Resource Logics with a Diminishing Resource

Extended Abstract

Natasha Alechina University of Nottingham Nottingham, UK nza@cs.nott.ac.uk

ABSTRACT

Model-checking resource logics with production and consumption of resources is a computationally hard and often undecidable problem. We show that it is more feasible under the assumption that there is at least one diminishing resource, that is, a resource which is consumed by every action.

KEYWORDS

Model-checking; resources

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1 INTRODUCTION

There has been a considerable amount of work on resource logics interpreted over structures where agents' actions produce and consume resources, for example [\[2,](#page-2-1) [3,](#page-2-2) [6](#page-2-3)[–9,](#page-2-4) [12](#page-2-5)[–14,](#page-2-6) [17–](#page-2-7)[19\]](#page-2-8). There exists also a large body of related work on reachability and nontermination problems in energy games and games on vector addition systems with state [\[1,](#page-2-9) [11,](#page-2-10) [15,](#page-2-11) [16,](#page-2-12) [21\]](#page-2-13). The resource logics considered in this paper are extensions of the Alternating Time Temporal Logic (ATL), [\[10\]](#page-2-14). For ATL under imperfect information and with perfect recall uniform strategies, ATL_{iR} , the model-checking prob-
lem is undecidable for three or more agents [20]. It is bourever lem is undecidable for three or more agents [\[20\]](#page-2-15). It is however decidable in the case of bounded strategies [\[23\]](#page-2-16).

In this paper we introduce a special kind of models for resource logics satisfying a restriction that one of the resources is always consumed by each action. This is a very natural setting that occurs in many verification problems. One obvious example of such a resource is time. Other examples include systems where agents have a non-rechargeable battery and where all actions consume energy, e.g., nodes in a wireless sensor network; and systems where agents have a store of propellant that cannot be replenished during the course of a mission and all actions of interest involve manoeuvring, e.g., a constellation of satellites. We call this special resource that is consumed by all actions a diminishing resource.

We study $RB \pm ATL^{\#}$ and $RB \pm ATL^{\#}_{iR}$, diminishing resource sions of Resource-Bounded Alternating Time Temporal Logic versions of Resource-Bounded Alternating Time Temporal Logic (RB±ATL) [\[5\]](#page-2-17). The model-checking problem for RB±ATL is known to be 2EXPTIME-complete [\[6\]](#page-2-3), while $RB \pm ATL^*$ model-checking is in PSPACE if resource bounds are written in unary. In the case of

Brian Logan University of Nottingham Nottingham, UK bsl@cs.nott.ac.uk

 $RB \pm ATL_{IR}^{\#}$, the result of [\[23\]](#page-2-16) does not apply immediately because
the bound is not fixed in advance, but its model checking problem the bound is not fixed in advance, but its model checking problem is decidable in EXPSPACE given encoding in unary. We also study RAL[#], a diminishing resource version of Resource Agent Logic (RAL) [\[13\]](#page-2-18). Decidability of RAL^* follows from the result on the decidability of RAL on bounded models [\[13\]](#page-2-18), but the PSPACE upper bound (for unary encoding) is new.

2 $RB \pm ATL^*$

The syntax of $RB \pm ATL^{\#}$ is defined relative to the following sets: $Agt = {a_1, \ldots, a_n}$ is a set of *n* agents, $Res = {res_1, \ldots, res_r}$ is a set of r resource types, Π is a set of propositions, and $B = \mathbb{N}^{Res^{Agt}}$ is a set of resource bounds (resource allocations to agents). Flements of set of resource bounds (resource allocations to agents). Elements of B are vectors of length *n* where each element is a vector of length r. We will denote by \mathcal{B}_A (for $A \subseteq Aqt$) the set of possible resource allocations to agents in A. Formulas of $RB \pm ATL^{\#}$ are defined by:

$$
\phi, \psi ::= p \mid \neg \phi \mid \phi \lor \psi \mid \langle \langle A^{b} \rangle \rangle \bigcirc \phi \mid \langle \langle A^{b} \rangle \rangle \phi \mathcal{U} \psi \mid \langle \langle A^{b} \rangle \rangle \phi \mathcal{R} \psi
$$

where $p \in \Pi$, $A \subseteq Agt$, and $b \in \mathcal{B}_A$. $\langle\!\langle A^b \rangle\!\rangle \bigcirc \phi$ means that a coalition A can ensure that the next state satisfies ϕ under resource coalition A can ensure that the next state satisfies ϕ under resource bound b. $\langle A^b \rangle \phi \mathcal{U} \psi$ means that A has a strategy to enforce ψ while
maintaining the truth of ϕ and the cost of this strategy is at most maintaining the truth of ϕ , and the cost of this strategy is at most b. $\langle (A^b) \phi \mathcal{R} \psi \rangle$ means that A has a strategy to maintain ψ until and including the time when ϕ becomes true or to maintain ψ forever including the time when ϕ becomes true, or to maintain ψ forever if ϕ never becomes true, and the cost of this strategy is at most b . The language is interpreted on the following structures:

