

A study on heat storage sizing and flow control for a domestic scale solar-powered organic Rankine cycle-vapour compression refrigeration system

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This paper presents the off-design modelling of a domestic scale solar organic Rankine cycle (ORC) and vapour compression cycle (VCC) in a coupled operation in different operating modes by using evacuated flat plate (EFP) collectors. Thermodynamic and parametric studies of such coupled system in literature usually assume that the isentropic efficiencies of expander and compressor and the heat exchanger pinch temperature differences are constant. Moreover, studies for directly coupling the ORC-VCC system with solar collectors are somewhat rare. Transient performance of the solar ORC-VCC considering the off-design behaviour of the system components needs to be investigated. A simulation for a period of 24hrs is conducted by considering the electricity and cooling demand of a 60 m² office building during a typical day in July for Istanbul. The effect of heat storage capacity on meeting the demand is investigated for a given area of EFP collectors. Moreover, the water flow rate to the boiler is controlled periodically to provide the demanded electricity and cooling. The required EFP collector area and heat storage unit volume have been determined to be 80 m² and 9.4 m³, respectively. For these design parameters, 25.6 kWh cooling and 18.76 kWh electricity can be generated during a typical day in July. Finally, a simulation is given for such design on a sunny winter day in February, 5.5 kWh electricity and 104 kWh heat can be produced.

Keywords: Solar Organic Rankine Cycle (ORC), vapour compression cycle (VCC), heat storage unit, off-design, control of flow rate

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36 **Nomenclature**

A	Area, m ²
c_1	Heat loss term, W m ⁻² K ⁻¹
c_2	Heat loss term, W m ⁻² K ⁻²
c_p	Specific heat, J kg ⁻¹ K ⁻¹
G	Solar irradiance, W m ⁻²
h	Specific enthalpy, J/kg
h_h	Heat transfer coefficient, W m ⁻² K ⁻¹
k	Thermal conductivity, W m ⁻¹ K ⁻¹
K_θ	Incident angle modifier
\dot{m}	Mass flow rate, kg s ⁻¹
M	Mass, kg
N	Rotation speed, RPM
Nu	Nusselt number
\dot{Q}	Heat rate, W
P	Pressure, Pa
Pr	Prandtl number
Re	Reynolds number
\bar{T}	Mean temperature, °C
T	Temperature, °C
U	Overall heat transfer coefficient, W m ⁻² K ⁻¹
v	Specific volume, m ³ /kg
\dot{W}	Power, W
x'	Vapour quality
X_p	Pump capacity fraction

Greek letters

η	Efficiency
ρ	Density, kg m ⁻³

Subscripts

ad	Adapted
am	Ambient
b	boiling
col	Collector
con	Condenser
comp	compressor
cw	Water in collector
eva	Evaporator
ex	Exhaust
exp	Expander
i	Isentropic
in	Internal expansion
l	liquid
leak	Leakage
<i>mec</i>	Mechanical
r	Refrigerant
<i>rc</i>	Refrigerant in cooling cycle
<i>su</i>	Supply
sw	Swept volume
<i>st</i>	Storage
st,N	Last node
v	Vapour
w	Water
<i>wo</i>	Water out from boiler
t	Tank
tur	Turbine

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1. Introduction

Electricity is becoming an increasingly crucial need for people, with electricity demand increasing day by day. Such electricity consumption has been triggered by a higher dependency and usage of electrical appliances in every dwelling, as well as the desire for improved living standards and more comfortable social environments using refrigeration systems. It is reported that in some cities, up to 50% of the supplied electricity during summer months is consumed by air conditioning applications [1]. Whilst this demand is being met by the suppliers, this will, however, cause further environmental concerns about fossil fuels' damage on environment and future shortage. Furthermore, indoor environments in these cities need to be heated for some periods during the year. Thus, fossil fuels are still used even if not by electrical heaters. Renewable energy is encouraged by governments and societies, therefore the use of renewable sources such as solar, geothermal and wind energy [2], [3],[4] to produce electricity offers great opportunity for reducing the fossil fuels consumption level.

Since solar thermal systems have a great potential to produce combined electricity, heating and cooling, solar thermal energy-related systems have been developed exponentially over the last decades. Solar trigeneration systems commonly have an absorption refrigeration cycle to obtain cooling from the collected solar heat [5], [6], [7]. To meet both electricity and cooling demand, a combination of a solar organic Rankine cycle (ORC) with a vapour compression cycle (VCC) can also be applicable. In this kind of systems, the expander shaft of the ORC and the compressor shaft of the VCC are coupled directly to reduce two-way energy conversion losses. Different from the absorption and desiccant refrigeration systems, the ORC-VCC system is flexible by the way of outputting power when there is no need to cooling. In a hot summer, most of solar heat can be used for to refrigeration, while less heat is used for cooling in spring and fall. When there is no need for cooling, the all available thermal energy can be converted to electricity and sent to the grid [8]. The present configuration has been investigated by a number of researchers but with some assumptions.

Some studies focused on a more effective system design by adding internal heat exchangers and recuperators [8],[9] , however, most studies were conducted to find the best working fluid through first and second law analysis [10], [11], [12], [13], [14], [15]. These kinds of parametric studies show performance of the system under a wide range of working conditions. However, during investigation of one parameter's influence on the system, all other parameters were held constant as if all components were operating according to design conditions'. Thus, isentropic efficiencies and heat exchanger pinch temperature differences were assumed as constant in the literature, despite it being known that system performance is related to operating conditions. To overcome this issue, system components need to be modelled and simulated in off-design operation.

The ORC-VCC system has a great capacity for using waste heat and solar source, however, studies for directly coupled this with a solar source are somewhat rare. A summary of the previous studies on

85 ORC-VCC systems is given in Table 1. Zheng et al. [16] investigated the performance of a solar
 86 Rankine cycle powered VCC by using zeotropic mixtures, although solar radiation was taken as
 87 constant in order to assess the performance of different refrigerants. The present study shows the
 88 transient performance of the ORC-VCC system using real solar radiation data. As is the nature of
 89 solar energy, the required solar energy is not available 24 hours to operate ORC-VCC, thus, when
 90 solar radiation is not available to drive the system, solar heat must be stored during the daytime.
 91 Therefore, a water storage tank is incorporated into system as a heat storage unit. Finally, a case study
 92 on meeting the cooling and electricity demand during a day, is conducted. To match the demand, a
 93 control strategy is adapted and its affect is investigated. Moreover, the system's performance in a
 94 sunny winter day operation in February is simulated to observe CHP mode performance. Thus, the
 95 cost effective performance of the system by operating in different modes can be clearly presented.

96 In summary, this study differs from the literature with a point of using transient analysis of the
 97 components and using solar energy as a heat source with integrating a water storage unit. The effect
 98 of the water storage capacity and control strategies on meeting the combined cooling and electricity
 99 demand are investigated. Moreover, the system configuration allows to operate even in winter by
 100 changing the operation mode from ORC-cooling to ORC-heating.

