

1 **Wi-Fi fingerprinting based on collaborative confidence level training**

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6 **Abstract:**

7 Wi-Fi fingerprinting has been a popular indoor positioning technique with the advantage that
8 infrastructures are readily available in most urban areas. However wireless signals are prone to
9 fluctuation and noise, introducing errors in the final positioning result. This paper proposes a new
10 fingerprint training method where a number of users train collaboratively and a confidence factor
11 is generated for each fingerprint. Fingerprinting is carried out where potential fingerprints are
12 extracted based on the confidence factor. Positioning accuracy improves by 40% when the new
13 fingerprinting method is implemented and maximum error is reduced by 35%.

14 **Keywords:**

15 Indoor positioning, Wi-Fi fingerprinting, collaborative positioning

16 **1 Introduction**

17 With the advancement in positioning as well as mobile technologies, location based
18 services (LBS) are no longer just trendy fantasies. LBS applications are expanding from military
19 and government sectors rapidly into commercial and civil applications. Therefore, the
20 fundamental requirement for positioning and navigation is becoming more demanding as
21 solutions are required in more complicated environments, where traditional positioning methods
22 such as Global Navigation Satellite Systems (GNSS) fails. This is known as the indoor positioning
23 problem and numerous methods have been explored over the years to improve positioning
24 performance in such environments [1,2]. Wireless network signal based positioning, such as Wi-
25 Fi fingerprinting, have become widely applied in indoor positioning due to high availability of
26 Wi-Fi signals in urban environments [3,4].

27 Yet Wi-Fi positioning is far from the perfect solution. Wi-Fi networks are not positioning
28 dedicated systems thus signals can be unstable, and sometimes unsuitable for positioning. Hence
29 accuracy and robustness cannot be guaranteed [5]. The complete process of Wi-Fi fingerprinting
30 is achieved in two phases, the training phase which must be carried out first to collect received
31 signal strength (RSS) measurements and the positioning phase to obtain positions based on the
32 fingerprints [6,7]. The positioning performance of fingerprinting relies on the applied positioning
33 algorithm as well as the accuracy and details of the fingerprint database. Therefore, in order to
34 achieve accurate positioning, a detailed database is required. This relies on carefully chosen
35 training points across the building as well as sufficient access points (AP) that covers the area of
36 interest, as more AP will give more information on the variation of signals when in different
37 locations. However, training can be very time consuming. Yet it must be retrained and updated
38 whenever the internal building structure or AP locations change [8,9]. Moreover, although many
39 buildings have been setup with dedicated dense wireless network enabling high accuracy
40 positioning, but most indoor environment still lack such coverage.

41 To reduce the time and human labour required for database training, Wi-Fi simultaneous
42 localisation and mapping (SLAM) had been applied to enable a quicker way of learning the signal
43 pattern around a new environment and allows the system to navigate in a new environment.
44 However inertial measurements and building information is required, and building information
45 may not always be accessible [10-12].

46 A basic requirement in fingerprinting is that the positions of the fingerprints must be
47 accurate and their RSS measurement should be up-to-date. Studies have looked into the possibility
48 of reducing training effort by reducing training points and training time [13]. Authors in [14,15]
49 looks into autonomous crowdsourcing method for training and updating the Wi-Fi database. For
50 crowd-sourced database, the accuracy of estimated positions of the training data is essential.
51 Collaborative positioning improves positioning accuracy and reliability by applying network
52 constraints on user's positioning measurements. Nearby users may form local networks where
53 relative constraints can be applied to adjust and share each other's measurements [16,17]. Authors

54 in [18,19] improve fingerprinting performance by allowing the user to interact with the system to
55 label locations and changes. However this requires active collaboration with the user who may
56 not be willing or could potentially make mistakes.

57 This paper looks into reducing the training effort by introducing a collaborative Wi-Fi
58 fingerprint database training (cFPDB) approach, which achieves quicker and more reliable
59 training. Gaussian Process (GP) regression is applied to generate fingerprints for the entire
60 database from a small amount of training data and a confidence factor is produced for each
61 fingerprint indicating how reliable it is. On the other hand, this solution especially addresses Wi-
62 Fi positioning problems in locations where dedicated network is unavailable and are covered only
63 by very sparse APs. With very few APs, users may not be able to observe enough signal variation
64 patterns for accurate positioning. An adaptive collaborative fingerprinting algorithm (WARCP)
65 based on the concept of collaborative positioning is also introduced which provides the location
66 reference for fingerprints as well as knowledge on the expected relationship between Wi-Fi
67 measurements collected by nearby users. Positioning flexibility is also improved as users have
68 the option of performing inertial navigation alone, with collaborative ranging aiding or Wi-Fi
69 fingerprint aiding based on available sensors and number of users.

70 This paper firstly introduces the collaborative Wi-Fi fingerprint training method and an
71 analysis on training data is presented to understand how much data is required for generating a
72 reliable database. WARCP is then discussed to achieve positioning based on the collaboratively
73 trained database and ranging constraint between users. Simulations are carried out based on the
74 proposed algorithms and discussed in Section 4. Both training and positioning results are analysed
75 for efficient and reliable Wi-Fi fingerprint training and positioning.

76 **2 Collaborative Wi-Fi database training**

77 *2.1 Wi-Fi fingerprinting*

78 Wireless network based positioning relies on measuring the signal strength of the received
79 signals. Wireless signal strength will attenuate as it travels from the transmitter (i.e. Wi-Fi APs)
80 to the receiver based on the signal path loss model [3],

$$P_{RX}(d) = P_{d0} - 10n \log_{10} d + a \cdot WAF + \varepsilon \quad (1)$$

81 where P_{d0} is the RSS in dB at a reference distance, usually 1m, away from the AP, n is the space
82 loss factor which varies in different environments, WAF is the wall attenuation factor and a is
83 the number of obstructions in between the receiver and AP, ε is a zero mean Gaussian distributed
84 noise. Positions can be obtained based on computing the change of signal strength from each AP
85 to the receiver. However, wireless signals are quite noisy due to interference and obstructions
86 inside buildings. Therefore the actual observation \tilde{P} and the expected $P_{RX}(d)$ from Eq.1 can
87 differ up to 20dB. Wi-Fi fingerprinting overcomes this problem by taking advantage of signal
88 disruptions in complicated environments. Although signals are easily disturbed and measurement
89 error ε is hard to predict, but as long as the building structure remains unchanged, the disturbance
90 reflected in the signal strength will remain alike in the same location. Therefore, the RSS
91 measurements from each AP form a pattern that reflects a specific location, known as fingerprints.

