1	Year-round performance assessment of a ground source heat
2	pump with multiple energy piles
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6	
7	ABSTRACT
8	The year-round performance of a ground source heat pump (GSHP) with multiple energy piles (EPs) is
9	investigated in this study based on a 3D transient heat transfer model. The GSHP heating and cooling capabilities
10	are simulated and assessed according to thermal energy demands of an air conditioned domestic building, its
11	coefficients of performance (COPs) obtained from numerical analyses and experimental tests are compared and
12	the largest difference between them is less than 8%. The maximum heating and cooling COPs of the GSHP are
13	3.63 and 4.73 respectively in the first year operation period, and the soil final temperature is lower than its initial
14	temperature, therefore the soil is not capable of recovering by itself due to the building unbalanced heating and
15	cooling loads. Finally, the effects of the soil thermal properties on its temperature and the GSHP COPs are
16	investigated and compared between the first year and tenth year operations, and it is found that the soil with low
17	volumetric heat capacity and high thermal conductivity could achieve a quick temperature recovery.
18	Keywords: Energy piles, GSHP, Ground heat extraction/injection, Soil thermal property, COPs
19	
20	1 Introduction
21	Shallow geothermal energy is one of the most popular renewable energy sources for efficient building air
22	conditioning with GSHP. A typical GSHP system is presented in Fig.1, which consists of three main components:
23	(i) ground heat exchanger (GHE), (ii) heat pump and (iii) ventilation system [1]. In winter, soil temperature is
24	higher than the mean ambient air temperature, and therefore the soil can be used as a heat source for space heating;
25	however, in summer, its temperature is lower than the average outdoor air's and the soil can be adopted as a heat
26	sink for space cooling. Thereby soil temperature is a very important parameter and should be clarified for
27	designing GHE, which is decided by the geographic location and regional climate condition. Numerous

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28 approaches have been developed to predict soil temperature, such as numerical [2, 3], analytical and semi-29 empirical [4-5], statistical and purely empirical methods [6]. Mihalakakou et al. [2] proposed a 3D transient numerical heat transfer model to assess the soil temperatures at different depths under a building foundation, and 30 31 got a very good agreement between numerical results and measurement data, the maximum soil temperature difference between them is less than 0.3 °C. Zoras et.al [3] developed a numerical response factor method to 32 33 simulate soil temperature variation under a normal square slab-on-ground floor, and found that the method precision relies on the depth of grid nodes regarding the time required for heat waves to penetrate at their locations. 34 35 Droulia et al. [4] calculated the subsurface soil temperature profile based on analytical and semi-empirical models, 36 and discovered that the semi-analytical approach only needs daily mean soil or air temperature, while the 37 analytical solution does not require any data at all. Elias et al. [5] studied soil temperature distribution by an 38 exponential-sinusoidal analytical model and compared their results with the analytical solution data, and found that the maximum soil temperature error is 0.3 °C at a depth of 0.1 m. Zheng et al. [6] presented a normal 39 40 methodology to calculate daily soil temperature based on the ambient air temperature and precipitation statistical 41 data, and examined soil temperature distribution under vegetation cover by the Leaf Area Index (LAI). Their results demonstrate that soil temperature under vegetation cover at regional and continental scales can be decided 42 43 through LAI. It is essential to sustain high soil temperature surrounding the GHE for good performance, so several 44 techniques are adopted to manipulate geothermal energy system design based on theoretical models [7-9]. Li and 45 Lai [10] developed analytical model targeting on heat conduction in infinite anisotropic and semi-infinite media, 46 and concluded that the anisotropy of the medium has little impact on the short time performance of GHE, while it has obvious effect on the long-term temperature response. Notably, soil thermal property is another vital factor 47 affecting ground heat transfer. Casasso and Sethi [11] descripted that soil thermal conductivity is a key source of 48 49 uncertainty when modelling the GSHPs. Their results reveal that a fluid temperature difference of 5.66 °C and 50 heat pump energy consumption difference of 12.5% exist for soil thermal conductivity difference of 1.5 W/(m·K). Lee [12] studied the impact of vertical heterogeneities of the soil thermal conductivity, and found that the adoption 51 52 of depth-averaged thermal parameters is appropriate.







Fig. 1. A typical GSHP system [1].

55 The amount of heat extracted/rejected from/to the soil in the GSHP system relies on building heating/cooling load. Correspondingly, the GHE should have the ability to meet the building thermal energy requirement. Over the 56 57 years, various analytical and numerical vertical GHE models have been proposed and utilized as the design tools, 58 which are also used to estimate the working fluid temperature in the GHE for thermal performance evaluation. 59 Moch et al. [13] developed two 2D axisymmetric analytical models to analyse thermal interaction between the soil and a helical BHE, and found that thermal properties of the soil have a significant influence on sizing the 60 geothermal installation. Al-Khoury et al. [14-16] proposed a 3D numerical model depicting thermal interactions 61 among inlet-pipe, outlet-pipe and grout. Their model addresses the formulation equilibrium, effects of thermal 62 resistance and finite element method (FEM) discretization. Ozudogru et al. [17] suggested a 3D numerical model 63 64 for vertical GHE based on FEM for simulating two cases, namely, an EP with double U-tubes and a BHE with a 65 single U-tube, and demonstrated that the model can be successfully used to predict vertical BHE and EPs 66 performances with different sizes and loop configurations.