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102 **Table 1.** Summary of the previous studies on ORC-VCC systems

Reference	Working fluid	$\eta_{tur-exp}$	Heat Source	Notes
[8]	R245fa	0.75	N.A Boiler temp. 190°C	Many modifications
[9]	R22-R134a-R290	0.8	Flue gas (input 180-200°C output 100°C)	Compared basic and regenerative cycles with exergy analysis.
[10]	R290-R600-R600a-R1270	0.8 (0.6-0.9)	N.A (Boiler exit 60-90°C)	Parametric study
[11]	R143a-R22-R134a-R152a-propane-ammonia-isobutane-butane	0.8	Source temperature fixed at 150°C air.	NTU, size parameter and isentropic volumetric flow ratio analysis and exergy
[12]	R134a-R1234yf-R1234ze(E)	0.8	N.A Boiler exit(102°C - 152°C)	Separate system, parametric study and feasibility were conducted
[13]	R123-R600-R245fa-R141b-R600a	0.75	N.A (Boiler temp. 90°C - 120°C)	Exergy and parametric study
[14]	R245fa,R123,R134a,R1234yf, R1234ze (E)	0.8	Hot water at 100°C	Separate system, exergy analysis. Pinch point heat exchanger analysis.

[15]	R1270-R290-RC318- R236fa-R600a- R236ea- R600- R245fa-R1234yf- R1234ze(E)	0.8 (0.6-0.9)	N.A(Boiler temp 60°C - 90°C)	Parametric study
[16]	Various pure fluids and zeotropic mixtures	0.85 (0.85-1)	Solar (expander inlet 60°C - 120°C)	Zeotropic mixtures investigated
[17]	R245fa (cooling R134a)	0.75	Engine Exhaust gas (Boiler exit 190°C)	Separate system, in experiment, flow rate was changed and η_{exp} varied.
[18]	R134a- R245fa	0.9-0.8-0.7	Bus engine exhaust gas-oil (310-360°C)	Transcritical cycle

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104 2. System description

105 The proposed system consists of four sub-systems, namely, an array of solar field, a heat storage unit,
106 an ORC block and the VCC. The ORC comprises four main units, specifically, pump, boiler,
107 expander and condenser. The refrigeration system also has four main units, namely, compressor,
108 condenser, expansion valve and evaporator. Although the present study focuses on summer
109 application to produce both power and cooling, the components were selected to allow for operation
110 in winter as well for production of electricity and heating. In order to operate the system in all
111 seasons, some operation modes need to be determined and these are given below:

112 **Mode 1- ORC-Cooling:** this operation mode covers the main part of the paper. Original ORC-VCC
113 operation is required during the summer period to generate enough power to produce cooling at the
114 same time. Fig.1a shows the schematic view of the system. Blue dashed lines show inactivity in this
115 mode; a detailed explanation of the operation will be given.

116 **Mode 2- ORC-Heating:** this mode can be used when heating is demanded by residents. If sufficient
117 heat is stored in the tank to drive the ORC which is directly related with the solar radiation profile in
118 that day, the system can operate the ORC cycle and condensing heat from the ORC can be used for
119 heating the property. As shown in Fig.1b, the evaporator of the refrigeration system turns into an ORC
120 condenser and blue dashed lines are inactivated.

121 **Mode 3- Heating:** solar energy may be unavailable or fairly weak on some days in winter. Thus,
122 water temperature in the tank cannot be increased to a high enough level. On these days the system is
123 unable to produce electricity from the ORC. However, heating is still demanded by the residents.
124 Lower temperature water in the tank can therefore be used for heating, a process which is commonly
125 studied, thus it will not be simulated in this study.

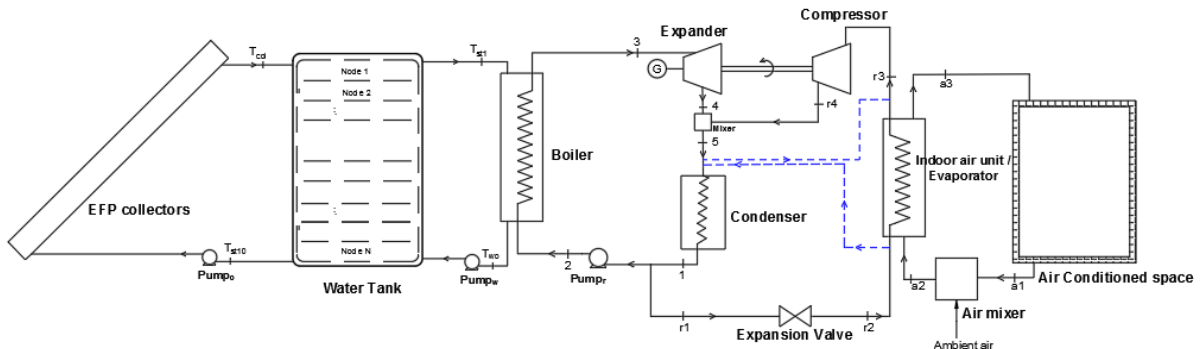
126 Since it is assumed that the system will operate smoothly in the three modes, solar collectors, heat
127 storage medium and expander were carefully selected on the following basis:

128 Evacuated flat plate (EFP) collectors were chosen as solar collectors given that they have advantages
129 over other types. They do not need a sun tracking system and they perform reasonably well even
130 under low radiation and low ambient temperature conditions when compared to conventional flat plate
131 collectors, thus there is a potential for use in winter [19]. Despite the higher cost, their ability to
132 operate during cold periods shows that EFP collectors are a good candidate for domestic trigeneration
133 systems. Water was chosen as the working fluid in the solar cycle. Given the temperature range of the
134 solar circuit which is below 150 °C, this also makes water a suitable working fluid which can be
135 directly coupled with a pressurised water tank. A water tank is used as a heat storage unit to provide
136 heat for the ORC, thus making a stable power generation for avoiding variation due to changing solar
137 irradiance. Moreover, it allows the operation of the ORC when solar radiation is insufficient or
138 unavailable. EFP collectors are used for heating water which comes from the bottom of the tank (T_{st10})
139 and is then discharged into the top of the water tank at a higher temperature (T_{col}).

140 High temperature water in the tank is used as a heat source for the ORC at (T_{st1}). A concentric tube
141 heat exchanger is adopted as a boiler for the ORC block and high-pressure working fluid is
142 evaporated in this boiler. After evaporating (3), high pressure and high temperature working fluid
143 enters into the expander. As an expander device, a scroll type expander was selected as these are well
144 adapted to small-scale Rankine cycle applications and further, offer the advantages of low rotational
145 speeds, reliability and ability to operate without significant performance reduction in different
146 operating conditions [20]. Regarding the working fluid selection, Saleh [15] reported that R600 and
147 R245fa achieved the best performance among other candidates in his parametric analysis. Therefore,
148 as seen in Table 1, the commonly preferred working fluid R245fa was chosen to use in this study.

