# A Note on Geographic Systems and Maps of Montserrat, West Indies

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#### Abstract

2 3 It is often critically important that geospatial data are measured and mapped accurately, 4 particularly for quantitative analyses and numerical modelling applications. Defining a 5 geographic coordinate system requires a non-unique combination of geodetic techniques (e.g. 6 ellipsoids, projections and geoids). The choice of geographic system presents scope for 7 ambiguity and confusion about geographic data, especially those archived without appropriate 8 metadata. Experience has shown that these confusions have been a repeating source of either 9 frustration or inadvertent error for those using geographic data from Montserrat. This is, in part, 10 probably due to common usage of multiple datums and the existence of numerous topographic 11 data sets recorded during the past 150 years. Here, we attempt to provide a brief introduction to geodetic principles and their application to Montserrat geographic data. The differences between 12 13 common datums are illustrated and we describe variations in magnetic declination as they apply 14 to field use of magnetic instruments. We include a record of the source of the large-scale 15 mapping data sets that have been used and analysed ubiquitously in the literature. The 16 descriptions here are intended as an introductory reference resource for those using geographic 17 data from Montserrat. 18 19 20 Number of Words: 3352 21 22 Number of References: 18 23 24 Number of Tables: 2 25 26 **Number of Figures:** 3 27 28 Abbreviated Title: Montserrat Geographic Systems & Maps

30 Accurate mapping is essential in most areas of geoscience. To understand geospatial data we 31 adopt coordinate systems in which we are able define position and velocity. However, the choice 32 and specification of the coordinate system is not unique and, over the centuries, geodesists have 33 derived a multitude of methods for describing three-dimensional (3D) geographical data. 34 Commonly, this invokes the use of a reference ellipsoid, which models the approximate shape of 35 the Earth's surface; a projection, which translates that ellipsoid into two dimensions (2D); and 36 sometimes a specific reference surface from which height is measured (e.g. sea level). Confusion 37 between different coordinate systems can be - and has been on occasions - a source of 38 significant error when using and comparing geospatial data. The explanations and data given 39 here include a brief summary of the most commonly used systems on Montserrat. Descriptions 40 and derivations of various ellipsoids, geoids and projections are widely available elsewhere (e.g. 41 Robinson et al., 1995). Specifications are also provided here to assist configuration of field tools 42 such as handheld GPS receivers. A summary of the changes in magnetic declination for 43 Montserrat since 1995 is also included. The information herein is intended purely as a practical 44 introduction for those using geospatial data from Montserrat, not as an exhaustive description of 45 cartographic methods.

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#### 47 1. Ellipsoids, Projections and Geoids

48 There exists a plethora of simple geometrical ellipsoidal models that approximately describe the 49 shape of the Earth. An ellipsoid's shape and size is defined by the lengths of its three mutually 50 perpendicular radii. A geodetic ellipsoid is symmetrical around its polar axis such that its shape 51 may thus be defined by just two parameters: the equatorial and polar radii (a and b, respectively). 52 These may be given explicitly or via a flattening factor, f, that relates a to b, where f = (a-b)/a. 53 Flattening is also often cited in inverse form: 1/f. The origin (centre) of any two ellipsoids may 54 be offset in space. An ellipsoid may thus be described by five parameters: the offset of its origin 55 from the Earth's centre of mass (dX, dY and dZ – see Figure 1); the equatorial radius; and either 56 the polar radius or the flattening factor. In some cases, additional parameters may be required 57 (e.g. coordinate axis rotation), but this will not apply herein. Ideally, an ellipsoid would 58 approximate mean sea level (or, more specifically, the geoid – see below) on a global scale. 59 However, this is not the case due to the unevenness that means even globally-defined ellipsoids 60 can vary from mean sea level by over 100 metres in some regions. Accordingly, this has given

rise to many different ellipsoid definitions, with models often optimised to fit sea level well overa particular geographical region.

