



# Structures in gas–liquid churn flow in a large diameter vertical pipe



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## ARTICLE INFO

### Article history:

Received 22 June 2015

Revised 12 September 2015

Accepted 12 September 2015

Available online 23 October 2015

### Keywords:

Gas–liquid flow

Wire Mesh Sensor

Conductance probes

Churn flow

Vertical pipe

## ABSTRACT

Gas–Liquid two phase co-current flow in a vertical riser with an internal diameter of 127 mm was investigated in the churn flow pattern. This paper presents detailed experimental data obtained using a Wire Mesh Sensor. It shows that the most obvious features of the flow are huge waves travelling on the liquid film. Wisps, large tendrils of liquid and the product of incomplete atomisation, which had previously detected in smaller diameter pipes, have also been found in the larger diameter pipe employed here. The output of the Wire Mesh Sensor has been used to determine the overall void fraction. When examined within a drift flux framework, it shows a distribution coefficient of  $\sim 1$ , in contrast to data for lower gas flow rates. Film thickness time series extracted from the Wire Mesh Sensor output have been examined and the trends of mean film thickness, that of the base film and the wave peaks are presented and discussed. The occurrence of wisps and their frequencies have been quantified.

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## Introduction

### Flow patterns in vertical pipes

Gas–liquid two-phase flow has many applications in the oil and gas, chemical and nuclear industries. When a two-phase mixture flows upwards in a vertical pipe, it is not possible to tell, a priori, how the phases are going to distribute themselves about the length and cross section of the pipe. Because of the infinite possibilities of distributions of the phases, researchers have tended to use flow patterns to describe the flows. These are broad descriptions of the flow. There is a consensus that the flow patterns for vertical flow are bubbly, slug, churn and annular. Some groups add other patterns such as wispy annular and dispersed bubble to this list. The identification of when each flow pattern occurs is difficult to determine. Direct observation through a transparent pipe section, particularly through a high speed camera, can allow visual and qualitative interpretation of the flow inside the pipe. However, this is very subjective, and in early projects such as by Bennett et al. (1965), researchers formed a consensus through anonymous voting. Visual observations are also problematic, because the flow at the pipe wall is often obscured by bubbles or waves on wall films, particularly at higher velocities, meaning that it is difficult to see what is happening deep inside the pipe through this approach alone. A more objective approach is to gather signals from instruments and then interpret those signals

quantitatively. What becomes obvious is that certain signatures are observed for particular types of flow, for example through the time series of void fraction and through the Probability Density Function (PDF). The PDF is a histogram of the occurrences of the different void fractions. This approach was used for example by Jones and Zuber (1975) and Costigan and Whalley (1997). For bubbly flow there is a single peak at low void fraction. Slug flow contains two peaks (1st peak–liquid slug, 2nd peak – large gas bubble). Churn flow occurs at void fractions above 0.5–0.6, and it has a single peak with a tail extending down to lower void fractions. Annular flow has a single narrow peak at high void fractions of usually greater than 0.8. Much of the published work to date concentrates on small diameter pipes from 10 to 50 mm. This is in contrast with the larger diameter pipes which are more common in industry (i.e.,  $\geq 75$  mm).

As noted above the early study of Bennett et al. (1965) gave a strong indication of difficulty of identifying which flow patterns were present at particular flow rates. Their experiments were on steam/water at 35 and 70 bar in a 12.7 mm pipe. They presented their results as plots of mass flux versus quality (steam mass fraction). Subsequently, Hewitt and Roberts (1969), who carried out experiments with air/water in a 32 mm diameter pipe at 3 bar, showed that if plotted as the momentum fluxes (the product of density,  $\rho_i$ , times superficial velocity,  $u_{is}$ , squared, with  $i = G$  for the gas and  $= L$  for the liquid) for the two phases their own data and those of Bennett et al. (1965) showed that the different flow patterns were found grouped in particular parts of the plot. Two questions arise from this: why do the different data sets agree and why are dimensional groups being employed rather than the usual dimensionless ones? The answer to the first question is that the momentum flux (or inertia force) is one

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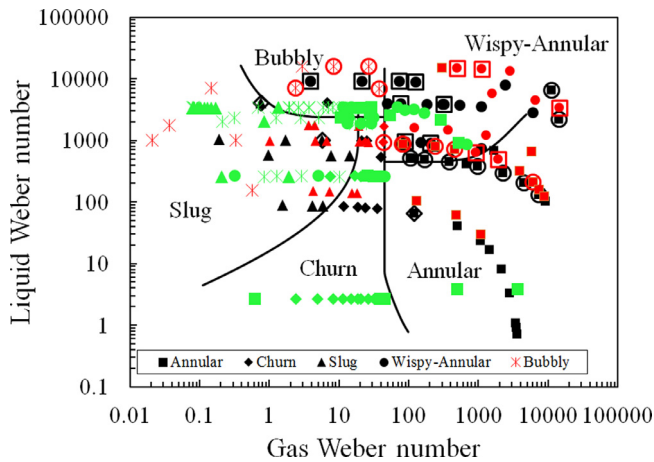
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**Table 1**

Ratio of pipe diameter to surface tension for experiments of [Bennett et al. \(1965\)](#) and [Hewitt and Roberts \(1969\)](#).

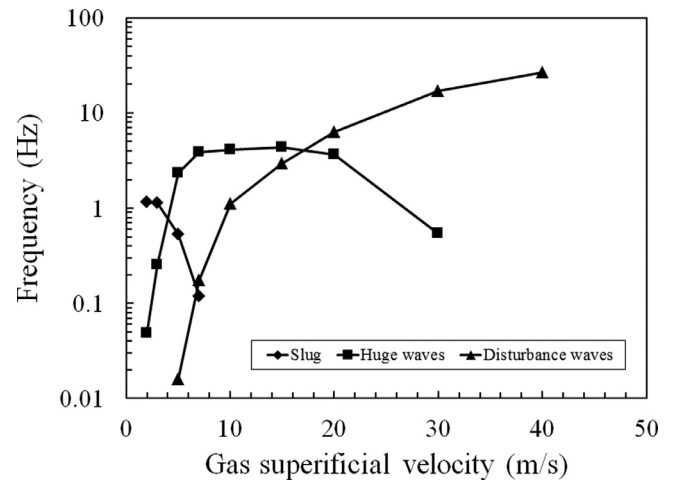
Fluids	Pressure (bar)	Pipe diameter (mm)	Pipe diameter/surface tension (kg/ms <sup>2</sup> )
Steam/water	35	12.7	0.45
Steam/water	70	12.7	0.72
Air/water	3	32	0.44



**Fig. 1.** Plot of liquid Weber number versus gas Weber number showing experimental flow pattern data of [Bennett et al. \(1965\)](#) (Steam/water – 12.7 mm diameter pipes – pressure 35 bar (Black symbols) and 70 bar (Red symbols)) and [Hewitt and Roberts \(1969\)](#) (Green symbols – air/water, 32 mm diameter pipe – pressure 4 bar) and transition lines adapted from [Hewitt and Roberts \(1969\)](#).

of the most important forces in determining flow pattern. The answer to why these dimensional plots work so well is probably due to the ratio of pipe diameter,  $D$ , to surface tension,  $\sigma$ , for the three different conditions studied. These are listed in [Table 1](#) where it can be seen that two of the values are almost identical and the third is close. This could explain the agreement between the different data sets. It points to a way of obtaining non-dimensional plots. If the momentum fluxes are multiplied by pipe diameter and divided by surface tension, the graph would be the same but with stretched axes. The combinations ( $\rho_i u_i^2 D / \sigma$ , where  $i$  is either gas or liquid) are Weber numbers, the ratio of inertial to surface tension forces. In much of gas/liquid flow with low viscosity liquids these are the most important forces. For example, in one of the most important phenomena which occurs in annular flows, the atomisation of drops from the wall film, it is a Weber number which controls the size and probably the flux of drops produced. In slug flow, the production of small bubbles from the tail of the large bubbles is similarly the balance of inertial and surface tension forces. The data from [Bennett et al. \(1965\)](#) and from [Hewitt and Roberts \(1969\)](#) have been replotted in terms of liquid and gas Weber numbers in [Fig. 1](#). Here the 35 bar steam–water data are plotted in black, the 70 bar steam–water data in red and the 3 bar air–water data in green. Where there was more than one flow pattern selected in the voting process, symbols for both patterns are plotted. There is some, but not strong, agreement with the boundaries between flow patterns suggested by [Hewitt and Roberts \(1969\)](#). This approach is for lower viscosity liquids. Obviously, a further refinement is required for more viscous liquids.

The fact that multiple flow patterns were selected for the same conditions might be taken as an indication of the difficulty of identifying the features of the flow from photographs taken through the transparent pipe wall but also through a wavy film on the wall or a layer of bubbles at the wall. However, it might also be evidence that the flow pattern transitions are not sharp but there is a gradual shift from the characteristics of one flow pattern to those of another with

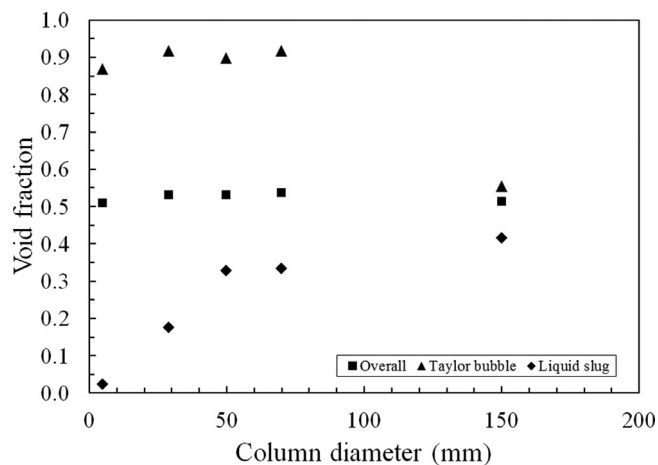


**Fig. 2.** Frequencies of slugs/huge waves/disturbance waves reported by [Sekoguchi and Mori \(1997\)](#). Pipe diameter = 25.8 mm, pressure = 2 bar, liquid superficial velocity = 0.4 m/s.

characteristics of both occurring simultaneously under some conditions. Further evidence of this gradual transition comes from the work of [Sekoguchi and Mori \(1997\)](#) who interrogated the gas–liquid flows using multiple probes, either axially or about a cross-section of the pipe. From the time resolved signals of all these probes they were able to identify individual examples of the structures which characterise each flow pattern. They found that more than one type of structure can occur at combinations of gas and liquid flow rates. [Fig. 2](#) illustrates the frequencies of the periodic structures that they obtained. The frequencies fall and rise systematically with increasing gas superficial velocity with regions where more than one structure is present. A similar plot, but for the lower superficial of 0.1 m/s was presented by [Hernandez Perez et al. \(2010\)](#).

#### Characteristics of individual flow patterns

Of the four major flow patterns, there is some consensus about the major mechanisms occurring in bubbly, slug and annular flows. *Bubbly* flow is recognised as consisting of bubbles dispersed in a liquid continuum. Recent work has noted the occurrence of waves of void fraction travelling up the pipe. [Taitel et al. \(1980\)](#) proposed that the transition to slug flow is based on the coalescence of bubble to form larger ones which eventually occupy the majority of the pipe cross-section and so become slug flow. The void fraction waves enhance the local bubble concentration at regular places along the pipe and encourage this coalescence process. It also explains why slugs occur regularly rather than randomly. *Slug* flow consists of alternate large, bullet-shaped bubbles (often called *Demitrescu* or Taylor bubbles) and liquid slugs containing small bubbles. There is creation of small bubbles from the tail of the Taylor bubbles with some of the newly created bubbles re-coalescing with the Taylor bubble whilst others passed deeper into the liquid slug. Models for slug flow have been proposed by [Fernandes et al. \(1983\)](#), [Sylvester \(1987\)](#), [deCachard and Delhaye \(1996\)](#) and [Brauner and Ullmann \(2004\)](#). Taylor bubbles have an obvious bullet shape separated by packets of liquid in smaller diameter pipes. Their velocities have a linear dependence on the mixture velocity (the sum of the superficial velocities of the gas and liquid) with a non-zero intercept,  $u_{ds}$ , which can be described by the rise velocity of an isolated Taylor bubble [ $Fr \sqrt{(gD)}$ ] with  $g$  being the acceleration due to gravity. For the air–water combination at near atmospheric pressure,  $Fr = 0.35$ . For more viscous liquids, the equation proposed by [Viana et al. \(2003\)](#) has been found to be accurate for viscosities up to 360 Pa s. However, as the pipe diameter increases there is an increasing quantity of small bubbles in the liquid slugs and the shape of the Taylor bubble becomes more complex, losing its



**Fig. 3.** Effect of pipe diameter on void fraction in liquid slug and in Taylor bubble region. All cases are for air–water and are taken from the same overall average void fraction. From Omebere-Iyari (2006). Data from: Omebere-Iyari and Azzopardi (2007) – 5 mm; Cheng et al. (2002) – 29 mm; Kaji et al. (2009b) – 52 mm; Kaji (2008) – 70 mm; Cheng et al. (1998) – 150 mm.

clear bullet shape. Indeed, at diameters  $> 100$  mm, there does not appear to be any slug flow. A reason for this can be seen in Fig. 3 where data from air–water experiments for the void fraction in the liquid slug and that in the Taylor bubble region from different pipe diameters, but for the same mean void fraction, have been plotted. The void fraction in the liquid slug increases from  $\sim$  zero because increased entrainment of gas from the tail of the Taylor bubble as the pipe diameter increases. At smaller pipe diameters, the void fraction in the Taylor bubble region is approximately constant but beyond  $\sim 100$  mm it decreases due to bubbles passing through the slug and into the film surrounding the Taylor bubble making it knobby and different from the idealised bullet shape. At the larger pipe diameters there are still periodic structures whose velocities, obtained from cross-correlation of time series from two probes at different axial locations show the same trend with flow rates as noted above.