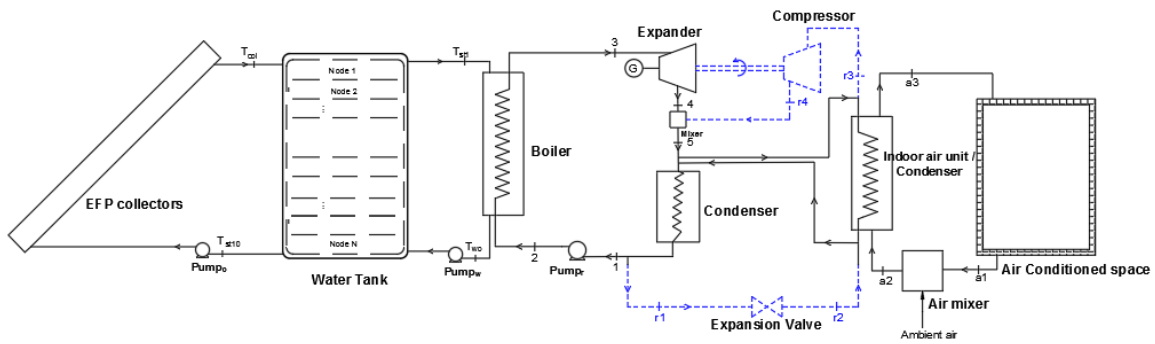
149 After the expander, the operating mode determines the path of the working fluid. For ORC-cooling
150 mode, the condenser is in common use by both the ORC and VCC systems, which lead the same
151 refrigerant circulating in both cycles, one comes from the expander (4), the other from the
152 compressor (r4), thereafter, the two are mixed in the auxiliary component mixer before entering the
153 condenser. Later, the refrigerant is separated through the two cycles after condensing. One path goes
154 into the pump (1) and leaves it with higher pressure (2). The other path is for the refrigeration cycle
155 (r1). Working fluid pressure and temperature is decreased by the expansion valve (r2) then via the
156 evaporator, the refrigerant is evaporated and provides cooling. After the evaporator (r3), working fluid
157 pressure and temperature is increased by the compressor.

158 For the ORC-heating mode, the compressor and expansion valve are not in use. The working fluid
159 directly enters the new condenser which was the indoor air unit evaporator in ORC-cooling mode
160 after the expander. While the fluid is condensing, taken heat is used for heating the room.



a)Cooling mode of ORC-VCC

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b)Heating mode of ORC-VCC

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Fig.1. Schematic views of heating and cooling modes of ORC-VCC

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165 For the air cooling section of the ORC-VCC system, the exhaust air from the conditioned space is
 166 mixed with ambient fresh air. This mixture is cooled at the evaporator and supplied to the conditioned
 167 space. The cooling load which impacts directly on the operation of the compressor, is calculated by
 168 using the software EnergyPlus [21] for the given data of Istanbul. A 60 m² office room was assumed
 169 for the case study and Fig.2 gives the cooling and electricity demands for the selected room during a
 170 typical day in July. To conduct the analysis, some assumptions were made:

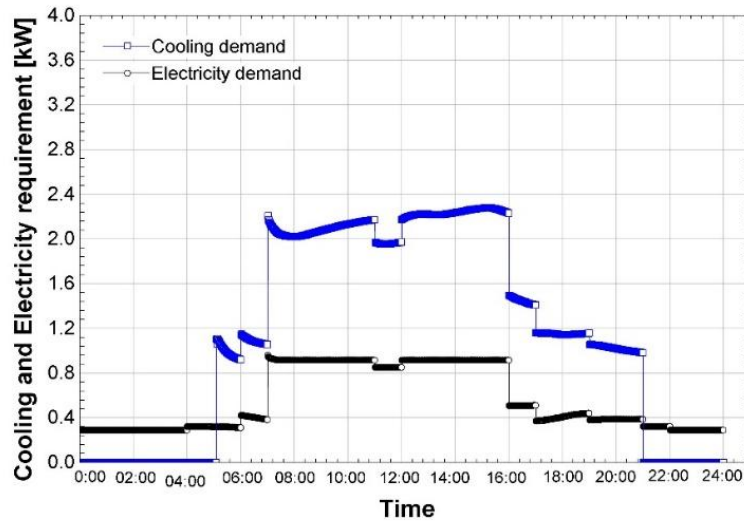
- 171 • For the cooling mode of the ORC-VCC system, the difference between the condensation
 172 temperature and the ambient air temperature was considered to be 10°C [22], [23]. This value
 173 is practically recommended for obtaining appropriate cost of heat exchanger [24].
- 174 • For the cooling mode of the ORC-VCC system, the evaporation temperature of the VCC is
 175 fixed at 5°C with assumption of no superheating. The conditioned space has a temperature of
 176 24°C and 50% relative humidity [14].
- 177 • For the heating mode of the ORC-VCC system, the VCC is not in use. The indoor air unit acts
 178 as the condenser of the ORC system and its condensation temperature was considered as 38°C
 179 [24].

- The mechanical efficiency of the compressor η_{mec} changes between 0.95-1 and it can be assumed as 0.95 [18].

182

183 According to the given assumptions, the corresponding P-h diagram of the ORC-VCC system for
 184 boiling temperature of 90 °C is given in Fig.3.

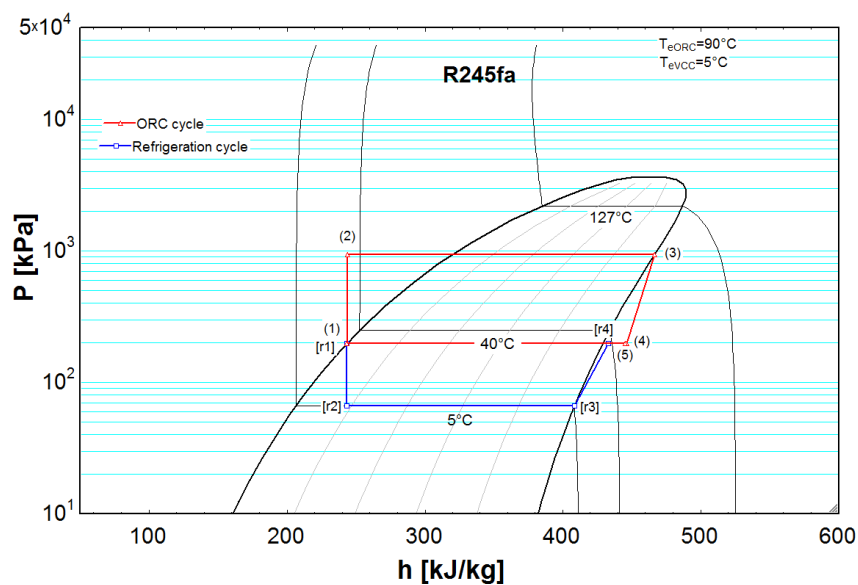
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187 **Fig.2.** Cooling and electricity demand during a typical day for an assumed office room

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190 **Fig.3.** P-h diagram of ORC-VCC system

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193 3. Modelling of components

194 3.1 Solar Collector

195 As solar collector TVP SOLAR HT-Power, a high efficiency evacuated flat plate collector has been
196 chosen for the study, given its potential in ORC systems was previously evaluated by Freeman et.al
197 [25], [26], Calise et.al [27] and Kutlu et. al [19]. Modelling of the evacuated flat-plate collector
198 follows the same assumptions as in the reference [26], $\eta_0=0.82$, $K_\theta=0.91$, $c_1=0.399$, $c_2=0.0067$, thus
199 the efficiency of the solar collector can be given by:

200

$$\eta_{col} = \eta_0 \cdot K_\theta - c_1 \frac{\bar{T} - T_{am}}{G} - c_2 \frac{(\bar{T} - T_{am})^2}{G} \quad (1)$$

201

$$\dot{Q}_{col} = \eta_{col} \cdot A_{col} \cdot G = \dot{m}_{cw} \cdot c_{p,cw} \cdot (T_{col} - T_{st10}) \quad (2)$$

202 3.2. Heat storage

203 A pressurised water tank is adopted as the heat storage unit. Its volume determines the energy storage
204 capacity and also the effect of its temperature levels on the performance. The water tank is modelled
205 in transient states by considering the thermocline behaviour. It is analysed using a one-dimensional
206 temperature distribution model [28]. Isothermal mixing zone methodology is used for simulations;
207 this multi node simulation allows the system to show potential temperature gradient inside the tank.
208 The cylinder volume has been divided into 10 equal layers. In every control volume, an energy
209 balance equation can be written considering the heat loss to the environment [6], [29]. By solving all
210 the energy balance equations simultaneously, the temperature distribution inside the tank can be
211 determined. Eq.(3) is the energy balance in the first control volume, Eq.(4) is the energy balance in
212 the internal volumes 'i'. Eq.(5) is the energy balance in the last control volume.

