GA₅₃ to also be higher, which is not reflected in the experimental data (Fig. 4b,g-l).

We solved this conundrum, by allowing each of the three GA20ox-mediated oxidation rates to be different between the native and heterologous enzymes, which led to reasonable agreement between the reduced model and data (Fig. 4b-l). Considering the estimated parameters (Table S4), the estimated conversion rate of GA₅₃ to GA₄₄ is approximately 20 times higher for AtGA20-oxidase1 and the conversion rates of GA₄₄ to GA₁₉ and GA₁₉ to GA₂₀ are approximately double that of the native enzyme. This explains why downstream GA concentrations are higher in the over-expression line (Fig. 4g-l) despite GA₅₃ concentrations being lower (Fig. 4b). These differences are likely due to differences in translation efficiency, protein degradation, or enzyme activity between the native and heterologous enzymes. The reduced model shows that the differences in GA20ox activity result in the GA₁ concentration having a higher maximum, but reducing to a similar level at the boundary between the DZ and EZ (at ca 18 and 25 mm from the leaf base for wildtype and UBI::GA20-OX-1, respectively), consistent with the GA₁ distribution controlling the DZ size via a threshold mechanism (i.e. the transition to the EZ occurring where GA₁ levels reduce below a threshold value) (9). We conclude that the reduced model recapitulates published data and identifies new details in the molecular regulation of GA metabolism, such as differential specificity in the activities of the native and heterologous gene product.

Drought and cold regulate distinct enzymatic reactions

Next, we used the reduced model to determine if and how GA distributions are affected by environmental stress and if this could explain the growth response. We applied the reduced model to published experimental data involving drought conditions (30), and newly collected data in cold conditions (31). Both stresses reduced leaf elongation rate by 20-30% (30, 31) (Fig. 5a,b), but this was due to different underlying cellular behaviours: a reduction in DZ size in drought (30, 45) (Fig. 5c, Table S3) and a reduction in division and elongation rates in cold (31) (Fig. 5d, S2).

Measured metabolite levels (in ng/g DW) showed GA₁ levels are reduced in both drought and cold (Fig. 5e). We first converted these measurements to concentrations (nM), taking into account cross-sectional area. In drought, cross-sectional areas are similar to those of the control (Fig. 5f), so that, as for the GA₁ measurements, GA₁ concentrations (in nM) are also reduced in drought (Fig. 5g). However, in cold, cross-sectional areas are much lower (Fig. 5f), resulting in GA₁

concentrations in cold that are in fact similar to those in control conditions (Fig. 5g). We concluded that drought, but not cold, reduces the GA₁ concentrations. Measured GA₅₃ levels (in ng/gDW) were little affected by drought or cold (Fig. S4), resulting in GA₅₃ concentrations that are increased in cold (once converted to nM), suggesting cold affects the pathway upstream of GA₅₃ (Fig. 5h). These observations illustrate the importance of conversion to nM concentrations when interpreting metabolite measurements.

Measurements of transcript levels revealed that drought reduces GA20oxidase and increases GA2oxidase levels (Fig. 5i,k), whereas cold reduces GA2oxidase levels (Fig. 5k). We first tested if these perturbed enzyme transcript levels cause the observed metabolite distributions, assuming identical oxidation rate constants, by fitting the reduced model to the control, cold and drought transcript and metabolite data. With this assumption, we were unable to reproduce the metabolite distributions (Fig. S18). The predicted difference between GA₁ in control and drought conditions is much less than observed, whereas GA₁ was predicted to be higher in cold than in control conditions, again in contrast to the data.

