
1 Parametric analysis of a cross-flow membrane-based parallel-plate 2 liquid desiccant dehumidification system: numerical and experimental 3 data

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10 **Abstract**

11 Operating parameters of a membrane-based parallel-plate liquid desiccant dehumidification
12 system are investigated in this paper. The liquid desiccant and air are in a cross-flow
13 arrangement, and separated by semi-permeable membranes to avoid carry-over problem. A
14 numerical model is developed to simulate the system performance, and validated by
15 experimental and analytical results. Impacts of main operating parameters on the system
16 performance (i.e. sensible, latent and total effectiveness) are evaluated, which include
17 dimensionless parameters (i.e. solution to air mass flow rate ratio m^* and number of heat
18 transfer units NTU), solution properties (i.e. concentration C_{sol} and temperature T_{sol}) and inlet
19 air conditions (i.e. temperature $T_{air,in}$ and relative humidity $RH_{air,in}$). It is found that m^* and
20 NTU are two of the most important parameters influencing the system effectiveness. Even
21 though the system performance can be improved by m^* and NTU , its increasing gradient is
22 limited when m^* and NTU exceed 1 and 4 respectively. Decreasing solution temperature does
23 not make a great improvement to the system performance, however, increasing solution
24 concentration is a good approach to enhance the latent effectiveness without influencing the
25 sensible effectiveness. The system shows the broad adaptability in various weather conditions,
26 and has the ability to provide relative stable state supply air.

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28 *Keywords:* liquid desiccant, membrane-based, dehumidification, numerical modelling

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37 Nomenclature

A	membrane surface area (m^2)
c_p	specific heat capacity (J/kgK)
C	concentration (%)
C_r^*	thermal capacity ratio
d	width of the rectangular channel (m)
D	diffusivity (m^2/s)
h	convective heat transfer coefficient ($\text{W/m}^2\text{K}$)
h_{fg}	condensation heat of water (J/kg)
h^*	operating factor
H	height of the dehumidifier unit (m)
k	thermal conductivity (W/mK)
L	length of the dehumidifier unit (m)
m^*	solution to air mass flow rate ratio
\dot{m}	mass flow rate (kg/s)
NTU	number of heat transfer units
NTU_m	number of mass transfer units
P	atmospheric pressure (pa)
pe	Peclet number
P_v	equilibrium vapour pressure of desiccant solution (pa)
Re	Reynolds number
RH	relative humidity (%)
T	temperature ($^{\circ}\text{C}$)
U	overall heat transfer coefficient ($\text{W/m}^2\text{K}$)
U_m	overall mass transfer coefficient ($\text{kg/m}^2\text{s}$)
\dot{V}	volumetric flow rate (l/min)
W	humidity ratio (kg/kg dry air)
X	solution mass fraction

Greeks

ε	effectiveness
δ	thickness of membrane (m)
ρ	density (kg/m^3)

Superscripts

* dimensionless

Subscripts

air air flow
crit critical value
desi desiccant
exp experimental
in inlet
lat latent
m mass transfer
mem membrane
num numerical
out outlet
sen sensible
sol solution flow
tol total

38

39 **1. Introduction**

40 The global energy consumption has increased significantly in past decades as a result of
41 growing population and rapidly developing economy. Buildings contribute to a significant part
42 of the global energy consumption. In particular, heating, ventilation and air-conditioning
43 (HVAC) systems are responsible for around 50% of the energy consumed in buildings [1]. In
44 hot and humid regions, occupants would feel uncomfortable and mildew would grow on
45 building interior walls without proper air dehumidification [2]. Thus the energy efficient air
46 conditioning system is of vital importance with considerations of improving occupant thermal
47 comfort and productivity. It has been shown that the building energy consumption could be
48 decreased by 20-64% with efficient dehumidification technologies [3].