213

$$M_{st1} \cdot c_{p,w} \cdot \frac{\partial T_{st1}}{\partial t} = \dot{m}_{cw} \cdot c_{p,cw} \cdot (T_{col} - T_{st,1}) + \dot{m}_w \cdot c_{p,w} \cdot (T_{st,2} - T_{st,1}) - U_t \cdot A_{st1} \cdot (T_{st,1} - T_{am}) \quad (3)$$

214

$$M_{st,i} \cdot c_{p,w} \cdot \frac{\partial T_{st,i}}{\partial t} = \dot{m}_{cw} \cdot c_{p,cw} \cdot (T_{st,i-1} - T_{st,i}) + \dot{m}_w \cdot c_{p,w} \cdot (T_{st,i+1} - T_{st,i}) - U_t \cdot A_{st,i} \cdot (T_{st,i} - T_{am}) \quad (4)$$

215

$$M_{st,N} \cdot c_p \cdot \frac{\partial T_{st,N}}{\partial t} = \dot{m}_{cw} \cdot c_p \cdot (T_{st,N-1} - T_{st,N}) + \dot{m}_{drawn} \cdot c_p \cdot (T_{wo} - T_{st,N}) - U_t \cdot A_{st,N} \cdot (T_{st,N} - T_{am}) \quad (5)$$

216 3.3. Expander

217 In the present study, a decision was made to use a scroll type expander as this is particularly well-
 218 adapted to small-scale Rankine cycle applications. A semi empirical model was adapted from the
 219 study, based on Lemort et al. [30]. Guiffarida [31] further improved the model for use with all
 220 refrigerant. This expander model was implemented to analyse the variation of the expander
 221 performance over the changing conditions. modelling is following same steps with reference, such as
 222 1) adiabatic pressure supply, 2) Isobaric supply cooling down, 3) internal leakage, 4) adiabatic and
 223 reversible expansion to the adapted pressure 5) adiabatic expansion at constant machine volume, 6)
 224 adiabatic fluid mixing 7) isobaric exhaust heating-up or cooling down. All detailed calculation
 225 procedures are not explained here but some important parts are given. Mass flow rate of the
 226 refrigerant is determined from Eq.(6)

$$\dot{m}_r = \rho_{su1} \cdot A_{su} \cdot \sqrt{2 \cdot (h_{su} - h_{su1})} \quad (6)$$

227

228 \dot{m}_r is refrigerant mass flow rate at the inlet port in the scroll expander. This mass flow rate includes
 229 leakage flows as well. After isobaric cooling down the refrigerant, leakage flow rate can be
 230 determined by Eq.(7) and Eq.(8):

$$\dot{m}_r = \rho_{su,2} \cdot V_{sw} \cdot \frac{N}{60} + \dot{m}_{leak} \quad (7)$$

$$\dot{m}_{leak} = \rho_{leak} \cdot A_{leak} \cdot \sqrt{2 \cdot (h_{su,2} - h_{leak})} \quad (8)$$

231 V_{sw} and N indicate swept volume and rotation speed, respectively.

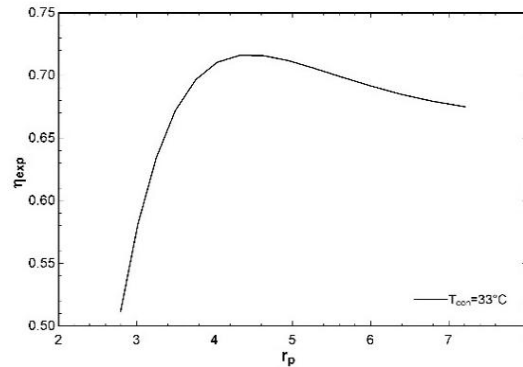
232 After leakage flow leaves from the main stream, rest of the working fluid expanded according to
 233 volumetric built in ratio. Then adiabatic expansion at constant volume occurs. Main stream refrigerant
 234 is mixed with leakage flow and finally exhaust heat transfer happens. After thermodynamic states are
 235 determined, internal expansion power can be found from Eq. (9):

$$W_{in} = (\dot{m}_r - \dot{m}_{leak}) \cdot [(h_{su,2} - h_{ad}) - v_{ad} \cdot (P_{ad} - P_{ex,2})] \quad (9)$$

236 Shaft power can be find from Eq. (10):

$$W_{shaft} = P_{in} - \frac{2 \cdot \pi \cdot N}{60} \cdot \tau_{loss} \quad (10)$$

237 Fig.4 shows the result of the model when the ambient temperature is held at 23 °C for refrigerant
 238 R245fa but supply pressure is varied.



239
 240 **Fig.4.** Variation of expander isentropic efficiency by pressure ratio
 241

242 3.4. Boiler

243 In the proposed system, there are three heat exchangers but the boiler is the most important
 244 component of the ORC because boiler uses hot water from the water tank to evaporate the refrigerant.
 245 It is expected that the temperature of the water varies with time due to consumption and charging for
 246 this reason, a sliding pressure operation is implemented in the modelling, which means that the
 247 evaporation pressure is determined from the water inlet temperature. However, effect of water inlet
 248 temperature is the not only consideration. Since one of the target of this study is controlling the
 249 evaporation temperature by changing water mass flow rate, the boiler needs to be modeled to obtain
 250 the effect of the water mass flow rate. By neglecting the pressure losses and making the study more
 251 practical, double pipe heat exchangers were selected as a boiler in the ORC. To conduct the off-design
 252 analysis of the heat exchanger, the effectiveness-NTU method was implemented.

$$NTU = \frac{U \cdot A}{C_{min}} \quad (11)$$

253
 254 Where NTU is number of transfer units, U is overall heat transfer coefficient. The boiler consists of
 255 two regions in one exchanger such as the single phase and evaporation regions as given in Fig.5. In
 256 off-design operation, the total length of the boiler is constant, however, regions may differ according
 257 to heat source conditions. Heat transfer coefficient can be determined as follows:
 258

$$h_h = \frac{Nu \cdot k}{d} \quad (12)$$

259

260 Here, Nu, k and d are Nusselt number, thermal conductivity of refrigerant and diameter of the tube.

261

262 Since flow inside tube is turbulent, the Nusselt number of single phase region for liquid water and
 263 pure liquid R245fa can be found with Gnielinski [32] equation:

$$Nu = \frac{\left(\frac{f}{8}\right) (Re - 1000) Pr}{1 + 12.7 \left(\frac{f}{8}\right)^{0.2} (Pr^{2/3} - 1)} \quad (13)$$

