

1 Ultrafast Exciton Transport at Early Times in Quantum Dot

2 Solids

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22 **Quantum dot (QD) solids are an emerging platform for developing a range of**
23 **optoelectronic devices. Thus, understanding exciton dynamics is essential towards**
24 **developing and optimizing QD devices. Here, using transient absorption microscopy, we**
25 **reveal the initial exciton dynamics in QDs with femtosecond timescales. We observe high**
26 **exciton diffusivity ($\sim 10^2 \text{ cm}^2\text{s}^{-1}$) in lead chalcogenide QDs within the first few hundred**
27 **femtoseconds after photoexcitation followed by a transition to a slower regime ($10^{-1}\sim 1$**
28 **cm^2s^{-1}). QD solids with larger interdot distances exhibit higher initial diffusivity and a**
29 **delayed transition to the slower regime, while higher QD packing density and**
30 **heterogeneity accelerate this transition. The fast transport regime only occurs in**
31 **materials with exciton Bohr radii much larger than the QD sizes, suggesting the transport**
32 **of delocalized excitons in this regime and a transition to slower transport governed by**
33 **exciton localization. These findings suggest routes to control the optoelectronic properties**
34 **of QD solids.**

35

36 Colloidal QDs have attracted great interest for fundamental studies of exciton and charge
37 dynamics in semiconductor nanostructures, as well as for their applications in various devices
38 including photodetectors¹, light emitting diodes (LEDs)², photovoltaics^{3,4} and field effect
39 transistors (FETs)⁵. Exciton transport in QD solids is generally believed to be determined by
40 the packing structure of particles^{1,2,6-9}. The requirement for exciton transport however differs
41 between the applications, for example, a photovoltaic cell requires fast exciton transport to the
42 charge-separating interfaces^{3,4}, whereas in a LED this can lead to undesired quenching of
43 luminescence^{2,6}. A comprehensive understanding of exciton transport physics in QD solids is
44 therefore needed, with the eventual aim of controlling these transport properties in order to
45 optimize device performance.

46

47 In comparison to the parallel issue of charge transport, the understanding of exciton transport
48 in QD solids is less developed, partly due to limitations of experimental techniques. While
49 FETs and Hall measurements under steady-state conditions provide a wealth of information on
50 charge transport⁵⁻⁷, excitons cannot be easily probed electrically in ensemble measurements.
51 Coupled with their short-lifetime and diffusion lengths (compared to charges), the studies of
52 exciton transport are limited to quenching or optical microscopy measurements. Time-resolved
53 microscopy has been particularly powerful in probing exciton transport, especially at linking
54 transport to the morphology of materials and probing time-dependent diffusion¹⁰⁻¹⁵. The
55 general consensus that emerges from these studies is that closer packing of QDs enables faster
56 exciton transport, while energetic/structural heterogeneity leads to reduction of diffusivity over
57 time^{11,13}. These conclusions together with the extracted diffusivities ($10^{-3} \sim 10^{-2} \text{ cm}^2 \text{ s}^{-1}$) fit well
58 within the picture of Förster resonance energy transfer (FRET) dominated hopping of localized
59 excitons¹⁴. However, due to experimental limitations these studies have probed exciton
60 transport in QD solids on pico/nano-second timescales following photoexcitation. As exciton
61 behaviour is time-dependent, those conclusions can also be limited by the timescale measured.

62

63 Here we directly probe the initial exciton dynamics in QD solids in the femtosecond (fs)
64 timescales following photo-generation. Surprisingly, we find that when the material has a Bohr
65 radius much larger than the QD size, excitons first undergo very fast transport (diffusivity of
66 $\sim 10^2 \text{ cm}^2 \text{ s}^{-1}$) within ~ 300 fs after photoexcitation and then switch into a much slower transport
67 regime ($10^{-1} \sim 1 \text{ cm}^2 \text{ s}^{-1}$). Intriguingly, reducing the interdot distance in the QD solids only
68 enhances transport in the slower regime, while it unexpectedly diminishes the initial fast regime.

69 Both QD packing density and heterogeneity have significant impacts on these transport regimes
70 and the transition between them.

71

72 **fs-TAM measurements on QD solids**

73 Femtosecond transient absorption microscopy (fs-TAM) with 13 fs temporal resolution and
74 13-25 nm spatial precision is employed to monitor exciton transport in the QD films in this
75 work (Fig. 1a, see Methods for full description). Briefly, a near diffraction-limited pump beam
76 (effective width σ of 107 ± 7.5 nm) with transform-limited pulse duration (9.2 fs) is delivered
77 onto the QD film, generating a Gaussian-shaped exciton density instantaneously. The spatial
78 evolution of exciton distribution is recorded by imaging it with a loosely focused (σ of 6.4 μm)
79 and transform-limited (6.8 fs) probe pulse at a series of variable time delays between pump and
80 probe pulses (Supplementary Fig. S1-2). It should be noted that although spatial resolution is
81 still limited by diffraction, by comparing subsequent TAM images it is possible to distinguish
82 the changes in the shape of the distribution as small as 13-25 nm^{16,17}.

83

84 Lead sulfide (PbS) QDs (1.68 eV as-synthesized) were chosen as the main material platform
85 in this work, as they are among the most intensively studied materials for QD-based devices
86 due to the great optoelectronic performance^{2,3,7}. A series of PbS QD solid-state films with
87 systematic variation in the interdot spacing was prepared. This was achieved by solution-phase
88 pre-exchange of the native oleic acid (OA) capping ligands arising from the synthesis to those
89 with shorter carbon chains (Fig. 1b), namely dodecanoic acid (12C), octanoic acid (8C),
90 hexanoic acid (6C) and butyric acid (4C) before film fabrication (Methods, Supplementary Fig.
91 S3). Hereafter, the QD films are denoted as the corresponding ligands. Both the
92 photoluminescence and excitonic features of the absorption spectra were maintained,

93 indicating successful ligand exchange without noticeable aggregation (Supplementary Fig. S4-
94 6).

95

96 Fig. 1c shows the conventional ensemble level transient absorption (TA) measurements of the
97 QD films (also Supplementary Fig. S7-11). A gradual red-shift of the photo-bleaching peak
98 feature can be seen when moving from QD films with OA to shorter ligands, which is consistent
99 with shorter interdot distance and hence stronger QD coupling^{11,18}. There was only minor signal
100 decay within the measurement time window of fs-TAM (Supplementary Fig. S12 and
101 Supplementary Table. 1), suggesting very little recombination and hence this is unlikely to
102 affect the transport measurements. We also observe negligible time-dependent spectral red-
103 shift in the films within the timescale of fs-TAM measurements (Supplementary Fig. S7-11c),
104 implying the excitons experience a homogeneous energy landscape on the timescales being
105 probed in this work.

