REVIEW PAPER



# Why do we observe significant differences between measured and 'back-calculated' properties of natural fibres?

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Abstract The drive towards sustainability, even in materials technologies, has fuelled an increasing interest in bio-based composites. Cellulosic fibres, such as flax and jute, are being considered as alternatives to technical synthetic fibres, such as glass, as reinforcements in fibre reinforced polymer composites for a wide range of applications. A critical bottleneck in the advancement of plant fibre composites (PFRPs) is our current inability to predict PFRP properties from data on fibre properties. This is highly desirable in the cost- and time-effective development and design of optimised PFRP materials with reliable behaviour. This study, alongside limited other studies in literature, have found that the experimentally determined (through single fibre tests) fibre properties are significantly different from the predicted ('backcalculated' using the popular rule-of-mixtures) fibre properties for plant fibres. In this note, we explore potential sources of the observed discrepancy and

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identify the more likely origins relating to both measurement and errors in predictions based on the rule-of-mixtures. The explored content in this discussion facilitates the design of a future investigation to (1) identify the sensitivity of the discrepancy between measured and predicted fibre properties to the various potential origins, (2) form a unified hypothesis on the observed phenomenon, and (3) determine whether the rule-of-mixtures model (in specific cases) can be improved and may be able to predict properties precisely.

Keywords Plant fibre - Natural fibre composites - Biocomposites - Rule-of-mixtures model

### Introduction

An abundant number of plant fibres are available on Earth from more than 1000 species of plants. While not all these plant fibres are useable, their most widespread is for textiles, pulp and paper products, insulation and animal husbandry (Lewin [2007](#page-9-0)). Owing to the impressive techno-ecological profile of cellulosic plant fibres (Fig. [1](#page-1-0)), in some cases making them competitive to even glass fibres, in recent years there has been a revival in interest in the development of plant fibre reinforced polymer composites (PFRPs) for a variety of applications (Faruk et al. [2012](#page-9-0); Shah [2013\)](#page-9-0):

<span id="page-1-0"></span>

Fig. 1 Comparison of typical strength and stiffness performance of various plant fibres and their reinforced composites (PFRPs) against E-glass and their reinforced composites (GFRPs). Adapted from Shah ([2014\)](#page-9-0)

- 1. PFRPs are go-to-solutions for automotive interior components, providing opportunities in (a) weight reduction due to good specific properties (Fig. 1), (b) cost saving, and (c) end-of-life disposal by incineration (Koronis et al. [2013](#page-9-0); Mougin et al. [2009\)](#page-9-0)
- 2. Plant fibres are abundant and low cost, and consequently PFRPs products (e.g. decking) have shown exceptional growth in the building and construction industry (Dittenber and Gangarao [2012\)](#page-9-0)
- 3. The high specific stiffness (Fig. 1), high vibration damping performance and aesthetic properties of PFRPs has led to a number of innovations in consumer goods, including musical instruments and high-performance sporting equipment (e.g. boards and rackets) (Pil et al. [2016\)](#page-9-0)

While PFRPs are being considered for many more applications, particularly in structural components (Shah et al. [2013a](#page-9-0)), there are several major bottlenecks. These include issues relating to long-term durability (vis. moisture and fire performance) and lack of extensive design data (particularly for complex loads, e.g. fatigue and creep, and complex behaviours, e.g. non-linear stress–strain response) (Bensadoun et al. [2016;](#page-8-0) Shah [2013](#page-9-0); Wambua et al. [2003](#page-9-0)). Stemming from the latter is another important bottleneck—our inability to accurately model the properties and behaviour of plant fibres (Trivaudey et al. [2015](#page-9-0)) and their composites (Andersons et al. [2015](#page-8-0); Shah [2016](#page-9-0); Summerscales et al. [2013;](#page-9-0) Virk [2010](#page-9-0); Virk et al. [2012](#page-9-0)).

It is highly desirable to be able to predict composite properties (and behaviour) from data on fibre properties. This provides a cost-effective and time-saving <span id="page-2-0"></span>route in developing optimised materials with reliable behaviour. Currently, this is not possible with plant fibres and PFRPs. This is in part due to the naturally variable, stochastic properties of plant fibres, but also due to a serious lack of studies relating plant fibre properties to composite behaviour.