In *annular* flow, the liquid travels partially as a film on the channel walls with the rest being carried by the gas as entrained drops. The drops are created from waves of the film interface and after transportation by the gas redeposit onto the film either ballistically, due to the momentum they obtained on creation, or by a diffusion-like process due to the turbulence in the gas. The fraction of liquid depositing by either one of these mechanisms can vary between 0 and 1.

There have been a number of mechanisms proposed for the transition from slug to churn flow as the gas flow is increased. Nicklin and Davidson (1962) identified that the difference between the downwards velocity of the falling film surrounding the Taylor bubble and the upwards velocity of the gas in the bubble could arrive at the conditions of flooding, i.e., the instability when the liquid is stopped or even forced upwards. This has been taken up by others; McQuillan and Whalley (1985) followed this suggestion and produced a transition criterion. The approach was modified by Jayanti and Hewitt (1992) who argued that, since there is a significant effect of film length on the flooding point in counter-current flow, the length of the Taylor bubbles should be taken into account. They used their own correlation to include this effect. Watson and Hewitt (1999) have compared the predictions of the correlations of Mishima and Ishii (1984), McQuillan and Whalley (1985), Brauner and Barnea (1986) and Jayanti and Hewitt (1992) with some extensive air/water data at 1.2, 3 and 5 bar in a 32 mm pipe. They found that only the equation of Jayanti and Hewitt (1992) predicts the correct trend. Support for the importance of flooding in the slug/churn transition has been provided by Kaji et al. (2009a). They measured void fraction time series from several, closely-spaced conductance probes. By selecting that data

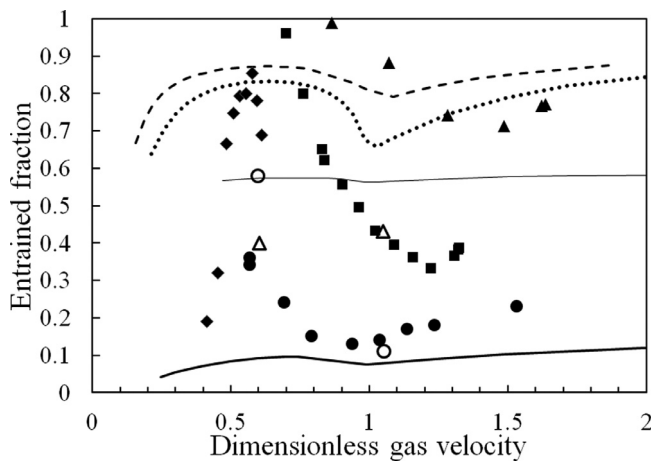
from the Taylor bubble sections and employing a cross-correlational analysis, they identified that there were waves with both upwards and downwards velocities present for a set of flow conditions, an occurrence that would be expected around flooding. Taitel et al. (1980) consider that churn flow is an entry effect associated with plug flow and have produced a model including a length effect. This approach implies that for infinitely long pipes only bubble, slug and annular flow should occur and thus a direct transition mechanism between plug and annular flows is required. However, in slug flow the film can be flowing downwards whilst in annular flow it flows upward, so an intermediate state might be expected between the film downflow and upflow, particularly from the evidence provided by flooding experiments. For this reason the Taitel et al.'s approach is not considered to be appropriate. Mishima and Ishii (1984) postulated that the transition between slug and churn flow results from a void fraction limitation. They calculated the mean void fraction over the length of a gas slug by a potential flow analysis and the mean void fraction over the total slug unit from a drift flux analysis. The transition was defined as the condition at which the void fractions were equal. Though their transitions showed good agreement with experiment it is not considered reliable because: (i) there is an apparently incorrect application of Bernoulli's equation; and (ii) they assumed that the plug length is determined when the film thickness reaches that calculated for a falling laminar film and that the length of the liquid slug is approximately zero. Both these are unreasonable assumptions and this approach is not considered suitable. Brauner and Barnea (1986) also used a limiting void fraction approach, and proposed that slug flow would change to churn flow when the void fraction in the liquid slugs between the Taylor bubbles became equal to the maximum packing void fraction for a cubic lattice of equal sized spherical bubbles (defined above as  $\varepsilon_g = 0.52$ ). Thus the transition line can be obtained replacing  $\varepsilon_g = u_{GS}/(u_{GS} + u_{LS}) = 0.52$ . Dukler and Taitel (1977) suggested that the transition might be caused by the length of the liquid slug separating two Taylor bubbles becoming too short and the wake behind the Taylor bubble breaking up the liquid slug. The findings of Pinto et al. (1998) give support to this concept. They reported that the second of two Taylor bubbles would accelerate into the tail of the first if liquid slug between them was less than 5 pipe diameters long.

### Churn flow

There is also a lack of agreement as to what constitutes churn flow. It is fairly certainly a gas continuous flow. There is growing agreement that there are huge waves present and some of the liquid is carried as drops. Sekoguchi and Mori (1997) and Sawai et al. (2004) using measurements from their multiple probes (92 over an axial length of 2.325 m) obtained time/axial position/void fraction information. From this they were able to identify huge wave from amongst disturbance waves and slugs. They classified individual structures as huge waves from their size together with the fact that their velocities depended significantly on the corresponding axial length. This was in contrast to disturbance waves where the velocity of individual waves only increased slightly with the axial extent of these waves. They also found that the frequency of huge waves first increased and then decrease with increasing gas superficial velocity. Similarly, their velocities were found to deviate from the line for slug flow velocities and pass through a maximum and then a minimum.

In churn flow part of the liquid could travel as entrained drops. In annular flow the fraction of entrained liquid will increase as the gas superficial velocity and pipe diameter, Azzopardi (2006). The position is less clear for churn flow. The measurement techniques which are suitable to determine entrained fraction for annular flow have limitations when applied in churn flow because they might not be able to distinguish between liquid carried as drops and that transported in huge waves. For example Barbosa et al. (2002) employed sampling probes at the pipe centre line and at 9.6 mm from the wall.





**Fig. 4.** Measured values of entrained fraction covering the churn and annular flow patterns. • Verbeek et al. (1992), pipe diameter = 50 mm, liquid superficial velocity = 0.01 m/s; ○ Westende et al. (2007), pipe diameter = 50 mm, liquid superficial velocity = 0.01 m/s; △ Westende et al. (2007), pipe diameter = 50 mm, liquid superficial velocity = 0.04 m/s; ■ Verbeek et al. (1992), pipe diameter = 100 mm, liquid superficial velocity = 0.01 m/s; ▲ Verbeek et al. (1993), pipe diameter = 100 mm, liquid superficial velocity = 0.05 m/s; ♦ van der Meulen (2012), pipe diameter = 127 mm, liquid superficial velocity = 0.04 m/s. Modelling — pipe diameter = 50 mm, liquid superficial velocity = 0.01 m/s; — pipe diameter = 100 mm, liquid superficial velocity = 0.01 m/s; ..... pipe diameter = 100 mm, liquid superficial velocity = 0.05 m/s; — pipe diameter = 127 mm, liquid superficial velocity = 0.04 m/s.

The diameter of the sampling probe facing upstream into the flow was 6.35 mm which means that waves higher than 6.4 mm would be sampled. Wang et al. (2013b) have shown evidence of wave heights much greater than this value. If porous wall film removal devices are employed, it is noted that the momentum of the liquid in the huge waves could carry them past the device and that liquid would not be sucked off so giving an over large value of entrained fraction. Another possible technique is to utilise Phase Doppler Anemometry which uses the scattering of laser light to obtain information on the velocity, size and number flux of drops. The technique breaks down at higher drop concentrations as the plethora of drops can obscure the laser beams invalidating the measurements. These problems are less at very low liquid flow rates. Such data can be examined to give indication of trends. Examples of such data are presented in Fig. 4 where the entrained fraction is plotted against a dimensionless gas velocity defined as  $u_{Gs} \sqrt{\rho_G / [(\rho_L - \rho_G)gD]}$ . The data come from the work of Verbeek et al. (1992, 1993), who used a porous wall film take of approach on 50 and 100 mm diameter pipes at a liquid superficial velocities of 0.01 and 0.05 m/s, Westende et al. (2007), who used Phase Doppler Anemometry on a 50 mm diameter pipe at liquid superficial velocities of 0.01–0.04 m/s, and van der Meulen (2012) who employed the same technique on a 127 mm diameter pipe with liquid superficial velocities  $\leq 0.04$  m/s. The data are plotted against dimensionless gas velocity, a form of Froude number as in churn flow the important forces are inertia and gravity. It is recognised that the surface tension force can also be important. However, the data considered here are all for air–water and so surface tension is essentially a constant. It can be seen that in the churn flow region the entrained fraction increases as the gas superficial velocity decreases. The position at which this increase takes place commences at higher gas velocities the larger the pipe diameter. Also shown in the figure are the predictions from the model of Ahmad et al. (2010). This is an empirical correction for churn flow to the model developed by Hewitt and Govan (1990) for annular flow. That employs equations for the rates of entrainment and deposition which are assumed equal to each other at equilibrium. The combined equation is then solved for entrained fraction. The correction proposed by Ahmad et al. assumes that churn flow occurs for  $u_g^* < 1$ , has the form  $9.73 - 8.73u_g^*$  and is applied to the expression for entrainment rate. It is seen that though it gives the

rise shown by the experimental data in churn flow, the exact values are not well predicted.

Models of the waves in churn flow have been published by Barbosa et al. (2001), Da Riva and del Col (2009) and Wang et al. (2012, 2013a, 2013b). They focused on the entry point of liquid through a porous wall section and modelling the growth of waves.

Under some conditions, churn flow exhibits flow reversals in the liquid layer near the wall. This was visualised by Hewitt et al. (1985) by using refractive index matching between the tube wall and the fluid to minimise optical distortion. A photochromic dye was dissolved in the liquid phase which could be activated using a pulsed laser beam to give a line in the liquid. In contrast to annular flow where the line was always distorted upwards, in churn flow it was seen that the line was distorted downwards in the film between waves and upwards when a wave passed up the pipe. Support for this observation has come from the work of Zangana and Azzopardi (2012) who made measurements of wall shear stress using a film mounted hot film probe whilst simultaneously measuring the film temperature upstream and downstream of the probe with flush mounted resistance thermometers. They found that in churn flow shear stresses that were both positive and negative were present indicating reversal of flow.