To resolve this discrepancy, we hypothesized that drought and cold regulate the GA pathway by additional mechanisms (e.g. translation, protein stability or enzyme activity). To test this theory, we fitted the reduced model to the data allowing the oxidation rate constants for either the GA20oxidase-mediated steps, the GA3oxidase-mediated step or the GA2oxidase-mediated steps to be different in cold and drought. To select among the resulting 16 possible cases (Table S5), we used the Akaike Information Criterion (AICc) (46), a statistical measure which assesses the goodness of fit whilst penalizing model complexity by taking into account the number of model parameters. Fitting the model and calculating the AICc in each case provided a means to select among the possible cases. Considering the AICc values obtained (Table S5), our results suggested that the rate constants governing the GA20oxidase-mediated steps are perturbed in drought and the rate constants governing the GA2oxidase-mediated steps are perturbed in cold (Fig. 5h-q). The parameter estimates (Table S6) suggest that in drought, the conversion rates of GA₅₃ to GA₄₄ and GA₁₉ to GA₂₀ are similar to those in control conditions, whereas the conversion rate of GA₄₄ to GA₁₉ is approximately doubled, providing an explanation as to why GA₁₉ concentrations are similar in drought and control conditions, while GA₄₄ is lower in drought. The parameter estimates suggest that in cold the degradation rates of both GA₂₀ and GA₂₉ are higher than in control conditions, so that overall degradation is substantially increased in cold despite the GA2oxidase transcript levels being lower.

Thus, our modelling approach identified specific GA enzyme activities impacted by drought and cold and explain the observed metabolite levels. Although in drought GA20oxidase transcript levels are lower than in control conditions (Fig. 5i), the reduced model predicted that GA20oxidase enzymes mediate the GA₄₄ to GA₁₉ oxidation step at a higher rate. This suggests that GA₁ synthesis in drought is similar to that in control conditions, and that the lower GA₁ concentrations are caused by increased degradation mediated by increased GA2oxidase transcript levels. In cold, the GA2oxidase transcripts are expressed at lower levels than in control conditions, but the rate constant associated with GA2ox-mediated GA₂₀ degradation is increased, explaining why GA₁ concentrations are similar in control and cold conditions.

Enzyme activity measurements support model predictions

To test the surprising model prediction that enzyme activities (relative to their transcript levels) increased in response to cold and drought, we performed further experiments to measure the enzyme activity directly. We considered six reactions for each condition: GA₅₃, GA₄₄ and GA₁₉ were used to determine GA20oxidase activities, and GA₁, GA₂₉ and GA₈ to obtain GA2oxidase activities. The enzymes were extracted from 10mm segments from the maize leaf growth zone. These data (Fig. S19) were used to calculate the oxidation rate constants (see SI for details).

In agreement with the model predictions, the oxidation rate mediated by GA2ox increased in cold conditions (Fig. 6). For drought, there was a trend for higher oxidation rates associated with GA20ox activity, also in support of the model predictions. Therefore, these *in-vivo* activity measurements support the *in-silico* prediction of increased specific enzyme activities in cold (GA2ox) and drought (GA20ox) conditions.

Discussion

GA regulates plant growth and growth response to environmental conditions (1, 2). Understanding how local bioactive GA levels are controlled is key to understanding these growth responses. However, often in studies of GA metabolism only static measurements are made of metabolite and transcript levels. Although static measurements have led to profound insight into how GA regulates growth, our innovative approach to use computational modeling in combination with *in-vivo* measurements allows us to expand our knowledge to the dynamics of the reactions in responses to heterologous transgenes and environmental conditions.

We present a mathematical model that simulates the key cellular and subcellular processes governing GA distribution in the maize leaf growth zone. The modelling revealed that the bioactive GA₁ distribution is predominantly determined by the spatial variations in metabolism. We validated the model by demonstrating that it recapitulates experimental data from both wild type and plants over-expressing the AtGA20-oxidase1 biosynthesis enzyme (UBI::GA20-OX-1). This revealed that the heterologous AtGA20-oxidase1 enzyme is substantially more active than the native maize version, with a much higher rate of conversion of GA₅₃ to GA₄₄.