106

107 The fs-TAM images of each film were recorded at the probe wavelength corresponding to the
108 photo-bleaching peak feature (10 nm bandwidth, shaded areas in Fig. 1c). Representative fs-
109 TAM images obtained from OA are shown in Fig. 1d (Supplementary Fig. S13-16 for other
110 samples). The series of fs-TAM images clearly show spatial expansion of exciton distribution
111 in the QD film. Since the initial exciton distribution resembles the diffraction-limit pump beam
112 and the spatial expansion occurs isotropically, we fitted the fs-TAM images with an isotropic
113 two-dimensional Gaussian function and extracted the corresponding width, σ , as shown in Fig.
114 1e (also see Supplementary Fig. S17-20 for the fitting quality). Near time-zero, the initially
115 created exciton distribution gives a width of 172 ± 8 nm, which is similar to the that (180 nm)

116 calculated by convoluting diffraction-limited pump and probe beams¹⁶. By 260 fs this
117 distribution expands to 224 ± 8 nm, clearly indicating exciton transport.

118

119 **Two distinct exciton transport regimes**

120 To quantitatively compare the transport dynamics in the QD solids, we employ the widely used
121 mean squared displacement model ($\text{MSD} = \sigma_t^2 - \sigma_0^2$) to quantify the time-dependent variance
122 of the spatial exciton distribution^{10,11,16,17}. The MSD profiles of the films over time are plotted
123 in Fig. 2a (Supplementary Fig. S21-22). We note that to account for spot-to-spot variations, the
124 results for each sample presented were obtained from at least five different spots and averaged.
125 The excitation density per QD, or $\langle N_{\text{abs}} \rangle$ was kept at ~ 0.04 , to create a similar excitation
126 condition for all samples and to minimize higher order effects. Interestingly, two distinct
127 transport regimes seem to exist in all MSD profiles: a very fast initial expansion of the exciton
128 distribution within the first ~ 300 fs upon photoexcitation, followed by a much slower
129 expansion (up to 4 ps time window). To test whether this is a two-step diffusion process or an
130 anomalous diffusion process, we fitted the MSD evolution with the power law equation of
131 $\text{MSD} = 2Dt^\alpha$, where D is the diffusivity and α is the diffusion exponent^{11,14,16,19}. We note that
132 the MSD profiles cannot be fitted by a single equation, due to the abrupt transition between the
133 two transport stages (Supplementary Discussion 1 and Fig. S23). Instead, the profiles can be
134 well-fitted within separated time ranges for all samples. The fitting results of OA are shown in
135 Fig. 2b as an example. Within the range of $t_0 < t < t_{\text{fast}}$, the dynamics can be well described by
136 the power law equation where $\alpha = 1$, signifying that the initial exciton transport is
137 diffusive^{11,13,14,16,19}. The corresponding diffusivity (D_{fast}) can therefore be extracted from the
138 slope of the fitted line. Similarly, for $t > t_{\text{slow}}$ the MSD profile can also be described by diffusive
139 motion with a much smaller diffusivity (D_{slow}). A transition period (where $t_{\text{fast}} < t < t_{\text{slow}}$) exists

140 between the fast and slow diffusive stages (also see Supplementary Fig. S24-25). Alternatively,
141 the slow diffusive stage can be described by a subdiffusive motion where $\alpha < 1$ (Supplementary
142 Table. 2) by including the transition period (blue curve, Fig. 2b). We found that whether we
143 take the description of diffusive or subdiffusive motion for the later slow transport the
144 conclusion is consistent with that discussed below (Supplementary Discussion 2). We also note
145 that the results are consistent when the pump fluence or repetition rate were modified, and
146 signal expansion was not observed in samples containing diluted QDs in polymer matrices
147 (Supplementary Fig. S26-31), hence the measurements were unlikely affected by Auger
148 recombination, QD charging and systematic artefacts.

149

150 The extracted diffusivities from the fast and slow transport stages have opposite response to
151 the reduction of ligand length in the QD solids (Fig. 2c). It has been generally believed that
152 reducing the ligand length can lead to shorter interdot distance, hence improved QD coupling
153 and transport^{1,6,7}. Consistent with this general perception, the diffusivities in the slow regime
154 increases with shorter ligands in the QD films (D_{slow} , red dots, Fig. 2c), apart from 4C (to be
155 discussed below). The values of D_{slow} from 0.67 to 1.5 cm² s⁻¹ were also comparable with
156 exciton diffusivities reported in other QD systems^{11,13}, suggesting the slow stage is likely
157 governed by a classical FRET hopping regime¹⁴.

158

159 Intriguingly, the extracted diffusivities from the fast regime (D_{fast}) decrease with reducing
160 ligand length, opposite to general perception of QD solids and the slow transport regime. The
161 highest D_{fast} was obtained from OA (longest ligand), followed by 12C, 8C and 6C (black dots,
162 Fig. 2c). 4C was again an exception, while its D_{fast} was higher than those with the medium-
163 length ligands, however still lower than that of OA. Moreover, the values of the extracted D_{fast}

164 are within the range from 99 to 280 $\text{cm}^2 \text{s}^{-1}$, which is three to four orders of magnitude higher
165 than those from D_{slow} .

166

167 We emphasize that the fs-time exciton transport in QD solids is revealed here experimentally
168 for the first time. It has been well demonstrated that the exciton diffusivity of disordered
169 material systems decrease over time^{10-12,19}, so high diffusivities in such an early-time range can
170 be expected. Nevertheless, the observed D_{fast} values are obviously too high to be described by
171 classical hopping in QDs, implying the fast regime is likely governed by a different mechanism.
172 Interestingly, the estimated t_{fast} also shows the same trend as D_{fast} (black dots, Fig. 2d),
173 indicating the films with longer ligands can sustain the initial fast transport for longer time.
174 Similarly, the trend in t_{slow} also suggests longer ligands postpone the transition from the fast to
175 the slow stage (red dots, Fig. 2d).