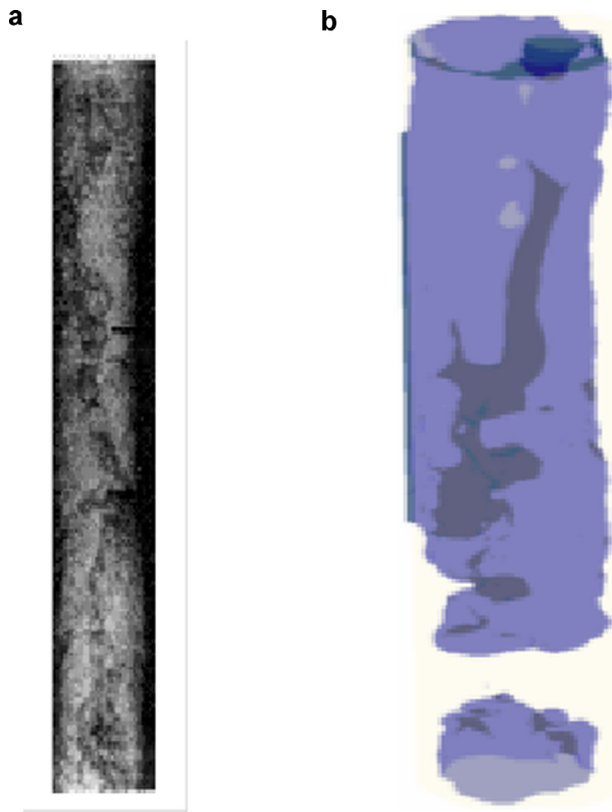
#### Wispy-annular flow

Another flow pattern that is identified by some researchers is wispy-annular flow. It was first reported by Bennett et al. (1965) who noted that if the liquid flow rate is increased in annular flow, large liquid objects may be observed within the gas core. These have been termed ‘wisps’. This has been classified as a separate flow pattern by Hewitt and Roberts (1969). It is noted that observation or photography through the transparent pipe wall to capture those structures that occur in the centre of the pipe can be made difficult by the liquid film on the pipe wall which at the flow rates of interest can have a wavy interface and contain bubbles and so obscure the view. X-ray photography experiments were more successful. An example of such a photograph is shown in Fig. 5(a). Prasser et al. (2002) who employed a Wire Mesh Sensor reported similar structures occurring in a 51 mm diameter pipe at liquid and gas superficial velocities of 1 m/s and 10 m/s respectively. From the output of a Wire Mesh Sensor, Hernandez Perez et al. (2010) recently reported the existence of similar structures in a vertical air–water flows in a 67 mm diameter pipe at atmospheric pressure, Fig. 5(b). They studied a mixture air and water and the flow rates corresponding to this image were liquid and gas superficial velocities of 0.25 m/s and 5.7 m/s respectively.

Sekoguchi and Mori (1997) applied a probe consisting of 257 needles facing upstream in a 26 mm diameter vertical pipe. An electrical current was applied between each needle and the pipe wall and the outputs were used to determine the distribution of the phases about the pipe cross-section resolved in time at a frequency of 400 Hz. An example of their results is reproduced in Fig. 6 and shows elements protruding into the gas core which can be identified as wisps.

Hawkes et al. (2000) used optical detectors to study the pulsations in the flow. They found two peaks in the power spectral density of the signal fluctuations. These were attributed to disturbance waves and wisps. Confirmation of this was obtained when they repeated the measurements after removing the wall film through a section of porous wall and only the peak corresponding to the wisps was observed.

Hawkes et al. (2001) have suggested that the wisps arise from agglomeration of the drops that are present in large concentrations within the gas core. However, it is noted that to form the wisp illustrated in Fig. 5b would require the agglomeration of 6000 drops of a diameter of 1 mm or 6,000,000 of a diameter of 100  $\mu\text{m}$ . Though there can be large number of drops present in annular flows, it seems unlikely that the very large numbers identified above would



**Fig. 5.** Wisps: (a) Hewitt and Roberts (1969), x-ray photography. Pipe diameter = 32 mm, gas superficial velocity = 3.1 m/s, liquid superficial velocity = 2.8 m/s; (b) Hernandez-Perez et al. (2010), Wire Mesh Sensor. Pipe diameter = 67 mm, gas superficial velocity = 5.7 m/s, liquid superficial velocity = 0.25 m/s.

be present and gives support to the source of wisps being incomplete atomisation, i.e., they are ligaments drawn out from waves on the film interface.

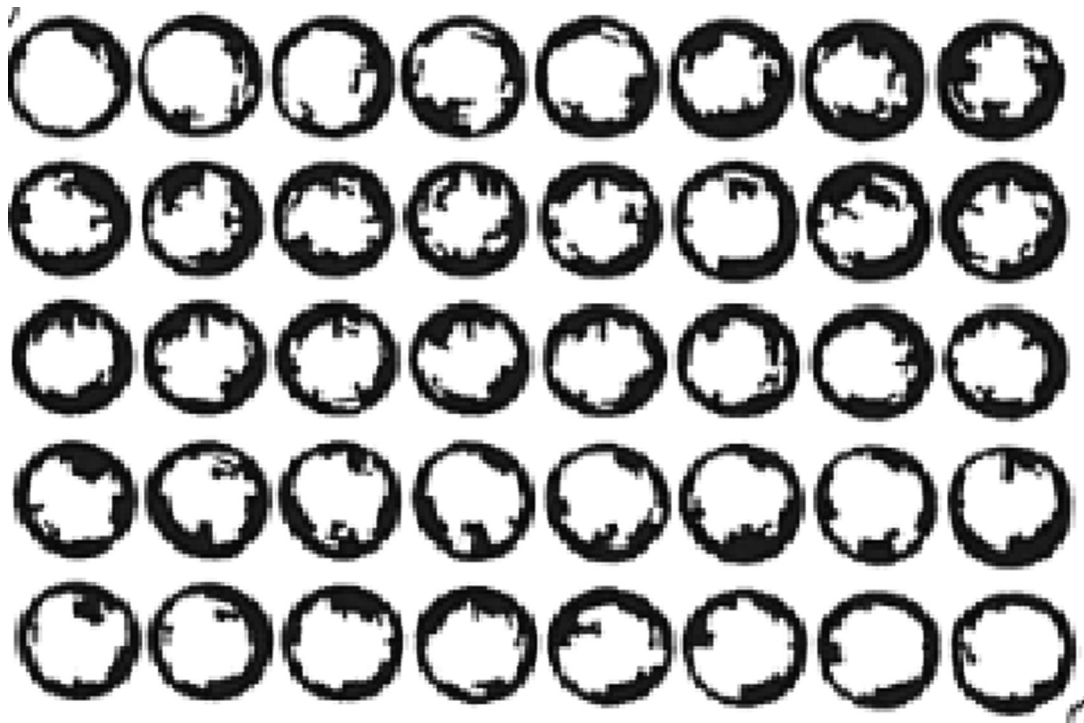
The number of publications on churn flow has increased recently. Apart of the modelling papers of Barbosa et al. (2001), Da Riva and del Col (2009) and Wang et al. (2012, 2013a, 2013b), those by Hernandez Perez et al. (2010), Szalinski et al. (2010) and Parsi et al. (2015a, 2015b) report on the application of Wire Mesh Sensors to air/liquid flows in 67 or 76 mm diameter vertical pipe. All used air as the gas. Hernandez Perez et al. and Parsi et al. employed water as the liquid whilst Szalinski et al. used a silicone oil (liquid viscosity = 5 mPa s, surface tension = 0.02 N/m). Parsi et al. also studied aqueous CMC solutions with viscosities 10 and 40 times that of water. Their gas and liquid flow rates, in terms of superficial velocities, were in the ranges of 3 to 38 and 0.1 to 0.76 m/s respectively. They all reported the presence of huge waves. They used the output of Wire Mesh Sensors to provide qualitative and quantitative information about the flow. Waltrich et al. (2013) examined bubbly, slug, churn and annular flow in a 48 mm diameter riser. They utilised a pair of intrusive needle probes which extended from the wall towards the pipe centre. By measurement the resistance between them they obtained time series information about the void fraction in their pipe.

#### Structure of the paper

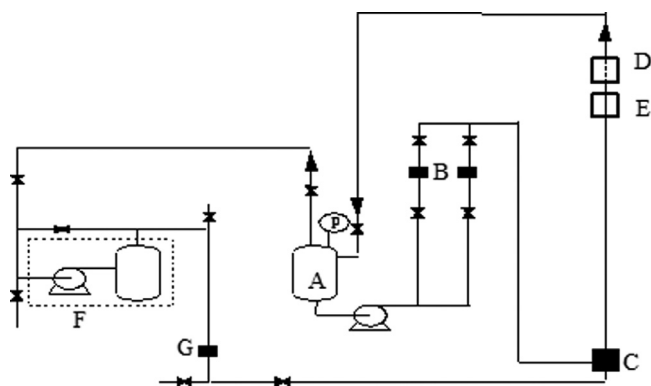
This paper reports on air/water churn flow in a large diameter vertical pipe employing Wire Mesh Sensors and other instrumentation. It presents the structures observed and then uses quantitative information on the flows examining it using:

1. a one dimensional approach;
2. a two and three dimensional approach.

In particular it identifies when wisps occur and on their frequencies of occurrence.



**Fig. 6.** Cross-sections of huge waves showing protrusions, i.e., wisps. Obtained by Sekoguchi and Mori (1997) using SS=CHOP probes, pipe diameter = 25.8 mm, gas superficial velocity = 5 m/s and liquid superficial velocity = 0.3 m/s.



**Fig. 7.** Experimental facility and instrumentation. A: liquid storage tank/separator; B: liquid flow meters; C: gas-liquid mixer; D: Wire mesh Sensor; E: conductance probes; F: compressor; G: gas flow meter.

## Experimental arrangements

### Experimental facility

The experiments conducted in the present study were carried out on a closed loop facility with a vertical riser (127 mm diameter pipe, 11 m tall). A schematic of the rig is given in Fig. 7. Air was provided by the pair of liquid ring pumps acting as the compressor (each with a 55 kW electric motor), it is metered a Küppers turbine flow meter (35–1030 m<sup>3</sup>/h) and fed into the bottom of the riser where it was mixed with water drawn from the combined liquid storage tank/phase separator and metered by one of a pair of Küppers turbine flow meters mounted in parallel (0.006–0.06 and 0.04–0.5 m<sup>3</sup>/min). The uncertainties associated with the flow meters were  $\pm 0.6\%$  for the gas and  $\pm 0.5\%$  for the liquid. The mixer was in the form of an annulus, the gas was introduced through a centre pipe whilst the liquid entered through the annulus. From the top of the riser the two-phase mixture was returned to the phase separator, the gas returning to the compressor. The system pressure was kept constant at 3 bar (abs) (gas density = 3.6 kg/m<sup>3</sup>). The superficial velocities studied were 3–16.5 m/s for the gas and 0.001–0.65 m/s for the liquid. The riser was provided with a Wire Mesh Sensor, placed at a height of 9.3 m from the mixer, and three conductance probes positioned 7.96, 8.06 and 8.32 m downstream of the mixer.

A large number of runs were carried out during which the Wire Mesh Sensor and the conductance probes were triggered simultaneously. A selection of runs was repeated to check for reproducibility. A good consistent accuracy demonstrated. Hewakandamby et al. (2014), using the facilities described here made measurements with the Wire Mesh Sensor positioned at 35.4 and 82.7 pipe diameters from the mixer with over a range of gas and liquid superficial velocities. Only at liquid superficial velocities below 0.03 m/s were there any significant differences between the mean void fractions obtained from the two stations implying that for higher liquid superficial velocities the flow was very close to being fully developed at the top station.

### Instrumentation

The Wire Mesh Sensor employed is based on the methodology of Prasser et al. (1998) and was designed and manufactured by Helmholtz-Zentrum Dresden-Rossendorf (HZDR). It has two orthogonal arrays of 32 very fine steel wires (0.1 mm diameter) stretched across parallel chords of the pipe cross-section. This gives a resolution of approximately  $4 \times 4$  mm<sup>2</sup>. The transmitting and receiving wires are separated by a small axial gap of 2 mm and measurements are taken at each crossing point of the wires. During the measuring cycle, one of the transmitter wires is activated successively while all the

others are kept at ground potential. All the receiver wires are sampled in parallel. The collected raw data are processed off line. Details are provided in Azzopardi et al. (2010).

The Wire Mesh Sensor instrumentation has been tested by making simultaneous measurements with it and with Electrical Capacitance Tomography by Azzopardi et al. (2010) and with  $\gamma$ -ray absorption by Sharaf et al. (2011). Good agreement between the instruments was achieved in both cases, usually within 2%. In the comparisons with Electrical Capacitance Tomography, excellent agreement was achieved between the two methods in both the overall (cross-section and time-averaged) void fraction and the time-varying time series of cross-sectionally averaged void fraction. Most recently, Zhang et al. (2013) have made simultaneous measurements using a Wire Mesh Sensor device placed 8 mm downstream of a plane at which an ultra-fast x-ray tomography system was operating. Radial profiles of time averaged gas fraction distributions show good agreement between both techniques.