92 The first step of fingerprinting is the training phase, where a number of locations, known
93 as training points (TPs), are selected within the area of interest and the RSS from all APs are
94 measured at each TP. These are stored into a database as one fingerprint. If the RSS are carefully
95 measured, APs are well spread out and the structure of the building is complicated enough, each
96 fingerprint should be unique referring to one specific location in the building. During the
97 positioning phase, the user measures the current RSS and compares it to the fingerprints in the
98 database. Usually, the mean location of k fingerprints with the smallest difference to the current
99 RSS, known as the k -nearest neighbours (kNN), is returned as the estimated position [20].

100 The biggest problem with fingerprinting is that the training process requires a huge
101 amount of human labour, especially in large complex buildings. This increases the possibility of

102 human error and time cost. Moreover, the database needs to be retrained and updated each time
103 the infrastructure changes to maintain an up-to-date database for accurate positioning.

104 *2.2 Database training*

105 Assuming that the RSS of a location is correlated to the RSS of a nearby TP based on
106 Eq.1, GP is applied to enable faster and more efficient training, which makes the database easier
107 to maintain and update.

108 For accurate database training, the selected TPs should cover the entire area of interest
109 and RSS should be collected over a period of time on each TP to fully reflect the variance and
110 stability of the signal from each AP. Each fingerprint is typically structured as
111 $\{(x_n, y_n) | RSS_{n1}, \sigma_{n1}, AP_1 \dots, RSS_{nm}, \sigma_{nm}, AP_m\}$, where (x_n, y_n) is the position of the n th
112 fingerprint, RSS_{nm} is the mean RSS and σ_{nm} is the standard deviation of the m th AP at the n th
113 TP, AP_m is the unique identification of the AP, usually the MAC address. The uniqueness of the
114 fingerprint is enhanced by the number of APs found and the amount of RSS collected.

115 As positioning is achieved by comparing RSS to the fingerprints, more fingerprints would
116 mean more detailed database, which potentially results in better positioning. The most
117 straightforward way of increasing fingerprints would be increasing TPs. However, it is almost
118 impossible to cover the entire floor plan with TPs due to the required amount of work. Therefore,
119 the entire area is usually divided into evenly distributed grids and a TP is placed at the centre
120 point of each grid, assuming that the RSS is the same within each grid. Typical grid sizes are
121 $1m \times 1m$, $2m \times 2m$ [21]. Smaller grids ensure a more detailed database, although it will be more
122 time consuming and laborious.

123 Based on the path loss model, we can see that the signal strength at each TP is correlated
124 to its distance to the AP. In locations with fewer obstructions, the signals behave according to the
125 model with a small noise. Hence less TPs are required as the RSS can be predicated from RSS at
126 nearby TPs based on Eq.1. GP is applied to predict the RSS of fingerprints that are near to but not
127 on TPs. In areas where training data has already been collected, GP increases the density of the

128 fingerprints without increasing the number of TP. If (x, z) are samples drawn from a noisy process
 129 [22],

$$z_i = f(x_i) + \varepsilon \quad (2)$$

130 where each x_i is an input sample and z_i is the target or observation value, ε is assumed to be a
 131 zero mean normally distributed noise. Gaussian process estimates the posterior distributions over
 132 the functions f from the training data which is specified by a mean function $m(x)$ and a
 133 covariance function, or kernel $k(x, x')$, which describes the correlation between two input values
 134 x_p and x_q . The squared exponential kernel is applied here,

$$k(x_p, x_q) = \sigma_f^2 \exp\left(-\frac{1}{2\ell} |x_p - x_q|^2\right) + \sigma_n^2 \quad (3)$$

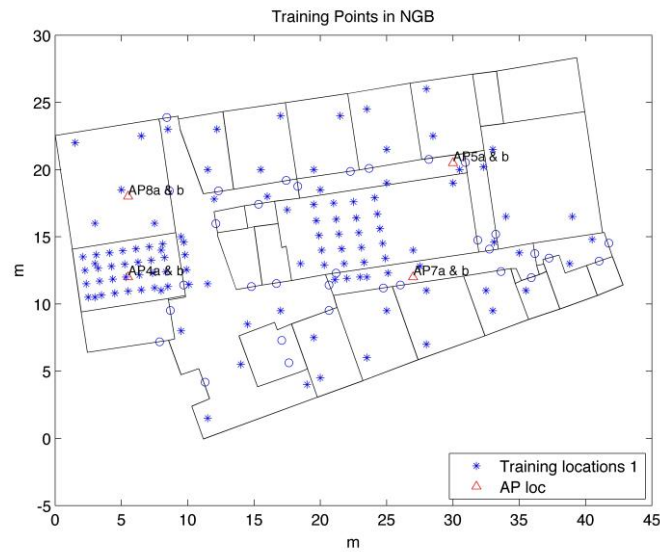
135 where σ_f^2 is the signal variance, ℓ is the length scale that describes the strength of correlation over
 136 a distance, σ_n^2 is the Gaussian observation noise. The RSS measurements and the locations of TPs
 137 are input into the system to train for the hyperparameters $\theta = \langle \sigma_n^2, \ell, \sigma_f^2 \rangle$, which define the
 138 predication functions. The predication process is then carried out based on the predicative
 139 distribution

$$p(z_* | x_*, X, Z) = \int p(z_* | f(x_*)) p(f(x_*) | x_*, X, Z) df(x_*) \quad (4)$$

140 The locations of the TPs are input as X while the RSS measured at the TPs are the target values Z .
 141 The desired fingerprints cover the building by 1m grids at locations x_* , and the RSS of the desired
 142 fingerprints z_* is predicted based on the trained predication functions.

143 To understand the required density and location setup of training data for generating
 144 accurate fingerprint database, different training methods are compared. A Toshiba laptop is used
 145 throughout the trials in this paper for consistency, whose wireless adapter is Intel® Centrino®
 146 Advanced-N 6200. Four APs are located on Floor A of Nottingham Geospatial Building (NGB),
 147 each transmitting signals on both 2.4GHz and 5GHz frequencies. As signal characteristics are
 148 different, thus the signals from different frequencies will be treated separately. A full database
 149 consists eight MAC address groups, each denoted as AP1a (2.4GHz), AP1b (5GHz), AP2a, AP2b,

150 AP3a, AP3b, AP4a and AP4b respectively. Locations of the APs are indicated in Figure 1. Figure
151 2 shows the spread of the RSS for 2.4GHz and 5GHz signals during 30 minutes.