In developing PFRPs, there are numerous studies that have measured the mechanical properties of single plant fibres (such as Andersons et al. [2005;](#page-8-0) Aslan et al. [2011;](#page-8-0) Bachtiar et al. [2010;](#page-8-0) Charlet et al. [2007b](#page-8-0); Defoirdt et al. [2010;](#page-8-0) Hu et al. [2010](#page-9-0); Virk et al. [2009b\)](#page-9-0) or PFRPs (such as Madsen et al. [2007](#page-9-0); Roe and Ansell [1985;](#page-9-0) Wambua et al. [2003\)](#page-9-0). Researchers who exclusively study the mechanical properties of PFRPs commonly apply the rule of mixtures (ROM) model to 'back-calculate' the mechanical properties of the reinforcing fibres. This allows appreciating the reinforcing potential of plant fibres by determining fibre properties from composite properties. Expectedly, the ROM (Eqs. 1 and 2) has become a widely used micromechanical model for PFRPs (Garkhail et al. [2000](#page-9-0); Madsen et al. [2009;](#page-9-0) Shah [2013](#page-9-0); Shah et al. [2012b](#page-9-0); Summerscales et al. [2013;](#page-9-0) Virk et al. [2012](#page-9-0)).

$$
E_c = \eta_{lE}\eta_o v_f E_f + v_m E_m \tag{1}
$$

$$
\sigma_c = \eta_{lS}\eta_o v_f \sigma_f + v_m \sigma'_m \tag{2}
$$

where,  $E_f$  and  $E_m$  are the fibre and matrix modulus,  $\sigma_f$ and  $\sigma'$ <sub>m</sub> are the fibre and matrix tensile stress (at the fibre failure strain),  $v_f$  and  $v_m$  are the fibre and matrix volume fraction,  $\eta_{\text{IE}}$  and  $\eta_{\text{IS}}$  are the reinforcement length distribution factors for stiffness and strength, and  $\eta_o$  is the reinforcement orientation distribution factor. For simplification, the length and orientation distribution factors are commonly assumed to be unity for yarn-reinforced, unidirectional PFRPs (Baets et al. [2014;](#page-8-0) Madsen et al. [2007](#page-9-0); Oksman et al. [2002;](#page-9-0) Virk et al. [2012](#page-9-0); Weyenberg et al. [2006](#page-9-0)). We also note here that the modified Kelly–Tyson equation (Eq. 2) is generally limited to (near-) unidirectional composites as significant fibre misalignment loads the (weaker) fibre-matrix interface rather than the composite as a homogeneous medium.

According to the authors' knowledge, other than the critical study described henceforth, there are only four studies in literature (Charlet et al. [2007a,](#page-8-0) [2010](#page-8-0); Oksman et al. [2002](#page-9-0); Virk et al. [2012](#page-9-0)) which inspect the mechanical properties of both the single plant fibres and their unidirectional PFRPs. These studies also compare the experimentally-determined (through single fibre tests) fibre properties with the predicted ('back-calculated') fibre properties. Peculiarly, in all cases, the experimentally measured fibre properties are consistently found to be significantly different from the predicted properties (at 5  $\%$   $\alpha$  significance level, based on two-talied t-tests); see Table [1](#page-3-0) for an amalgamation of literature findings. On the other hand, the experimentally measured and 'back-calculated' properties of synthetic fibres (such as E-glass and carbon) tend to be concurrent (Harris [1999;](#page-9-0) Shah et al. [2014](#page-9-0)).

This manuscript conducts an independent analysis, and then outlines and evaluates possible sources of the observed phenomenon. The discussion aims to be a useful premise for future studies improving models (including the ROM) for natural fibre composites, and enabling reliable prediction of composite properties from fibre data.