176

177 **QD packing morphologies and exciton dynamics**

178 Important questions then arise on the underlying mechanisms that dictate the two distinct
179 transport regimes and why they have reversed trends of diffusivities when changing the ligand
180 length. To further elucidate these, we looked into the quality and packing of the QD solids. We
181 first compared the PLQY of the QD solids with those of the corresponding QD solutions (Fig.
182 3a). The PLQY of the QDs in solution were all around 35 ~ 40%, indicating they had similar
183 level of surface defects. In contrast, the drop of PLQY when cast into films was more
184 significant with shorter ligands, consistent with the expectation of better QD coupling and
185 concomitant PL quenching^{6,20}. We then performed grazing incidence small angle x-ray
186 scattering (GISAXS) to reveal the actual interdot distance and packing heterogeneity (Fig. 3b
187 and Supplementary Fig. S32). We found the average interdot distance (core-to-core) decreased

188 from ~ 37.2 Å for OA to ~ 31.5 Å for both 8C and 6C, whilst 4C maintained an unexpectedly
189 large separation of ~ 35.5 Å (red dots, Fig. 3c, Supplementary Table. 3). The similar interdot
190 distances between 8C and 6C (also diffusivities, Fig. 2c) can be attributed to the minor
191 difference in ligand length and factors such as heterogeneity²¹. The QD packing disorder
192 (FWHM of the peaks) gradually increased with shorter ligands (black dots, Fig. 3c). With this
193 we attribute the unexpectedly large interdot distance of 4C to its high packing heterogeneity,
194 which can lead to voids in the film (Supplementary Fig. S33). This can cause 4C to be an
195 exception to the trend from Fig. 2c, as the diffusivities should vary based on the actual effective
196 interdot distance of QDs instead of the absolute ligand length. We then correlate the
197 diffusivities from Fig. 2c with the actual interdot distance of the films, and again confirm that
198 D_{slow} increases with reduction of the actual interdot distance, while D_{fast} has the opposite trend
199 (Fig. 3d).

200

201 In addition, the transition time between the two regimes is shorter in QD films with a higher
202 level of packing disorder ($t_{trans} = t_{slow} - t_{fast}$, Fig. 3e), although it is difficult to decouple this
203 from the effect of shorter interdot distance. Nevertheless, despite the fact that 4C has an average
204 interdot distance between those of OA and 8C/6C, it has the shortest t_{trans} among all. For
205 example, by comparing the MSD profiles of OA and 4C, it clearly suggests packing disorder
206 accelerates the transition between the two transport regime (Fig. 3f).

207

208 **The origin of the unusually fast exciton transport**

209 Both the trend and values of D_{slow} are consistent with FRET hopping. In contrast, the values of
210 D_{fast} and its trend with interdot distance are highly unusual. This transport phase is still diffusive
211 in nature (as $\alpha = 1$), which seems to rule out ballistic ($\alpha = 2$) or coherent ($\alpha > 1$) motion^{14,22,23}.

212 One possible explanation is the transport of delocalized rather than localized excitons at early
213 times^{8,24} (see Supplementary Discussion 3 and 4). The range of interdot distances (31.5 Å~37.2
214 Å) should already allow decent coupling in lead chalcogenide QDs^{7,25,26}. In addition, PbS has
215 an exciton Bohr radius of 18 nm and the QDs studied here are 2.2 nm in diameter, so the highly
216 confined regime may allow for large wavefunction leakage into neighbouring QDs²⁷⁻³⁰.

217

218 To test the above hypothesis on exciton delocalization, we perform further fs-TAM
219 measurements on cadmium chalcogenides (CdSe, CdS), cesium lead iodide (CsPbI₃)
220 perovskite and lead selenide (PbSe) QDs. As shown in Fig. 4a-c, we observe no obvious growth
221 in the MSD profiles of CdSe, CdS and CsPbI₃ QD solids with OA ligands. Interestingly, similar
222 to PbS, PbSe QD solids also show the fast and slow transport regimes (Fig. 4d, also see
223 Supplementary Discussion 3). We note that the exciton Bohr radii of lead chalcogenide QDs
224 are very large, about 18 and 46 nm for PbS and PbSe, respectively²⁹, while those for cadmium
225 chalcogenides and perovskites are only about 3-6 nm³¹⁻³³. The exciton Bohr radius indicates
226 the size of exciton and hence the potential extent of delocalization³⁴. For cadmium
227 chalcogenides and perovskite QDs, the largest possible ratio between the Bohr radius and
228 typical particle radius (r_B/r_p) is about 1 to 4, without considering ligands (Supplementary
229 Discussion 3). This implies very small possible exciton delocalization in these materials (Fig.
230 4e, small Bohr radius case), so with OA it cannot be supported. On the other hand, the r_B/r_p
231 ratio for lead chalcogenides can be >15, when considering OA ligands in PbS it can still be
232 around 10 (~18.6 Å effective radius). Therefore, a large delocalization extent can still be
233 expected even with relatively large interdot distance (Fig. 4e large Bohr radius case,
234 Supplementary Fig. S34). Based on this, we suggest that the fast transport regime observed
235 here is based on the presence of exciton delocalization. Theoretical predictions suggest that
236 delocalized excitons can transfer to sites that are energetically resonant but spatially far away

237 due to the enhanced net transition dipole moment from superposition of individual QD
238 wavefunctions, leading to a ‘supertransfer’ mechanism (Supplementary Fig. S35)^{35,36}. These
239 delocalized excitons will eventually localize as they energetically relax and explore the density
240 of states within the QD solid, leading to the transition to the hopping based slow regime. Further
241 experimental and theoretical investigations are called for to investigate this phenomenon at
242 early times, as the physics that drives this mechanism is generally not well captured within
243 current models.

244

245 The important remaining question is why the initial fast transport is less efficient in QD solids
246 when decreasing interdot distance (Fig. 3d). Here, we suggest one aspect of disorder that has
247 been largely overlooked – the QD packing density that increases with shorter interdot distance
248 (Supplementary Discussion 3). Conventional sources of disorder in QD solids include size
249 polydispersity, surface defect states and packing heterogeneity^{3,5,11}. But assuming the same
250 polydispersity and defect level per QD, increasing the packing density would unavoidably
251 increase the number of QDs in the transport path, potentially broadening the density of states
252 explored by the excitons within the same distance. This problem is normally not noticeable for
253 QDs with little delocalization, as the transport mechanism is most likely based on hopping of
254 localized excitons, and short interdot distance is the most prior condition for any transport to
255 occur (Fig. 4e). For lead chalcogenides where a large delocalization is already expected,
256 reducing the distance further has very minor advantage to initial delocalization, but only
257 increasing the number of QDs/disorder sites in the transport path (Fig. 4f-g). This would
258 accelerate the transition to the hopping transport regime³⁰. Similar observations have been
259 made in carrier transport of organic semiconductors such as rubrene thin films, where the
260 highest mobility was found in a packing direction with larger intermolecular distance^{37,38}.