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Figure 1 TPs selected for full fingerprint database

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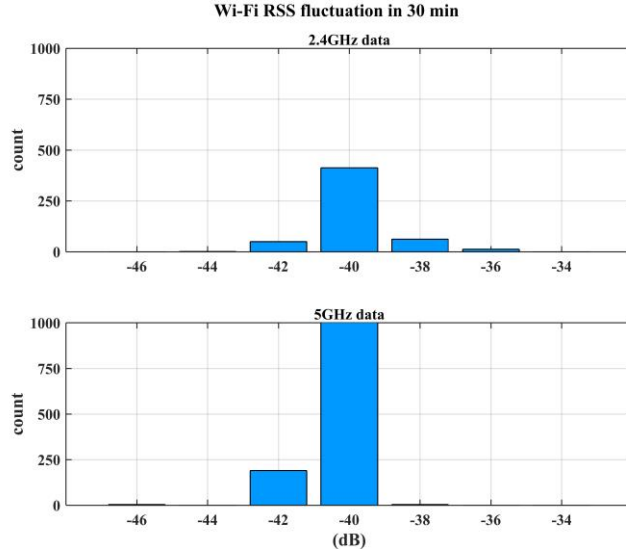
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56 TPs are selected to cover the entire accessible area in NGB Floor A to establish the ground truth for the fingerprint database, i.e. the best possible database from conventional training. On average, two TPs are located inside a small office and four to six TPs are located in large rooms. The laptop is placed at each location to collect the Wi-Fi RSS data for around thirty minutes until at least 100 vectors from each of the four APs have been collected. The mean and standard deviation of all the collected RSS from all APs at each TP is obtained and sorted into the training input vector. GP is then applied based on the training data to increase the fingerprint density to $1m \times 1m$. The resulting fingerprints are stored into a database, denoted as sDB. The training data were collected while the receiver was static and placed over the TP to obtain more stable information of the signal. Training for the 56 TPs takes around 37 hours in total.



165 **Figure 2 Wi-Fi RSS fluctuation in 30 minutes**

166 Two rooms are further selected to compare the database quality of different TP densities.
 167 Another 24 and 32 TPs are selected respectively in two rooms, R1 and R2, so that the TP density
 168 in the rooms are 1m×1m. A local database is generated for each room based on this set of TPs.
 169 R1 is a small meeting room with no obstructions and simple furnishing. R2 is a heavily obstructed
 170 store room with metal shelves and electronic equipment. ΔRSS is the difference between the RSS
 171 of fingerprints from the two different databases at the same location. The difference for each AP
 172 is listed in Table 1.

173 A larger ΔRSS is seen in R2 which is the heavily obstructed room. Therefore, signals are
 174 noisier and less predictable in such places. Hence more TPs are required to generate better
 175 database. However, the difference for 5GHz signal is smaller. This is due to that it is less able to
 176 penetrate obstructions and the signal pattern for different locations are more unique.

177 **Table 1 Mean ΔRSS between fingerprints generated from different TP density (dB)**

	AP1		AP2		AP3		AP4	
	a	b	a	b	a	b	a	b
R1	2.65	2.12	3.19	2.78	1.77	3.34	8.92	2.97
R2	10.94	3.77	8.00	7.65	17.68	12.62	8.16	5.89

178

179 2.3 Collaborative training

180 As the indoor wireless environment can alter caused by changes in the wireless hardware,
181 the building structure or even furnishings. Therefore, each fingerprint database must be
182 maintained and updated. Re-training can still be laborious work even when GP is applied.
183 Collaborative database training (cFPDB) is proposed here to save time and also enhance database
184 quality.

185 cFPDB fundamentally relies on collaborative positioning between a number of mobile
186 users to estimate the reference positions of the TPs and the relationship between the training data.
187 First of all, the basic collaborative positioning algorithm in cFPDB is introduced. Collaborative
188 positioning constrains the measurement error of users by applying a relative ranging constraint.
189 The basic navigation is achieved from inertial measurements and propagated forward based on
190 the dead reckoning model at each step,

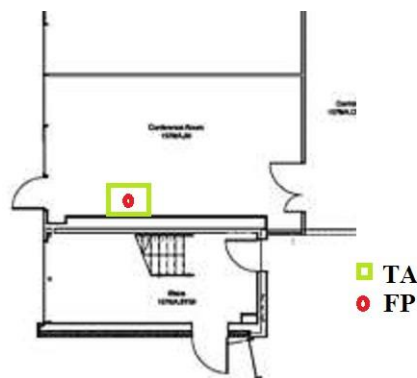
$$\begin{bmatrix} \hat{x}_k \\ \hat{y}_k \end{bmatrix} = \begin{bmatrix} \hat{x}_{k-1} + \hat{s}_{(k|k-1)} \cos \hat{\theta}_{(k|k-1)} \\ \hat{y}_{k-1} + \hat{s}_{(k|k-1)} \sin \hat{\theta}_{(k|k-1)} \end{bmatrix} \quad (5)$$

191 where $[\hat{x}_k, \hat{y}_k]$ is the user position at time k , $\hat{s}_{(k|k-1)}$ is the estimated step length between time
192 $k - 1$ and k , $\hat{\theta}_{(k|k-1)}$ is the heading estimation during the step. Low-cost inertial system
193 measurements tend to drift badly after initialisation [23,24]. Therefore, the inertial measurement
194 errors need to be constrained by external measurements, e.g. relative ranging measurements
195 between users that can be obtained from high precision wireless units such as Ultra-wideband
196 sensors [17]. This estimated position serves as the reference location of the measured RSS, i.e.
197 the location of the TPs during dynamic data collection.

198 Collaborative training is carried out during the collaborative positioning process and this
199 means that only one RSS is collected at a specific location and no knowledge of the signal
200 fluctuation pattern could be obtained initially. While the signal strength could vary up to 20dB or
201 even more at any single location when the equipment is static, this may increase further when the
202 receiver is moving. In conventional training, the fluctuation pattern is captured by extending the

203 training time over hours or even days. In cFPDB, extracting signal features obtained by different
204 users passing previous TPs during different periods helps to capture this pattern.