63 Adopting an ellipsoid as a simplified geometrical representation of the Earth allows for 64 geometrical translation of features on the surface of that ellipsoid onto a 2D plane (i.e. a map). 65 However, in performing such translations (projections), geometrical relationships (e.g. distance, azimuth, shape, area, etc.) cannot *all* be fully preserved on any single map. The method for 66 67 projecting information from the ellipsoid onto a map thus depends on which properties takes 68 precedence and requires the according compromises. Numerous projections exist, but focus is 69 given here only to those in common use on Montserrat. The Transverse Mercator (TM) method 70 offers a suitable strategy for map projection on Montserrat and is described in brief in the next 71 section. For small areas, such as Montserrat, distortions due to the curvature of the ellipsoid can 72 usually be neglected. It is notable, however, that such assumptions may be inappropriate for 73 precision applications (e.g. ground deformation surveying). 74 A geoid is an equipotential surface that closely aligns with mean sea level around the globe –

typically to within a couple of metres of local mean sea level – and can be measured through
precise gravitational surveying. Unlike an ellipsoid, the geoid is complex in its shape, with
undulations caused by the heterogeneous distribution of mass around the Earth. Recent geoid
models have been derived using a combination of data from spaceborne gravity surveys (e.g.
GRACE and GOCE). The geoid offset for a specific location – given as the vertical offset
between the geoid model and an ellipsoid – may be computed using published model spherical

81 harmonic coefficients or interpolated from gridded geoid data (NGA, 2012).

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#### 83 **2. Datums Used On Montserrat**

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85 For reasons discussed below, the two most commonly used ellipsoids are the Clarke 1880 and 86 World Geodetic System 1984 (WGS84) ellipsoids. Geographic coordinates are usually expressed 87 either in terms of geodetic latitude and longitude (in degrees) or via a TM projection. Heights are 88 measured relative to a vertical reference surface – usually the ellipsoid or, sometimes, a geoid 89 model. It is important to be sure that a common datum (the combination of ellipsoid, projection 90 and vertical reference) is used when considering multiple spatial datasets. Similarly, it is critical 91 that the implications of the projection (i.e. distortion) are considered in analyses where spatial 92 data are manipulated or analysed quantitatively.

93 Pre-eruption maps of Montserrat are derived from aerial photographs acquired in the 1950s on 94 behalf of the British Government's Directorate of Overseas Surveys (DOS, 1983). The map data 95 derived from these surveys were plotted using the Clarke 1880 ellipsoid and either geodetic 96 coordinates or a customised metric TM projection, referred to herein as the British West Indies 97 (BWI) grid. This datum is used by the Government of Montserrat Lands and Survey Department 98 and was initially adopted by staff and colleagues at the Montserrat Volcano Observatory (MVO; 99 e.g. Kokelaar, 2002). In recent years, the use of the WGS84 and Universal Transverse Mercator 100 (UTM) datum has become more prevalent for representing data gathered on Montserrat as it 101 provides a standardised approach to referencing geographic data. The following summaries 102 describe these systems and appropriate parameters are given in Tables 1 and 2.

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### 104 2.1 Earth-Centred Earth-Fixed Coordinates

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Positions given in Earth-Centred Earth-Fixed (ECEF) coordinates refer to a 3D Cartesian
coordinate system, with its origin at the Earth's centre of mass (the WGS84 origin, as shown in
Figure 1) and axes aligned as follows: the *Z* axis is approximately aligned with Earth's axis of

109 rotation (the International Earth Rotation Service, IERS, Reference Pole). The X axis is

110 perpendicular to Z and passes through the IERS Reference Meridian (near the Greenwich

111 Meridian), and the *Y* axis is mutually perpendicular to *Z* and *X* (NIMA, 2004).

112 Values of position, distance, angle and velocity can be defined explicitly and unambiguously in

this system without the need of a reference surface or projection. This can be advantageous when

114 handling position or velocity data outside of a geographic context, as there is no distortion due to

115 projection. However, ECEF coordinates bear no intuitive relation to other features on the Earth

and are often not useful for cartographic or geographic applications.

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# 118 2.2 Ellipsoids

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120 Two ellipsoids have been used predominantly in mapping Montserrat over the past century: the

121 WGS84 ellipsoid and the more region-specific Clarke 1880 ellipsoid. Geodetic coordinates

122 (degrees of latitude and longitude) can be used in conjunction with any ellipsoid but a given

123 position will mark a different position on the ground, depending on the ellipsoid used.