261

262 **Conclusion**

263 With the above results, the early time exciton dynamics are summarized in Fig. 4f-g (also see
264 Supplementary Fig. S36-37). Immediately after photoexcitation, delocalized excitons are
265 generated in the QD solids studied here and diffuse quickly (fast transport). With larger (but
266 still closely-packed) interdot distance and/or homogeneous packing (Fig. 4f), a low level of
267 disorder allows faster transport and longer duration. However, when an exciton is eventually
268 localized, the hopping transport is not efficient at such distances. With shorter interdot distance
269 (Fig. 4g), the higher packing density can introduce more QDs (disordered sites) in the path.
270 This promotes the localization process and limits the transport rate and duration. High packing
271 heterogeneity can further accelerate the localization. However once the exciton is localized, it
272 can still transport through the QDs relatively efficiently by hopping due to the short interdot
273 separation, as one would normally expect in longer timescales.

274 In summary, our work has revealed the surprising early-time transport dynamics of excitons in
275 QD solids. We observed the transition from a very fast to a slow regime over time. Since this
276 is only found in QDs with large excitonic Bohr radii, we suggest these observations are related
277 to the localization process of initially delocalized excitons. Counterintuitively, the initial
278 regime was faster and sustained for longer in QD solids with larger interdot distance. We
279 attribute this to disorder arising from higher QD packing density (hence disorder density) and
280 structural heterogeneity that accelerate exciton localization, under the context that a large
281 extent of delocalization exists. This study sheds light on the factors that dictate exciton
282 transport in QD solids on fs timescales and provides design rules to engineer QD solids to tailor
283 the desired transport properties in these systems on a range of timescales.

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298

299 **Author contributions**

300 Z.Z., J.S. and A.R. conceived the project. Z.Z. performed the sample synthesis and fabrication.
301 Z.Z. and J.S. performed fs-TAM and other optical measurements. D.T.W.T., M.P.W., A.J.R.
302 and R.A.L.J. supported and performed the GISAXS measurements and analysis. SY.H and M.L.
303 provided input into the sample preparation. J.X. conducted electron microscopy measurements.
304 S.D. contributed to PLQY measurements. SJ.H. provided input to the design of experiments
305 and discussion of results. Z.Z., J.S. and A.R. wrote the paper with input from all authors.

306 Correspondence and requests for materials should be addressed to J.S. or A.R.

307

308 **Competing interests**

309 The authors declare no competing interests.

310

311 **Supplementary information**

312 This file contains Supplementary Figures 1-37 and Supplementary Tables 1-4.

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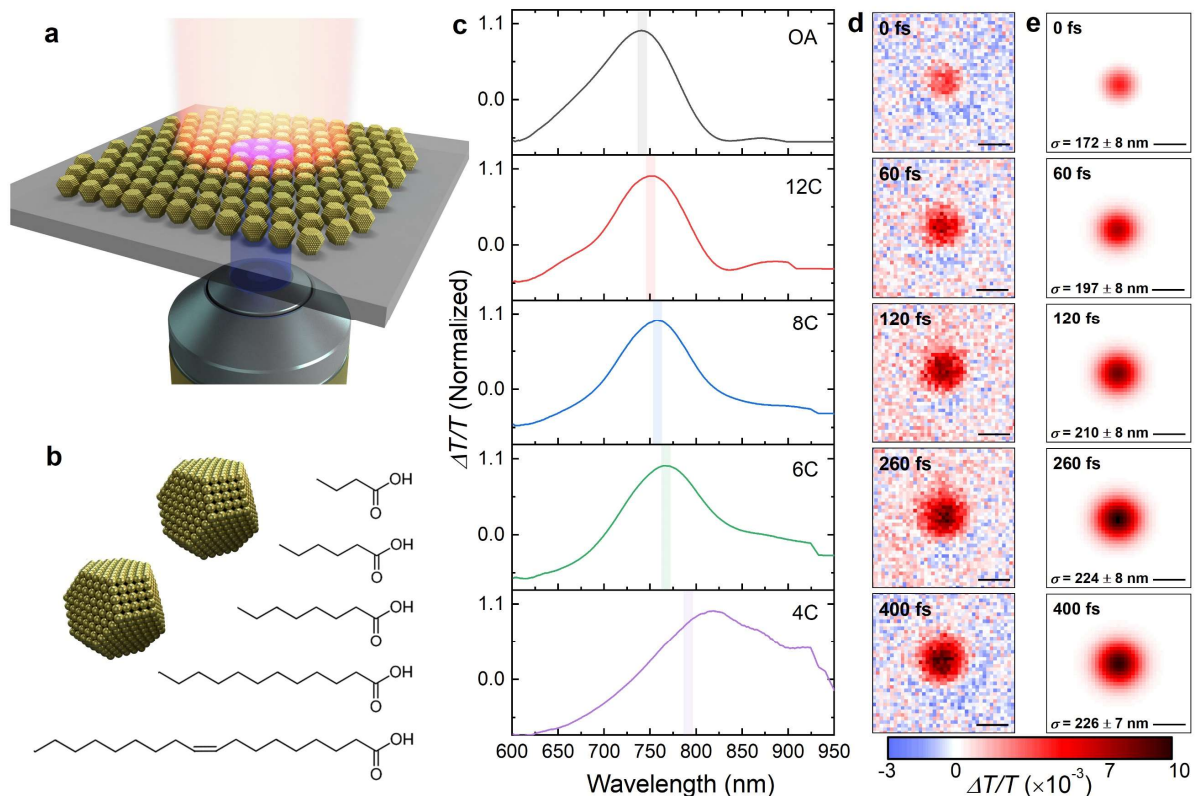
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330 **Fig. 1 fs-TAM measurement of QD thin films with different capping ligands. a,**331 Schematic representation of the fs-TAM measurement. A near diffraction-limited (σ of $107 \pm$ 332 7.5 nm) and transform-limited (9.2 fs, 580 nm) pump beam is delivered onto the QD film333 (blue beam), together with a counter-propagating loosely focused (σ of $6.4 \mu\text{m}$) and334 transform-limited (6.8 fs) probe pulse (orange beam). Note that the actual samples are thicker

335 films containing multiple layers of QDs with thicknesses of several hundred nm, and the QD

336 packings contain certain levels of disorders. **b,** The interdot distance of the films were

337 modified by the selection of surface ligands. The ligand exchange was performed to replace

338 the original OA ligands to 12C, 8C, 6C or 4C ligands in solution-phase prior to film

339 fabrication. **c,** Normalized TA spectra of the QD films with different ligands at 1 ps pump-

340 probe time delay. Gradual red-shifts of the peaks were observed with shorter ligands. The fs-