264

265 where f can be calculated with Petukhov [33] equation:

$$f = (0.79 \ln Re - 1.64)^{-2} \quad (14)$$

266

267 When boiling of the refrigerant R245fa takes place, fluid is in a two-phase state (saturated mixture).

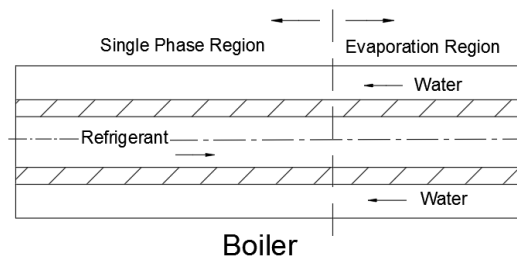
268 For boiling in the evaporator, the Kenning-Cooper correlation is used as given by Sun and Mishima
 269 [34] based on their findings.

$$Nu_b = [1 + 1.8X^{-0.87}] 0.023 Re_l^{0.8} Pr_l^{0.48} \quad (15)$$

270

271 where X is the Martinelli factor which is given from vapour quality x:

$$X = \left(\frac{1-x}{x}\right)^{0.9} \left(\frac{\rho_v}{\rho_l}\right)^{0.5} \left(\frac{\mu_l}{\mu_v}\right)^{0.1} \quad (16)$$



272

273 **Fig.5.** Schematic of boiler single and two-phase regions boundary

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275 **3.5. Compressor**

276 An important parameter of the VCC unit is compressor work. The compressor is directly coupled with
 277 the expander, so the compressor work equation can be included with mechanical transmission
 278 efficiency. The equation is given as:

$$\dot{W}_{comp} = \frac{\dot{m}_{rc} \cdot (h_{r4} - h_{r3})}{\eta_{mec} \cdot \eta_i} \quad (17)$$

279 Here, η_{mec} and η_i are mechanical and isentropic efficiency of the compressor, respectively. η_{mec}
 280 changes between 0.95-1 and it can be assumed as 0.95 [18]. However, η_i changes with condensation
 281 and evaporation pressure ratio. So, the following equation is used [35].

$$\eta_i = 0.874 - 0.0135 \cdot \frac{P_{con}}{P_{eva}} \quad (18)$$

282

283 where P_{con} and P_{eva} are condensation and evaporation pressures.

284

285 **3.6. Evaporator**

286 As previously mentioned, in cooling mode, evaporation temperature is kept constant, the refrigerant
 287 mass flow rate varies according to cooling requirements and this affects compressor work under
 288 different ambient conditions. In the calculations, cooling load is known parameter and taken from
 289 EnergyPlus data. Since evaporator inlet and outlet conditions are determined primarily, the mass flow
 290 rate of the refrigerant in cooling cycle can be found.

$$\dot{Q}_{cooling} = \dot{m}_{rc} \cdot (h_{r3} - h_{r2}) \quad (19)$$

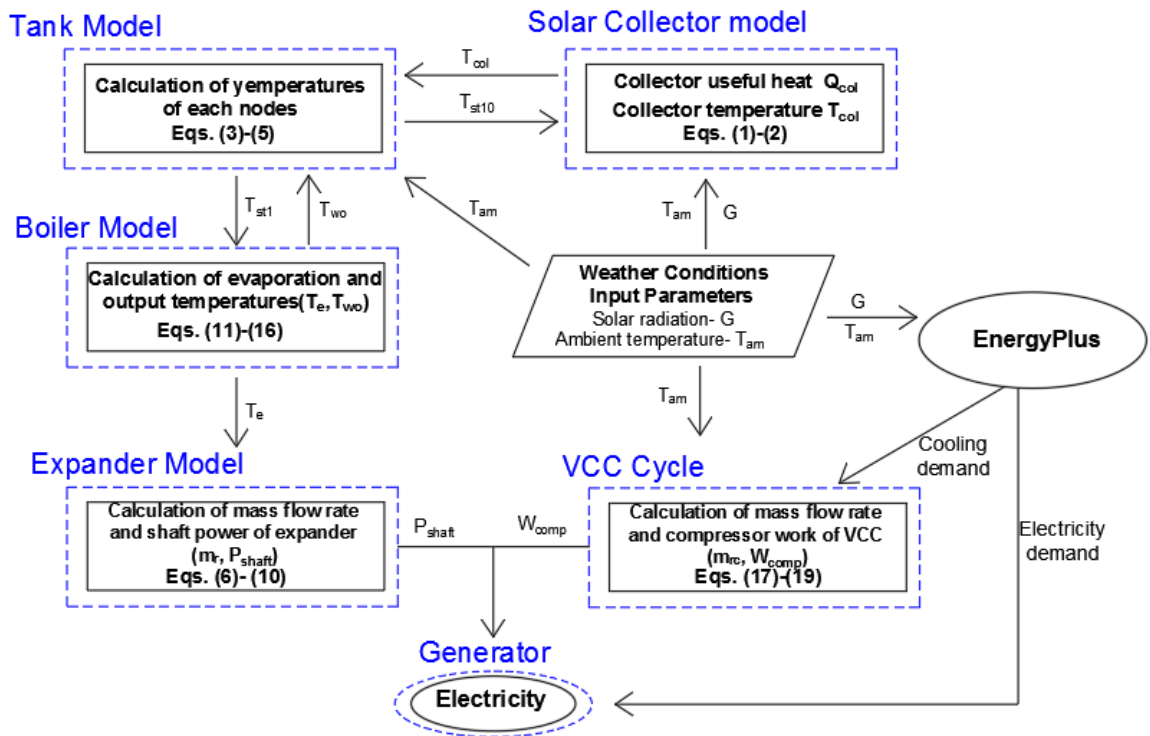
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292 **4. Results and discussions**

293 In order to evaluate the system performance, design conditions need to be determined first. These
 294 are determination of the design evaporation and condensation temperatures and later, the boiler is
 295 dimensioned as operation of the ORC depends on boiler performance. Transient mathematical model
 296 has been built in Matlab environment and results have been presented by using EES (Engineering
 297 Equation Solver) software. When design conditions are determined, the simulation is run, and
 298 collector and storage dimensions are changed until the system output matches with the desired output.
 299 The calculation procedure is briefly summarized in Fig.6. Useful solar heat is collected by the EFP
 300 collectors. This useful heat and collector water inlet temperature effects the output temperature which
 301 is mixed with the first element of the tank. Tank model gives temperature distribution of the water in
 302 tank. It is effected by two circulation waters one to the collector side and the other to the boiler side.
 303 Boiler model determines the evaporation temperature of the working fluid and also effects on tank
 304 temperature gradient as well. Expander model calculates the mass flow rate and shaft power output.
 305 The solar ORC and VCC systems are evaluated as separate systems except their condensing parts
 306 because VCC performance mainly depends on compressor electricity consumption and it can be

307 calculated from the cooling load which is variable. Calculated mass flow rate from the evaporator is
 308 used to obtain compressor work. The compressor work is taken from the expander shaft and the rest
 309 of the energy is transmitted to the generator to generate electricity.