### Experimental procedure

#### Materials and preparation

Bobbins of Linum usitatissimum flax rovings (396 tex, 20 tpm) and Corchorus olitorius tossa jute yarns (206 tex, 190 tpm) were supplied by Safilin (France) and Janata and Sadat Jute Ltd (Bangladesh), respectively. Properties of the yarns are detailed in Shah et al. [\(2012c,](#page-9-0) [2014\)](#page-9-0). Unidirectional mats were prepared using a drum-winding system and hydroxyethylcellulose binding agent (Shah et al. [2014](#page-9-0)). Aligned composite laminates (250 mm square, 3–3.5 mm thick) of varying fibre volume fractions were then fabricated using the vacuum infusion technique in a rigid aluminium mould tool. Resin infusion was carried out under vacuum at 200–300 mbar absolute pressure. The matrix used was an orthophthalic unsaturated polyester resin (Reichhold Norpol 420-100), mixed with 0.25 wt% NL49P accelerator and 1 wt% Butanox M50 MEKP initiator. Post cure was carried out at 55  $\degree$ C for 6 h after ambient cure for 16 h. From the manufacturer's datasheet, the polyester resin has a tensile modulus  $E_m$  of 3.7 GPa, tensile strength  $\sigma_m$  of 70 MPa and failure strain  $\varepsilon_m$  of 3.5 %.

<span id="page-3-0"></span>

'Back-calculated' from the composite properties

Difference of means two-tailed t-test ( $\alpha = 0.05$ ). If  $p \lt \alpha$  (i.e.  $p \lt 0.05$ ), the difference in means is statistically significant

Difference of means two-tailed t-test ( $\alpha = 0.05$ ). If  $p < \alpha$  (i.e.  $p < 0.05$ ), the difference in means is statistically significant

Number of specimen tested, gauge length, strain rate, strain range used to measure elastic modulus, technical fibre bundle or elementary fibre

gauge length, strain rate,

strain range used to measure elastic modulus,

fibre bundle or elementary fibre

technical

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d

Number of specimen tested,

# Cellulose

## Test methods

Single fibres, separated carefully from yarns, were glued onto a card frame (using Araldite Rapid adhesive) and their 'apparent' diameter was determined from the mean of three measurements along the fibre length using an optical microscope. Single fibre tests were then conducted on a Hounsfield testing machine equipped with a 5 N load cell, at a cross-head speed of 1 mm/min. 25 samples were tested at gauge lengths of 10 mm and 25 mm. The stress–strain curve of each fibre was used to measure its tensile modulus  $E_f$  (the maximum slope), ultimate tensile strength  $\sigma_f$ , and failure strain  $\varepsilon_f$ .

For the PFRP laminates, tensile tests were conducted according to ISO 527-4:1997 using an Instron 5985 testing machine, equipped with a 100 kN load cell and an extensometer. At least six 250 mm long and 15 mm wide specimens were tested at a crosshead speed of 2 mm/min. The stress–strain curve of each specimen was used to measure its tensile modulus  $E_c$  [in the strain range of 0.025–0.10 %, following (Baets et al. [2014;](#page-8-0) Shah et al. [2012a](#page-9-0))], tensile strength  $\sigma_c$  and failure strain  $\varepsilon_c$ .

# Results

Table 1 presents the measured single plant fibre tensile properties. For both flax and jute fibres, it is evident that the mean tensile stiffness is higher and the mean tensile strength is lower when tested at a longer gauge length. However, due to the large standard deviations (coefficient of variance of 25–60 %), the difference in means is not statistically significant (at  $\alpha = 0.05$ ). These observations are in agreement with literature findings (Defoirdt et al. [2010](#page-8-0); Virk et al. [2009b\)](#page-9-0). At a gauge length of 10 mm, the measured tensile stiffness and strength is 43.0 GPa and 827 MPa for flax fibres, and 17.3 GPa and 533 MPa for jute fibres.

The influence of fibre volume fraction on PFRP tensile stiffness and strength is illustrated in Figs. [2](#page-4-0) and [3](#page-4-0); a strong linear correlation  $(R^2 > 0.95)$  is observed. Applying the ROM's (Eqs. [1](#page-2-0) and [2,](#page-2-0) with  $\eta_{\text{LE}}$ ,  $\eta_{\text{OS}}$ ,  $\eta_{\text{o}} = 1$ ) to the results in Figs. [2](#page-4-0) and [3](#page-4-0) yields the 'back-calculated' modulus and strength for (1) flax and (2) jute fibres to be (1) 68.0 GPa and 874 MPa, and (2) 44.0 GPa and 555 MPa, respectively (Table 1).