124 In recent decades, the WGS84 ellipsoid has become an international standard for geodetic 125 applications, against which other systems' parameters are conventionally referenced. The origin 126 of the coordinate system (Figure 1) is taken as the Earth's centre of mass, measured and updated 127 using satellite and orbital measurements, and is coincident with the ECEF origin. The WGS84 128 ellipsoid was devised as an approximate fit to the global mean sea level (via the geoid), and thus 129 typically results in regional deviations of many tens of metres. The WGS84 ellipsoid reference 130 surface is around 41 m above sea level near Montserrat (Figure 2), for example. Due to changes 131 in the location of the Earth's centre of mass and the accuracy with which it can be measured, the 132 WGS84 has undergone several revisions since it was first realised. While the differences 133 between versions are small – usually negligible for navigation purposes, for example – they can 134 be significant for precision surveying applications.

135 The Clarke 1880 ellipsoid differs in both shape (more oblate) and origin (offset by about 540 m) 136 from the WGS84 ellipsoid (Table 1, Figure 1). The Clarke 1880 ellipsoid surface is about 137 equivalent to sea level in the Lesser Antilles region and the British Ordnance Survey adopted it for 20<sup>th</sup> Century mapping work. Significant horizontal and vertical offsets can exist between 138 139 coordinates referenced to the Clarke 1880 ellipsoid versus the WGS84 ellipsoid. For example, a 140 point in Montserrat defined by geodetic coordinates (lat./ long.) on the Clarke 1880 ellipsoid 141 would be about 400 m northeast of the point with the same coordinates on the WGS84 ellipsoid. 142 The offset is due to the difference in ellipsoid shape and origin and the exact difference depends 143 on the three-dimensional position of the point in question. Furthermore, the vertical difference 144 between the two ellipsoids also varies spatially. In Montserrat, the offset is around 38 m 145 (WGS84 is higher); variations are illustrated in Figure 2. These examples highlight the 146 importance of explicit datum referencing to avoid position ambiguity or errors.

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### 148 2.3 Projections

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The common map projection employed for Montserrat is the TM projection. The TM method figuratively uses a cylinder, wrapped around the ellipsoid, with its central axis parallel to the ellipsoid's equatorial plane. The great circle at which the ellipsoid meets the cylinder is the 'central meridian' on the ellipsoid. The projection is then performed by 'unwrapping' the cylinder from the ellipsoid, translating features on the ellipsoid onto a 2D plane (see illustrations by Robinson *et al.*, 1995). Distortion caused by this type of projection is minimised along the

156 chosen central meridian and it is therefore ideal to select a central meridian close to the region of

- 157 interest. Northing and Easting coordinates may then be measured, in units of length, eastward
- 158 from the central meridian and northward from the equatorial plane, respectively. Often, an

arbitrary offset is applied to the Easting coordinate so that positions west of the central meridian

160 do not have negative values. TM projections can thus be readily tailored to specific cartographic

161 requirements, as desired, and can be applied to any ellipsoid. The BWI grid is an example of a

162 TM projection used for mapping parts of the West Indies region (e.g. DOS, 1983), typically in

163 conjunction with the Clarke 1880 ellipsoid (Table 2).

164 The UTM system is a series of standardised TM projections that cover the globe in a series of

165 sixty numbered 'zones'; each zone has its own central meridian, spaced six degrees of longitude

166 from the next zone. Any position in the world can be identified by values of Easting, Northing

167 and UTM Zone number, and whether the point is in the northern or southern hemisphere.

168 Subdivision of latitudinal zones in the UTM system (denoted by letters) is somewhat redundant

as long as the hemisphere is specified. The UTM system uses the WGS84 ellipsoid (Table 2).

170 Montserrat falls within UTM Zone 20Q (also 20-North or 20N – the latter raising ambiguity with

171 latitude Zone N).

It is notable that the choice of TM projection does not inherently define the vertical reference
surface (ellipsoid or geoid) against which elevation is measured. However, two common pairings
have generally been used on Montserrat: the Clarke 1880 ellipsoid with BWI TM grid *or* the
WGS84 ellipsoid with UTM grid.