310

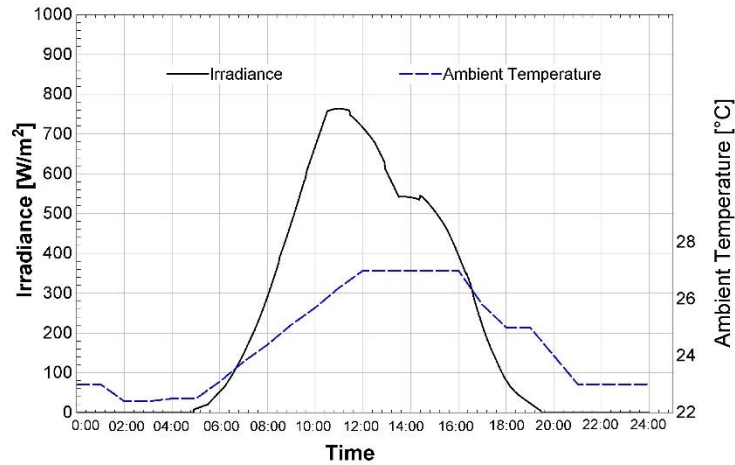


311

312 **Fig.6.** Calculation procedure of the system

313 4.1. Determining of Design Conditions

314 Condensing temperature of the ORC can be determined first, as it depends on the ambient temperature
 315 for air cooled condensers. Fig.7 shows ambient air temperature and solar irradiance variation during a
 316 warm day in July in Istanbul. Since the water tank is a finite heat storage, it is necessary to choose
 317 matched requirements to avoid over usage of the contained heat. Thus, before selecting the design
 318 conditions and parameters, the total electricity demand of the room is required. Variation of
 319 compressor work and total demands including electrical appliances as given in Fig.8. The compressor
 320 work was calculated according to the cooling load given in Fig.2. It is found that the maximum
 321 compressor work and total demand are 0.4kW and 1.35 kW, respectively.

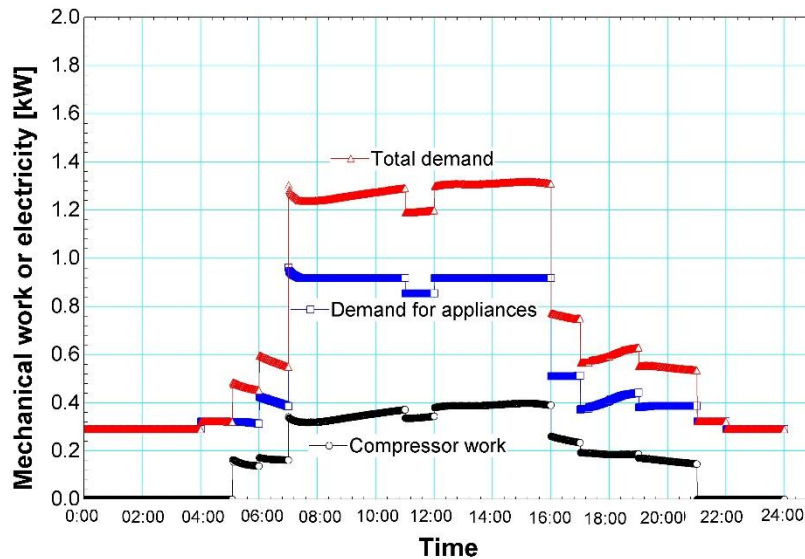


322

323

Fig.7. Weather data for a typical warm day in Istanbul

324



325

326

Fig.8. Mechanical work or electricity demand of the system over time

327

328 To provide 1.35 kW of work from the expander shaft, the design evaporation temperature is selected
 329 as 95 $^{\circ}\text{C}$ when considering the generator efficiency and safety factor. A volume of 150 L hot water
 330 tank is the standard household size in practice. However, in this study, charging and discharging heat
 331 levels are elevated compared to the conventional domestic water tanks. To maintain the required
 332 amount of heat to the system, the heat storage tank can be selected from 1.5 m^3 to 9 m^3 . To provide
 333 useful solar heat for running the system at given design conditions, a 60 m^2 collector area was chosen
 334 preliminarily, to be the same as the floor area of the simulated office room. In Table.2, design
 335 conditions for the ORC unit are summarised.

336

337

Table 2. Selected design conditions and system specifications

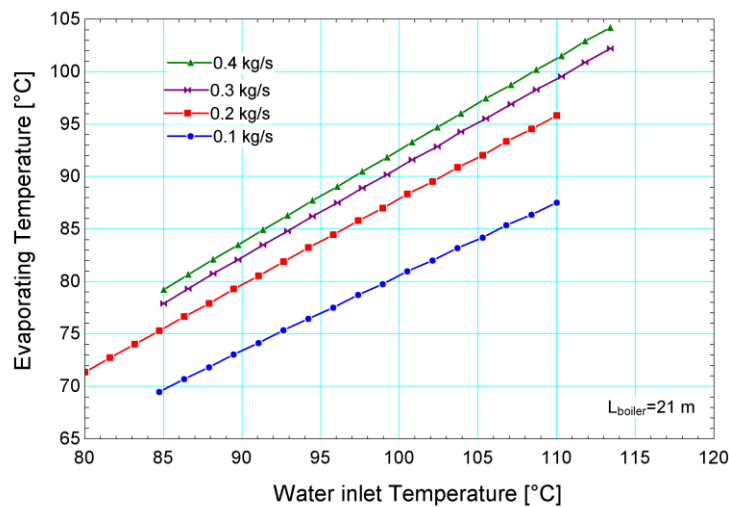
Parameter	Value	Parameter	Value	Parameter	Value
Collector area	60 m ²	Evaporation temperature in boiler	95 °C	Boiler water side diameter	0.016 m
Collector flow rate	0.02 kg/s	Water inlet Temperature	105 °C	Boiler refrigerant side diameter	0.007 m
Tank volume	3.5 m ³	Circulating water flow rate	0.3 kg/s	Length of boiler	21 m
Condensation temperature	36 °C	Heat from source:	15.6 kW	Expander shaft output	1.437 kW

338

339 **4.2. Off-design characteristics and control strategy**

340 Off-design performance of the system is based on the performance of the boiler given that work
 341 output is related to the evaporation temperature and this temperature is directly related to the source
 342 conditions which come from the water tank. Two parameters determine the evaporation temperature
 343 in the boiler. The first is source temperature; as solar energy is not constant during the day, the water
 344 tank is exposed to charge and discharge operations. In the day time, the tank is charged by the
 345 collected useful heat and its temperature is increased in spite of ORC runs at the same time. As a
 346 result of this increment, evaporating temperature and work output increase. The other parameter is
 347 mass flow rate of the water. The mass flow rate also has an influence on the evaporation temperature.
 348 The effects of the parameters are given in the Fig.9. This trend reveals the off-design operation of the
 349 system.

350



351

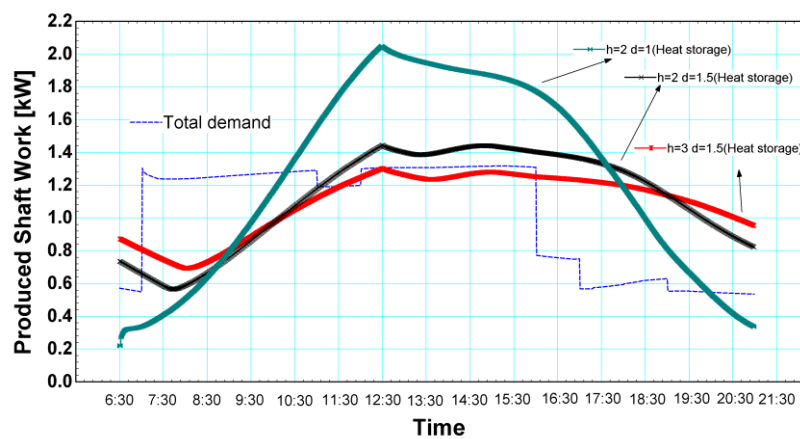
352 **Fig.9.** Evaporation temperature variation according to water inlet temperature and mass flow rates.