205 The ranging measurement r between the users builds a link between the collected training
206 data. Two thresholds, the separation threshold δ_{sep} and integration threshold δ_{int} , is defined to
207 identify three different kinds of relationships between the data. If r is above δ_{sep} , it would be
208 regarded that the users were not in the same area of interest. Their training data will be stored
209 separately and used to generate individual databases. If r is within δ_{sep} but above δ_{int} , the
210 training data would be considered to be within the same area of interest and used to generate the
211 same database. As it is almost impossible for users to pass the exact same locations during
212 collaborative training, TP is expanded into training areas (TA). Any training data that are within
213 a range of δ_{int} would be regarded to reflect the signal pattern for the same TA and adjusted to
214 form fingerprints with knowledge of the signal variation for the TA. Figure 3 shows an indication
215 of the relationship between a TA and fingerprint location. The RSS of the fingerprint is assumed
216 to represent the RSS for the entire TA. These thresholds are set according to the expected
217 correlation between fingerprints, which can be affected by the environment and the stableness of
218 the RSS in nearby training locations. This will not differ much in the same building, hence the
219 same threshold can be applied throughout.

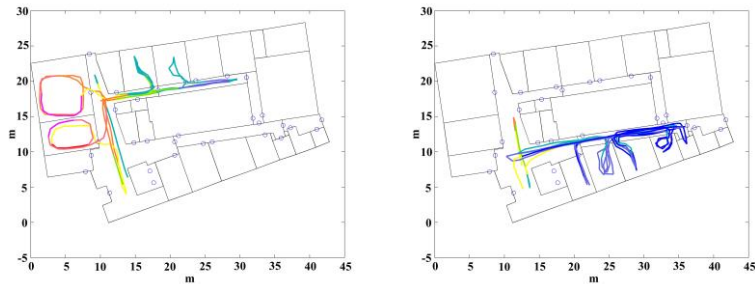


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221 **Figure 3 A fingerprint representing the training area (Green grid indicating a**

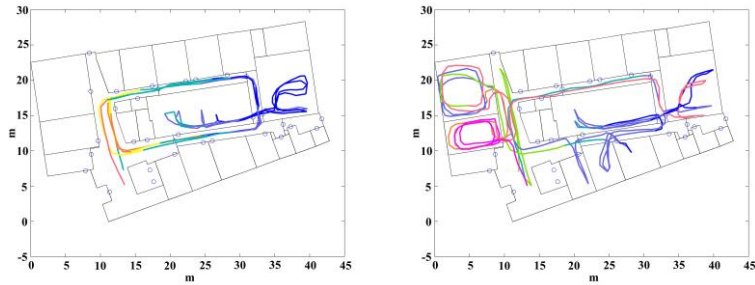
222 **training area, red circle is a fingerprint in the TA)**

223 To build the collaborative database dynamically, four different trajectories, denoted as T1,
 224 T2, T3 and T4, of varying length and locations within NGB Floor A are chosen where training
 225 data will be collected during the collaborative positioning phase. Each user follows one of the
 226 different routes and collects training data at each step, shown in Figure 4, where blue indicates
 227 low RSS and red indicates high RSS values. The data collected along different trajectories are
 228 combined to generate collaborative fingerprint databases using GP, denoted as cDB.
 229 Collaborative training greatly extends the training data coverage and increases the amount of data
 230 for each TA. cDB fingerprints are generated from more sufficient data and longer time span.
 231 Hence captures the RSS fluctuation and environment disturbances.



232

233 (a) Collaborative training data of T1 (b) Collaborative training data of T2



234

235 (c) Collaborative training data of T3 (d) Collaborative training data of T4

236 **Figure 4 Collaborative training data from AP1a**

237 The RSS of the training data along the dynamic trajectories are compared to the RSS of
 238 the TPs of sDB by extracting those that are within a certain distance to the static TPs and
 239 measuring the Δ RSS. The RSS difference for distances from 1m up to 4m is listed in Table 2,
 240 where Δ RSS indicates the mean difference, Std dev. indicates the standard deviation of the RSS
 241 difference. Signal acquisition is less stable while the receiver is moving thus it can be anticipated

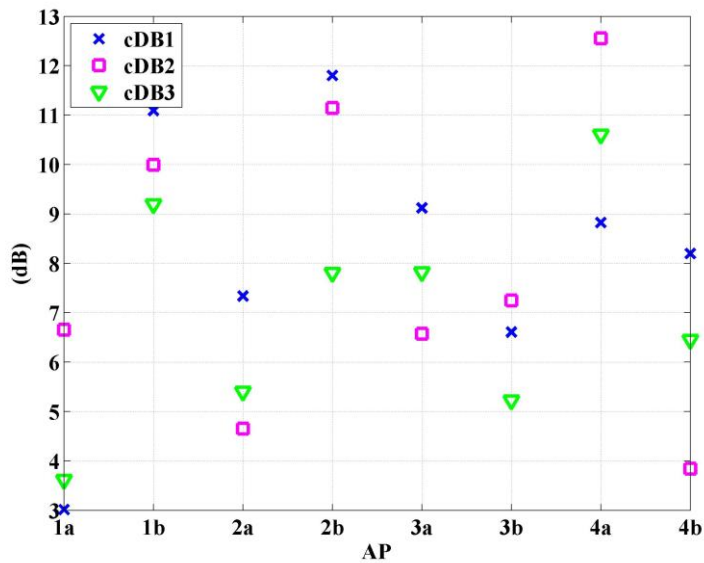
242 that the RSS of the dynamic training data are noisier and differs to that of the static TP RSS. From
 243 the data listed in Table 2, we can see that even though the Δ RSS between training data is almost
 244 10dB even at 1m, but stays within 15dB up to 3m, which is actually within the RSS fluctuation
 245 range. While the difference increases when the distance is 4m, the standard deviation actually
 246 drops. This indicates that correlation fails between the two points and their RSS is steadily
 247 different as they are too far apart. According to the Δ RSS here, the integration threshold can be
 248 set to 2m or 3m depending on the environment, i.e. whether it is more like R1 or R2.