The conductance probes consisted of two metallic rings (3 mm thick) separated by a 25 mm thick acrylic resin ring mounted flush with the wall of the test section. An A.C. voltage (20 kHz) was imposed across the two rings and the current passing was obtained and used to determine the resistance of the gas-liquid mixture and hence its void fraction. The current (determined from the voltage across a resistor mounted in series with the rings) exhibits a non-linear relationship with void fraction and so they require calibration. For Churn and Annular-type flows this is carried out by placing non-conductive cylinders inside the pipe and filling the annulus between the cylinder and pipe wall with the conductive liquid.

The conventional probe calibration approach usually assumes that the liquid film is totally liquid. In reality, in gas-liquid churn and annular-type flows, the continuous trapping and folding actions of the large waves at the interface transport gas bubbles into the liquid film. The presence of a considerable amount of bubbles in the liquid film was reported in both air-water horizontal and vertical annular-type flows by Jacowitz and Brodkey (1964), Hewitt et al. (1990) and Omebere-Iyari (2006). Rodriguez and Shedd (2004) quantified the bubble size distribution, bubble mean diameter and bubble number concentration in the wall film of a horizontal annular flow in a pipe of 15.1 mm diameter. They reported that bubbles had an exponential distribution of sizes with average diameters between 15% and 45% of the film thickness at gas superficial velocities ranging from 28 to 65 m/s and liquid superficial velocities from 0.019 to 0.14 m/s. Around 100 bubbles/cm<sup>2</sup> exist in the wall film at a gas superficial velocity 28 m/s.

To check the uncertainty introduced by the presence of bubbles, a new calibration approach was devised. In order to simulate gas bubbles in the liquid film during annular-type flows, spherical glass beads were used, inserted into the liquid layer between the pipe wall and the inserted cylinder. The effect of the beads (bubbles) could give an uncertainty in the film thickness of 20%. It is noted this is an upper limit when the gap is full of beads. However, the large uncertainty means that it might not be appropriate to use it for void fraction and film thickness measurements. However, huge waves are still seen in the Conductance Probe output, the time traces from two, axially-displaced of the instruments can be cross-correlated to provide a delay time from which wave velocities can be extracted.

## Results and discussion

The Wire Mesh Sensor outputs give time series of cross-sectionally resolved phase distribution. This can be used to provide visualisation of the time varying cross-sectional distribution of the phases as well as time sequences of phase variation across a narrow slice of the pipe. In addition, quantitative data can be obtained at a number of levels of detail. In this section, the information is presented on: (1) flow patterns and structures present; (2) mean (time



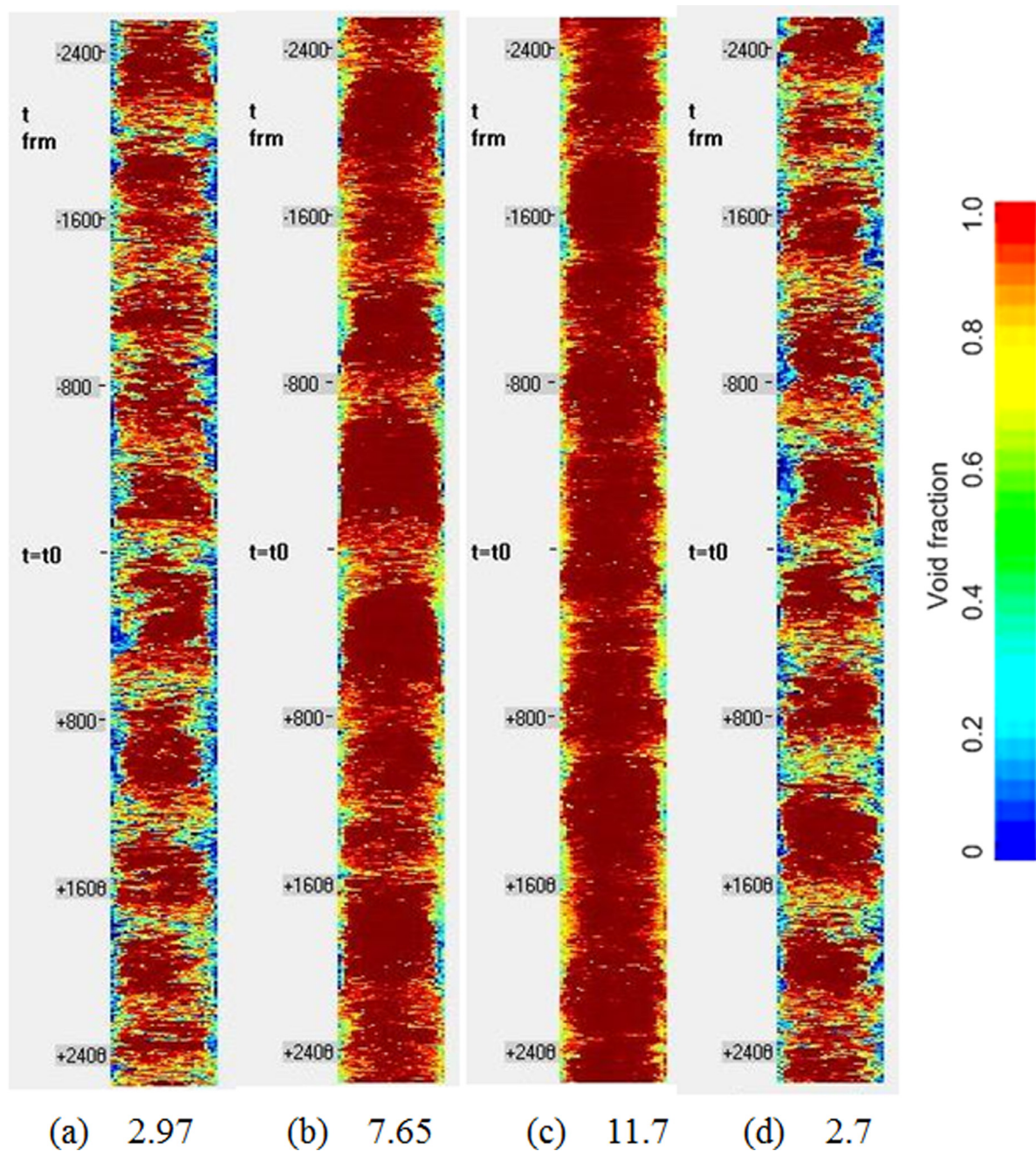


Fig. 8. Sectional view of flow in the pipe for different gas superficial velocities. (in m/s) Liquid superficial velocities are 0.66 m/s for (a) to (c) and 0.56 m/s for (d).

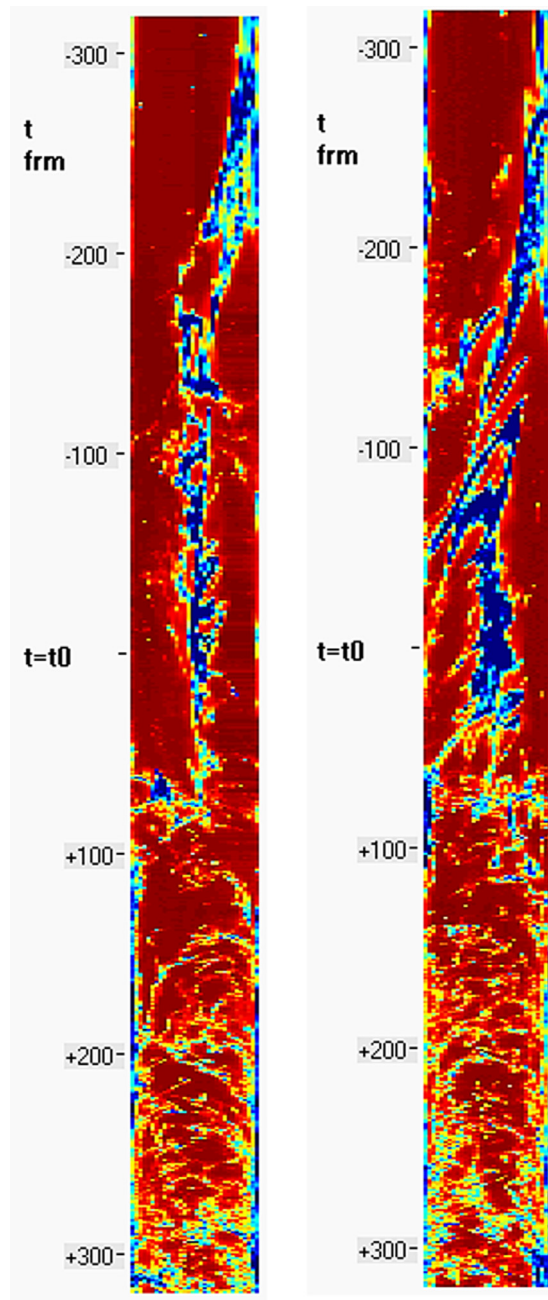
and space averaged) void fraction; (3) time series of cross-section averaged void fraction, velocities and frequencies of the periodic structures found in the flow and (4) the flow rates at which wisps occur and their frequencies.

#### Interfacial structures

Images made up of the time sequences of the phase distribution across a pipe diameter have been created. Examples from four gas velocities are shown below in Fig. 8(a–d). The information is held in the form of pixels of  $4 \times 4$  mm. These are coloured according to the amount of liquid within that area. In these, the reddish-brown colour represents 100% gas whilst blue is 100% liquid. Light blue, orange and yellow represent intermediate values according to the scale in Fig. 8. When used in conjunction with the time series of cross-

sectional phase distributions, it is seen that the flow pattern is essentially churn flow. There are very obvious regular huge waves. These are most evident for the lower gas and highest gas flow rates. The peaks of the waves can penetrate up to 1/3 of the pipe diameter from the wall. The waves are not totally symmetrical and though they occur on both sides of the pipe at approximately the same time, the two sides can have significantly peak thicknesses. As the gas superficial velocity increases the peak heights decrease as seen in Fig. 8(a–c). This aspect will be discussed quantitatively in below.

Another feature of the flow structures that has been observed are wisps similar to those reported by Hernandez Perez et al. (2010). Fig. 9 shows an example of such a structure illustrated by two orthogonal time series of the phase distributions about a diameter. It is noted that the wisp is an approximately cylindrical body with a diameter which can be greater than 20 mm and a length of the order of the pipe di-



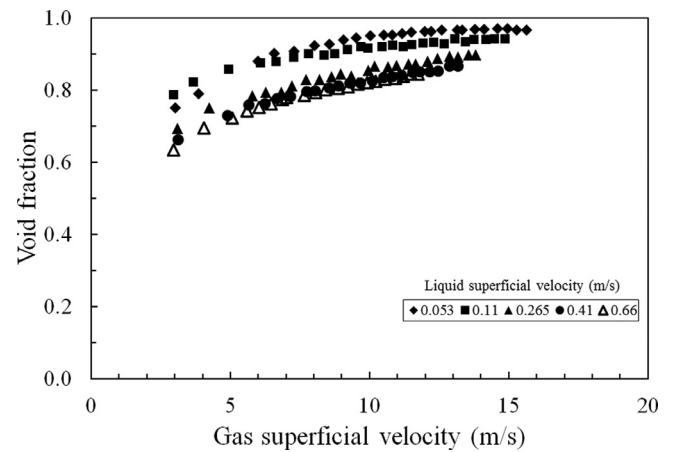
**Fig. 9.** Illustration of a wisp in the gas core of the pipe in the present experiments. Gas superficial velocity = 3 m/s, liquid superficial velocity = 0.265 m/s.

ameter. Given the solidity of the liquid body with these dimensions, use of the term wisp, with its connotations of lightness, must be considered poetic.