<span id="page-4-0"></span>

Fig. 2 Rule of mixtures relation for tensile modulus (Eq. [1](#page-2-0)) of unidirectional jute and flax polyester composites at various volumetric compositions



Fig. 3 Rule of mixtures relation for tensile strength (Eq. [2\)](#page-2-0) of unidirectional jute and flax polyester composites at various volumetric compositions

Comparing the measured and predicted fibre properties (Table [1\)](#page-3-0), it is found that for both flax and jute fibres:

- 1. the predicted fibre stiffness is significantly different (at  $\alpha = 0.05$ ) from the measured fibre stiffness at both gauge lengths,
- 2. the predicted fibre strength is significantly different (at  $\alpha = 0.05$ ) from the measured fibre strength at a gauge length of 25 mm, but insignificantly different from the measured fibre strength at a smaller gauge length of 10 mm, and
- 3. the predicted values are higher than the mean of the measured values, particularly in the case of fibre stiffness.

The observations that the measured and predicted fibre properties are significantly different are consistent with the other literature studies introduced earlier (Charlet et al. [2007a](#page-8-0), [2010;](#page-8-0) Oksman et al. [2002](#page-9-0); Virk et al. [2012\)](#page-9-0). However, as is clear from Table [1,](#page-3-0) it is not always consistent amongst the studies whether measured fibre properties are higher or lower than predicted properties. This indicates that a variety of possible sources may lead to the observed phenomenon, depending on the protocols of the studies.

# Discussion

The discrepancy between the measured and predicted values for the plant fibre reinforcements observed in literature and our study (Table [1](#page-3-0)) would be categorically attributable to, either or both, (1) the experimental error in measuring the tensile properties of plant fibres and their composites, and (2) the suitability, if not validity, of the ROM for PFRPs. The possible sources within each category are listed in Table [2](#page-5-0). In many cases, there would be an overlap between and within categories. In addition, in some cases, the effects may be different on strength and stiffness.

## Measurement conditions

The first question that arises is 'what are we testing?' Fibre extraction processes, including retting, decortification, scutching, and hackling, almost always reveal technical fibre bundles rather than individual elementary fibres. One of the most important nomenclature issues in plant fibre testing is the need for clarity between elementary fibres and technical fibres; the latter consist of bundles of multiple elementary fibres bound together by pectin-rich middle lamella (Fig. [4](#page-5-0)). Tests on technical fibre bundles tend to reveal substantially lower mechanical properties (both stiffness and strength) than elementary fibres (Bos et al. [2002;](#page-8-0) Oksman et al. [2002;](#page-9-0) Zeng et al. [2015\)](#page-9-0). Indeed, many fibre types, such as jute, sisal and hemp, are difficult to (completely) separate into elementary fibres from the technical fibres. Hence, it is common to use technical fibres to manufacture plant fibre composites. However, it is debatable whether the 'reinforcing unit' within a composite is a technical fibre or elementary fibre (or perhaps neither, or both due to any averaging effects). Scientists measuring the properties of elementary fibres will often separate

<span id="page-5-0"></span>Table 2 Possible sources of observed differences in measured and predicted fibre properties

Measurement conditions	Applicability of the ROM
What are we testing?	What is the 'quality' of the fibre/matrix interface in PFRPs?
Elementary fibre versus Technical fibre	Can fibre geometries/properties be considered uniform?
	Have misorientations in the reinforcement (due to yarn twist, for instance) been accounted
How are we testing?	for?
Fibre test parameters (e.g. gauge length, strain rate)	Do the fibres deform elastically?
	Possible effects of process history (such as residual stresses from resin cure shrinkage, damage to fibres during moulding)
How are we analysing the data?	
Fibre cross-section shape and area	
Strain range in which tensile modulus is determined	



Fig. 4 Microscopy image of the tested tossa jute staple yarn consisting of multiple technical fibres. The irregular crosssection technical fibres are themselves bundles of elementary fibres. Each elementary fibre is visible with a central lumen, and a thick lignified secondary cell wall

elementary fibres from technical fibre bundles by hand (Charlet et al. [2007a](#page-8-0), [2010\)](#page-8-0).