249 **Table 2 Δ RSS between dynamic and static TPs (dB)**

	1m	2m	3m	4m
Δ RSS	9.85	12.55	13.39	19.36
Std dev.	10.61	10.49	15.91	8.58

250

251 Three different cDBs are generated and their fingerprints are compared to those of sDB.
 252 cDB1 is generated from the training data along T1 and T2; cDB2 is generated from T1 and T3;
 253 cDB3 is generated from T1,T2,T3 and T4. Figure 5 plots the mean RSS difference between the
 254 fingerprints of each AP in cDB and sDB. As more data is used to generate the database, the
 255 fingerprint RSS of the cDB approaches that of the sDB.



256

257 **Figure 5 Δ RSS between cDB and sDB (dB)**

258 **3 Fingerprinting based on confidence level**

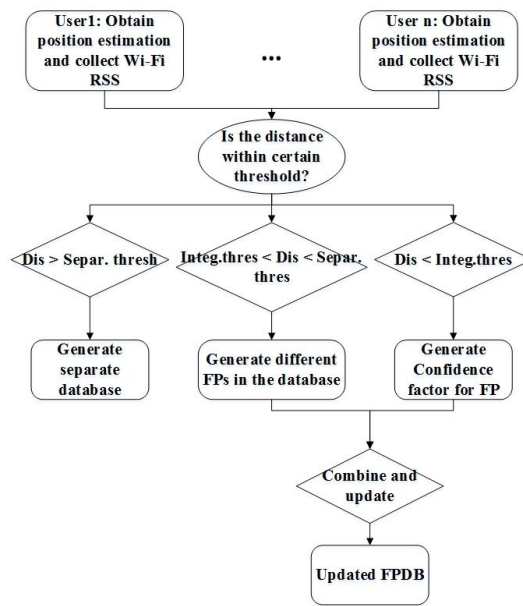
259 *3.1 Fingerprint confidence factor*

260 As dynamic training data contain large signal variances, they should be treated
261 appropriately when applied to generate databases. During the cFPDB process, the system keeps
262 track of all previously and currently collected training data by storing them along the timeline.
263 When new training data is picked up at a TA that has been trained previously, the mean of all
264 RSS from all history data is used as the RSS to generate the fingerprint in GP. The standard
265 deviation of RSS is computed to generate a confidence factor for the fingerprint at the location.
266 The confidence factor vector consists of two values, i.e. the training data difference level Δ_{sgn}
267 and the confidence level η_{CF} .

268 The difference level Δ_{sgn} is updated by measuring the sign of the Δ RSS between the new
269 RSS at the TA and the RSS of the fingerprint representing the TA. A positive Δ_{sgn} indicates that
270 the RSS is increasing and negative Δ_{sgn} indicates decreasing RSS. The confidence level η_{CF} for
271 each fingerprint in the entire building is generated from the training data standard deviation,
272 which indicates how much signal strength variance to expect at each specific fingerprint location.
273 Smaller η_{CF} means higher confidence with the current RSS of the fingerprint stored in the
274 database. There would not be enough training data to compute the standard deviation of
275 fingerprints at the beginning of a training process. Hence it is given a low η_{CF} , assuming that the
276 collected data is trustworthy. The confidence level only decreases when the amount of training
277 data accumulates and shows obvious fluctuation.

278 If the Δ_{sgn} for a location is always positive or negative, it would be assumed that the RSS
279 is constantly increasing or decreasing, indicating a possibility of permanent change in the Wi-Fi
280 properties at the location. If the confidence level goes over a given threshold under such
281 conditions, the RSS of the old fingerprint will be replaced with new RSS data. η_{CF} for the

282 fingerprint is then reset to the initial value which represents a high confidence level. If Δ_{sgn}
 283 changes randomly, the collected RSS is assumed to be within the signal strength random
 284 fluctuation range. In such cases, the signal fluctuation range is reflected by η_{CF} . In general, the
 285 difference level Δ_{sgn} keeps track of the direction of change of the fingerprint along the time axis
 286 while the confidence level η_{CF} reflects the expected signal fluctuation at the location, giving the
 287 user an updated knowledge of how trustworthy the fingerprints are. The procedure of generating
 288 the confidence factor is shown in Figure 6.



289

290

Figure 6 Flowchart for collaborative fingerprint database training

291 3.2 Collaborative Wi-Fi fingerprinting

292 In conventional fingerprinting, potential fingerprints are usually found by defining a
 293 variance boundary τ_{FP} first. If RSS_P is collected at an unknown location P and RSS_{FP} are the
 294 fingerprints from the database, any fingerprints from the database that fit within

$$RSS_P - \tau_{FP} < RSS_{FP} < RSS_P + \tau_{FP} \quad (6)$$

295 are extracted as potential fingerprints. However, deciding the value of τ_{FP} can be difficult. If the
 296 given τ_{FP} is underestimated, there is a possibility that no potential fingerprints will be extracted

297 if either RSS_p or RSS_{FP} is noisy. Yet if τ_{FP} is overestimated, too many potential fingerprints may
 298 be found, introducing large location ambiguities.

299 Fingerprints generated from the cFPDB process take the form of
 300 $\{(x_i, y_i) | AP_1, (RSS_1, \eta_{CF_1}, \Delta_{sgn}) \dots, AP_n, (RSS_n, \eta_{CF_n}, \Delta_{sgn})\}$. The confidence factor generated
 301 during the training process is used here to help decide the value of τ_{FP} , as below

$$\tau_{FP} = a \cdot \eta_{CF} \quad (7)$$

302 where a is a coefficient defining the relationship between the two values. It is adjusted from 1.5
 303 to 3 until potential fingerprints are found. From examining the trial data, it has been found that
 304 we might choose $a = 1.5$ in open areas and $a = 3$ in heavily obstructed areas.

305 As the database training is carried out during a collaborative positioning phase, the
 306 collaborative measurements can also be applied in fingerprinting when available. Hence the Wi-
 307 Fi adaptive collaborative fingerprinting algorithm (WARCP) is proposed. The steps of WARCP
 308 are given as below:

- 309 1. Each user propagates based on the DR model as in Eq.5;
- 310 2. At each step, user i takes a set of Wi-Fi RSS measurement RSS_p^i from each AP, if more
 311 than one user is found, ranging measurements r_{ij} are also obtained between user i and j ;
- 312 3. RSS_p^i is stored to update the database; fingerprinting is then performed by considering
 313 both the confidence factor and the distance between the potential fingerprints following
 314 Eq.6. When M and N potential fingerprints are found for user i and j , the distance
 315 between pairs of potential fingerprints are measured,

$$dist_{FP} = \sqrt{(x_{FP_m} - x_{FP_n})^2 + (y_{FP_m} - y_{FP_n})^2}, (m = 1, 2, \dots, M; n = 1, 2, \dots, N) \quad (8)$$

316 Fingerprints that obey Eq.9 will remain as potential fingerprints,

$$|dist_{FP} - r_{ij}| \leq \varepsilon_{range} \quad (9)$$

317 Where ε_{range} is defined based on the expected noise of the ranging measurement.

318 4. Position estimations are obtained from the weighted average of the remaining potential
319 fingerprint positions.