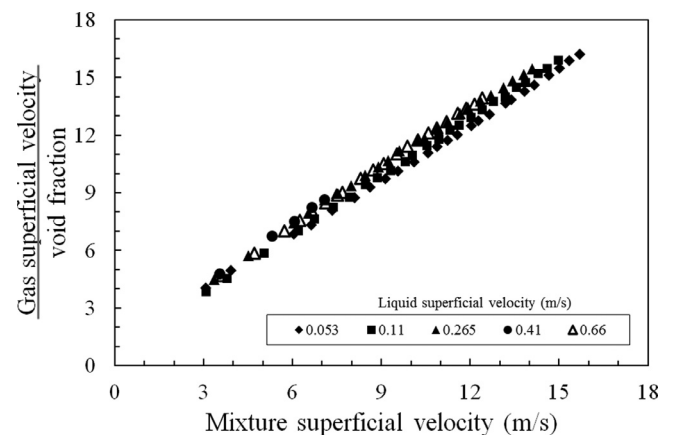
#### Mean void fraction

Fig. 10 presents the (time and cross-sectionally) averaged void fraction obtained from the Wire Mesh Sensor measurements. The data was obtained for a series of liquid superficial velocities (0.053–0.66 m/s) and gas velocities between 3 and 15 m/s. The figure illustrates that the void fraction depends on both gas and liquid flow rates but that the dependency is not strong. This is not unexpected from published data in this range of flow rates.

To quantify the relationship between void fraction and the phase flow rate the Drift Flux approach, proposed by



**Fig. 10.** Effect of gas and liquid superficial velocity on time and cross-section averaged void fraction.



**Fig. 11.** Plot of gas velocity (gas superficial velocity/void fraction) versus mixture velocity.

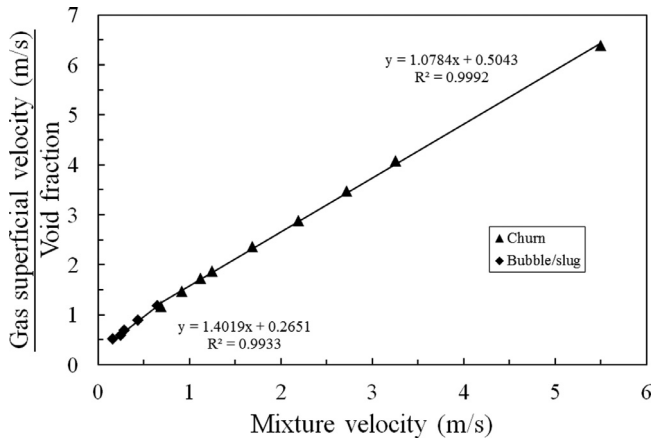
**Table 2**  
Parameters for the linear drift flux fits.

Liquid superficial velocity (m/s)	Distribution coefficient	Drift velocity (m/s)	Regression coefficient
0.053	0.96	0.99	0.9995
0.11	1.01	0.72	0.9998
0.265	1.01	1.28	0.999
0.41	1.04	1.23	0.9992
0.66	1.05	0.97	0.9996

Zuber and Findlay (1965) and employed by Sawai et al (2004) for churn flow, has been followed. Fig. 11 shows a plot of gas velocity (gas superficial velocity divided by void fraction) against mixture velocity (the sum of the superficial velocities of the gas and the liquid,  $u_m$ ). A linear relationship is expected as seen in Fig. 11. The coefficients of the linear equation and regression coefficient (a measure of the goodness of fit) are tabulated in Table 1. The values are close to those reported by Sawai et al. (2004), i.e., 0.99, 0.83 for liquid superficial velocities <0.2 m/s and 1.07, 0.74 for liquid superficial velocities ≥0.2 m/s. These values are slope and intercept respectively in both cases (Table 2).

For the standard Drift Flux approach the two parameters of the linear fit are usually taken to be the distribution coefficient, describing the effect of the radial profile effects, usually identified as  $C_0$ , and the drift velocity,  $u_d$ , the velocity as the gas velocity tends towards zero, i.e., in slug flow the velocity of a Taylor bubble in a stagnant liquid. It is not obvious how to interpret the concept of drift velocity in





**Fig. 12.** Plot of gas velocity (gas superficial velocity divided by void fraction) against mixture velocity (the sum of the superficial velocities for the two phases) for air-silicone oil data in a 67 mm vertical pipe. Liquid superficial velocity = 0.1 m/s. Also show are the linear regression lines fitted to the data from churn and bubbly/slug flows and their characteristics (equation and regression coefficient).

the churn flow region. Interpolation to zero flow rate does not appear to have physical meaning. In their paper, Zuber and Findlay (1965) illustrated, using the data of Wallis et al. (1963), that the plot of gas velocity against mixture velocity had two slopes with distinct distribution coefficients, one for slug flow and one for annular flow. Note they do not mention churn flow. However, the points termed annular at the lower velocities in the Wallis et al. data are effectively churn flow. A similar behaviour is found in the data of Azzopardi et al (2010) for air-silicone oil in a 67 mm diameter vertical pipe for a liquid superficial velocity of 0.1 m/s, which covers both the bubbly/slug and churn flows. These data are best fitted by two straight lines as shown in Fig. 12. These have distribution coefficients of 1.4 and 1.1 and drift velocities of 0.27 and 0.5 respectively for bubbly/slug and churn. The value of 0.27 m/s agrees well with expected the rise velocity of a Taylor bubble, which has a value of 0.28 m/s for the pipe diameter of 67 mm

From the equations for the two straight lines, Eqs. (1) and (2),

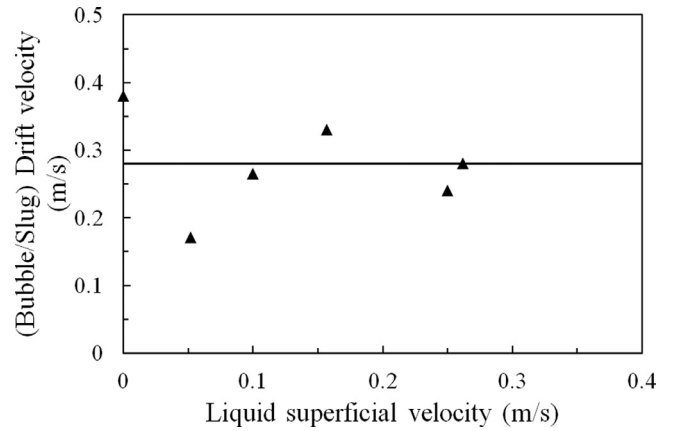
$$\left(\frac{u_{gs}}{\varepsilon_g}\right)_s = C_{0s}u_m + u_{ds} \quad (1)$$

$$\left(\frac{u_{gs}}{\varepsilon_g}\right)_c = C_{0c}u_m + u_{dc} \quad (2)$$

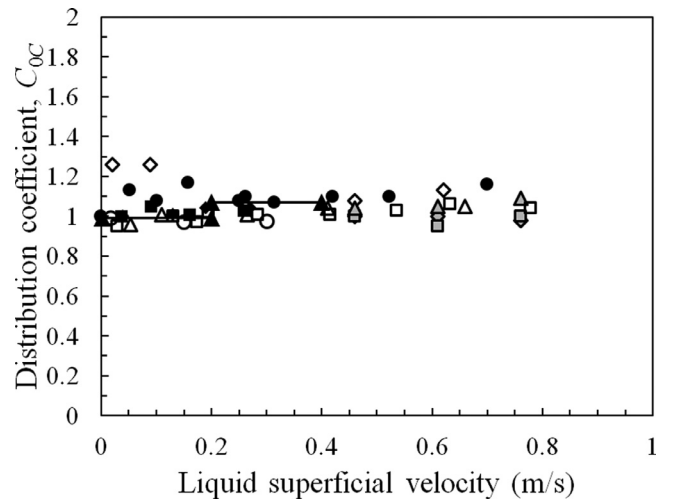
where  $u_{gs}$  is the superficial velocity of the gas and  $\varepsilon_g$  is the void fraction,  $C_{0s}$  is the slope for the slug flow line,  $C_{0c}$  is the slope for the churn flow line,  $u_{ds}$  is the intercept for the slug flow line,  $u_{dc}$  the intercept for the churn flow line and  $u_m$  is the mixture velocity (the sum of the superficial velocities for the gas and the liquid). If it is recognised, that there will be a transition mixture velocity,  $u_{mtr}$ , where the lines cross, which can be obtained from combining Eqs. (1) and (2). Eq. (2), for churn flow, can be rewritten eliminating  $u_{dc}$  as

$$\left(\frac{u_{gs}}{\varepsilon_g}\right)_c = C_{0c}u_m + u_{ds} + (C_{0s} - C_{0c})u_{mtr} \quad (3)$$

This gives four parameters to be specified. The drift velocity for the bubbly/slug flows,  $u_{ds}$ , can be described by the rise velocity of an isolated Taylor bubble [ $Fr\sqrt{(gD)}$ ]. For the air-water combination at near atmospheric pressure,  $Fr = 0.35$ . For more viscous liquids, the equation proposed by Viana et al. (2003) has been found to be accurate for viscosities up to 360 Pa s. This description agrees with the values obtained from the air-silicone oil data from a 67 mm diameter pipe introduced above. However, as shown in Fig. 13, there is significant scatter. For the distribution coefficients for slug flow,  $C_{0s}$ , there are



**Fig. 13.** Drift velocities for the bubble slug region for air-silicone oil flows in a 67 mm diameter vertical pipe. The line is  $0.35\sqrt{(gD)}$ . The viscosity of the silicone oil is 5 mPa s.



**Fig. 14.** Distribution coefficients for churn flow from different sources. Details and symbols are provided in Table 3. The data from Sawai et al. (2004) are linked with lines to indicate that they gave values for greater and less than a liquid superficial velocity of 0.2 m/s.

proposals by Guet et al. (2004, 2006). However more development is required. Data for the distribution coefficient for churn flow,  $C_{0c}$ , has been gathered from the literature and these are plotted together with those from the present work in Fig. 14. Information about the geometry and liquid physical properties involved are listed in Table 3. As seen in the plot, most of the data are reasonably approximated by 1.0 as suggested by Zuber and Findlay (1965). On the whole, they lie in a narrow band between 0.9 and 1.1 and show no strong trend with liquid superficial velocity, pipe diameter and physical properties.

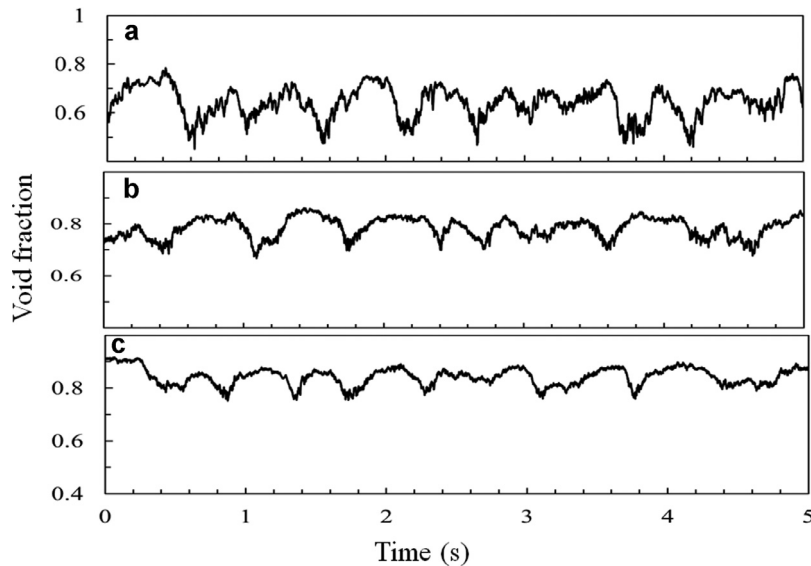
When gas superficial velocities were extracted from the mixture velocities at transition, it was seen that they corresponded to the slug/churn transition velocities determined from the examination of the Probability Density Function plots of the void fraction time series as reported by Szalinski et al. (2010). This approach, fitting void fraction data using Eqs. (1) and (2) and solving for the transition velocity provides an independent means of identifying flow pattern transitions.

This approach is in contrast to those of other workers who seek a single, seamless, though-complex drift flux equation covering all flow patterns. This is a laudable aim in that it means that designers do not need to worry about flow patterns. The latest such version is comes from Bhagwat and Ghajar (2014), who review and tabulate equations from previous, similar approaches. Their approach provides a sigmoid equation for the distribution coefficient going from 2 at low flow rate

**Table 3**

Geometry and liquid physical properties for data used in Fig. 14.