Definition 2.1. A resource-bounded concurrent game structure with diminishing resource (RB-CGS[#]) is a tuple $M = (Agt, Res,$
S $\Pi = Act, d \in \mathcal{S}$) where: S, Π , π , Act, d , c , δ) where:

- Agt, Res and Π are as above; the first resource type in Res is the distinguished diminishing resource;
- S is a non-empty finite set of states;
- $\pi : \Pi \to \varphi(S)$ is a truth assignment that associates each $p \in \Pi$ with a subset of states where it is true;
- Act is a non-empty set of actions;
- $d : S \times Aqt \rightarrow \wp(Act) \setminus \{\emptyset\}$ is a function that assigns to each s [∈] S a non-empty set of actions available to each agent $a \in Aqt$.
- $c : S \times Act \to \mathbb{Z}^r$ is a partial function that maps a state s and
an action σ to a vector of integers where a positive (peoptive) an action σ to a vector of integers, where a positive (negative) integer in position *i* indicates consumption (production) of resource r_i by the action. The first position in the vector is always at most −1.
- δ : $S \times Act^{|Agt|} \rightarrow S$ is a partial function that maps every $s \in S$ and $\sigma \in d(s, a_1) \times \cdots \times d(s, a_n)$ to a state resulting from executing σ in s.

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In what follows, we use the usual point-wise notation for vector comparison and addition, and, given a function f returning a vector, we denote by f_i the function that returns the i-th component of the vector returned by f. Given an RB-CGS[#] M and a state $s \in S$, a *joint action by a coalition* $A \subseteq Aqt$ is a tuple $\sigma = (\sigma_a)_{a \in A}$ such that $\sigma_a \in d(s, a)$. The set of all joint actions for A at state s is denoted by $D_A(s)$. Given a joint action by Agt , $\sigma \in D_{Agt}(s)$, σ_A denotes the joint action executed by A as part of $\sigma : \sigma \to (\sigma)$. the joint action executed by A as part of σ : $\sigma_A = (\sigma_a)_{a \in A}$. The set of all possible outcomes of a joint action $\sigma \in D_A(s)$ at state s is: out(s, σ) = {s' ∈ S | ∃σ' ∈ D_{Agt}(s) : σ = σ'_A ∧ s' = δ(s, σ')}. A strategy for a coalition $A \subseteq Agt$ in an RB-CGS[#] M is a mapping
 $E \sim S^+ \rightarrow 4at |A|$ such that for sygny $A \subseteq S^+$, $E_{\infty}(\lambda) \subseteq D_{\infty}(\lambda[1,1])$ $F_A: S^+ \to Act^{|A|}$ such that, for every $\lambda \in S^+$, $F_A(\lambda) \in D_A(\lambda[[\lambda]])$.
A computation λ is consistent with a strategy F_A ; iff, for all $i, 1 \leq$ A computation λ is consistent with a strategy F_A iff, for all $i, 1 \leq$ $i < |\lambda|, \lambda[i+1] \in out(\lambda[i], F_A(\lambda[1,i]))$. We denote by $out(s, F_A)$ the set of all computations λ starting from s that are consistent with F_A . Given a bound $b \in \mathcal{B}$, a computation $\lambda \in out(s, F_A)$ is b-consistent with F_A iff, for every $i \ge 0$, for every $a \in A$, b_a – $\sum_{j=0}^{j=i-1} c(F_a(\lambda[0,j])) \geq c(F_a(\lambda[0,i])).$
A computation λ is h-maximal for

A computation λ is b-maximal for a strategy F_A if it cannot be extended further while remaining b-consistent. The set of all maximal computations starting from state s that are b-consistent with F_A is denoted by *out* (*s*, F_A , *b*).