320 Fingerprinting reliability is improved here as potential fingerprints are selected according
321 to Eq.6 where τ_{FP} changes adaptively. Therefore, a fingerprint with high confidence level, i.e.
322 small η_{CF} , would also be given a small τ_{FP} . It would not be chosen as a potential fingerprint
323 unless its RSS_{FP} is reliable and close to RSS_p . If a fingerprint's confidence level is low, its
324 possibility of being selected as potential fingerprint is increased as the range of $RSS_{FP} \pm \tau_{FP}$ is
325 larger. This is to decrease its possibility of being discarded when it differs from RSS_p due to
326 fluctuation, but its location is actually close to the true location.

327 **4 Simulations and trials**

328 *4.1 Dynamic training*

329 To examine how data is integrated to update the database, the training data of T4 is
330 collected in two rounds. The first round in the building is part 1(P1) and the second round part 2
331 (P2). The training data of P1 and P2 are used to generate two individual databases, P1-DB and
332 P2-DB. The combination of P1 and P2 is used to train for another database, T4-DB. The
333 difference in dB for the fingerprints of each database and the fingerprints of sDB is measured and
334 plotted in Figure 7.

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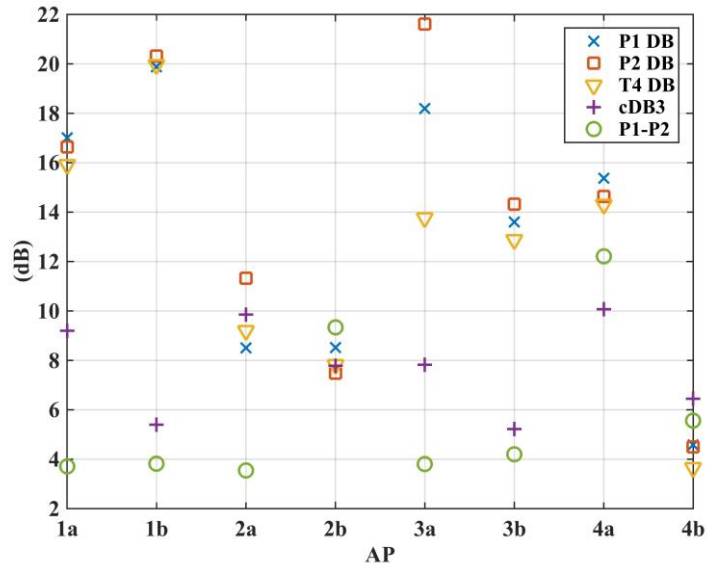


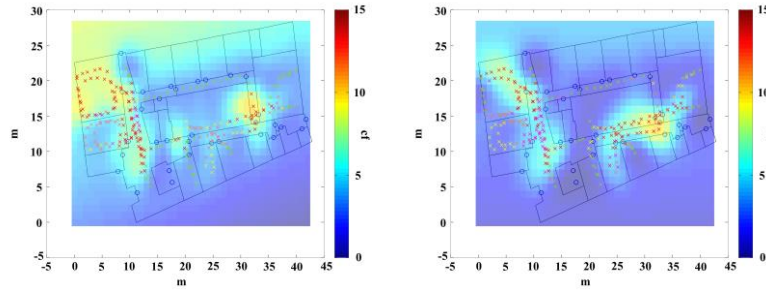
Figure 7 Δ RSS between T4-DB and sDB

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337

338 In most cases, the difference between the dynamic trained database and sDB is reduced
 339 when P1 and P2 data is combined together. The difference is further reduced when more data is
 340 integrated with T4 to form cDB3. The difference between the fingerprints generated from P1 and
 341 P2 is indicated by green circles. However, there are still instances when the difference of RSS is
 342 continuously different from each other, resulting in a large difference from sDB, e.g. AP2b.
 343 Another instance is AP1b, where the difference between P1 and P2 is not very large, but because
 344 both are very different from sDB, their combined data still results in a large bias, as indicated by
 345 the yellow ∇ . During the training process itself, it is hard to decide which data is biased or not.
 346 Hence we can only record the variance of all collected data and indicate its likelihood of being at
 347 a certain signal strength level.

348 To build up the collaborative database cDB3, new training data is stored and compared to
 349 old data iteratively. Each time a new data is collected at a TA where data has been collected
 350 previously, the variance of the signal strength is measured and applied to generate the confidence
 351 factor as described in Section 3.1. Figure 8 plots the confidence level of AP3 for Floor A that is
 352 derived by updating the database from T4-P1 with T4-P2, T1 and T2. Blue areas indicate a small
 353 η_{CF} , i.e. high confidence in the fingerprint, and red areas vice versa.



(a) Confidence level map for AP3a (b) Confidence level map for AP3b

Figure 8 Fingerprint confidence level map

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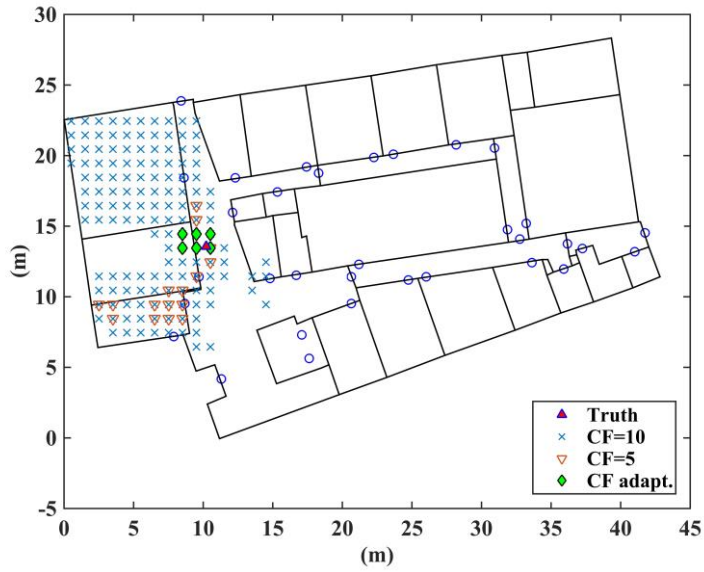
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The RSS of the training data is also plotted on the map for reference. The resulting η_{CF} is higher in areas where the training data changes rapidly between each training. Furthermore, the confidence indicator for 5GHz signals is smaller in general than that of 2.4GHz signals. The RSS of the 5GHz signals remain relatively stable for different regions of the building hence the fingerprint pattern is more unique, producing lower η_{CF} . 2.4GHz signals, on the other hand, have greater ranging distance and penetrate walls better. However, this causes noisier training data and higher η_{CF} .