Source	Pipe diameter (mm)	Liquid physical properties Density (kg/m <sup>3</sup> )	Viscosity (mPa s)	Surface tension (N/m)	Symbol
Govier and Short (1958)	63.5	1000	1	0.073	◇
Wallis et al. (1963)	24.8	1000	1	0.073	□
Sawai et al. (2004)	25.8	1000	1	0.073	▲
Azzopardi et al. (2010)	67	900	5	0.02	●
Waltrich et al. (2013)	48	1000	1	0.073	○
Hewakandamby et al. (2014)	127	1152	12.2	0.064	◆
	127	1166	16.2	0.061	■
Parsi et al. (2015a, 2015b)	76	1000	1	0.073	◆
	76	1000	10	0.073	■
	76	1000	40	0.073	▲
Present work	127	1000	1	0.073	△

**Fig. 15.** Examples of void fraction time series corresponding to image in Fig. 8. Liquid superficial velocity = 0.66 m/s. Gas superficial velocity = (a) 2.97; (b) 7.65; (c) 11.7 m/s.

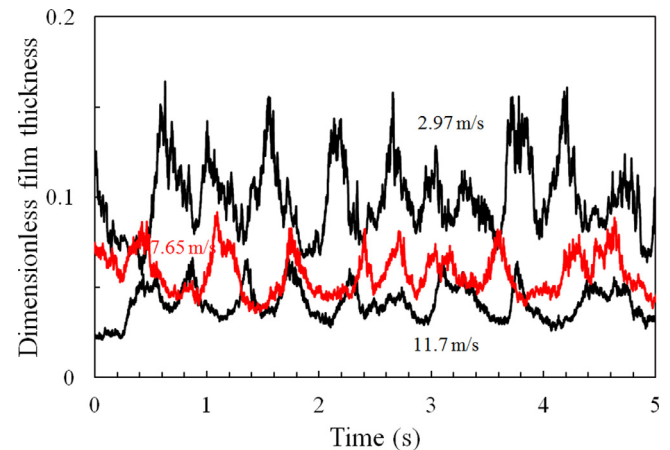
to 1 at much higher ones (at conditions pertaining to churn flow). Compared to what is reported here, their change is more gradual.

#### Basic flow – film thicknesses and huge waves

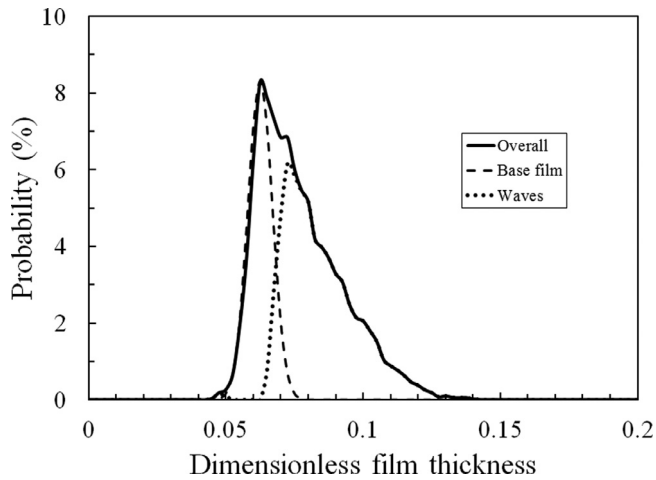
A great deal of information can be gained from the time series of the cross-sectionally averaged void fraction,  $\varepsilon_g$ . Examples of these are shown in Fig. 15. These are all for a liquid superficial velocity of 0.66 m/s and different gas superficial velocities as marked on the figure. However, this does not tell us anything about the wall film. With the assumption of all the liquid measured being in the film and cylindrical symmetry, film thicknesses,  $\delta$ , made dimensionless by the pipe diameter,  $D$ , can be obtained from

$$\frac{\delta}{D} = (1 - \sqrt{\varepsilon_g}) \quad (4)$$

This operation has been carried out and the film thickness traces corresponding to the void fraction traces shown in Fig. 15 are given in Fig. 16. It is noted that film thicknesses are 2–15% of the pipe diameter. The variation of film thickness with gas superficial velocity can be tracked through the overall average thickness, the average of the base film and the average height of the structures on the film. The overall average is straight forwards to obtain, it is the mean value of the time series of dimensionless film thickness. The other two are a bit more complicated to extract. However, a useful approach has been proposed by Sawai et al. (2004). Consider a Probability Density Function of the dimensionless film thickness an example of which is illustrated in Fig. 17. It can be seen that the curve can be divided into

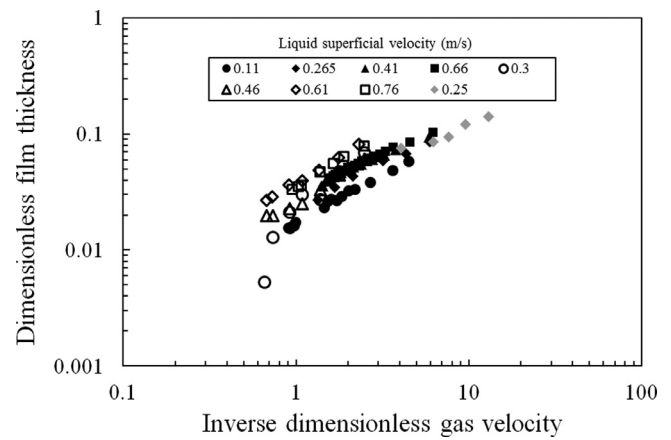
**Fig. 16.** Examples of film thickness made dimensionless by the pipe diameter. Liquid superficial velocity = 0.66 m/s. Gas superficial velocity as marked by each trace.

two sub-curves one of which is in the form of a Gaussian and is at the lower end. This is taken to describe the base film with the ripples on its surface giving the width of the Gaussian. The dimensionless film thickness at which this curve peaks can be taken as the base film thickness. For the mean peak height, the values for individual peaks are extracted and averaged. The analysis of the Probability Density Function curve can be extended to extract the fraction of liquid in the waves.



**Fig. 17.** Example of a Probability Density function of dimensionless film thickness. This shows how the complex shape can be divided between a Gaussian curve representing the base film and the ripple on it and a second, not necessarily Gaussian, curve representing the waves. These two distributions are the basis of the method of extracting proportions of liquid in the film and huge waves as proposed by [Sawai et al. \(2004\)](#). For this example, the gas superficial velocity = 5.1 m/s and the liquid superficial velocity = 0.66 m/s.

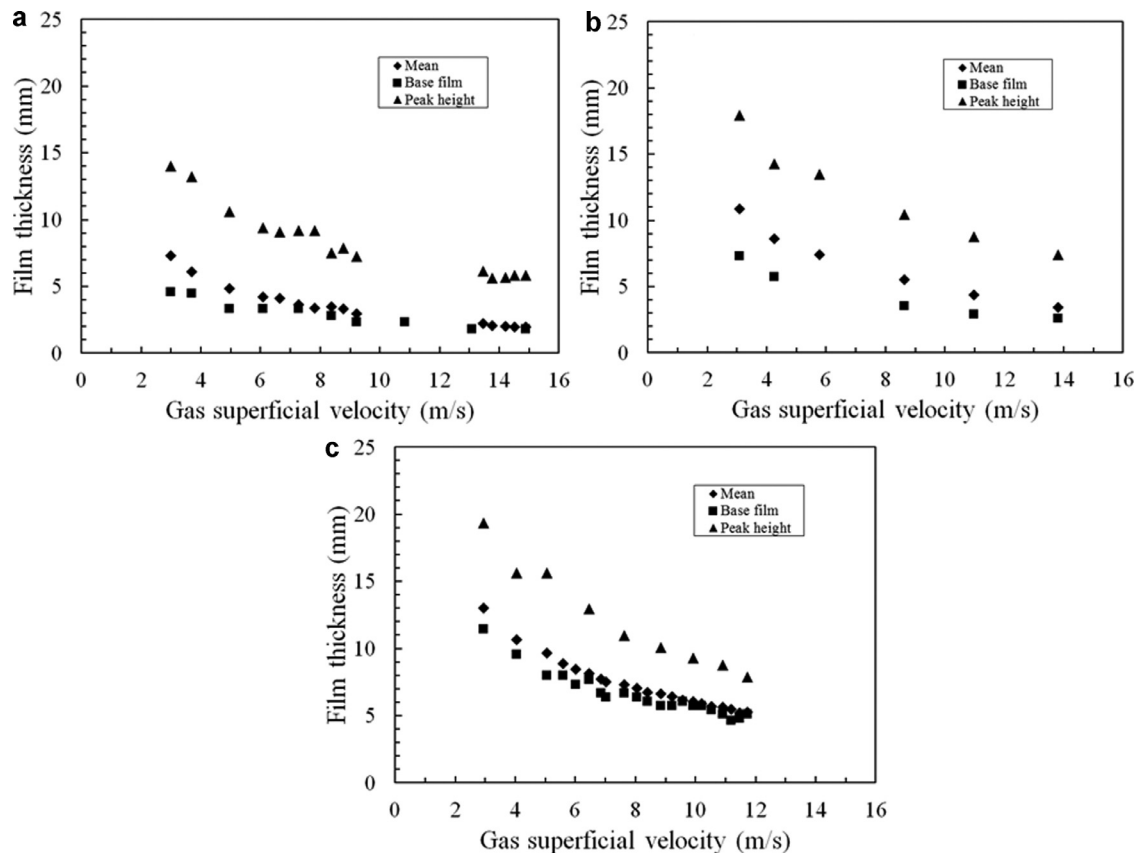
Values of the mean film thickness, that corresponding to the base film and of the average height of huge waves are plotted in [Fig. 18](#) for liquid superficial velocities of 0.11, 0.265 and 0.66 m/s. The base film thickness is seen to be slightly below the equivalent mean film thickness. Examination of the visualisations of the flow, such as those shown in [Fig. 8](#), indicated that the huge waves occupied only 20% of the film interface. This is confirmed by the work of [Sekoguchi and Mori \(1997\)](#), though it is noted that their data were from a smaller diame-



**Fig. 19.** Dimensionless mean film thickness plotted against dimensionless gas velocity. Closed symbols – present work. Liquid superficial velocity • 0.11 m/s; 0.26 m/s; ▲ 0.41 m/s; ■ 0.66 m/s. Open symbols – [Parsi et al. \(2015\)](#). Liquid superficial velocity ○ 0.3 m/s; △ 0.46 m/s; ◊ 0.61 m/s; ◻ 0.76 m/s. Grey symbols – [Hernandez Perez et al. \(2010\)](#). Liquid superficial velocity = 0.25 m/s.

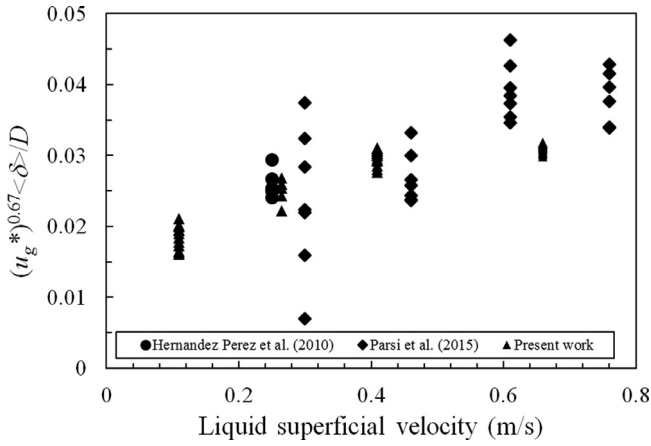
ter pipe. From this it is not surprising that the mean film thickness is close to that of the base film.

The mean film thickness data, together with that from other sources, i.e., [Hernandez Perez et al. \(2010\)](#), [Parsi et al. \(2015a, 2015b\)](#), have been examined to determine parametric trends. [Fig. 19](#) shows the mean film thickness data, non-dimensionalised by the pipe diameter, plotted against the inverse dimensionless gas velocity,  $1/u_g^* = \sqrt{[(\rho_L - \rho_G)gD]/\rho_G u_G^2}$ . This shows that data from different pipe diameters are similar. In general, the dimensionless film thickness data depend on  $u_g^*$  to the power of  $\sim -0.67$ . A similar trend has

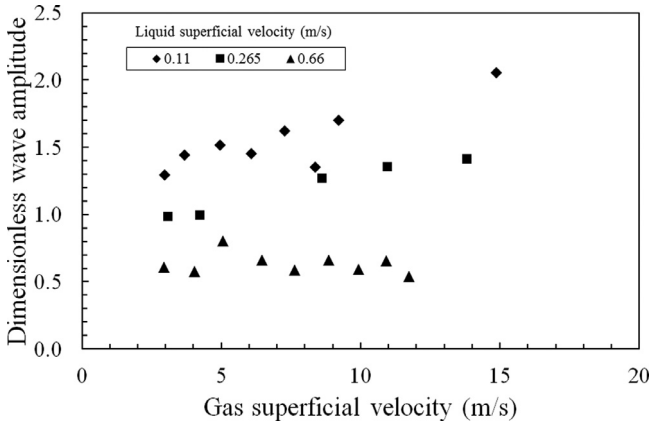


**Fig. 18.** Mean, base and mean wave peak film thicknesses. Liquid superficial velocity (m/s) – (a) 0.11; (b) 0.265; (c) 0.66.