The model also allowed us to obtain drought and cold responses that could not be deduced from the gene expression and metabolite distributions alone. The modelling suggested that the GA₁ concentrations in the stressed conditions are not the result of changes in enzyme transcript levels alone. Instead, oxidation rates associated with specific enzymes were increased in the stressed conditions, suggesting that stress-induced post-transcriptional regulation of enzyme activities has a major effect on GA₁ levels under these conditions. Subsequent enzyme-activity assays validated these model predictions, suggesting that further studies of GA oxidation enzymes at the protein level are needed to understand the regulation of bioactive GA levels and growth.

The predicted GA₁ distributions provide an explanation for how GA metabolism regulates the growth dynamics. Higher GA₁ concentrations in UBI::GA20-OX-1, and the lower GA₁ concentrations under drought shift the position at which the GA₁ reaches a threshold value thought to determine the DZ length (9, 30) (i.e. a larger DZ in UBI::GA20-OX-1, and a smaller DZ in drought). The modelling enabled us to identify which specific oxidation steps are affected in these cases to create this GA₁ distribution and growth response. The reduction in leaf growth in cold is due to a different cellular mechanism: a reduction in division and elongation rates rather than DZ length (31). Our study revealed that once converted to nM concentrations, the GA₁ distribution in cold is approximately the same as in control conditions, explaining why the growth zone lengths are not affected. Our findings therefore suggest that the growth inhibition by cold does not appear to be regulated by the GA pathway.

While the model predictions generally agreed well with the experimental measurements, there are naturally some differences. These differences may be caused by variability in the data (for instance, differences between the predictions and data at the GA₁ peak in the control case in Fig 5o, may be caused by the relatively large standard errors in the measured GA₁ levels in this region, shown in Fig 5e). Additional differences may be caused by biological phenomena or variability not explicitly considered in the model.

Fitting the model to the data required us to develop a reduced model. Although cell-based models, which simulate populations of dividing, growing cells, are often used to investigate hormone dynamics (13, 29, 47), the simulation times involved typically make formal parameter estimation impractical. Simulations are particularly slow for the maize leaf growth zone which contains ~1400 cells in each file (31), in contrast to only ~70 in *Arabidopsis* (48). This made it necessary to derive a continuum approximation of the cell-based model. This approach, to move from the Lagrangian (or material) viewpoint to the Eulerian (or spatial) one, has played a major role in understanding plant growth kinematics (49-51), although has received limited attention by hormone modellers (52, 53). We also considered methods for integrating spatially varying inputs (i.e. components that are regulated by upstream processes not included in the model) via b-spline representations. There is much potential to translate these modelling approaches to study dynamics in other cell-based systems.

Our study demonstrates the usefulness of a detailed model of GA metabolism within the growing maize leaf. To gain a more complete insight, this model could be extended, for example, to investigate the downstream GA signalling pathway and growth regulation, the parallel pathway that mediates the synthesis of the bioactive GA₄ (which is the main bioactive GA in other species such as *Arabidopsis* (54)), GA metabolism dynamics in other plant organs or how GA metabolism enzymes are regulated by other hormones (29, 55). Furthermore, the transcript and metabolite measurements used here are from the whole leaf segment, although in *Arabidopsis* roots, GA levels and responses have been shown to vary between tissues (8, 56, 57). Studying whether differences between tissues exist in maize leaves could motivate a more detailed 2D or 3D model that incorporates cellular geometries and tissue-specific processes. Such model developments would be able to reveal further details the intricate and interacting multiscale interactions involved in organ growth regulation.

Methods

Modelling

Full details of the mathematical model are provided in the SI. We defined a cell-based model integrating growth, metabolism and dilution (SI, §2), and used this to derive a reduced model (SI, §3). We simulated the reduced model by specifying growth using experimental measurements (SI, §2.3.1), and used the metabolite and transcript data to estimate the **reduced** model parameters using Matlab's `lsqnonlin` optimization algorithm (SI §2.3.2-4).

Plant Material and Growth conditions

Plant material and growth conditions were as described in (31) (cold) and (30) (drought).