Three different τ_{FP} are chosen to extract potential fingerprints based on the RSS measurements observed at a given location. Figure 9 shows the potential fingerprints extracted when different thresholds are given, $\tau_{FP} = 5$, $\tau_{FP} = 10$ or $\tau_{FP} = a \cdot \eta_{CF}$. As shown in the figure, too many fingerprints are extracted when $\tau_{FP} = 10$. Even though the fingerprints close to the true location are extracted, but those that are almost 10m away are also considered as potentials. When $\tau_{FP} = 5$, not enough fingerprints that are close to the true location are found. When τ_{FP} is set adaptively according to η_{CF} , the potential fingerprints are more suitable as all extracted fingerprints are located near the true position. Table 3 lists the average distance from selected potential fingerprints to the true location throughout a whole trajectory when given different τ_{FP} and also comparing the results for different frequencies. While 5GHz signal fingerprints are slightly closer to the true location, the best result is still achieved when both frequencies are used.



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Figure 9 Potential fingerprints extracted based on different τ_{FP}

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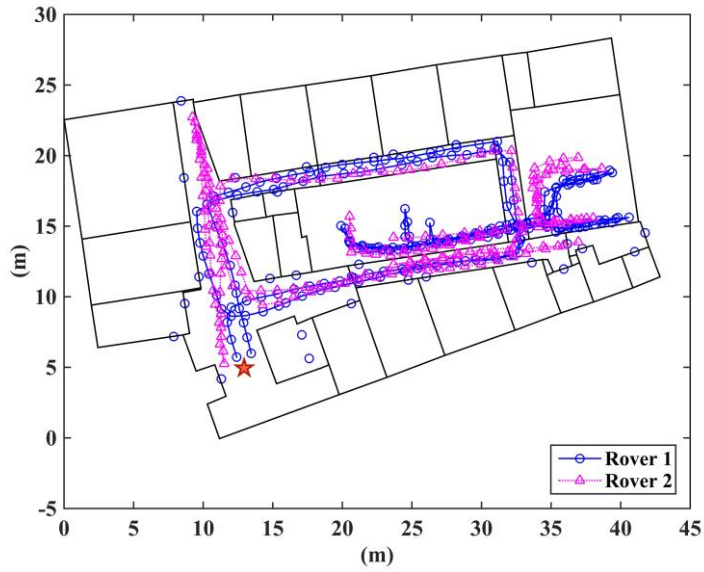
Table 3 Fingerprinting error for different τ_{FP} (m)

τ_{FP}	$a \cdot \eta_{CF}$		Dual	$a \cdot \eta_{CF}$	
	5dB	10dB		2.4GHz	5GHz
Error	16.48	15.51	9.07	11.37	9.69

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379 4.2 Collaborative Fingerprint positioning

380 To evaluate the performance of the fingerprinting method based on the improved
381 fingerprint database, an indoor positioning trial is carried out in NGB with two rovers starting
382 from the same point, indicated by the red star in Figure 10. Both rovers wear a foot-mounted IMU
383 to obtain inertial measurements and carry a laptop to collect the Wi-Fi RSS. Relative ranging
384 measurements are simulated based on the indoor performance of UWB units so that the mean is
385 the true distance with a standard deviation of 3m. To enhance the effectiveness of the constraint
386 provided by relative ranging, both rovers start at the same place but travel in different directions
387 so they do not follow each other.



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Figure 10 Trajectory for Rover 1 and Rover 2

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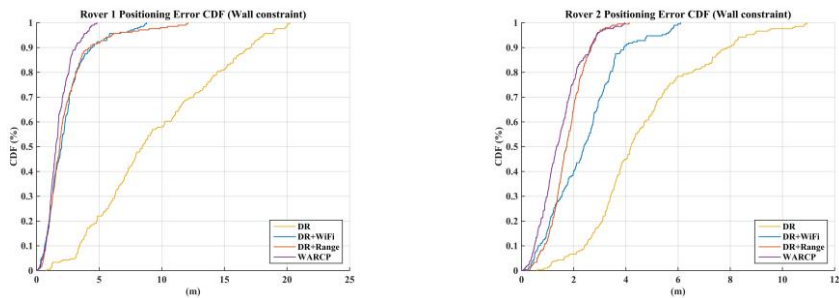
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The collected data is used to compare the performance of different positioning algorithms by processing the data using the data from different sensors each time respectively. DR indicates positioning achieved from just inertial measurements. DR+Wi-Fi indicates the result of integrating DR and fingerprinting with confidence factor. DR+range indicates the result achieved by correcting inertial measurements with ranging measurements. WARCP indicates the result of integrating fingerprinting with ranging and confidence level as introduced in Section 3.2. The cumulative distribution functions (cdf) of the positioning errors of the two rovers are plotted in Figure 11.