**Fig. 20.** Product of dimensionless mean film thickness times the dimensionless gas velocity raised to the power of 0.67 plotted against liquid superficial velocity. Pipe diameters: Hernandez Perez et al. (2010) = 67 mm; Parsi et al. (2015a, 2015b) = 76 mm; present work = 127 mm.

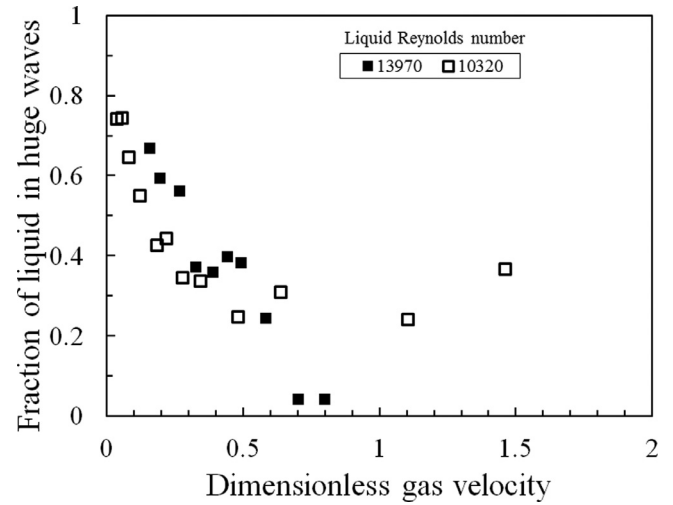


**Fig. 21.** Mean wave amplitude non-dimensionalised by mean film thickness.

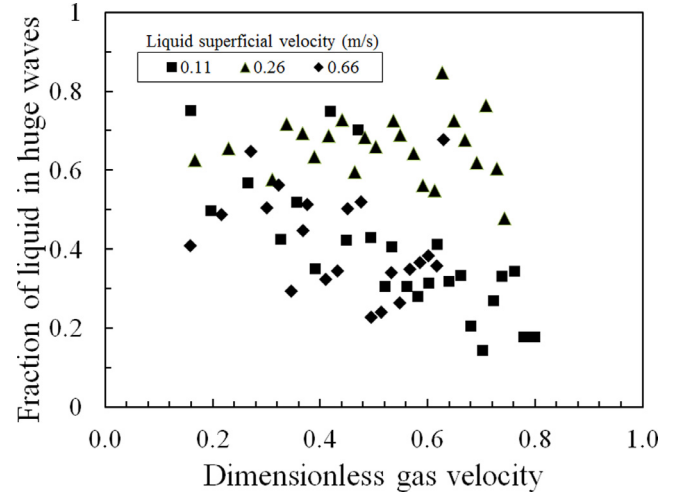
been reported by Kaji and Azzopardi (2010) for pipes of diameters between 5 and 50 mm. If the data are replotted as  $u_g^{*0.67} <δ>/D$  against the liquid superficial velocity, it can be seen in Fig. 20 that there is a small but significant relationship. The greatest scatter is seen for the data of Parsi et al. (2015a, 2015b) for their lowest liquid and highest gas superficial velocities. It is possible that these data are in annular flow.

Wave amplitudes, the difference between peak heights and base film thicknesses made dimensionless by the mean film thicknesses, can also be extracted. The values obtained are illustrated in Fig. 21; they show only a small effect of gas superficial velocity but a stronger effect of liquid superficial velocity.

The fraction of liquid in the film, which is travelling in waves as opposed to in the base film, has been determined using the method proposed by Sawai et al. (2004). As shown in Fig. 17, is not unreasonable to assume that the contribution of the base film in a plot of the Probability Density Function of dimensionless film thickness can be described by a Gaussian function. The difference between the overall Probability Density Function and this Gaussian is the part of the liquid in the huge waves. The fraction of liquid in waves is plotted in Fig. 22 for a liquid superficial velocity of 0.11 m/s and shows a gradual decrease as the gas velocity increases. Also shown is the nearest equivalent data from the work of Sawai et al. (2004). This was obtained in a smaller diameter pipe, 25.8 mm. The particular data set is chosen on the basis of the nearest liquid Reynolds number ( $ρ_L u_{LS} D / η_L$ ) to the data from the present work. Both results show similar trends. The decrease in liquid fraction in the waves probably



**Fig. 22.** Fraction of liquid in waves, i.e.,  $P_W$  in the paper of Sawai et al. (2004) plotted against a dimensionless gas velocity,  $ad[\rho; \rho_G u_{GS}^2 / (\rho_L - \rho_G) g D]$ . Open symbols are data of Sawai et al. (2004) from a pipe diameter of 25.8 mm, closed symbols are from present work from a pipe diameter of 127 mm.



**Fig. 23.** Effect of gas and liquid superficial velocities on fraction of liquid in waves, i.e.,  $P_W$  in the paper of Sawai et al. (2004).

marks a transition towards annular flow whose Probability Density Function signature has no tail unlike churn flow. Data for a number of liquid superficial velocities are shown in Fig. 23. For higher liquid superficial velocities the fraction of liquid in the waves takes a value of  $\sim 0.5$  with a decrease becoming visible at the highest gas flow rate shown for the data from the liquid superficial velocity of 0.26 m/s. This indicates that the transition to annular flow occurs at higher gas velocities as the liquid velocity increases. This is contrary to the boundaries proposed by Hewitt and Roberts (1969) and illustrated in the modified version of their map shown in Fig. 1 and by Barnea (1986) who indicate a boundary which is almost independent of liquid flow rate. In contrast, the boundary proposed by Sekoguchi and Mori (1997), based on the flow rates at which huge wave and disturbance wave frequencies are equal, indicates higher liquid flow rates and the gas flow rate increases. These types of plots show a way of discriminating between churn and annular flow.

It is reasonable to ask: how representative are the circumferentially averaged film thickness values discussed above? This might be made clearer on examination of one frame from the Wire Mesh Sensor output displayed in Fig. 24. The circles marked on this figure correspond to the base, mean and wave peak film thickness values. It is

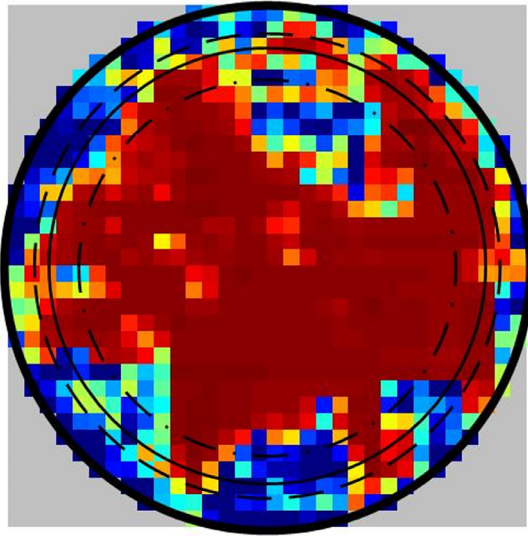


Fig. 24. Single frame of Wire Mesh Sensor output showing distribution of the phases about the cross-section. Gas superficial velocity 3 m/s, liquid superficial velocity = 0.265 m/s.

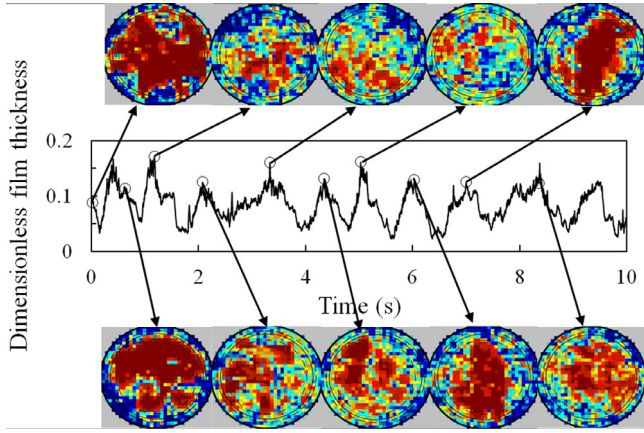


Fig. 25. Sequence frames of Wire Mesh Sensor output showing distribution of the phases about the cross-section together with time trace of dimensionless film thickness focussing on crests of huge waves. Gas superficial velocity = 3 m/s, liquid superficial velocity = 0.265 m/s.

clear from the figure that the film is not circumferentially uniform. There are large protrusions into the core at several positions around the pipe. These are probably parts of a huge wave. The part at the top is an example of the start of atomisation, i.e., the formation of a ligament which might be interpreted as a wisp. Also seen in the core of the pipe are a number of drops which appear in yellow as they do not occupy the whole of the particular pixel. A number of further examples of such views are shown in Fig. 25 where they are identified with the positions of the (averaged) dimensionless film thickness time trace to which they correspond. Most of these frames are from the peaks of waves. A second sequence, Fig. 26, provides views from positions along two huge waves and the portion in between which contains a large wisp. These show the multidimensional complexity present. It is noted that though the Wire Mesh Sensor gives a great deal of information, it does not provide the fine detail that would be necessary for advanced mathematical modelling. For that an alternative approach such as the Brightness Based Laser Induced Fluorescence, employed by Cherdantsev et al. (2014) would be required.

Indirect evidence about the transport of liquid entrained as drops can be found in the wall shear stress,  $\tau_w$ , measurements of Zangana and Azzopardi (2012). They employed the same flow facility as the

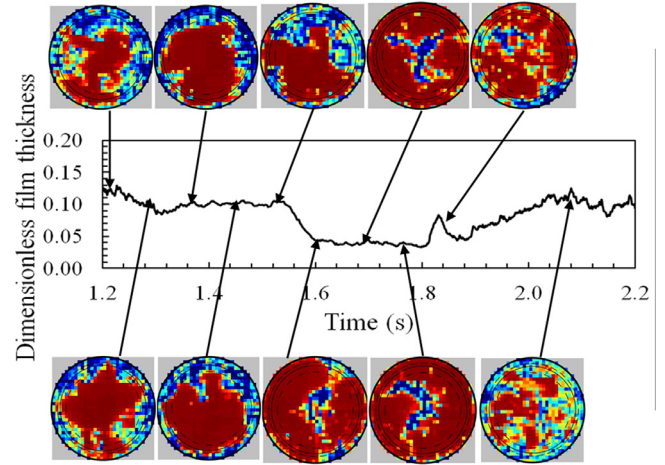


Fig. 26. Sequence frames of Wire Mesh Sensor output showing distribution of the phases about the cross-section together with time trace of dimensionless film thickness illustrating changes over two huge waves and a wisp. Gas superficial velocity = 3 m/s, liquid superficial velocity = 0.265 m/s.