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177 2.4 Geoids & 'Sea Level'

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179 The Earth Gravitational Model 1996 (EGM96; NGA, 2012) is used as the reference geoid for the 180 WGS84. Earlier and more recent geoid models exist, with varying sophistication and accuracy. 181 The WGS84 geoid provides a separate alternative as a standard vertical reference surface with 182 the attraction that it is, by definition, close to the average ocean surface level. Figure 2 shows the 183 vertical offset of the WGS84 EGM96 geoid from the WGS84 ellipsoid around Montserrat. The 184 geoid has not generally been used as a vertical reference for Montserrat geographic data owing 185 partly to the additional complexity of computing or interpolating geoid offsets (e.g. Figure 2). 186 However, it is necessary to recognise that multiple vertical datums exist in the WGS84. Heights

referenced to the geoid (EGM96) are often used for larger-scale mapping and/or spaceborne

- 188 surveying such as the Shuttle Radar Topography Mission (SRTM) global topography model.
- 189 A third convention for measuring topographic height is mean sea level. Sea level can be

190 measured using one or more tide gauges in the area of interested. Commonly, however, heights

191 given 'above sea level' (asl) refer directly to the geoid height (NIMA, 2000). This introduces

ambiguity in the use of the term 'sea level'. There are currently no reference tide gauge sea level

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## 195 2.5 Maps of Montserrat

measurements on Montserrat.

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197 The most widely available published map of Montserrat (DOS, 1983) is referenced to the Clarke 198 1880 ellipsoid and has coordinates expressed in the BWI TM grid (Easting and Northing, in 199 metres, height in feet) and in geodetic coordinates (latitude and longitude, in degrees and 200 minutes). DEMs derived from this map (described later), along with various archived 201 georeferenced data from Montserrat, use the same system. Since about 2009, MVO have adopted 202 the WGS84 ellipsoid as a reference and use the UTM grid (Zone 20Q, Easting and Northing in 203 metres, ellipsoidal height also in metres). Datum parameters (given in Table 2) may be used to 204 correctly configure instruments, such as handheld GPS receivers, and software appropriately. 205

# 206 **3. Converting Between Coordinate Systems**

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208 It is often desirable or necessary to convert geospatial data from one coordinate system to 209 another. For example, quantitative analyses might be performed using ECEF coordinates and 210 then converted to geographic coordinates for visualisation. Conversion formulae are derived 211 from the geometrical form of each reference system, and are described widely in the literature. 212 There also exist numerous programs and web-based tools for performing coordinate 213 transformations. The software tools named here do not represent an exhaustive list of available 214 options but are given as a starting point. A comprehensive database of reference systems is 215 maintained online by Butler et al. (2012). 216 The ArcGIS software package (ESRI, Redlands, California) and open source equivalents (e.g.

217 QGIS; www.qgis.org) are popular and powerful interfaces for handling and manipulating

218 geospatial data. Such data may be explicitly assigned to a map datum and the software is

219	generally capable of relating or converting data between multiple coordinate systems. ArcGIS				
220	and many similar programs use the Geospatial Data Abstraction Library (GDAL, 2012) to				
221	perform datum translations. GDAL may be freely downloaded and used as a standalone, multi-				
222	platform program. Programs such as GDAL and proj (Evenden, 2003) perform command-line				
223	and batch-mode conversion that allows straightforward incorporation into other programs and				
224	scripts. Coordinate systems are often indexed using a unique European Petroleum Survey Group				
225	(EPSG) code, as listed by Butler et al. (2012) and in Table 2. The following example command				
226	uses the 'cs2cs' command in proj to convert a position on Montserrat (near the volcanic vent)				
227	from Clarke 1880 BWI TM to WGS84 UTM 20Q coordinates:				
228	Input:				
229	cs2cs +init=epsg:2004 +to +init=epsg:32620				
230	380915 1847084 700				
231	Output:				
232	587842.27 1847829.34 661.98				
233	In this example, EPSG codes (Table 2) are used as shorthand for the two map datums. Datum				
234	parameters and other details (such as output precision) can be specified explicitly and input				
235	values can be typed (as in this example) or given as an input file. Extensive documentation is				
236	available for these and other conversion programs and the reader is directed there for further				
237	information.				
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239	4. Digital Maps of Montserrat				
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241	Digital Elevation Models (DEMs) are grids, rasters or point files containing topographic height				
242	information. They are an extremely useful resource for many geospatial applications. In the				
243	context of Montserrat, DEMs have been essential for measuring topographic changes during the				
244	Soufrière Hills Volcano (SHV) eruption as well as for providing constraint on numerical models				
245	of eruptive processes. The following descriptions briefly document the origin of large scale				
246	Montserrat DEMs that have been widely used by the volcanology community.				
247	The British Ordnance Survey's Directorate of Overseas Surveys (DOS) used photogrammetric				
248	survey data – collected in the mid 20 <sup>th</sup> Century – to generate a series of published topographic				
249	maps. In 1986 G.Wadge manually digitised the latest edition (DOS, 1983) from original DOS				
250	acetate contour sheets. DEM accuracy is affected by error in photogrammetric topography				