Hormone profiling

For hormone profiling, sampling, extraction, purification and hormone metabolic profiling were performed as described in (9). Data for the UBI::GA20OX-1 experiment (Fig. 4) was previously published in (9).

Transcript levels

Enzyme transcript levels were measured as described in (9). Transcript data for the UBI::GA20OX-1 experiment (Fig. 4) is as in (9). In the drought-cold experiment (Fig. 5), *GA20ox* levels are the summation of the measured levels of *GA20ox1*, *GA20ox2.1* and *GA20ox2.2*, *GA3ox* is the level of *GA3ox2*, and *GA2ox* levels are the summation of *GA2ox3.1*, *GA2ox3.2*, *GA2ox4*, *GA2ox6.2*, *GA2ox7.1* and *GA2ox7.3*, each measurement being the mean of n=3-7 replicates for positions 0-30, located around the GA maximum, and 95 mm, located at the end of the growth zone, and of n=1-3 replicates for positions 35-85 mm where GA levels are relatively stable.

Kinematic analysis

Kinematic analysis and measurements of division-zone length were performed as described in (32). The cross-sectional areas were calculated by measuring the volumes of 1cm segments of leaf.

Assay of gibberellin metabolism enzymes

Enzymes were extracted from 10 segments of the 4th maize leaf, and enzyme activities were measured directly as described in SI §1.

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Author contributions

L.R.B., H.N. and G.T.S.B conceptualized the study; L.R.B. and S.P.P. developed, reduced and parameterised the mathematical model, H.N., B.R., E.P. and H.A.E. performed the lab-based experiments; L.R.B. and G.T.S.B. wrote the manuscript; all authors contributed to analyzing the results and data, and to editing the manuscript.

Figure legends

Figure 1 | Model summary. (a) Schematic representation of the maize leaf showing the division, elongation and mature zones. We model the leaf as a file of cells, with cytoplasmic expansion in the division zone and vacuolar expansion in the elongation zone. (b) The gibberellin biosynthesis and degradation network. In the network diagram, red boxes are used for the metabolites, blue boxes are used for the enzymes, pink stars label the components modelled as input/forcing functions (parameterised via data on GA_{53} metabolite levels and gene expression levels of *GA20ox*, *GA3ox* and *GA2ox*), whereas green stars label the components

that are solutions of the ODEs (which are fitted to measurements of the corresponding metabolites). (c-g) Growth dynamics for maize leaf 4, B73. (c) Experimental measurements of cell lengths away from the leaf base, data show averages calculated via interpolation using measurements from n=3 leaves. (d) Cell velocities calculated from data in panel (c). (e) Cell's relative elongation rates calculated from data in panel (d). (f) Cell division rates calculated from data in panels (c) and (d). (g) Experimental data for the leaf cross-sectional area (mean \pm s.e. with n=10). Panels c-f show bars at the x-axis marking the DZ region (n=3). The corresponding growth dynamics for other cases are shown in Figs. S1-3.

Figure 2 | Summary and predictions of the reduced model, fitted to the control wild-type data for B73. (a) Schematic summarising the differences between the original cell-based model and the reduced model. (b-k) Measured and predicted distributions of GA metabolites and enzymes along the maize leaf. Data for B73 maize are shown with red stars and fitted reduced model predictions with solid blue lines. Panel i also shows the mean position of the boundary between the DZ and EZ (dashed black lines, Table S3, n=3). Metabolite data (panels b, f-k) show mean concentrations calculated from mean values from data on metabolite levels (Fig S4), dry weight (Fig S3c) and leaf cross-sectional area (Fig S3a). Transcript data (panels c-e) show mean values for n=3-7 (positions 0-30 and 95 mm) and n=1-3 (positions 35-85 mm).