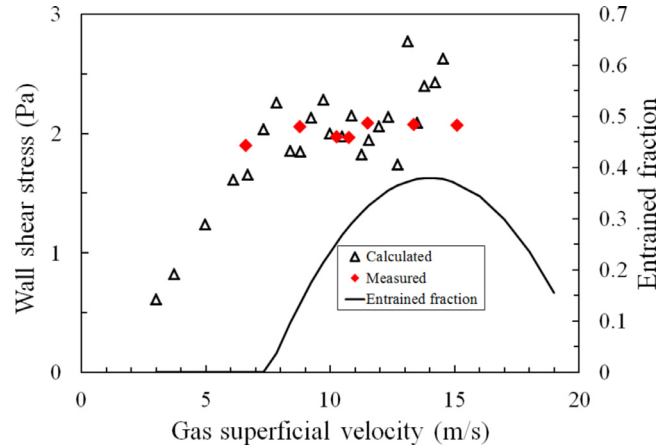


Fig. 27. Wall shear stress measured by Zangana and Azzopardi (2012),  $\blacklozenge$ , using a hot film probe together with values,  $\Delta$ , calculated employing the film thickness obtained from the Wire Mesh Sensor with allowance for the entrained fraction shown. The corresponding entrained fraction values are plotted as the solid line.

present work and used a carefully calibrated hot film probe and monitored temperature of the liquid at the wall either side of the hot film probe to determine the direction of flow. Examples of their results are shown in Fig. 27 together with values calculated from

$$\tau_w = \frac{f_F \rho_L u_F^2}{2} \quad (5)$$

The friction factor,  $f_F$ , was calculated using the standard Blasius relationship using the Reynolds number ( $Re = \rho_L u_F D_{HF} / \eta_L = \rho_L u_{sl} D / \eta_L$ ), and  $u_F$  is the mean velocity of the film – obtained from the liquid flow rate and  $D_{HF}$  is the hydraulic diameter for the film which is equal to  $4\delta(D-\delta)/D$  and  $\delta$  is the mean film thickness determined above but allowing for the fact that some of the liquid was travelling as entrained drops and  $\eta_L$  is the liquid viscosity. Because of the poor agreement between the available methods for calculating the entrained fraction,  $E_f$ , and experimental data shown in Fig. 4,  $E_f$  was calculated from the empirical equation

$$E_f = E_{f0} - A(u_{GS} - u_{Gsp})^2 \quad (6)$$

The constants,  $E_{f0}$ , the peak entrained fraction,  $u_{Gsp}$ , the gas superficial velocity at which the peak occurs and  $A$ , were adjusted to give a good fit between the measured and calculated wall shear stress. The values of entrained fraction calculated are shown in Fig. 27. The shape

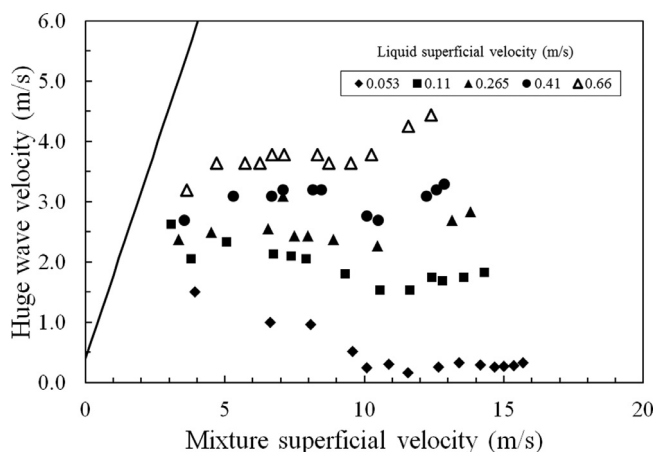


Fig. 28. Velocities of huge waves calculated from time delay obtained from cross-correlation of time traces from two adjacent conductance probes.

shows the same trend as the available data plotted in Fig. 4 which was from a lower liquid flow rate. In spite of the difference in flow rates between the data in Figs. 4 and 27, the good agreement between measured and calculated wall shear stress gives some confidence that the entrained fraction is as shown in Fig. 27.

The velocity of the periodic structures has been calculated from the delay times obtained by cross-correlating the times series from two axially-separated conductance probes. The results are displayed in Fig. 28 together with the line showing the value that would be expected for slug flow,  $1.4u_m + 0.35\sqrt{(gD)}$ . As expected, the values determined from the experiments are all below the slug flow line. The deviation appears to occur at higher gas superficial velocities for larger values of liquid superficial velocity. These results also show the maxima and minima found in all other churn flow data as presented by Azzopardi (2006). If the data in Fig. 28 is examined further, it is seen that a great part of it lies in almost horizontal lines, indicating they this velocity is almost independent of gas flow rate. This is seen more clearly if they are plotted as the ratio of huge wave velocity to liquid superficial velocity against gas superficial velocity. The data still appear independent of gas flow but do not collapse on to one line indicating a more complex dependence on liquid flow rate.

Frequency characteristics of the times series can be obtained using Power Spectrum analysis. Here, Power Spectrum Densities (PSD) have been obtained by using the Fourier transform of the auto covariance functions of the time series of cross-sectionally averaged void fraction. From the variation of PSD with frequency, the most probable frequencies, the peak frequency, have been extracted. The results are presented in Fig. 29 and show that frequency increases with increasing liquid superficial velocity and passes through a minimum with increasing gas superficial velocity.

For annular flow, a mechanistic model may be applied employing force balances on the wall film and the drop laden gas core. In this the fraction of liquid entrained as drops as well as the wall and interfacial shear stress need to be specified. This would enable film thicknesses to be calculated. Though there are reasonable methods to determine entrained fraction in annular flow, as shown in Fig. 4, the same cannot be said in churn flow and so the approach cannot be implemented.

#### Occurrence and frequencies of wisps

The conditions at which wisps occurred from all the published sources described above have been plotted on the modified Hewitt and Roberts flow pattern map, i.e., a plot liquid Weber number against gas Weber numbers. These conditions are shown in Fig. 30 together with the conditions at which wisps were identified in the present study. The plot illustrates that wisps occur over broad

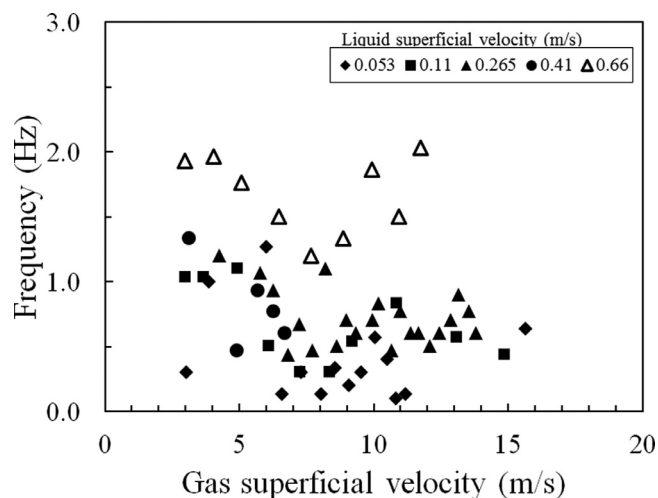


Fig. 29. Effect of flow rate on frequency extracted from cross-sectionally averaged void fraction determined from the Wire Mesh Sensor.

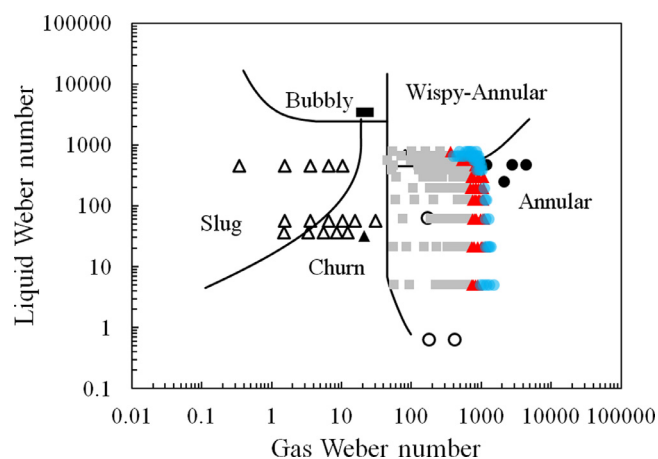


Fig. 30. Flow pattern maps showing conditions at which Big wisps, small wisps and no wisps occur. ■ Big wisps; ▲ Small wisps; ● No wisps. Other observations of wisps: ■ Hewitt and Roberts (1969); ▲ Sekoguchi and Mori (1997); ● Hawkes et al. (2000); ◆ Prasser et al. (2002); ○ Omebere-Iyari et al. (2008); △ Hernandez Perez et al. (2010).

swathes of gas and liquid flow rates. They appear to be smaller at higher gas velocities and are not visible at gas velocities above a critical value. This might be explained by the origins of wisps. The study of Hernandez-Perez et al. (2010) indicates that the wisps might be a product of a process of incomplete atomisation from the liquid film. This phenomenon could be considered as a function of the gas inertia imparted to waves on the liquid film with the counterbalancing force of surface tension, i.e., a Weber number. Hinze (1955) related the drop break-up to the Weber number and showed that beyond a critical Weber number the drop will break up. Azzopardi (1983) suggested a similar phenomenon with the source being waves and that the break up process involved the formation of ligaments, i.e., wisps. Support for the proposal that wisps are a form of ligaments pulled from the huge waves might be drawn from a similarity to the ratio of wisp and wave frequencies. The former were extracted from examination of the time series of the distributions of the phases about the cross-section, an example of which is shown in Fig. 24. The wave frequencies were determined from the peaks in the Power Spectral Densities of the cross-sectionally averaged time series of void fraction. The ratios obtained are shown in Fig. 31 for two liquid superficial velocities together with equivalent data from Hernandez Perez et al. (2010). It is noted that there can be values of the ratio greater than 1.0. Study of the Wire Mesh Sensor output shows more than one wisp



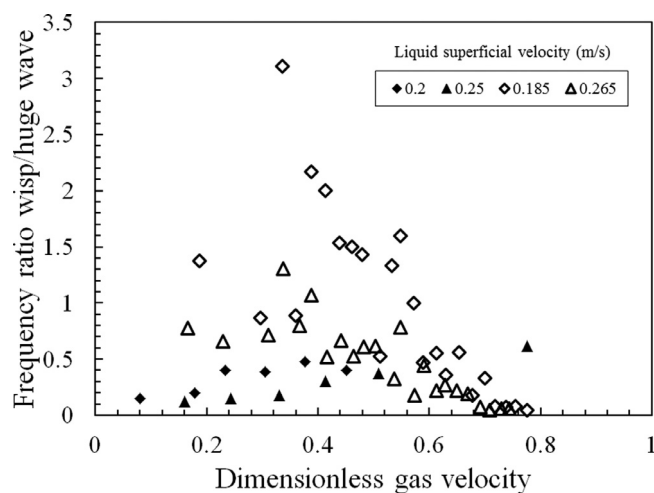


Fig. 31. Ratio of the frequencies of wisps to those of huge waves plotted against dimensionless gas velocity. Open symbols – present work; closed symbols – Hernandez Perez et al. (2010).

can be associated with a particular huge wave. This is not surprising if the wisps are considered ligaments, part of the process of atomisation. These arise from instabilities at different points of the wave surface.

## Conclusions

From the above, the following conclusions can be drawn:

- The flow in the 127 mm diameter pipe over range of gas superficial velocities of 3–15 m/s and liquid superficial velocities of 0.053–0.66 m/s is in the churn flow pattern with its characteristic huge waves. It also shows wisps similar to those reported by Hernandez Perez et al. (2010).
- The cross-sectional and time averaged void fraction for churn flow can be described by a drift flux type equation. For this flow pattern the distribution coefficient takes a value of  $\sim 1.0$  as expected for flows with gas continuous core. The equivalent to the drift velocity is best described by the drift velocity for slug flow plus the mixture velocity at the transition to churn flow times the difference in distribution coefficients for slug and churn flows.
- Mean film thicknesses together with those for the base film and the peaks of the waves have been extracted from the Wire Mesh Sensor output. These data together with that from published papers show a strong trend with gas flow rate and a weaker one with liquid flow rate. There seems to be little effect of pipe diameter. However, it is clear that the waves are not circumferentially uniform.
- Wisps of different sizes have been observed over most the range of flow rates studied with the exception of the higher gas velocities. This is in agreement with many of the observations of wisps reported in the literature. The frequency of occurrence of wisps decreases with increasing gas superficial velocity. Their values are usually, but not always, lower than the corresponding frequency of huge waves. There is clear evidence that wisps arise from huge waves and are part of an incomplete atomisation process.

## Acknowledgements

SS was supported by an EPSRC studentship as part of Grant number EP/F016050/1. This research study has been undertaken within the Joint Project on Transient Multiphase Flows and Flow Assurance. The Authors wish to acknowledge the contributions made

to this project by the UK Engineering and Physical Sciences Research Council (EPSRC) and the following: Advantica; BP Exploration Operating Co. Ltd.; CD-adapco; Chevron; ConocoPhillips; ENI; ExxonMobil; FEESA; IFP; Institutt for Energiteknikk; Norsk Hydro; PDVSA (INTERVEP); Petrobras; PETRONAS; ScandpowerPT; Shell; SINTEF; Statoil and TOTAL. This provided support for GPvDM. The Authors wish to express their gratitude for this support.

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