Recently, EPs have received more attention, because a GSHP with EPs is one of the most effective strategies for building air conditioning [18, 19], thereby a number of research works have been implemented on its thermal characteristics [20-24]. Olgun et al. [1] analysed 30-year operation characteristics of EPs to evaluate the longterm performance with balanced and unbalanced heating loads under different climatic conditions, and discovered temperature variation of the soil surrounding an EP mainly depends on the seasonal energy requirement. Gashti et al. [25] proposed a 3D numerical heat transfer model based on finite element theory to assess the performance of steel pile foundations by Comsol Multiphysics package. Their study results show that temperature difference

between the pile wall and inlet fluid is around 25–33%, and there is a big temperature fluctuation near the tube 74 75 curve at the EP end. Li et al. [26] simulated the soil temperature surrounding an EP, and deduced that the influence of pile thermal load on the soil temperature decreases with radial distance. Capozza et al. [27] investigated the 76 77 long-term and seasonal behaviours of a GSHP unit by CaRM simulation tool to figure out unbalanced thermal load profiles for two office buildings in Italy, and found that the soil temperature depends mainly on the annual 78 79 heating and cooling loads. Kim et al. [28] used TRNSYS program to assess the performance of a GSHP system with vertical BHEs, and discovered that the COPs of heating and cooling could be individually improved by up 80 81 to 25.2% and 15.1% with a systematic approach. Darkwa et al. [29] studied the long-term performance of a single 82 BHE, and presented that the yearly mean thermal energy rejected into the BHE is approximately 4.5 times more 83 than the amount extracted. Pasquier and Marcotte [30] developed a quasi-3D numerical model for a single BHE 84 as well, and considered thermal capacitances of both the grouting material and working fluid. Their results 85 illustrate that the error of the working fluid temperature is lower than the measurement uncertainty. Retkowski 86 and Thöming [31] presented a mixed-integer nonlinear programming method to minimize the year-round running 87 cost of vertical BHE system, but thermal interaction between BHEs is not considered. Lee et al. [32] compared the transient performance features between a hybrid GSHP using a heat storage bath and a pure one, and found 88 89 that the mean COP of the hybrid GSHP system is around 7.2% higher than that of the pure one at the optimum 90 operating condition. Kurevija et al. [33] analysed the long-term thermal disturbance between boreholes in Zagreb 91 using the g-functions, and adopted a constant energy efficiency for heat pump unit. Ghoubali et al. [34] 92 investigated a heat pump performance with simultaneous domestic hot water heating, space heating and cooling functions using TRNSYS software under three different weather conditions in France, and a maximum seasonal 93 COP of 2.28 is achieved. Kizilkan and Dincer [35] deduced exergy and energy assessments of a GSHP system in 94 Ontario, Canada, and found that the system performance in cooling mode is slightly lower than that in heating 95 96 mode. Zhao et al. [36] developed a 3D transient model to investigate thermal behaviours of different GHEs, such as, U-shaped, W-shaped and spiral-shaped. Their numerical results present that the spiral-shaped GHE provides 97 98 the lowest temperature working fluid under the same initial and boundary conditions. Luo et al. [37] carried out 99 numerical and experimental studies of a GSHP with four different kinds of GHEs including double-U, triple-U, double-W and spiral-shaped under an intermittent operating condition, and found that the double-U type has the 100 101 lowest energy performance and its thermal efficiency only accounts for 67~69% that of the spiral or double-W category. Hamada et al. [38] studied the field performance of a GSHP with EP system, and discovered that the 102 system heat output accounts for around 90% of the predicated value and the mean COP for space heating is 3.9. 103

Currently, there is a need to fill the research gap in studying the multiple EPs year-round performance with consideration of "thermal short-circuiting" and soil thermal property effects, even though few mathematical models focusing on heat transfer in the shallow EPs have been produced. The objectives of this paper are to investigate the year-round performance of a GSHP with multiple EPs and identify the influence of soil thermal property. In this study, a 3D numerical model is used to discretize the EP components and working fluid along the U-tube pipe for accurate representation of heat transfer procedure, heat extraction and injection capacities are calculated through C code.

111 2 Numerical model

114

An existing 3D transient heat transfer numerical model based on finite volume method (FVM) [39] is adopted in
this study, the effect of "thermal short-circulating" between two pipes of a U-tube in EP is taken into account, and

the initial and boundary conditions are established. Thermal partial differential equations of the model are

discretized at spatial nodal points and solved by linear approximation method. The major elements in heat transfer

116 process are the nearby soil, concrete piles, polyethylene U-tube pipes and working fluid. In order to develop a full

117 3D transient heat transfer model, the simplifying assumptions in this study are made as follows:

1) The ground is regarded as a homogeneous medium with mean thermal physical properties.

119 2) Initial soil surface temperature is assumed as the undisturbed ground surface temperature.

- 3) Heat transfer in the solid region is regarded as pure heat conduction and the effect of groundwater flow isnegligible.
- 122 4) A profile of velocity in U-tube pipe is uniform.