353 Operation of the system is given as the basis: the ORC-VCC system operation starts at 06:30 to
 354 provide shaft work to the compressor; for cooling purposes, the collector pump operates and collected
 355 solar energy is accumulated in the storage, at the same time the ORC produces electricity for
 356 supplying to the electrical appliances. The water mass flow rate from tank to boiler is selected as 0.3
 357 kg/s to match with the demand via previously designed heat exchanger. The peak period ends at 16:00
 358 and the other period which requires less work begins. In this period, the mass flow rate of water is
 359 reduced to 0.1 kg/s to prevent excessive use of the heat source. This period is completed by 21:00 and
 360 energy in the tank is stored for the next day. There still exists an electricity requirement in the
 361 building, but this requirement can be met from the grid or a storage battery.

362

363 4.3. Simulations

364 To simulate the system, initial tank temperature selection is an important issue. As one-day simulation
 365 is carried out for a typical day, the temperature is not uniform in the tank due to the thermocline
 366 behaviour of the water. Normally, the initial temperatures of the water layers in the tank are the final
 367 temperatures of the previous day. However, this study considers only one day, thus, the initial
 368 temperatures need to be determined by iteration. Firstly, an assumed temperature value is given to all
 369 water layers and simulation is executed. The final temperatures of the first simulation are used as the
 370 initial temperatures of the next simulation. The steps were repeated until the end temperature
 371 distribution matches the initial temperature distribution [19]. It can be said that all of the useful solar
 372 energy charged to the tank is used for driving the ORC and the rest is transferred to the ambient as
 373 heat losses. The useful heat gain trend is directly affected by the solar irradiance pattern during the
 374 day. To observe the effect of the heat storage volume on the system performance, Fig.10 is plotted by
 375 using constant water mass flow rate during all periods.



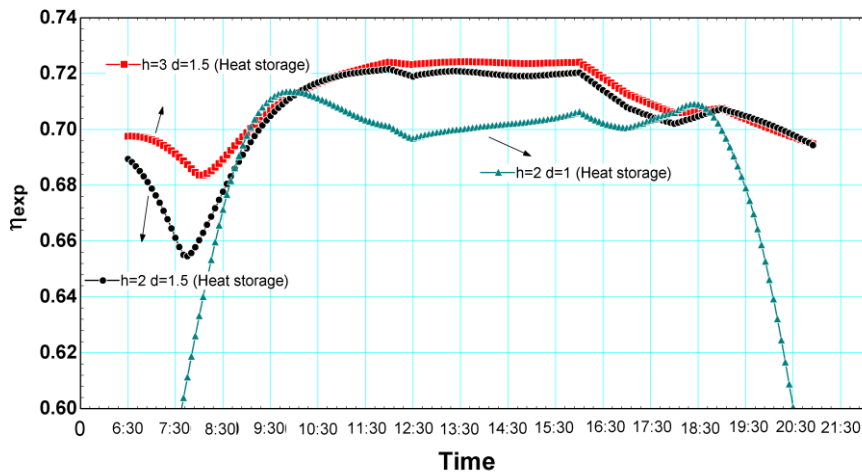
376

377 **Fig.10.** Produced shaft work versus time for various heat storage dimensions ($m_w=0.3$ kg/s,
 378 $A_{collector}=60m^2$)

379 Since temperature increment is higher when using the constant solar collector area in smaller heat
 380 storages, peak output yields higher than the demand. A problem occurs, however, in the early morning
 381 period as output in this period cannot fulfil the demand. One solution is an increment to the storage
 382 capacity to avoid excessive temperature fall at night-time, however, using higher capacity storage
 383 decelerates the temperature increase at midday. As seen from Fig.10, when 3 m high and 1.5 m
 384 diameter heat storage units area used, produced work is getting closer to the demand but does not
 385 fulfil the midday demand as the temperature of the storage is not high enough.

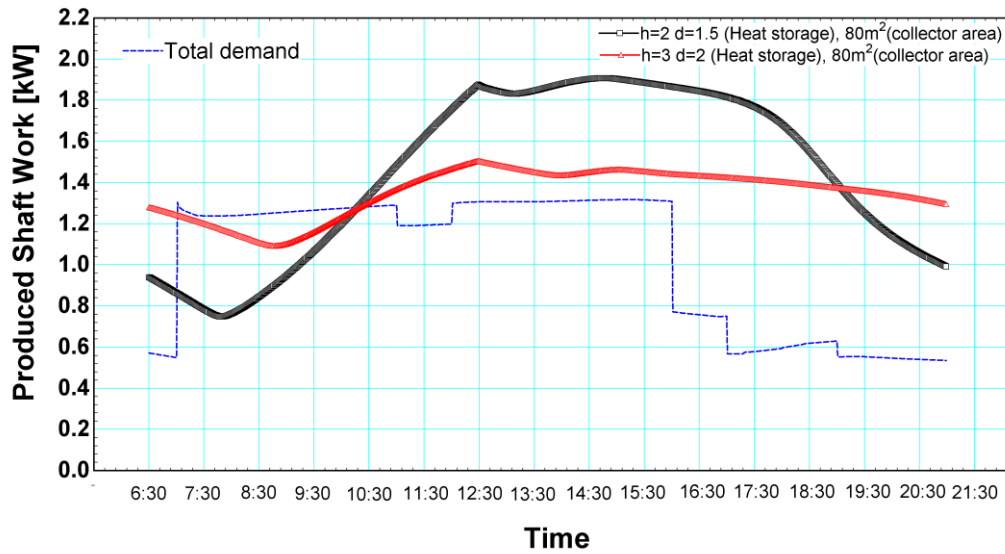
386 Fig.11 shows expander efficiencies for using various storages. Since temperature alteration is high in
 387 small capacity storages, expander performance variation is considerable. For the bigger storages,
 388 expander performance can be further stabilised by avoiding excessive changes to the operating
 389 temperature.