Not only are the properties of technical fibres substantially different (lower) than elementary fibres, it is also observed from Table [1](#page-3-0) that back-calculated (predicted) properties of the reinforcing unit fall intermediate to measured technical and elementary fibre properties. For instance, Oksman et al. ([2002\)](#page-9-0) measured the tensile properties of sisal technical fibres and of composites incorporating them; they found that the 'back-calculated' properties of the reinforcing unit was substantially (40-70 %) higher than that of the measured technical fibre properties (Table [1](#page-3-0)). In contrast, Charlet et al. ([2007a,](#page-8-0) [2010\)](#page-8-0) in their studies on flax fibres have found that the measured elementary fibre properties were substantially (up to 70 %) higher than 'back-calculated' fibre properties of composites comprising of technical fibres (Table [1\)](#page-3-0). To elucidate more on this aspect, perhaps a thorough study needs to be done which examines elementary and technical fibre properties, alongside composites manufactured from both the elementary and technical fibres.

Another important aspect that the debate on the fundamental reinforcing unit raises is that in the case where composites comprise of technical fibres, interactions and damage mechanisms between elementary fibres within bundles (such as frictional sliding) (Charlet et al. [2007a;](#page-8-0) Charlet and Beakou [2011](#page-8-0); Charlet et al. [2010](#page-8-0)) are unaccounted for by the ROM, which considers a two-scale system: fibre embedded in a matrix, as opposed to elementary fibres bound in technical fibre bundles which are embedded in a matrix. Therefore, predictions from the ROM may not be representative of a technical or elementary fibre anyway, but of an 'effective' reinforcing unit. This is not an issue for many synthetic fibres, such as glass fibres, as they are independent circular cross-section elements.

The second question that arises is 'how are we testing?' Two test parameters known to have a notable effect on measured fibre properties are specimen gauge length and applied rate of extension. In general, natural fibre tensile properties tend to increase with decreasing gauge length; the influence on strength and failure strain can be substantial at smaller gauge lengths. This has been demonstrated even through Weibull analysis of extensive data (such as in Virk et al. [2009a](#page-9-0)). Other than weak-link scaling effects, the selection of test gauge length is particularly important in the case of technical fibres, as the gauge length will determine whether at least one elementary fibre within the technical fibre bundle is being gripped from end to end.

Fibre testing parameters affect the measured properties which are used as benchmarks for comparison with predicted properties. Notably, the predicted fibre strength from the ROM is, strictly speaking, the fibre strength at the critical fibre length (Harris [1999](#page-9-0)). Therefore, ideally, the measured fibre strength should be at the critical fibre length as well. As this may be difficult to obtain (if the critical length is submillimetre, for example), it may be useful to estimate the fibre strength at the critical length (e.g. based on Weillbull analysis of fibre testing data at various gauge lengths) for comparison with the predicted fibre properties.

The third question that arises is 'how is the experimental raw data analysed?' Due to the irregular cross-section of plant fibres, cross-section area has been a significant source of error in many fibre testing studies. More recently, it has been demonstrated that the true cross-section area (measured through microscopy and image analysis) can be up to 1.42 to 2.55 times lower than the apparent cross-section area (calculated based on an assumed circular cross-section shape and measurement of mean diameter) (d'Almeida et al. [2012](#page-8-0); Thomason et al. [2011,](#page-9-0) [2012](#page-9-0); Virk [2010](#page-9-0)). This implies that measured tensile properties based on assumed circular cross-section fibres underestimate fibre properties (strength and stiffness) by 40–70 %. This would be a notable and most likely source of difference between measured and predicted fibre properties. Virk et al. [\(2012](#page-9-0)) have reported that correcting for the fibre cross-section area leads to a better (although not exact) matching in measured and 'back-calculated' jute fibre properties. Consequently, Summerscales et al. ([2013\)](#page-9-0) have proposed the inclusion of a fibre area correction factor in the modified rule of mixtures for natural fibre composites.