- retrieval exacerbated by dense vegetation on the island and digitisation error. The latter was
  estimated at about 1/3 of the 50-foot contour interval (G. Wadge, pers. commun.). The resulting
  '1995', or 'pre-eruption', DEM (at 10 m grid intervals, available at www.nerc-essc.ac.uk/~gw)
- has since been used extensively by the research community. The original DEM was generated
- using the Clarke 1880 ellipsoid and BWI TM grid.
- 256 The accumulation of erupted volcanic material since 1995 has resulted in major changes in the 257 island's topography and coastline. Various surveying work has been conducted throughout the 258 eruption to measure and record these changes at different spatial and temporal scales (e.g. Jones, 259 2006; Wadge et al., 2008). An airborne LiDAR survey was commissioned by MVO in 2010 and 260 yielded the most extensive and detailed topographic survey recorded since the start of the 261 eruption. The survey was conducted using a helicopter-mounted scanner with on-board high-rate 262 GPS tracking which was later processed using ground control GPS data supplied by MVO. The 263 survey covered most of the island to the south of the Centre Hills, except for regions above about 264 750 m (asl), which could not be surveyed due to low cloud cover. The 2010 DEM has 1-metre 265 grid intervals and we estimate an RMS point error of 0.17 m from independent GPS 266 measurements. The original DEM data used WGS84 UTM 20Q coordinates with heights 267 referenced to the WGS84 (EGM96) geoid, later converted to ellipsoid height values. 268 Space-borne topographic surveying provides an attractive alternative to airborne and ground-269 based surveying methods, providing wide, contemporaneous. Generating of DEMs using satellite 270 radar interferometry can be impeded by degradation of active volcanic terrain – a problem that 271 will be reduced in data from recent, high-repeat rate satellite missions (e.g. Ferrucci & Tait, 272 2011). DEM data from such endeavours are typically adjusted to fit existing topographic data 273 (e.g. SRTM) and thus adopt the cartographic conventions of the original DEM. Georeferenced 274 satellite topography and imagery data (e.g. radar intensity images, Wadge *et al.*, 2011) 275 commonly use the WGS84 UTM systems, with either geoid or ellipsoid vertical reference. 276 Bathymetric data around Montserrat have been compiled and updated in a similar fashion: original data were derived from 1:50000 scale British Admiralty sea charts based on 19th and 20th 277 278 Century surveys. Numerous additional surveys conducted since 1998 have been used to map 279 bathymetric changes around Montserrat, particularly the evolution of submarine deposits 280 offshore from the Tar River Valley (due east from SHV). Le Friant et al. (2004; 2010) 281 documented the details of various bathymetric surveys. An estimate of near-shore bathymetry –

- usually inaccessible to large survey ships was given by Wadge *et al.* (2010). The map in
  Figure 2 shows a current DEM, combining data from recent surveys.
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#### 285 **5. Magnetic Declination**