123 In terms of the working fluid flow region, energy equations of the inlet and outlet pipes are setup separately

- 124 because of the different flow directions.
- 125 2.1 Mathematical equations
- 126 For heat transfer analysis, the EP is classified into two regions: solid and fluid regions.
- 127 2.1.1 Energy balance in solid region
- 128 The solid region includes soil, grout and pipe, where heat transfer is regarded as 3D transient heat conduction.
- 129 The soil is divided into one hundred (100) layers in the vertical direction in order to interpret the fluid temperature
- 130 variation. Therefore, energy balance equation of the soil domain is given as:

131
$$\rho_{\text{soil}} c_{\text{soil}} \frac{\partial T_{\text{s}}}{\partial t} = \frac{\partial}{\partial x} (k_{\text{soil}} \frac{\partial T_{\text{s}}}{\partial x}) + \frac{\partial}{\partial y} (k_{\text{soil}} \frac{\partial T_{\text{s}}}{\partial y}) + \frac{\partial}{\partial z} (k_{\text{soil}} \frac{\partial T_{\text{s}}}{\partial z})$$
(1)

132 Grout as heat transfer medium in EP has high thermal conductivity and storage capacity. Hence, energy balance

equation of the backfill material (grout) domain is given as:

134
$$\rho_{\text{grout}} c_{\text{grout}} \frac{\partial T_{\text{g}}}{\partial t} = \frac{\partial}{\partial x} (k_{\text{grout}} \frac{\partial T_{\text{g}}}{\partial x}) + \frac{\partial}{\partial y} (k_{\text{grout}} \frac{\partial T_{\text{g}}}{\partial y}) + \frac{\partial}{\partial z} (k_{\text{grout}} \frac{\partial T_{\text{g}}}{\partial z})$$
(2)

135 Heat transfer through the pipe is treated as pure heat conduction as well, and defined as 3D heat conduction versus

time. Thus, the corresponding energy conservation equation can be written as:

137
$$\rho_{\text{pipe}} c_{\text{pipe}} \frac{\partial T_{\text{p}}}{\partial t} = \frac{\partial}{\partial x} (k_{\text{pipe}} \frac{\partial T_{\text{p}}}{\partial x}) + \frac{\partial}{\partial y} (k_{\text{pipe}} \frac{\partial T_{\text{p}}}{\partial y}) + \frac{\partial}{\partial z} (k_{\text{pipe}} \frac{\partial T_{\text{p}}}{\partial z})$$
(3)

Where ρ_{soil} , ρ_{grout} and ρ_{pipe} are densities of soil, grout and pipe (kg/m³) respectively; c_{soil} , c_{grout} and c_{pipe} are thermal capacities of soil, grout and pipe (J/kg·K), respectively; k_{soil} , k_{grout} and k_{pipe} are thermal conductivities of soil, grout and pipe (W/m·K), respectively; T_s, T_g and T_p are temperatures of soil, grout and pipe (°C), respectively; t is time (s).

142 2.1.2 Energy balance in fluid region

143 Heat convection occurs between the pipe and working fluid, the average temperature of the upward flow fluid is

- equal to that of the downward flow fluid, so $V_1 = -V_2 = (-) V_1$.
- 145 The fluid in the inlet pipe (downward flow) can be modelled as:

146
$$\rho_{\text{fluid}} c_{\text{fluid}} \frac{\partial T_{\text{inlet}}}{\partial t} + (\rho c v)_{\text{f}} \frac{\partial T_{\text{inlet}}}{\partial z} = k_{\text{fluid}} \frac{\partial^2 T_{\text{inlet}}}{\partial z^2} + b_{\text{ig}} (T_{\text{grout}} - T_{\text{inlet}})$$
(4)

147 Similarly, the fluid in the outlet pipe (upward flow) is modelled as:

148
$$\rho_{\text{fluid}} c_{\text{fluid}} \frac{\partial T_{\text{outlet}}}{\partial t} + (\rho c v)_{\text{f}} \frac{\partial T_{\text{outlet}}}{\partial z} = k_{\text{fluid}} \frac{\partial^2 T_{\text{outlet}}}{\partial z^2} + b_{\text{og}} (T_{\text{grout}} - T_{\text{outlet}})$$
(5)

149 Where, ρ_{fluid} is density of working fluid (kg/m³); c_{fluid} is thermal capacities of working fluid (J/kg·°C); k_{fluid} is 150 thermal conductivity of working fluid (W/m·K); T_{inlet} and T_{outlet} are inlet and outlet fluid temperatures (°C), 151 respectively; b_{ig} is reciprocal of thermal resistance R_{ig} between inlet pipe and grout (W/m²·K); and b_{og} is reciprocal 152 of thermal resistance R_{og} between outlet pipe and grout (W/m²·K).