49 The traditional cooling coil system has several advantages for its ability to remove sensible heat
50 load within a conditioned space effectively, good stability in performance, long life and a
51 reasonable electrical coefficient of performance (COP) of between 2 and 4. However it is
52 inefficient in dealing with latent heat load [4, 5]. In the conventional cooling coil system, air
53 dehumidification is achieved simply by cooling the air below its dew point for condensation in
54 order to reduce its moisture content. This results in wet cooling coil surfaces that may cause
55 growths of mould and bacteria, and consequently leads to undesirable healthy issues and poor
56 indoor air quality [4, 6]. Furthermore, the air leaving the cooling coil is normally overcooled

57 and needs to be re-heated to an appropriate supply temperature. Therefore, this combined
58 process consumes a considerable amount of energy to cool (typically using a vapour
59 compression system) and heat (using hot water or electricity) the supply air [7]. Drawbacks of
60 the traditional cooling coil system can be avoided by using a liquid desiccant dehumidification
61 system. In this system dehumidification is achieved by using liquid desiccant to absorb water
62 vapour from moist air directly. The liquid desiccant system has some merits, for example, it is
63 more energy efficient, healthy and environmentally friendly than the conventional system [8-
64 10]. Furthermore, it has a better ability in handling latent heat load and removing pollutants
65 with low temperature heat sources, such as solar thermal energy and waste heat [4, 11]. The
66 traditional liquid desiccant system uses packed beds in the dehumidifier and regenerator, where
67 air and desiccant solution are in direct contact. In such a system small desiccant droplets are
68 carried over by the supply air to the conditioned environment, which badly affects occupant
69 health, building structure and furniture [2]. Furthermore, this system has potential drawback of
70 large pressure drop when the air flows through packed beds, which increases the operating cost.
71 Selectively permeable membrane has been used to replace packed beds as heat and mass
72 transfer medium to overcome the desiccant droplet carryover problem. In the membrane-based
73 liquid desiccant dehumidification system air and desiccant are separated by the membranes.
74 Furthermore, other harmful gases are also prevented from permeating to supply air side through
75 membranes.

76 Many researches on the membrane-based liquid desiccant dehumidification have been
77 conducted. Mahmud et al. [3] tested a novel run-around membrane energy exchanger (RAMEE),
78 which consists of two counter-cross-flow membrane energy exchangers. According to their
79 results, during summer test conditions, the total effectiveness increases with desiccant flow rate,
80 but decreases with air flow rate. By contrast, the total effectiveness changes little with air and
81 desiccant flow rates under winter test conditions. Moghaddam et al. [12] experimentally and
82 numerically evaluated the performance of liquid desiccant system. They focused on the effect
83 of thermal capacity ratio (Cr^*) on the performance of a counter-flow liquid-to-air membrane
84 energy exchanger (LAMEE), and found that numerical model agrees with experimental data
85 for the latent and total effectiveness of the LAMEE, and all effectiveness increase with Cr^*
86 under all test conditions. They [13] also investigated the influences of various heat and mass
87 transfer direction and desiccant solution on the steady state performance of a small-scale
88 counter-flow LAMEE, and their research results indicate that changing the solution
89 concentration is one way to control the supply air outlet humidity ratio. Moghaddam [14]
90 experimentally and numerically studied solution-side effectiveness for a membrane energy
91 exchanger as dehumidifier and regenerator, and found that the difference between the air-side
92 and solution-side latent effectiveness is negligible. Moghaddam et al. [15] further tested the
93 performance of a small-scale single-panel LAMEE under different conditions (e.g. heating and