Given an RB-CGS# M and a state s of M , the truth of an RB \pm ATL# formula ϕ with respect to M and s is defined as follows (omitting the cases for propositions, \neg and \wedge):

- $M, s \models \langle \langle A^b \rangle \rangle \langle \rangle \phi$ iff \exists strategy F_A such that for all b-maximal $\lambda \in \text{out}(s, F, b) \setminus \{1\} \geq 2$ and $M, \lambda[2] \models \phi$. $\lambda \in out(s, F_A, b) : |\lambda| \ge 2$ and $M, \lambda[2] \models \phi;$
- $M, s \models \langle \langle A^b \rangle \rangle \phi \mathcal{U} \psi$ iff \exists strategy F_A such that for all b-
maximal $\lambda \in \mathcal{U}$ $\{f, h\}$ $\exists i$ such that $1 \le i \le |\lambda|$. M $\lambda[i]$ \models maximal $\lambda \in out(s, F_A, b)$, ∃i such that $1 \le i \le |\lambda|$: $M, \lambda[i] \models$ ψ and M , $\lambda[j] \models \phi$ for all $j \in \{1, \ldots, i-1\}.$
- $M, s \models \langle A^b \rangle \phi \mathcal{R} \psi$ iff \exists strategy F_A such that for all b-
maximal $\lambda \in \mathcal{S}$ and (s, k) either $\exists i$ such that $1 \le i \le | \lambda |$. maximal $\lambda \in out(s, F_A, b)$, either ∃i such that $1 \le i \le |\lambda|$: $M, \lambda[i] \models \phi \text{ and } M, \lambda[j] \models \psi \text{ for all } j \in \{1, \ldots, i\}; \text{ or,}$ $M, \lambda[j] \models \psi$ for all j such that $1 \le j \le |\lambda|$.

The following theorem is proved by demonstrating a model-checking algorithm for $RB \pm ATL^{\#}$, see [\[4\]](#page-2-19):

THEOREM 2.2. The model-checking problem for $RB \pm ATL^{\#}$ is decidable in PSPACE (under unary encoding).

3 RB \pm ATL#_{*R*}

In this section, we study RB \pm ATL $_{iR}^{\#}$, RB \pm ATL $^{\#}$ with imperfect
information and perfect recall. To model imperfect information. information and perfect recall. To model imperfect information, RB-CGS[#] are extended with an indistinguishability relation \sim_a on states, for every agent a. This relation can be lifted to finite sequences of states. Strategies under imperfect information should be uniform: if agent a is uncertain whether the history so far is λ or λ^r ($\lambda \sim_a \lambda^r$), then the strategy for a should return the same
action for both λ and λ^r . $F(\lambda) = F(\lambda^r)$. A strategy F_k for a group action for both λ and λ' : $F_a(\lambda) = F_a(\lambda')$. A strategy F_A for a group of agents A is uniform if it is uniform for every agent in A. In what follows, we consider strongly uniform strategies [\[22\]](#page-2-20), that require the existence of a uniform strategy from all indistinguishable states:

• $M, s \models \langle \langle A^b \rangle \rangle \bigcirc \phi$ under strong uniformity iff there exists a uniform strategy F_{L} such that for all s'_{L} surhere $a \in A$ uniform strategy, F_A , such that, for all s' \sim_a s where $a \in A$, for all $\lambda \in out(c', F, h)$ | $\lambda \ge 1$ and M λ [2] $\vdash a$ for all $\lambda \in out(s', F_A, b), |\lambda| > 1$ and $M, \lambda[2] \models \phi$.

The truth definitions for $\langle (A^b)^b \rangle \phi \not\sim (A^b)^b \phi \not\sim (\phi^b)^b \phi \not\sim (\phi^b)^c \psi$ are also modified to require the existence of a *uniform* strategy from all states s'
indictinguishable from s by any $a \in A$ indistinguishable from s by any $a \in A$.

THEOREM 3.1. The model-checking problem for $RB \pm ATI^{\#}_{iR}$ is independent conditional matrix encoding). decidable in EXPSPACE (under unary encoding).

4 RAL[#]

RAL[#] is obtained by modifying the definition of RAL [\[13\]](#page-2-18) for the diminishing resource setting. The sets Aqt , Res, and Π are as before. An endowment (function) η : Agt \times Res $\rightarrow \mathbb{N}$ assigns resources to agents: $\eta_a(r) = \eta(a, r)$ is the amount of resource agent a has of resource type r. En denotes the set of all possible endowments. Formulas of $\overline{\text{RAL}}^{\#}$ are defined by:

$$
\phi, \psi ::= p \mid \neg \phi \mid \phi \land \phi \mid \langle \langle A \rangle \rangle_B^{\downarrow} \bigcirc \phi \mid \langle \langle A \rangle \rangle_B^{\eta} \bigcirc \phi \mid \langle \langle A \rangle \rangle_B^{\downarrow} \phi \mathcal{U} \psi \mid
$$