153 2.2 Multiple EPs model

The single EP has limited heat transfer capacity, so the EP system is normally designed with multiple piles. One arrangement of multiple EPs is shown in Fig.2, sixteen EPs are installed in rectangular shape. A 3D FVM model using a rectangular coordinate system [39] is applied for the EPs performance assessment. The entire soil volume is discretized and each EP is represented by a square column circumscribed by the borehole radius. The soil and working fluid temperatures within the EPs are worked out simultaneously by using an iterative approach. The simulated region is discretized as a finite number of contiguous non-overlapping cell cubes. A black cube (P point) in Fig.2 (e) is regarded as the control volume and its six neighboring nodes are identified as west, east, south,

- 161 north, top and bottom in which the corresponding cell faces are denoted by w, e, s, n, t' and b respectively, while
- 162 ϕ , ω , j represent a nodal point in direction of x, y and z axes, respectively.



Fig. 2. Schematic diagram of discretised model: (a) 3D multiple EPs model; (b) 3D single EP model; (c) top
discretised cross-section of single model; (d) top discretised cross-section of multiple EPs model; (e) arbitrary
cube cell [39].

167 Integration of Eqs. (1) - (5) over the control volume and a time interval from t to $(t + \Delta t)$ gives

$$168 \qquad \int_{CV} \left[\int_{t}^{t+\Delta t} \rho c \frac{\partial T}{\partial t} dt \right] dV = \int_{t}^{t+\Delta t} \left[(kA \frac{\partial T}{\partial x})_e - (kA \frac{\partial T}{\partial x})_w \right] + \int_{t}^{t+\Delta t} \left[(kA \frac{\partial T}{\partial y})_n - (kA \frac{\partial T}{\partial y})_s \right] + \int_{t}^{t+\Delta t} \left[(kA \frac{\partial T}{\partial z})_{t'} - (kA \frac{\partial T}{\partial z})_b \right]$$
(6)

Where, A is surface area of the control volume, CV is its control volume. Thereby, the left side of the volumeintegral of the temporal derivative can be written as

171
$$\int_{CV} \left[\int_{t}^{t+\Delta t} \rho c \frac{\partial T}{\partial t} dt \right] dV = \rho c (T_{p} - T_{p}^{0}) \Delta V$$
(7)

172 Where, $\frac{\partial T}{\partial t} = \frac{1}{\Delta t} (T_p - T_p^0)$, this term has been discretised by a first-order (backward) differencing scheme, in

173 which T_P^0 is value of T at time t and T_P is value at time (t+ Δ t), with Δ t is time step, and Δ V=dxdydz.

174 The fully implicit discretisation method is applied to this proposed model, thereby the value of ε is set equal to 1.

175
$$I_{\rm T} = \int_{t}^{t+\Delta t} T_{\rm p} dt = [\varepsilon T_{\rm p} + (1-\varepsilon)T_{\rm p}^0]\Delta t$$
(8)

176 2.3 Initial and boundary conditions

177 Cecinato and Loveridge [40] illustrated that the hetero-thermal zone should be accounted for EP design. The

ground temperature is a sinusoidal wave function of time and depth, and can be expressed as [41, 42]:

179
$$T_{soil}(Z, t_{year}) = T_{mean} - T_{amp} \cdot exp(-Z \times \sqrt{\frac{\pi}{365}}) \cdot cos[\frac{2\pi}{365} \cdot (t_{year} - t_{shift} - \frac{Z}{2} \times \sqrt{\frac{365}{\pi \cdot \alpha}})]$$
 (9)

180 Where T_{soil} (Z, t_{year}) is undisturbed ground temperature at time (t) and depth (Z) (°C); T_{mean} is mean surface 181 temperature (average air temperature) (°C); T_{amp} is amplitude of surface temperature [(maximum air temperature 182 – minimum air temperature)/2] (°C); Z is depth below the surface (surface=0) (m); α is thermal diffusivity of soil 183 (m²/day); t_{year} is current time (day); t_{shift} is day of the year when the coldest air temperature occurs (day).

Boundary conditions are classified into two categories, the first is expressed in terms of temperature at the boundary while the second is presented in terms of temperature gradient. In the case of the first boundary condition, at z = 0, the inlet pipe temperature is equal to the fluid temperature:

187
$$T_{inlet}(0,t) = T_{fluid}(t)$$
 (10)

188 In terms of the second boundary condition, at z = 0, heat flux at the exit of outlet pipe is depicted as:

189
$$\frac{\partial T_{\text{outlet}}(0,t)}{\partial z} = 0 \tag{11}$$

190 2.4 COPs of heat pump

A vapour-compression heat pump model is used in this study and its parametric model reflecting the effect ofcompressor rotation speed is adopted [43].

193
$$m_{\rm r} = V_{\rm c} \omega \rho_{\rm r,suc} \cdot \left[1 + C_{\rm v} \left(1 - \frac{P_{\rm r,cond}}{P_{\rm r,evap}}\right)^{\frac{1}{n}}\right]$$
(12)

194
$$\Delta \xi_{\text{comp}} = \xi_{\text{r,dis}} - \xi_{\text{r,suc}} = \frac{n}{n-1} \cdot \frac{P_{\text{r,evap}}}{\rho_{\text{r,suc}}} \cdot \left[\left(\frac{P_{\text{r,cond}}}{P_{\text{r,evap}}} \right)^{\frac{n-1}{n}} - 1 \right]$$
(13)

195
$$Q_{el} = \frac{m_r \Delta h_{comp}}{\eta_{comp}}$$
(14)

196 Where, m_r is refrigerant mass flow rate (kg/s); V_c is compressor swept volume (m³); ω is compressor rotational 197 speed (rev/s); $ρ_{r,suc}$ is compressor suction refrigerant density (kg/m³); C_v is compressor volumetric coefficient, P 198 is pressure (kPa); ξ is specific enthalpy (kJ/kg), n is polytropic compression coefficient; $η_{comp}$ is compressor 199 mechanical efficiency; Δξ is specific enthalpy change (kJ/kg); Q_{el} is electrical energy consumption (kW).