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287 Magnetic declination (the difference in angle between magnetic and true north) changes in space 288 and time. It is important to account properly for declination in work that requires the use of a 289 magnetic compass (e.g. surveying, wind vane installation, etc.). In Montserrat, a correction of 290 about 14°W is required, and this has changed at an average (not constant) rate of about 3'W/yr 291 during the course of the eruption. Figure 3 shows the variation of magnetic declination on 292 Montserrat since 1995, estimated using the International Geomagnetic Reference Field (IGRF-293 11; Finlay et al., 2010). Magnetic inclination (dip of the magnetic field from horizontal) is 294 usually not as critical for standard surveying purposes; on Montserrat, magnetic inclination dips 295 at about  $40^{\circ}$  and changes by about  $0.2^{\circ}/\text{yr}$  (becoming shallower). Alternative magnetic field 296 models and further information are available from NOAA (2012).

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### 298 **6. Summary**

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This note is intended as a brief introduction, to highlight and document geodetic practices as they have been used in geoscience on Montserrat. We have included a rudimentary description of the fundamental geodetic tools used for handling and manipulating geospatial data and highlight the importance of understanding the influence of their use and mis-use. We have also indicated the conventions that have been used most commonly by researchers during the course of the eruption on Montserrat.

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**Table 1.** Parameters for two ellipsoids commonly used on Montserrat (from Butler *et al.*, 2012).

Name	Offset (to WGS84)			Equatorial	Inverse flattening
	dX (m)	dY (m)	dZ (m)	radius, a (m)	ratio, <i>1/f</i>
WGS 1984	-	-	-	6378137.000	298.257223563
Clarke 1880	174	359	365	6378249.145	293.465000000

Table 2. Parameters that define the two TM projections most commonly used for Montserrat
 geographic data (from Butler *et al.*, 2012).

Parameter	BWI grid	UTM Zone 20N (= Zone 20Q)
Ellipsoid	Clarke 1880	WGS 1984
Projection	Transverse Mercator	Transverse Mercator
Central Latitude	0°	0°
Central Meridian	62° West	63° West
False Easting (m)	400000	500000
False Northing (m)	0	0
Scale Factor	0.9995	0.9996
EPSG Code	2004	32620

# 391 Figure Captions

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**Figure 1.** Cartoon illustration of typical geodetic ellipsoids. The WGS84 ellipsoid (black) has its origin at the Earth's centre of mass (black dot). The rotational pole, *Z*, and the prime meridian, *X*,

395 are defined by the IERS reference pole and meridian (IRM), respectively, as described in the

396 text. The equatorial and polar radii define the flatness of the ellipsoid. Ellipsoids are

397 conventionally defined by parameters relative to the WGS84 frame. Here, the Clarke 1880

398 ellipsoid (red) has an origin that is offset in each of the X, Y and Z dimensions (red dot), as

defined in Table 1. The radius and flattening of the ellipsoids also differ. The flattening and

400 offset in this figure is exaggerated for illustrative purposes. The WGS84 *X*, *Y* and *Z* axes also

401 form the orthogonal Earth-Centred Earth-Fixed coordinate axes.

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403 **Figure 2.** Map of Montserrat and surrounding bathymetry (grey contours with 100 m intervals;

404 see text for description of DEM). Vertical offsets from the WGS84 ellipsoid are shown for the

405 Clarke 1880 ellipsoid surface (blue contours, 50 cm intervals) and the WGS84 (EGM96) geoid

406 (red contours, 5 cm intervals). The complexity in the geoid model derives from local and

407 regional heterogeneities of mass distribution in the Earth. All height contours are measured in

408 metres from the WGS84 ellipsoid surface (negative values are below the ellipsoid). The coastline 409 of Montserrat is thus shown by a contour at -40 m, rather than at 0, because of the ellipsoid-geoid

of Montserrat is thus shown by a contour at -40 m, rather than at 0, because of the ellipsoid-geoid
 vertical offset. Horizontal coordinates are given as metres in Easting and Northing using the

411 WGS84 UTM Zone 20Q datum (see Table 2).

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413 **Figure 3** Magnetic declination at 16°42'N 62°11'W (southwest flank of SHV) between 1995 and

414 2015, according to the IGRF-11 model. These corrections may be used to calibrate field

415 compasses or adjust uncorrected azimuth data.

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