$$
\langle \langle A \rangle \rangle_B^{\eta} \phi \mathcal{U} \psi \mid \langle \langle A \rangle \rangle_B^{\downarrow} \phi \mathcal{R} \psi \mid \langle \langle A \rangle \rangle_B^{\eta} \phi \mathcal{R} \psi
$$

where $p \in \Pi$, $A, B \subseteq Agt$, and $\eta \in$ En. Unlike in $RB \pm ATL^{\#}$, in $RAL^{\#}$
there are true true of as an entire modelling $\#A \mathbb{R}^{\#}$. there are two types of cooperation modalities, $\langle \langle A \rangle \rangle_B^{\downarrow}$ and $\langle \langle A \rangle \rangle_B^{\eta}$. In hoth cases, the actions performed by agents in $A \cup B$ consume and both cases, the actions performed by agents in $A \cup B$ consume and produce resources (actions by agents in $A \alpha \cup B$) do not change produce resources (actions by agents in $Agt \ (A\cup B)$ do not change their resource endowment). The meaning of $\langle\langle A \rangle\rangle_B^{\eta} \varphi$ is otherwise the same as in RB \pm ATL[#]. The formula $\langle\langle A \rangle \rangle_B^{\downarrow} \varphi$ requires that the strategy uses the requires *currently* available to the agents strategy uses the resources *currently* available to the agents.

The models of RAL^* are $RB\text{-}CGS^*$. Strategies are also defined as for $RB \pm ATL^*$. However, to evaluate formulas with a down arrow, such as $\langle A \rangle_B^{\downarrow} \bigcirc \varphi$, we need the notion of *resource-extended*
computations A *resource-extended* computation $\lambda \in (S \times Fn)^+$ is a computations. A resource-extended computation $\lambda \in (S \times En)^+$ is a sequence over $S \times En$ such that the restriction to states (the first sequence over $S \times$ En such that the restriction to states (the first component), denoted by $\lambda|_S$, is a path in the underlying model. The projection of λ to the second component is denoted by $\lambda|_{En}$. A (η, s_A, B) -computation, λ , is a resource-extended computation iff for all $i = 1, \ldots$ with $\lambda[i] := (s_i, \eta^i)$ there is an action profile $\sigma \in d(i)$ such that $\sigma \in d(\lambda | S[i])$ such that:

- $\eta^0 = \eta$ (η describes the initial resource distribution);
• $F_{\lambda}(\lambda|\eta|1/\lambda) = \pi_{\lambda}(\lambda)$ follow their strategy).
- $F_A(\lambda|_S[1, i]) = \sigma_A(A)$ follow their strategy);
- $\lambda |_{S}[i + 1] = \delta(\lambda |_{S}[i], \sigma)$ (transition according to σ);
- for all $a \in A \cup B$: $\eta_a^i \ge c(\lambda | S[i], \sigma_a)$ (each agent has enough resources to perform its action). resources to perform its action);
- for all $a \in A \cup B$: $\eta_a^{i+1} = \eta_a^i c(\lambda | S[i], \sigma_a)$ (resources are undated). updated);
- for all $a \in Agt \setminus (A \cup B)$ and $r \in Res: \eta_a^{i+1}(r) = \eta_a^i(r)$ (the resources of graphs not in $A \cup B$ do not change) resources of agents not in $A \cup B$ do not change).

 $out(s, \eta, F_A, B)$ is the set of all (η, F_A, B) -computations starting in s. The truth definition is given with respect to a model, a state, and an endowment η :

• $M, s, \eta \models \langle \langle A \rangle_B^{\downarrow} \bigcirc \varphi$ iff there is a strategy F_A for A such that for all $\lambda \in out(s, n, F_A, B)$. $|\lambda| > 1$ and M. $\lambda |s[2], \lambda |s_n[2] \models \varphi$ for all $\lambda \in out(s, \eta, F_A, B), |\lambda| > 1$ and $M, \lambda|_{S}[2], \lambda|_{En}[2] \models \varphi$

and similarly for $\langle (A) \rangle_B^{\perp} \varphi \mathcal{U} \psi$ and $\langle (A) \rangle_B^{\perp} \varphi \mathcal{R} \psi$. The cases for $\langle (A) \rangle_B^{\perp} \varphi$ φ , $\langle \langle A \rangle \rangle_B^{\zeta} \varphi \mathcal{U} \psi$, $\langle \langle A \rangle_B^{\zeta} \varphi \mathcal{R} \psi$ quantify over $\lambda \in out(s, \zeta, F_A, B)$.

THEOREM 4.1. The model-checking problem for $RAL^{\#}$ is decidable in PSPACE (under unary encoding).

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