341 TAM data was taken near the corresponding positive $\Delta T/T$ photobleaching peaks with a

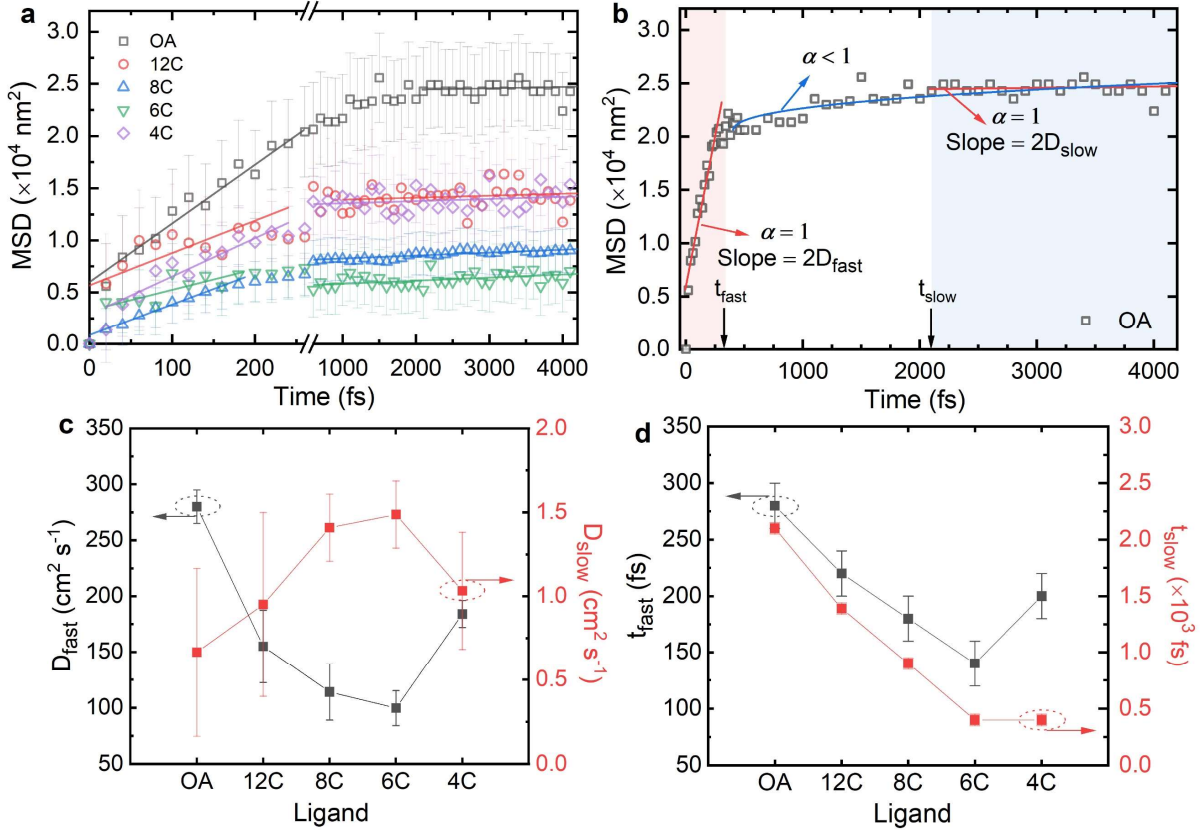
342 bandwidth of 10 nm (shaded area). **d**, Representative fs-TAM images of OA at 0, 60, 120,
343 260 and 400 fs pump-probe delay, respectively. The spectral bandwidth of 10 nm was
344 achieved by using a bandpass filter (730 nm) in the imaging path. **e**, The corresponding
345 exciton distribution images retrieved by fits with isotropic two-dimensional Gaussian
346 functions. The σ values represent the width of exciton distribution at the corresponding time
347 delay. Clear expansion of exciton distribution over time can be observed. The standard error
348 represent 95% confidence intervals from the σ values obtained from five measurement spots
349 on the sample. Scale bars, 500 nm.

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355 **Fig. 2 Quantitative fs-TAM measurement results of the series of QD thin films. a,** Time
 356 evolution of the $\text{MSD} = \sigma_t^2 - \sigma_0^2$ profile, while σ_0^2 represents the variance of the spatial
 357 exciton distribution near zero pump-probe delay. The error bars are standard error calculated
 358 from those of σ over several measurement spots on the samples (see page 5 in Supplementary
 359 Information for detailed calculation). The solid lines are the fits within the respective time
 360 range based on the power law of $\text{MSD} = 2Dt^\alpha$, where $\alpha = 1$. **b,** The fitted curves and
 361 resultant parameters extracted for a representative QD film, OA as an example. The MSD
 362 profile within the time range of $0 < t < t_{fast}$ and that of $t > t_{slow}$ can be well described by the
 363 diffusive motion such that $\alpha = 1$ from the power law equation (red lines), where the
 364 diffusivities of D_{fast} and D_{slow} can be extracted from the slope of the corresponding fitted
 365 lines. The MSD profile after t_{fast} can also be described by a subdiffusive motion (blue curve,
 366 $\alpha < 1$), while conclusions from the two fitting methods are consistent (Supplementary
 367 Discussion 2). **c,** The extracted diffusivities of the initial fast transport regime (D_{fast}) and the

368 slow regime (D_{slow}) of the series of QD films. The two transport regimes show opposite
369 response to the variation of ligands. **d**, The estimated time duration of the initial fast stage
370 (t_{fast}) and the time taken (from 0 fs) for the excitons to enter the slow transport regime (t_{slow}).
371 The error bars presented in **c-d** represent the uncertainty of the fitting parameters in the fitting
372 process using the power law equation.