200 The COPs of heat pump are defined as:

$$201 \qquad \text{COP}_{h} = \frac{Q_{\text{heating}}}{Q_{\text{el}}}$$
(15)

$$202 \qquad \text{COP}_{c} = \frac{Q_{\text{cooling}}}{Q_{\text{el}}}$$
(16)

- $\label{eq:cooling} \text{Where } \text{COP}_{h} \text{ and } \text{COP}_{c} \text{ are heating and cooling } \text{COPs, respectively, } Q_{heating} \text{ and } Q_{cooling} \text{ are heating and cooling } Q_{cooling} \text{ are heating and } Q_{cooling} \text{ are heating and } Q_{cooling} \text{ are heating } Q_{cooling} \text{ are heating$
- 204 capacities (kW), respectively.
- 205 **3 Methodology**
- 206 3.1 Building and soil property
- The numerical model is used to investigate a GSHP performance in a two-storey residential building in the UK. The building with the total floor area of 144 m² is designed for one family of four persons, and its monthly heating and cooling energy requirements are shown in Fig.3 [44]. The maximum heating energy is 366 MJ, while the
- 210 minimum is 128 MJ. By contrast, the maximum cooling energy is 173 MJ and the minimum is 110 MJ.





Fig. 3. Monthly heating and cooling energy requirements.

As shown in Fig. 4, the ground consists of four geological layers: (1) the first layer, 0~2.22 m, is made of slightly sandy clay, light grey and very sandy slightly clay gravel; (2) the second layer, 2.22~3.3 m, consists of orange brown mottled grey black and coarse gravel; (3) the third layer, 3.33~5.5 m, is only very soft, red brown, slightly gravel; and (4) the forth layer, 5.5~10 m, is formed with very soft, red brown, slightly gravel clay.

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- 218

Profile	Depth	Material categories	Thermal conductivity	Density
	0~2.22m	Mixed gravel and coarse sand	1.30 W/(m·K)	2277 kg/m ³
	2.22~3.3m	Sand gravel	1.15 W/(m⋅K)	2094 kg/m ³
	3.3~5.5m	Slightly Gravel	1.68 W/(m·K)	2223 kg/m ³
	5.5~10m	Slightly Gravel Clay	1.75 W/(m·K)	2392 kg/m ³
		Weighted average	1.5 W/(m·K)	2260 kg/m ³



Fig. 4. The profile of the geological layers within a depth of 10 m [44].

221 3.2 Multiple EPs system

222 Total 16 EPs are utilized in this study and arranged in rectangular shape as shown in Fig. 2, the working fluid is

a mixture of glycol and water. Table 1 gives the EP parameters [44, 45].

Table 1 Characteristics of the EPs in the experimental system.

Description	Value
Fluid density	1035 kg/m ³
Fluid kinematic viscosity	$4.94 \text{x} 10^{-6} \text{ m}^2/\text{s}$
Fluid heat capacity	3795 J/(kg · K)
Fluid thermal conductivity	0.58 W/(m·K)
Pipe density	950 kg/m ³
Pipe heat capacity	2300 J/(kg · K)
Pipe outside diameter	0.032 m
Pipe inside diameter	0.013 m
Shank spacing	0.06 m
Grout thermal conductivity	2 W/(m · K)
Grout density	1860 kg/m^3
Grout heat capacity	840 J/(kg · K)
EP diameter	0.3 m
EP depth	10 m

225 3.3 Heat pump unit

The EPs are connected to a 5.9 kW Greenline HT Plus heat pump [44, 45] which produces hot water at a temperature range of 35 °C to 65 °C. Table 2 presents technical data of the Greenline HT Plus [46]. The indoor

- 228 air temperature is used to control the heat pump unit operation, and the set-points are 18 °C and 27 °C for heating
- and cooling respectively. The main parameters of the initial condition are shown in Table 3.

Table 2 Nominal specification of the heat pump [44].

Description	Value
Emitted /Supplied output at 0/35°C	5.9/1.3 kW
Emitted /Supplied output at 0/50°C	5.4/1.7 kW
Minimum flow heating medium	0.14 l/s
Nominal flow heating medium	0.20 l/s
Superheat	3 °C
Subcooling	4 °C
Refrigerant R407C mass flow rate	0.02 kg/s
Evaporating temperature (dew point)	-1 °C
Condensing temperature (dew point)	58.9 °C
Evaporating pressure	4.5 bar
Condensing pressure	24.7 bar

Table 3 Initial condition and basic parameters.