Another important source of error in differences in measured and predicted fibre stiffness is the selection of the strain range in which the fibre and composite stiffness is measured. Both plant fibres and their reinforced composites demonstrate substantial nonlinearity in tensile stress–strain response. While the stress–strain behaviour of plant fibres can be a mix of strain hardening (i.e. increasing stiffness with strain), strain softening (i.e. decreasing stiffness with strain) and linear (Fig. [5a](#page-7-0); Pickering et al. [2007](#page-9-0); Placet et al. [2014\)](#page-9-0), leading to variations in stiffness of  $\pm 30\%$ along the stress–strain curve (Fig. [5](#page-7-0)b), plant fibre composites exhibit a substantial (up to 50 %) reduction in stiffness initially (in the strain range of 0–0.4 %) before stabilising (Fig. [5](#page-7-0)b; Bensadoun et al. [2016](#page-8-0); Kersani et al. [2015;](#page-9-0) Shah [2016;](#page-9-0) Shah et al. [2012a](#page-9-0)). Such variations in stiffness with applied strain make it difficult to compare measured (from single plant fibre tests) and predicted (using ROM for composites) fibre stiffness. This is also because stresstransfer and damage mechanisms may be different in plant fibres and their reinforced composites (Shah [2016\)](#page-9-0). Note that here we do mention 'damage', as stiffness variation with applied strain is an accepted indicator of damage accumulation, and it is wellknown that the 'yield strain' of plant fibres and their composites is as low as 0.15 % (Hughes [2012](#page-9-0); Kersani et al. [2015](#page-9-0); Shah et al. [2012a\)](#page-9-0).

Of course, there are other possible sources. This includes experimental bias; for example, Charlet et al. (Charlet et al. [2007a](#page-8-0), [2010](#page-8-0)) have suggested the unintentional use of strongest fibres for tensile tests in their experiments.

#### Applicability of the ROM

Other than experimental error, discrepancies between measured and predicted properties may be a result of incorrect predictions using inappropriate models (i.e. ROM model). Here, we explore some of the basic assumptions in the ROM model and discuss them in light of plant fibres and PFRPs.

The ROM assumes a perfect interface; one of the first topics that often comes up when discussing PFRPs is the 'quality' of the fibre matrix interface. However, the interface is only an issue in (a) short fibre composites (where fibre length is at or below the critical fibre length), and (b) polyolefin-based thermoplastic composites (due to high viscosity and poor wettability/impregnation of the fibres, as well as incompatibility between non-polar matrix and relatively polar fibres, particularly when lacking chemical compatibilisers and coupling agents); refer to (Shah [2013\)](#page-9-0) for detail. As all studies referred to in Table [1](#page-3-0) employ long fibre reinforcements [much longer than

<span id="page-7-0"></span>

Fig. 5 Plant fibres and their reinforced composites exhibit nonlinearity in stress–strain response. a Plant fibres may show linear, non-linear (strain-softening or strain-hardening) or even multiple non-linearity in stress–strain response. Adapted from

the critical fibre length (Shah [2013;](#page-9-0) Shah et al. [2014](#page-9-0))], and use a thermosetting matrix (with low viscosity and high polarity), the interface is not a likely source of discrepancy in predicted and measured fibre properties. This is in agreement with the assessment made by Charlet et al. (Charlet et al. [2007a,](#page-8-0) [2010\)](#page-8-0). This is further supported by our observation that the ROM applies to a range of fibre volume fractions for the same input parameters (Figs. [2](#page-4-0) and [3\)](#page-4-0).

The ROM also assumes uniform fibre properties; this is certainly not the case with plant fibres, which exhibit a significant, natural, stochastic scatter in properties. While it is important to note that such a scatter in properties is not visible at the composite scale, the composite properties and fracture behaviour may be influenced more by the proportion of fibres with lower strength/stiffness, based on the weak-link scaling theory. The ROM also assumes that fibres are elastic; as mentioned earlier this is also not the case with plant fibres. Plant fibres exhibit complex mechanical behaviour, which is elasto-visco-plastic (Placet et al. [2014](#page-9-0)).