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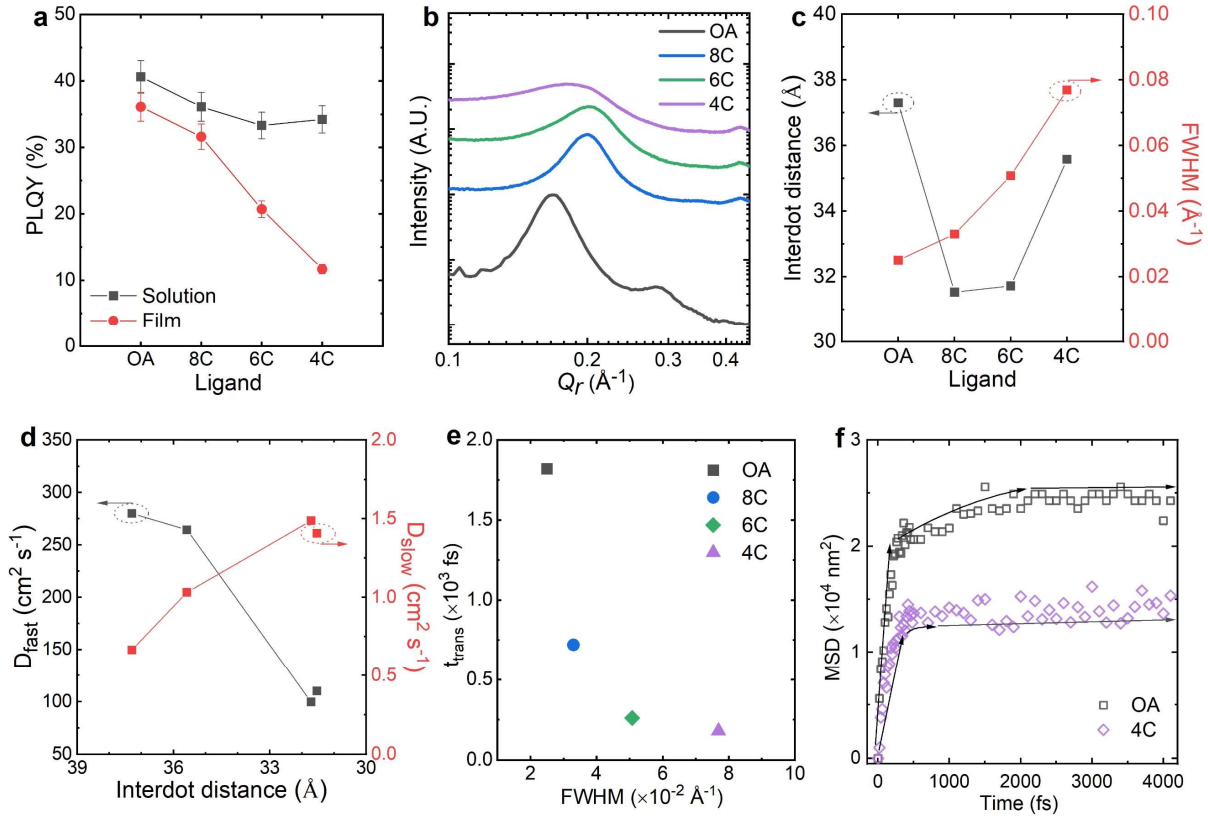
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380 **Fig. 3 Quality and structural information of the QDs and films with different ligands**

381 **and correlation to the fs-TAM results. a**, PLQY of the QDs in both solution- and solid-

382 state with different ligands. A more significant quenching in the PLQY can be observed from

383 films with shorter ligands. No chemical or thermal treatment was applied to the films,

384 indicating that the quenching of PLQY arises from improved QD coupling due to closer

385 interdot distance. The error bars were calculated based on the system error of the PLQY set-

386 up (see Methods). **b**, Radially integrated GISAXS intensities of QD solids (normalized).

387 Lower Q_r value of the 1st order scattering peaks indicates larger average separation between

388 the QDs, while the peak width indicates discrepancy of the separation. **c**, The fitted interdot

389 distance and FWHM of the 1st order scattering peaks from **b**. We ascribe the FWHM to a

390 relative deviation in the core-to-core spacing of the QDs and hence level of packing disorder

391 in the samples. **d**, Correlation between the actual interdot distance (core-to-core) with the

392 diffusivities of the fast and slow regimes. The D_{fast} decreases with reducing interdot distance

393 while D_{slow} clearly shows an opposite trend. **e**, Correlation between the transition time ($t_{trans} =$
394 $t_{slow} - t_{fast}$) with the FWHM (level of packing disorder) of the 1st order scattering peaks in **b**.
395 The decreasing t_{trans} with increasing FWHM indicates higher level of disorder leads to faster
396 transition from the fast to the slow regime. **f**, Comparison between the transition of transport
397 regimes in OA and 4C, the arrows indicate the trend of MSD evolution.

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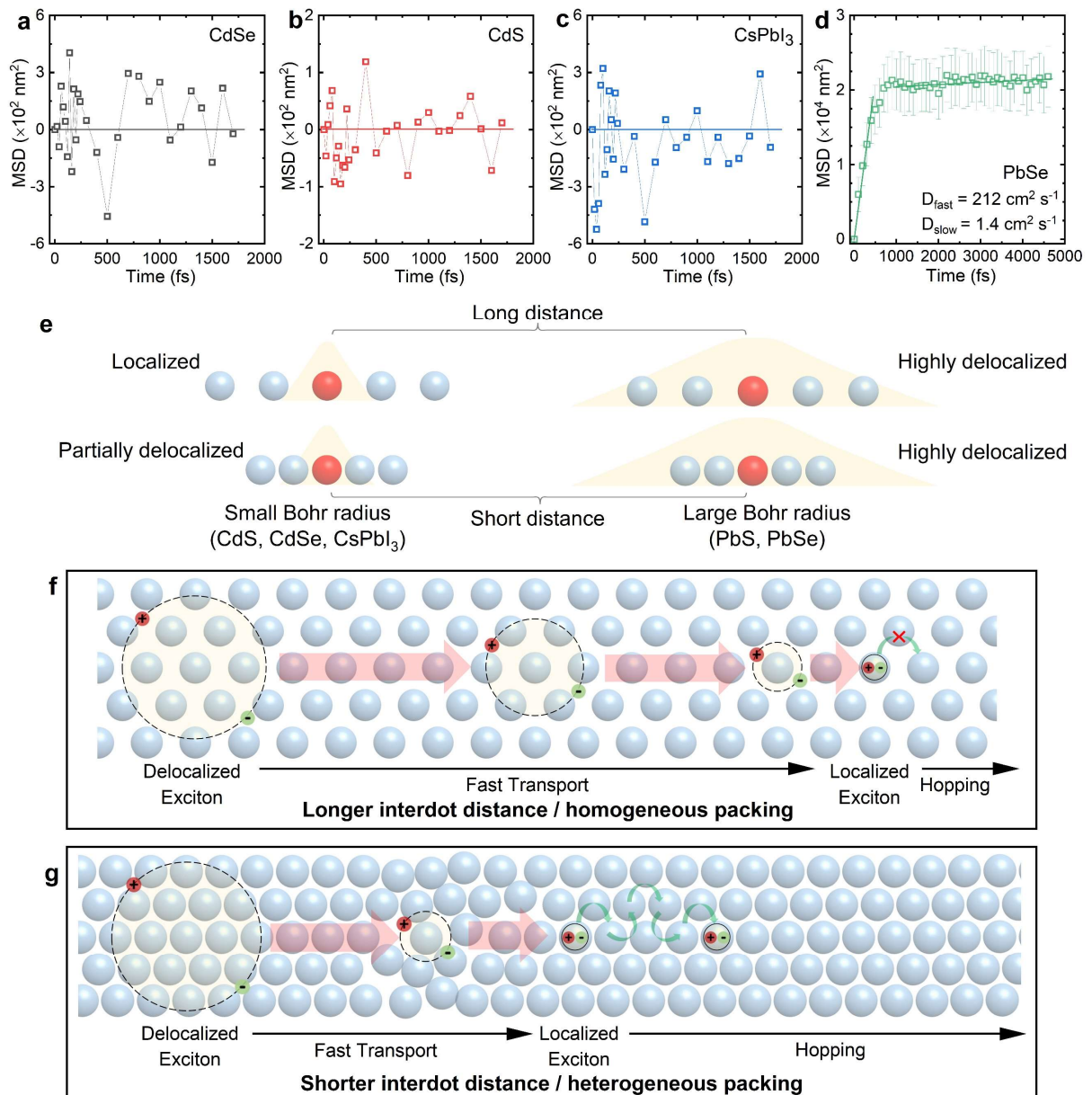
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406 **Fig. 4 fs-TAM measurement results of other QD materials and schematics of exciton**