Description	Value
Initial ground surface temperature	10.4 °C
Soil body temperature (soil far field boundary)	15.0 °C
Soil bottom temperature	15.5 °C
Fluid inlet temperature	1.2 °C

233

234 3.4 Simulation program

235 The year-round operation process is divided into four periods according to the local climate conditions. The first is heating period from 05th/November/2007 to 30th/April/2008, the second is the first soil temperature natural 236 recovery period from 1st/May/2008 to 15th/June/2008, the third is cooling period from 16th/June/2008 to 237 15th/September/2008, and the last one is the second soil temperature natural recovery period from 238 16th/September/2008 to 4th/ November /2008. The flowchart of simulation program is presented in Fig.5. The 239 nodal temperature in the equivalent cube is calculated at each step until the time required for the fluid to flow 240 through the pile heat exchangers is reached. The related parameters including temperatures and heat transfer rates 241 242 are obtained in the process. After that, the program will output the simulation data if the results meet the precision requirement and stop, otherwise the time t will be iterated ($t = t + \Delta t$) and the simulation process starts again. 243 244

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- 246
- 247



254 4 Results and discussion

255 Before the numerical model is utilized to simulate the system performance, it needs to be validated at first. As mentioned in the previous paper [50], the numerical model has been verified by experimental data with less than 256 257 8% error. To further validate the numerical model, the experimental data of the heat pump unit in literature [46] are adopted, which are available from November/2007 to May/2008. Fig.6 illustrates the COP_h comparison 258 259 between the numerical results and experimental data in heating mode, the maximum error is 7.14 % noticed at the beginning of operating stage, and the average error is 6.34 %, thereby the simulation results are effectively 260 supported by the experimental data. Therefore, the 3D numerical model can be utilized to study the annual energy 261 262 performance of the GSHP with multiple EPs.









265 4.1 Heating period in the first year operation

The system heating performance is simulated and presented in Fig. 7. As can be seen from this figure, the system 266 267 is capable of meeting the building heating energy demand referring to Fig.3, the system daily thermal energy 268 outputs are lower during the first and last few days than those in the middle period. Notably, the system maximum daily thermal energy output is approximately 2037 MJ on the 116th day, and the minimum value is around 185 269 MJ on the 172nd day. The building daily internal mean temperatures are shown in Fig.8, it is found that the average 270 temperature of 18.9 °C in heating period is higher than the set value of 18 °C. On the other hand, during the middle 271 272 period of heating season, the system runs in the most of time so that the ground has no sufficient time to recover. 273 Hence, the ground temperature surrounding the EPs is relatively low, which leads to a low temperature working 274 fluid flowing into the heat pump evaporator, correspondingly a low COP. The maximum value of daily heat

- extracted from the soil is approximately 1382 MJ on the 116th day, and the minimum value is about 129.8 MJ on
- 276 the 172^{nd} day.



277 278

Fig. 7. Daily variations of thermal energy output in heating period.



279 280

Fig. 8. Daily variation of mean internal temperature in heating period.





Fig. 9. Daily variation of ground heat extracted in heating period.

283 4.2 Cooling period in the first year operation

The GSHP is able to meet the building cooling energy requirement (referring to Fig.3) throughout the first year operation period. As shown in Fig. 10, the system maximum daily cooling output is approximately 712 MJ on the 54th day, while the minimum is about 22.6 MJ on the 63rd day. Typically, the indoor temperature fluctuates within

an acceptable range during the system operation period as indicated in Fig. 11, it is found that the average indoor temperature of 25.4 °C in cooling period is lower than the set value of 27 °C because the system cooling output is larger than the building cooling load. Fig.12 descripts the daily variation of heat rejected into the ground. The maximum rejected heat is approximately 865.4 MJ on the 54th day, while the minimum value is about 27.5 MJ on the 63rd day.



293

Fig. 10. Daily variations of cooling energy output.





Fig. 11. Daily variations of internal temperature in cooling period.



296



Fig. 12. Daily variations of ground heat rejected in cooling period.

^{4.3} Soil temperature in the first year operation

- In this study, there are two periods used for soil natural recovery as mentioned in Section 3.4. The regression equation developed by Shang et al. [49] is adopted for predicting the soil temperature variation under natural recovery condition. The variations of soil temperature nearby the EPs (soil temperatures in all the diagrams are at
- 302 5 m depth underground) throughout the year are illustrated in Fig.13.



Fig. 13. Daily variations of soil temperature: (a) heating period; (b) the first soil natural recovery period; (c)
 cooling period; (d) the second soil natural recovery period.

The soil temperature decreases from 14.85 °C at the start to 10.81 °C in the heat extraction period, while it increases from 10.81 °C to 11.60 °C in the first soil natural recovery period. In terms of the heat rejection period, it can be seen that the soil temperature has a dramatically increase from 11.60 °C to 13.37 °C. In the subsequent period, the soil temperature decreases slowly from 13.37 °C to 12.59 °C. The final soil temperature of 12.59 °C is reached which is below its initial temperature of 14.85 °C as expected, therefore the soil has no ability to recover by itself due to the building unbalanced heating and cooling loads.