Other than assumptions at the fibre scale, assumptions at the reinforcing product scale (i.e. tow or yarn), would also affect the accuracy of prediction from the ROM. In particular, misorientation in the form of fibre waviness, yarn twist and fabric crimp may influence properties and need to be accounted for when backcalculating fibre properties. For example, Shah et al. [\(2013b](#page-9-0)) have proposed a modified Krenchel

orientation distribution factor to account for misoriline) and the composite (solid line) is not constant as a function of applied strain. Adapted from Shah [\(2016](#page-9-0))

Pickering et al. [\(2007](#page-9-0)). b Plot of normalised stiffness against normalised strain reveals that the stiffness of the fibres (dotted

entation due to yarn twist in plant yarn reinforced composites. Yarn twist is observed to have a notable effect on composite properties; a yarn surface twist angle of  $30^{\circ}$ , typical of plant fibre staple yarns, would lead to a drop in composite tensile strength by over 70 %. Not correcting for fibre misorientation would lead to a much smaller predicted fibre tensile strength than would be expected/measured.

Finally, process history of composite manufacture may influence the predicted fibre properties from the ROM. For example, damage of fibres (elementary or technical) during compression moulding may lead to composites with lower properties than would be expected; that is, the measured fibre properties would be higher than the back-calculated fibre properties, simply because in the latter case, the fibres have been mechanically compromised. This has been suggested by Charlet et al. ([2007a](#page-8-0), [2010\)](#page-8-0) as an important factor as they observed notably lower 'back-calculated' fibre properties.

Other factors, such as the presence of voids (e.g. luminal porosity), and residual stresses due to cure shrinkage of the matrix, may also lead to discrepancies in predictions based on the ROM. However, these are not likely to be important factors; it has been shown for example that void content below 4 % in PFRPs does not lead to a significant deviation in the ROM model prediction (Madsen et al. [2009;](#page-9-0) Shah et al. [2012b](#page-9-0)). However, higher porosity content, particularly at the

<span id="page-8-0"></span>fibre/matrix interface and within the matrix may lead to deviations in the model prediction (Madsen et al. [2009\)](#page-9-0).

## **Conclusions**

This study, alongside a handful of studies in literature (Charlet et al. 2007a, 2010; Oksman et al. [2002](#page-9-0); Virk et al. [2012](#page-9-0)), have found that the experimentally determined (through single fibre tests) fibre properties are significantly different from the predicted ('backcalculated' using the ROM) fibre properties for natural fibres. While the studies do suggest potential sources of the discrepancies, there is no consensus. Of course, as testing methodologies are different in the various studies, the sources are also likely to be different.

In the discussion so far, we have explored potential origins and identified some as being key. The likely origins relating to measurement (in order of importance) are (1) error in fibre cross-section area, (2) strain range in which stiffness is determined for such non-linear materials, (3) differences in elementary and technical fibre properties, and (4) gauge length at which single plant fibre test is carried out. The likely origins relating to errors in predictions based on the ROM are (1) nonuniform fibre properties which are stochastic in nature (i.e. can be analysed statistically, but not predicted precisely), (2) misorientations in the reinforcement, and (3) effects of processing history, (4) plant fibre and PFRP behaviour is not entirely elastic (and is actually varied). The effects of some of the above origins of discrepancies are quantifiable, while others not.

The explored content in this discussion facilitates the design of a future investigation to (1) identify the sensitivity of the discrepancy between measured and predicted fibre properties to the various potential origins, (2) form a unified hypothesis on the observed phenomenon, and (3) determine whether the ROM model (in specific cases) can be improved and may be able to predict properties precisely.

While it is highly desirable to be able to predict composite properties (and behaviour) from data on fibre and matrix properties when designing with composites, we recommend that currently, a more pragmatic approach in the case of natural fibre composites is to base designs on tests on composite samples.

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