407 **delocalization in QD solids. a-c,** MSD profiles of CdSe, CdS and CsPbI₃ QD solids,

408 respectively. There is no exciton transport observed at early times. **d,** MSD profile of PbSe

409 QDs. Similar to PbS QDs, fast and slow transport regimes can clearly be observed, the

410 corresponding diffusivities are 212 and 1.4 $\text{cm}^2 \text{ s}^{-1}$, respectively. The error bars are standard

411 error calculated from those of σ over several measurement spots on the samples. **e,** Schematics

412 of exciton delocalization in QDs with small and large Bohr radius (wavefunction leakage).

413 With small Bohr radius the exciton delocalization is highly dependent on the interdot distance

414 (left), while that with large Bohr radius can still highly be delocalized even when the interdot
415 distance is relatively large (right). **f**, Schematic of early-time exciton transport in QD solids
416 with relatively long (but still closely-packed) interdot distance and/or homogeneous packing.
417 **g**, Schematic of the case in QD solids with shorter interdot distance and/or heterogeneous
418 packing. The excitons in both cases are likely delocalized initially, while the QD packing
419 density and level of heterogeneity would affect the diffusivities and the localization process.
420 Once the excitons are localized, the conventional hopping regime applies.

421

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519

520 **Methods**

521 **Sample preparation**

522 **Synthesis of PbS QDs.** The synthesis of PbS QDs was carried out following modified
523 versions of previously reported methods³⁹. Briefly, lead oxide (0.45 g), oleic acid (1.4 g) and
524 1-octadecene (10 g) were loaded in a three-neck flask and degassed at 110 °C for 2 h.
525 Subsequently, the reaction flask was flushed with nitrogen and the temperature was lowered
526 to 50 °C. A solution containing bis(trimethylsilyl)sulfide (210 µL) in 1-octadecene (5 mL)
527 was rapidly injected into the lead precursor solution. After 2 min, the reaction flask was
528 cooled down to ambient temperature (~25 °C) with a water bath. The PbS QDs were first
529 extracted by adding hexane and acetone, followed by centrifugation. The QDs were further
530 purified three times with hexane and acetone. After purification, the QDs were re-dispersed
531 in toluene at a concentration of 50 mg mL⁻¹ and stored in a nitrogen filled glovebox. Before
532 ligand exchange, the dispersion was filtered with a 0.45 µm PTFE syringe filter to remove
533 residual impurities.

534 **Ligand exchange.** The ligand exchange of QDs were performed according to literature with
535 some modifications⁴⁰. In a nitrogen filled glovebox, the purified QDs (50 mg mL⁻¹ in toluene)
536 were first loaded into separated sample vials and kept under magnetic stirring. The liquid
537 phase ligands (8C, 6C and 4C) were slowly added into the QD dispersion by using a
538 micropipette. Typically ~ 0.1 mmol of ligands are added to 100 mg of QDs. As the 12C
539 ligand is solid-state, it was first dissolved in toluene (~50 mg mL⁻¹) before being added into
540 the QD dispersion. After the ligands were added, the QD dispersions were further stirred for
541 about 30 min. The exchanged QDs were purified by adding extra toluene and acetonitrile,
542 followed by centrifugation. The purification process was repeated by another twice to remove

543 residual ligands. The purified QDs were then dispersed in hexane at a concentration of ~ 50
544 mg mL^{-1} and filtered. The hexane solvent is then removed by vacuum-drying and the QDs
545 were finally dispersed in toluene at a concentration of 300 mg mL^{-1} (based on the initial
546 amount for exchange). Note that the QDs with OA ligands (the QD stocks without ligand
547 exchange) were also further purified three times with toluene and acetonitrile to keep
548 consistency of the purification conditions over all samples.

549 **Film sample fabrication.** All QD film samples were deposited on high precision microscope
550 cover glasses (purchased from Marienfeld Superior) with the size of $18 \times 18 \text{ mm}$ and
551 thickness No. 1.5H ($170 \pm 5 \mu\text{m}$). The substrates were handled with extra care as they are
552 very thin and fragile. The substrates were cleaned subsequently by mild sonication with
553 detergent, isopropanol, acetone and deionized water followed by drying with a nitrogen gun.
554 The deposition of QD films were performed inside a nitrogen filled glovebox. Typically, 50
555 μL of the QD dispersion was dispensed on the substrate and then spin-dried at 1500 rpm for 1
556 min . The film samples were stored inside the glovebox overnight to allow the solvent to fully
557 evaporate. The samples were encapsulated inside the glovebox before any optical
558 measurements, and we found that a good encapsulation was the key to a successful fs-TAM
559 measurement as the pump and probe pulse lasers were focused on very small areas on the
560 samples. Air leakage caused the samples to quickly degrade (which appears as a ‘burnt’ hole
561 on the film as observed by the microscope) or very inconsistent results from spot to spot on
562 the same sample. To encapsulate a sample, the QDs deposited near the edges of the substrate
563 were first removed by a cotton stick wetted with hexane. Another coverslip was then placed
564 onto the substrate (with some carbon tapes to fix the position), and the edges were sealed
565 with epoxy. A schematic of a typical finished sample are shown in Supplementary Fig. S3.

566

567 **Characterizations**

568 **UV-Vis-NIR absorption measurement.** The absorption spectra of the samples were
569 measured using a Shimadzu UV-3600 Plus. The solution samples were measured (inside a
570 quartz cuvette) together with a reference sample with neat solvent. For film samples, an
571 integrated sphere was used to minimize scattering effects.