312 4.4 Heat pump electricity consumptions and COPs in the first year operation

Fig. 14 depicts electricity consumptions of GSHP unit during heating and cooling periods in the first year operation. It can be seen that electricity consumption gradually reduces when the heating/cooling load drops (referring to Fig. 3). The maximum daily electricity consumption in the heating period reaches approximately 665 MJ, the mean being 450 MJ, while the minimum is about 55 MJ. Obviously, the consumption in the cooling period 317 is far lower than that in the heating periods, the maximum value of electricity consumption is only around 153 MJ

318 on the 54th day, the mean being 70 MJ, while the minimum is about 4.9 MJ on the 63^{rd} day.



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Fig. 14. (a) Power consumption variation in heating period; (b) Power consumption variation in cooling period.



321 322

Fig. 15. Daily variations of COPs in the first year: (a) heating period; (b) cooling period.

The COP variations in the heating and cooling periods are described in Fig.15. The maximum value of COP_h is approximately 3.63, the average being 3.41, while the minimum reaches around 3.11. By contrast, the maximum value of COP_c is approximately 4.73, the average being 4.64, while the minimum is around 4.44. Some previous studies have presented the similar COP variations. For example, the seasonal COP_h of a GSHP in Venice, Italy, is 4 and its COP_c is 4.2 in literature [21]. Additionally, the COP range of 3.85 to 4.20 is achieved by a GSHP system in Hong Kong [50]. The monthly COP is investigated through experiment in literature [51], the mean values of 3.03 and 4.33 are presented for heating and cooling respectively.

330 4.5 Performance in the tenth year

Fig.16 illustrates the system mean heating and cooling energy outputs for the tenth year operation. Notably, the system is still capable of meeting the building heating and cooling requirements. In order to make the soil full recovery, the extra energy should be provided, for example, hot water from a solar collector can be circulated through the EPs to recharge the ground, thereby ameliorating the whole system performance. Fig.17 presents the COP variations for the tenth year operation. The maximum COP_h over the heating period is approximately 3.21, the average being 2.82, while the minimum reaches around 2.47. By contrast, the maximum COP_c is



approximately 4.40, the average being 4.31, while the minimum is around 4.08.



Fig. 16. Daily variations of mean energy output in the tenth year: (a) heating period; (b) cooling period.





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Fig. 17. Daily variations of COPs for the tenth year: (a) heating period; (b) cooling period.

342 4.6 Influence of soil thermal property

Soil is typically stratified with different materials, including sand, clay, rock and so on. In order to analyze the soil temperature variation surrounding the EPs, gravel, pebbly clay and mild clay are selected as the representatives, their properties, such as volumetric heat capacity, thermal conductivity and diffusivity, are given in Table 4.

	Soil type	Volumetric heat capacity MJ/(m ³ ·K)	Thermal Conductivity W/(m·K)	$\begin{array}{l} \mbox{Thermal diffusivity} \\ (m^2/s) \times 10^{-6} \end{array}$
	Gravel	2.48	1.50 ~1.70	0.50
	Pebbly Clay	2.68	1.42	0.73
_	Mild Clay	3.45	0.96~1.36	0.78

Table 4 Soil thermal properties.

348

Fig. 18 displays the soil temperature variations surrounding the EPs for the first year operation period. The soil temperature variations have the similar tendencies, and are relatively small. In terms of the mild clay, heat extraction for 180 days brings approximately 4.10 °C temperature decrease (from 14.58 °C to 10.48 °C), while for the pebbly clay, the temperature reduction is around 4.09 °C (from 14.72 °C to 10.63 °C), the similar situation

for the gravel, the temperature drops about 4.04 °C (from 14.85 °C to 10.81 °C). During the continuous heat 353 354 rejection period, the gravel, pebbly clay and mild clay temperatures rise 1.77 °C, 1.74 °C and 1.67 °C, respectively. As for the first natural soil recovery period, it can be seen from Fig.18 (b) that the gravel, pebbly clay and mild 355 356 clay temperatures increase 0.79 °C, 0.74 °C and 0.72 °C respectively. By contrast, during the second natural soil recovery period, their temperatures decrease 0.77 °C, 0.79 °C and 0.82 °C individually. When the first year 357 operation is completed, the gravel, pebbly clay and mild clay temperatures decrease 2.26 °C, 2.27 °C and 2.3°C 358 respectively compared with their initial temperatures. It is found that the gravel with relatively low volumetric 359 heat capacity and high thermal diffusivity makes thermal energy migrate quickly, and the mid clay with low 360 thermal conductivity and high volumetric heat capacity can store more energy. As a result, it can be deduced that 361 362 the soil with high thermal conductivity and low volumetric heat capacity has the ability to recover quickly.