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(a) Positioning error cdf of Rover 1 (b) Positioning error cdf of Rover 2

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Figure 11 Positioning error cdf for each different algorithm

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4.3 Results and analysis

402 The mean positioning error of each algorithm for both rovers is listed in Table 4, where
403 DR/Wi-Fi indicates results of DR integrated with conventional Wi-Fi fingerprinting, DR/Wi-Fi
404 (cf) indicates results of DR integrated with improved Wi-Fi fingerprinting with confidence factor.
405 Although four APs used for Wi-Fi positioning here seems like a very sparse network for
406 fingerprinting, but the realistic situation is that inside most buildings, the number of APs are only
407 setup to ensure network coverage and not fitted to meet the density requirement for fingerprinting.
408 Results indicate that the accuracy of fingerprinting with confidence factor improves by 36% for
409 Rover 1 and 50% for Rover 2 compared to conventional fingerprinting with very few available
410 APs. The performance of integrating DR with improved Wi-Fi fingerprinting is similar to that of
411 DR integrated with ranging. While Wi-Fi fingerprinting gave slightly better results for Rover 1,
412 ranging results were better for Rover 2. Wi-Fi fingerprinting results are not given alone because
413 with only four APs, the performance is very unstable. Although accuracy can be quite good during
414 some periods, but the robustness is too low for comparison. Furthermore, as Table 4 shows,
415 integrating improved Wi-Fi with DR enhance accuracy compared to conventional Wi-Fi with DR.
416 This clearly shows the improvements on fingerprinting with the improved method.

417 **Table 4 Positioning error of different algorithms (m)**

	DR/Wi-Fi	DR/Wi-Fi(cf)	DR/Ranging	WARCP
Rover 1	3.67	2.32	2.35	1.76
Rover 2	5.05	2.40	1.76	1.47

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420 The integration of DR, fingerprinting and ranging, i.e. WARCP, improves positioning
421 accuracy further as the mean error is reduced by around 10% compared to DR/Wi-Fi and
422 DR/ranging integration method. Although the average performance difference between the three
423 integrations is not immense, but the maximum error reduces by 35% when WARCP is
424 implemented. As the accuracy level when integrating DR with Wi-Fi and ranging was around the
425 same level, thus the improvement seen here is once more improvement on fingerprinting. While
426 this study focus on the overall improvement of positioning accuracy when integrating low
427 accuracy inertial measurement with Wi-Fi fingerprinting and collaborative ranging, this system
428 shows more freedom of choosing the appropriate positioning algorithm based on what sensor and
429 measurement is available.

430 As the indoor environment is complicated and prone to change, the WARCP algorithm
431 allows users start its own navigation by using only the inertial measurement from a mobile device
432 (i.e. DR). As more nearby users are found, DR/Ranging can be applied to enhance positioning
433 accuracy by constraining the inertial drift. While collaborative positioning is performed, users
434 can help to train for a Wi-Fi fingerprint database through the collaborative training process which
435 can be stored on to a central server and shared to all local users. When users lose the relative
436 constraint from nearby users, collaborative positioning can no longer be applied, but
437 fingerprinting can be performed when the database is available, which achieves almost the same
438 accuracy level as collaborative positioning. When both Wi-Fi signals and relative ranging
439 measurements are available to the user, the collaborative fingerprinting phase of WARCP can be
440 applied to obtain positioning estimation, which is the most accurate.

441 WARCP allows the system to search for different choice of integration when different
442 signals and measurements are available. Integrating Wi-Fi and relative ranging with inertial
443 navigation not only enhance the positioning accuracy, but most importantly, the positioning
444 robustness is improved as positioning estimation can be obtained even in changing environments
445 where signals are intermittently available.

446 **5 Conclusions**

447 Wi-Fi fingerprinting is a popular method for indoor positioning as Wi-Fi signals are
448 widely available in most urban areas and infrastructures are already well established. However,
449 Wi-Fi signals are not positioning dedicated, hence suffer instability and disturbance from the
450 changing environment and obstructions, which can cause instability in positioning accuracy.
451 Inertial measurements from mobile devices are useful to indoor positioning users as they are
452 available regardless of the environment. But due to the large heading drift of low-cost inertial
453 sensors, errors must be constrained by external measurements to achieve reasonable positioning.
454 This paper presents an improved Wi-Fi fingerprinting method for both phases of fingerprinting
455 which is fundamentally based on indoor pedestrian inertial navigation but also enhance inertial
456 navigation performance, as described in cFPDB and WARCP.

457 During the training phase, cFPDB is applied where the RSS measurements from a number
458 of mobile users are collected during different periods and different locations. Measurements are
459 either sorted into training data for different TAs depending on the distance between the location
460 of the data, where fingerprints are generated and updated based on the data of each TA. When
461 updated with new measurements, the fingerprints in the database are given a confidence factor
462 which indicates both the long-term change direction of the RSS and the expected short-term signal
463 fluctuation at the location of the fingerprint. The positioning procedure is then carried out using
464 WARCP, which allows the system to navigate using available measurement flexibly. Potential
465 fingerprints are extracted based on the confidence factor associated with each fingerprint and then
466 further selected by ranging measurements when available.

467 With the proposed methods, fingerprint database can be setup during the positioning
468 phase when users enter an environment without prior database. Previous databases can also be
469 updated by gathering information from surrounding users. Both history data and new data are
470 applied to update the database so users not only know the current RSS of the fingerprints but also
471 have an idea of how much signal variance to expect at each location. Therefore, during the

472 positioning phase, fingerprints are selected based on whether the current measurement lies within
473 the RSS range of the fingerprint.

474 Fingerprint based positioning is improved by 40% compared to conventional
475 fingerprinting when the confidence factor is considered. By applying WARCP, which includes
476 ranging measurement constraint, positioning error is further reduced, especially the maximum
477 error which is reduced by 35%. The application of integrating ranging measurements with
478 fingerprinting during training and positioning gives the user more freedom of choosing
479 positioning algorithms based on what information is available. The training effort of fingerprint
480 database is also greatly reduced as training data can be obtained from crowdsourcing.

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561 **Tables**

562 Table 1 Mean ΔRSS between fingerprints generated from different TP density (dB)

	AP1		AP2		AP3		AP4	
	a	b	a	b	a	b	a	b
R1	2.65	2.12	3.19	2.78	1.77	3.34	8.92	2.97
R2	10.94	3.77	8.00	7.65	17.68	12.62	8.16	5.89

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Table 2 Δ RSS between dynamic and static TPs (dB)

	1m	2m	3m	4m
Δ RSS	9.85	12.55	13.39	19.36
Std dev.	10.61	10.49	15.91	8.58

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Table 3 Fingerprinting error for different τ_{FP} (m)

τ_{FP}	$a \cdot \eta_{CF}$				
	5dB	10dB	Dual	2.4GHz	5GHz
Error	16.48	15.51	9.07	11.37	9.69

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Table 4 Positioning error of different algorithms (m)

	DR/Wi-Fi	DR/Wi-Fi(cf)	DR/Ranging	WARCP
Rover 1	3.67	2.32	2.35	1.76
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