572 **Photoluminescence quantum yield.** PLQY measurements were made following the
573 procedure of a previous study⁴¹. Temperature and current controlled laser diodes (Thorlabs)
574 were used to generate stable laser beams (520 nm). These were focused through a small hole
575 onto samples suspended in a Spectralon coated integrating sphere (Newport 819C-SL-5.3)
576 modified with a custom baffle extension. Light from the experiment was collected using an
577 optical fibre connected to an Andor Kymera 328i Spectrometer housing a DU490A-1.7
578 InGaAs detector. The system was calibrated with a reference lamp (Ocean Optics) prior to
579 the measurement.

580 **Transmission electron microscope (TEM).** Transmission electron microscopy was
581 performed using a FEI Tecnai F20 TEM at 200kV accelerating voltage and imaged with a
582 Gatan Orius SC1000 CCD camera. Samples of dilute QD solutions ($<0.1 \text{ mg mL}^{-1}$) were
583 dropcast from toluene onto 200-mesh carbon-coated Cu grids (Agar AGS160).

584 **Femtosecond transient absorption spectroscopy.** An amplified diode Yb:KGW laser
585 system (Pharos, Light Conversion) at 38 kHz repetition rate provided ~ 180 fs pulses at 1030
586 nm. White light continuum (WLC) probe was generated in 4 mm YAG crystal and two 90°
587 off-axis parabolic mirrors were used to recollimate and focus the WLC to $\sim 100 \times 100 \mu\text{m}$ spot
588 on the sample. Other part of the fundamental was used to generate a third harmonic (453 nm,
589 HIRO, Light Conversion) to amplify another WLC generated in 3 mm sapphire via non-
590 collinear optical parametric amplification (NOPA) process in type I BBO crystal. The NOPA

591 output was centred at 540 nm, and then pre-compressed to ~ 15 fs using chirped mirrors and
592 fused silica wedges. After that, pump beam was delayed in respect to the probe beam by a
593 translation stage (Thorlabs, DDSM100/M) and focused to 545×360 μm spot-size on the
594 sample by a spherical mirror.

595 A sequence of probe pulses with and without the pump was generated by mechanical
596 chopping of the pump at 9.5 kHz. Transmitted probe beam through the sample was split with
597 a 950 nm dichroic mirror (Thorlabs). The visible part was imaged with a Silicon photodiode
598 array camera (Stresing Entwicklunsbüro) after dispersing it in a visible spectrograph (550 nm
599 blazed grating). The near-infrared portion of the probe was dispersed in an IR spectrograph
600 (1200 nm blazed grating) and imaged on an InGaAs photodiode array camera (Sensors
601 Unlimited). Data acquisition was shot-to-shot in respect to the chopper frequency. Offsets
602 due to the differing spectral response of the detectors was accounted for in the post-
603 processing of data.

604 **Femtosecond transient absorption microscopy (fs-TAM).** A Yb:KGW laser system
605 (Pharos, Light Conversion) provided 200 fs, 30 μJ pulses at 1030 nm with 200 kHz repetition
606 rate. The output fundamental beam was divided by a beam splitter and seeded two broadband
607 white light continuum (WLC) stages. The probe WLC was generated in a 3 mm YAG crystal
608 and adjusted to cover the wavelength range from 650-950 nm by a fused-silica prism-based
609 spectral filter. The pump WLC was generated in a 3 mm sapphire crystal to achieve bluer
610 WLC to 500 nm. The red-edge of pump beam is selected by 650 nm short-pass filter
611 (Thorlabs, FESH650). A set of chirped mirrors (pump; 109811, Layertec, probe; DCM9,
612 Venteon) and a pair of fused silica wedges (Layertec) compressed the pulses to 9.2 fs (pump)
613 and 6.8 fs (probe), as verified by second-harmonic generation frequency-resolved optical
614 gating (SHG-FROG) (see Pulse characterization, Supplementary Fig. S2). The pump pulse
615 was further pre-compressed with another set of chirped mirrors (109811, Layertec) to

616 compensate the dispersion in the microscope optics. The corresponding cross-correlation
617 curve simulated with the retrieved pump and probe temporal profiles given in Supplementary
618 Fig. S2 reveals an effective time resolution of 13 fs. A mechanical translation stage
619 (Newport, CONEX-AG-LS25-27P) was used to delay the probe with respect to the pump. A
620 clean TEM00 mode for pump was achieved with a pinhole and was collimated to completely
621 fill the aperture of objective lens. The pump beam was then focused onto the sample by an oil
622 immersion objective (100x, effective NA of 1.1) to the near diffraction limited spot (ca. 263
623 nm (FWHM) and 111 nm (width)) while the probe pulse was delivered into the sample with
624 the relatively large focal spot (ca. 15 μm) from the opposite direction. The transmitted probe
625 pulse was collected by the same objective and sent to an EMCCD camera (QImaging,
626 RoleraTM Thunder). The total magnification of the imaging system was 288x. The scattered
627 pump light was rejected by a 650 nm long-pass filter (Thorlabs, FEL650) inserted in front of
628 the camera. Differential imaging was achieved by modulating the pump beam at 30 Hz by a
629 mechanical chopper. We applied no gain to the EMCCD camera during the measurements.
630 Moreover, fs-TAM images were obtained by averaging images taken over 50 runs at 5
631 different spots of each films.

632 The probing wavelengths were selected (using a bandpass filter with 10 nm width) according
633 to the photo-bleaching peak position of the corresponding samples, as shown in the TA
634 results. The wavelengths are 740 nm for OA, 750 nm for both 12C and 8C, 770 nm for 6C
635 and 780 nm for 4C.

636 **Grazing incidence Small angle scattering (GISAXS) measurement.** GISAXS was
637 performed on the Xuess instrument equipped with an Excillum MetalJet liquid gallium X-ray
638 source. Alignment was performed on silicon substrates via three iterative height (z) and
639 rocking curve (Ω) scans, with the final grazing incidence angle set to $\Omega = 0.2^\circ$. Scattering
640 patterns were recorded on a vertically-offset Pilatus 1M detector with a sample to detector

641 distance of either 332 or 553 mm, calibrated using a silver behenate standard to achieve a q-
642 range of 0.045 – 2.0 Å⁻¹. Two-dimensional images were recorded with exposure time of 600
643 s. The images were masked to remove the sample horizon, detector module gaps and
644 beamstop and radially integrated from the apparent beam centre. Data correction and
645 reduction was performed using the GIXSGUI MATLAB toolbox⁴². Two-dimensional
646 scattering data was reduced to one-dimensional via radial integration, which was performed
647 with a mask to remove contributions from “hot pixels”, the substrate horizon and reflected
648 beam. The core-to-core spacing and FWHM were obtained by fitting a Gaussian to the
649 scattering peaks.

650

651 **Data availability**

652 The data underlying all figures in this article is publicly available from the University of
653 Cambridge repository at <https://doi.org/10.17863/CAM.80070>.

654

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