390 In order to meet the electricity demand, the collector area is increased to 80 m² and simulations have
 391 been conducted for two different storage sizes. Fig.12 shows that increments in collector and heat
 392 storage size are still not enough to meet the demand. As a solution, the mass flow rate of the water
 393 needs to be controlled for different periods, so power output and heat rejection rates can be controlled.
 394



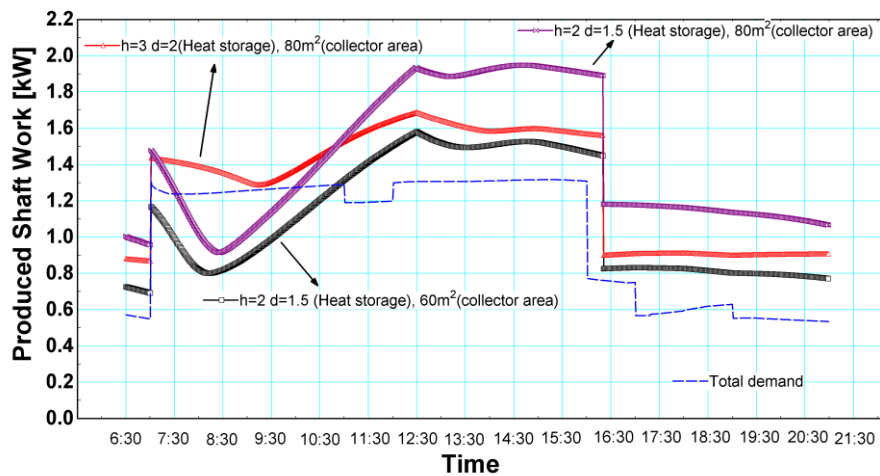
395
 396 **Fig.11.** Expander efficiency for various heat storage dimensions ($m_w=0.3$ kg/s, $A_{collector}=60m^2$)
 397

398
 399
 400
 401
 402



403
 404 **Fig.12.** Produced shaft work by time for various heat storage dimensions ($m_{w2}=0.3$ kg/s,
 405 $A_{\text{collector}}=80\text{m}^2$)
 406

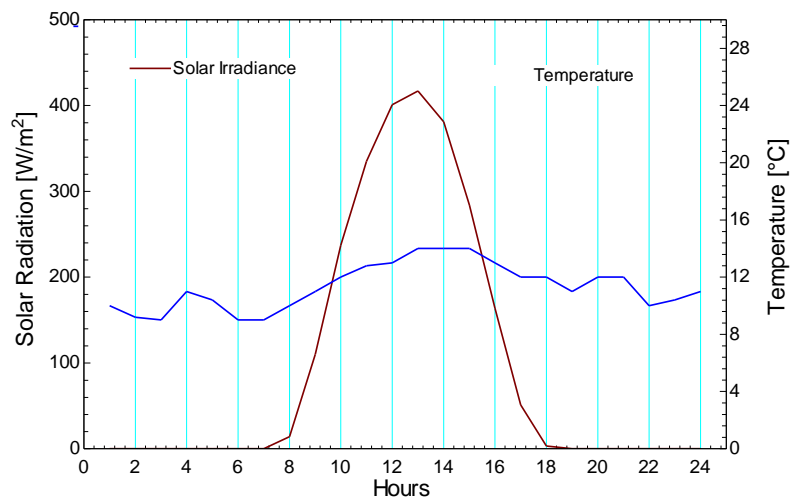
407 In Fig.13, the mass flow rate is controlled for three different cases. Firstly, a case using a 60 m^2
 408 collector area and 2 m height with 1.5 m diameter storage tank has been analysed. Although
 409 performance is improved by controlling the mass flow rate, there is still a problem in the morning
 410 period, as the temperature of the tank at the end of the day does not satisfy the requirement in early
 411 morning, until the sufficient solar radiation is received. An increment to the storage capacity to avoid
 412 excessive temperature fall in the night period can be applied, however, it may require a larger
 413 collector area. To observe the phenomenon, a second case has been analysed. When the heat storage
 414 size is held constant and the collector area is increased to 80 m^2 , over production occurred at midday,
 415 however, the problem still exists in the early morning. As a final case, the storage size is also
 416 increased with the collector area. With these final changes, produced work fulfils the demand.



417
 418 **Fig.13.** Produced shaft work by time with control strategy ($m_{w1}=0.1$ kg/s, $m_{w2}=0.3$ kg/s)

419 **4.4. ORC-heating mode**

420 One of the advantages of the proposed system is that it should operate and show a good performance
421 in winter days without any modification by switching to CHP mode. In this mode, the compressor
422 does not run and the VCC indoor air unit evaporator operates as the ORC condenser, which is given in
423 Fig.1b. Since this heat exchanger located in the air conditioning cycle, what would normally be
424 wasted condensing heat can be used for heating purpose. The condensation temperature is adjusted at
425 38 °C to heat up the indoor unit blowing air. This temperature is identical to the condensing
426 temperature in ORC-cooling mode. More specifically, the ORC operation would not be affected by
427 the mode switch as a result of the same condensing temperature and pressure. However, electricity
428 output is expected to decrease, as solar heat would be lower than in the summer. Fig.14 shows
429 weather condition for a sunny day in February. Solar radiation is quite good but ambient weather
430 temperature is around 12 °C which shows heating is needed. Solar collectors and ORC work same as
431 with the ORC-cooling mode but expander outlet is directed to the indoor heat exchanger. Fig.15
432 shows instant electricity generation by the ORC, the magnitude of the production looks not satisfying
433 but electricity production in daily basis is 5.5 kWh. The reason is lower tank temperature. Since solar
434 irradiance is not good in previous days, water tank temperature reduces and it causes lower
435 evaporation temperature with lower electricity output. It should be noted that while electricity is
436 produced its useful condensing heat, almost 7kW, can be used for space heating. Required heat is
437 transferred to the indoor air and the rest is ejected by the outdoor condenser as seen in Fig.1b.



438

439

Fig.14. Solar radiation and ambient temperature profile on a sunny winter day

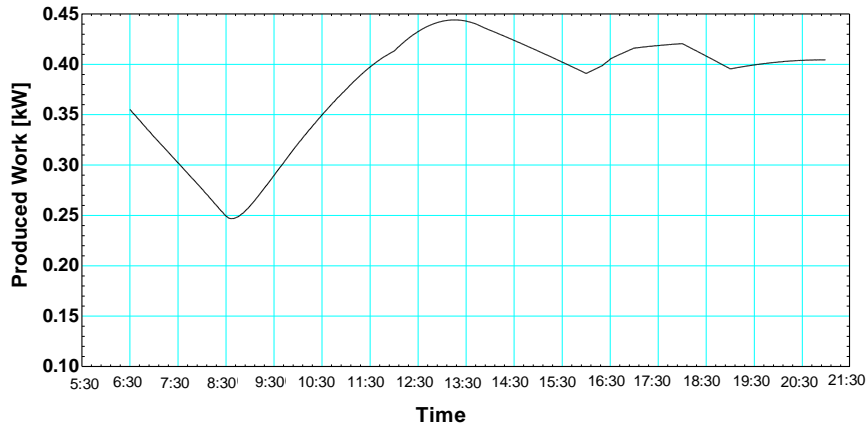


Fig.15. Produced shaft work in the heating mode of ORC-VCC

5. Conclusion

In this study, the modelling of the solar ORC-VCC system integrated with a sensible heat storage unit operating at off-design conditions has been presented. Electricity and cooling demand from the end user has been also considered from the point of view of control strategies. In the solar part, evacuated flat plate collectors have been used and collectors linked with a sensible heat storage unit. The heat storage unit has been modelled on the multi node analysis method to obtain thermocline phenomena. A transient analysis has been conducted to predict system outputs considering the off-design performance; in this way the analysis differs from the steady-state models. As working conditions have an influence on expander performance, electricity output is also effected. It is shown that water flow rate control strategies are promising and can improve the precision between the produced work and the demand. Sizes of the components have been determined according to summer conditions for Istanbul for ORC-cooling mode. It was found that to meet electricity and cooling demand for studied office, 80 m² collector array and 9.4 m³ heat storage are required. Additionally, this system with selected components have been analysed for a winter day as ORC-heating mode and 5.5 kWh electricity and 104 kWh heating load potential has been obtained.

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