Fig. 19 presents the mean soil temperature variations in the tenth year operation. The gravel, pebbly clay and mild clay temperatures decrease 4.02 °C, 4.05 °C and 4.07 °C respectively in the heat extraction period. For the heat rejection period, the soil temperatures of the three soil types rise 1.77 °C, 1.83 °C and 1.89 °C individually. As for the two natural soil recovery periods, the gravel, pebbly clay and mild clay temperatures rise 0.79 °C, 0.73 °C and 0.68 °C respectively at the end of the first period, while at the end of the second recovery period, their temperatures reduce 2.25 °C, 2.26 °C and 2.29°C individually. Finally, the gravel, pebbly clay and mild clay temperatures could reach 7.92 °C, 7.73 °C and 7.50 °C individually at the end of the tenth year operation. Fig. 20 gives the mean COPs of the first year and tenth year operations, it can be seen that the tenth year COP_h , in terms of the mild clay, pebbly clay and gravel, reduce 19.28%, 18.64% and 17.30% respectively compared with that of the first year's. Similarly, the tenth year COP_c reduce 9.17%, 8.37% and 7.11% individually for the three soil types. This is because the soil is not capable of recovering by itself. As a result, the auxiliary system, such as solar collector, has to be adopted to charge the ground in this case.





Fig. 19. Soil temperature variation in mild clay, pebbly clay and gravel in the tenth year operation.







381 5 Conclusions

The year-round performance of a GSHP with multiple EPs system is simulated through a 3D transient heat transfer numerical model. Sixteen concrete piles are utilized for heat exchange with soil in this study, which have a depth of 10 m. A 5.9 kW nominal heat pump is connected with the EPs, which is used to provide heating and cooling

- for a typical low-energy home. The soil temperature variations under different operation conditions are investigated as well. The following conclusions are obtained:
- (1) In the first year operation, the maximum heat output of the heat pump is 2037 MJ while the minimum is 185
 MJ, and the maximum cooling output is 712 MJ and the minimum is 22.6 MJ.
- 389 (2) The maximum heat extraction from the ground is 1382 MJ in the first year operation while the minimum is
- 390 129.8 MJ, and the maximum heat rejection into the ground is 865.4 MJ and the minimum is 27.5 MJ.
- 391 (3) The soil is not capable of recovering by itself because of the building unbalanced heating and cooling loads.
- 392 (4) The maximum electricity consumption reaches 665 MJ in the first year heating period, while the maximum
 393 electricity consumption in the first year cooling period is only 153 MJ.
- (5) In the first year operation, the maximum COP_h is 3.63, the average being 3.40, and the minimum is 3.11; the
- $maximum COP_c$ is 4.73, the average being 4.63, and the minimum reaches 4.44. By contrast, in the tenth year
- operation, the maximum COP_{h} is 3.21, the average being 3.82, and the minimum is 2.47; the maximum COP_{c} reaches 4.40, the average being 4.31, while the minimum is 4.08.
- (6) The soil temperature order from high to low is gravel, pebbly clay and mild clay at the end of the first year
 operation. So the soil with high thermal conductivity and low volumetric heat capacity is more easily
 recovered.
- (7) The system tenth year performance is lower than the first year's, and its mean COP_h decrease 19.28%, 18.64%
 and 17.30% respectively for the gravel, pebbly clay and mild clay, while its average COP_c reduce 9.17%,
- 403 8.37% and 7.11% individually.
- 404 For the future research work, the effect of groundwater advection on the soil temperature will be investigated.

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Nomenclature		
A Area (m ²)		
b Reciprocal of thermal resistance		
c_p Heat capacity (J/(kg·K))		
d Diameter (m)		
C _v Volumetric coefficient of compressor		
h Heat transfer coefficient $(W/(m^2 \cdot K))$		
H Height (m)		
k Thermal conductivity (W/m·K)		
1 Length (m)		
m _r Refrigerant mass flow rate (kg/s)		
n Polytropic compression coefficient		
P Pressure (kPa)		
Q Energy capacity (kW)		
R Thermal resistance $(W/m^2 \cdot K)$		
V _c Swept volume of compressor (m ³)		
Greek Letters		
α Ground thermal diffusivity (m ² /day)		
Δd Shank spacing (m)		
Δh Specific enthalpy change (kJ/kg)		
ΔT Temperature gradient (°C)		
Δt Time interval (s)		
Δx , Δy , Δz Space interval at different directions		
η Efficiency		
ρ Density (kg/m ³)		

τ	Period of a temperature cycle (s)	
μ	Dynamic viscosity (N·s/m ²)	
ν	Kinematic viscosity (m ² /s)	
δ	Pipe wall thickness of square cross-section pipe (m)	
$\rho_{r,suc}$	Compressor suction refrigerant density (kg/m ³)	
Δψ	Temperature interval (°C)	
ω	Rotational speed of compressor (rev/s)	
ξ	Specific enthalpy (kJ/kg)	
Δξ	Specific enthalpy change (kJ/kg)	
Subscrip	ts	
ave	Average	
b	Borehole	
с	Compressor	
cond	Condenser	
el	Electricity	
evap	Evaporator	
f	Fluid	
g	Grout	
ig	Inlet pipe and grout	
og	Outlet pipe and grout	
р	Pipe	
S	Soil	
v	Vapour	
w,e,s,n,b,	t West, east, south, north, bottom, top	
r	Refrigerant	
Abbreviations		
BHE	Borehole heat exchanger	
СОР	Coefficient of performance	

CV	Control volume
EP	Energy pile
FEM	Finite element method
FVM	Finite volume method
GHE	Ground heat exchanger
GSHP	Ground source heat pump
3D	Three-dimensional