Figure 3 | Analysing the reduced model predictions for control, wild-type dynamics. (a-c) Effect of model components on the predicted cytoplasmic GA₁ concentration: (a) with (solid line) and without (dashed red line) dilution; (b) with (solid line) and without (dashed red line) cell movement away from the leaf base; (c) with (solid line) and without (dashed red line) dilution and cell movement away from the leaf base. (d,e) Degradation/oxidation of GA₂₀ by GA2ox (production rate of GA₂₉) and GA3ox (production rate of GA₁) in (d) B73 (e) B104 wild-type leaves. Data show mean \pm s.e. for n=4. (f) Effect of the oxidation rates on the predicted GA₁ distribution. (g) Effect of setting the GA₅₃ concentrations to be spatially constant on the predicted GA₁ distribution. (h) Effect of setting the enzyme transcript levels to be spatially constant on the predicted GA₁ distribution (for panels f-h, see Figs. S12-16 for the corresponding predictions of the other components). Panels a-c also show the mean position of the boundary between the DZ and EZ (dashed black lines, Table S3, n=3).

Figure 4 | Effect of GA20ox over-expressing line (UBI::GA20-OX-1) on GA pathway. (a) Relative elongation rates for wild type and GA20ox over-expressing line (UBI::GA20-OX-1), calculated from mean cell velocity data given in Fig S2 (n=3). (b-l) Measured and predicted distributions of GA metabolites and enzymes along the maize leaf for wild type (blue) and the GA20ox over-expressing line (UBI::GA20-OX-1) (red). Predictions are from the reduced model with estimated parameters given in Table S4. Metabolite data (panels b,g-l) show mean concentrations calculated from mean values from data on metabolite levels (Fig S5), dry weight (Fig S3c) and leaf cross-sectional area (Fig S3b). Transcript data (panels c-f) show mean values for n=3. Panel j also show the mean position of the boundary between the DZ and EZ for wild type (dashed blue line) and UBI::GA20OX-1 (dashed red line), n=3.

Figure 5 | Influence of drought and cold on GA pathway. (a) B73 maize plants subjected to cold conditions. (b) B73 maize plants subjected to drought conditions. (c) Measured DZ lengths in control (blue), drought (green) and cold (red) condition (mean \pm s.e. with n=3 replicates). (d) Relative elongation rates in control (blue), drought (green) and cold conditions (red). (e) Measured bioactive GA₁ levels (in ng/gDW) in control (blue), cold (red) and drought (green) conditions (mean

± s.e. with n=3 replicates). **(f)** Measured leaf cross-sectional areas in control, cold and drought conditions (mean ± s.e. with n=10 for drought, and n=12 for cold). **(g)** Mean GA concentrations (in nM) calculated using data in panels **d** and **e** and Fig S3. **(h-q)** Metabolite and enzyme distributions in control (blue), cold (red) and drought (green) conditions. Data shown with stars and fitted model predictions with solid lines. Panels (d,e,h,o) show bars at the x-axis marking the mean DZ region for control (blue), drought (green) and cold (red) conditions (n=3). Predictions in panels h-q are using the reduced model and assuming that the activity of the GA20oxidase is changed under drought whereas the activity of the GA2oxidase is changed under cold conditions. Metabolite data (panels h, l-q) show mean concentrations calculated from mean values from data on metabolite levels (Fig S4), dry weight (Fig S3c) and leaf cross-sectional area (Fig S3a). Transcript data (panels i-k) show mean values for n=3-7 (positions 0-30 and 95 mm) and n=1-3 (positions 35-85 mm).

Figure 6 | Reaction rates calculated from measurements of enzyme activity for control (blue) drought (green) and cold (red) conditions. (a-c) Reactions mediated by GA20oxidase: GA₅₃ to GA₄₄ **(a)**; GA₄₄ to GA₁₉ **(b)**; and GA₁₉ to GA₂₀ **(c)**. **(d-f)** Reactions mediated by GA2oxidase: GA₁ to GA₈ **(d)**; GA₂₉ to GA₂₉ catabolite **(e)**; and GA₈ to GA₈ catabolite **(f)**. Data show mean ± s.e. calculated from degradation rate data (Fig S19, n=3) and enzyme transcript levels (Fig 5h-j, n=1-7).

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