94 humidifying, cooling and humidifying and cooling and dehumidifying), and discovered that the
95 system effectiveness always increases with number of heat transfer units (NTU) under all test
96 conditions. Abdel-Salam et al. [16] numerically investigated the performance of a counter-flow
97 membrane liquid desiccant air-conditioning system. They focused on the effects of different
98 operating parameters on the system overall energy performance and revealed that the system
99 COP at the design condition is 0.68, while the sensible heat ratio (the ratio of the sensible to
100 total energy removed from the supply air) is in the range of 0.3 to 0.5 under different climatic,
101 operating and design conditions. Vali et al. [17] developed a numerical model to evaluate the
102 performance of a counter-cross LAMEE by considering effect of the system design parameters,
103 such as aspect ratio and entrance ratio. They found that the effectiveness is in the range between
104 the effectiveness of pure counter-flow and pure cross-flow LAMEEs with the same membrane
105 area, and the counter-cross-flow LAMEE would have the same performance as a counter-flow
106 LAMEE when the membrane area of practical design is increased by 10%. Huang et al. [18]
107 numerically and experimentally assessed the performance of a quasi-counter flow parallel-plate
108 membrane contractor, and observed that the cooling and dehumidification effectiveness are
109 deteriorated significantly compared to a cross-flow one's. Huang et al. [19, 20] also investigated
110 novel internally-cooled parallel-plate membrane contractors with cross-flow and quasi-counter
111 flow configurations, and found that their effectiveness can be significantly improved compared
112 to adiabatic one. Hollow fiber membrane contractor is another type and has attracted more
113 attention recently. Performances of hollow fiber contractors with parallel and cross flow
114 configurations have been studied in many papers [21-24]. Huang et al. [25, 26] conducted
115 several researches into an elliptical hollow fiber membrane tube bank, which is a more normal
116 case in reality, the local and average Nusselt and Sherwood numbers under the conjugate heat
117 and mass transfer boundary condition are obtained. Applications of membrane-based liquid
118 desiccant humidification in real industry have also been reported [27-29].

119 As discussed previously, many experimental studies have been carried out to investigate the
120 performance of the membrane-based system [3, 12-15, 30]. A few studies evaluate the
121 performance of liquid desiccant system numerically [12-17] by examining the effects of several
122 operating and design parameters on the effectiveness of LAMEE or the overall energy
123 performance. Several numerical investigations [18-20, 31, 32] used models that solve
124 momentum equation and continuity equation to obtain velocity field, energy and mass equation
125 to obtain concentration and temperature distributions. These studies focus on the basic heat and
126 mass transfer of a parallel plate membrane-based contractor. However, limited researches have
127 been carried out to evaluate the performance of a cross-flow membrane-based parallel plate
128 liquid desiccant system numerically by considering comprehensive operating parameters. In
129 this study, the conjugate heat and mass transfer in a cross-flow membrane-based parallel-plate
130 liquid desiccant (using lithium chloride as desiccant) dehumidification system is investigated

131 by numerical modelling, the influences of three groups of main parameters (i.e. dimensionless
 132 parameters: NTU and solution to air mass flow rate ratio m^* , solution properties: temperature
 133 T_{sol} and concentration C_{sol} , and inlet air conditions: temperature $T_{air,in}$ and relative humidity
 134 $RH_{air,in}$) are assessed. Moreover, the interactions of different parameters on the system
 135 performance are also investigated. This work provides a comprehensive parametric study on
 136 the membrane-based liquid desiccant dehumidifier performance, which supplies valuable data
 137 for the optimum design in the dehumidification and air-conditioning systems in practice.

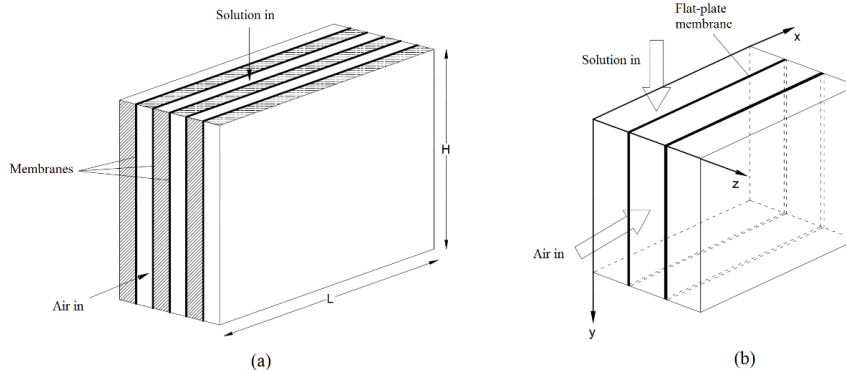
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139 2. Numerical model

140 2.1. Governing equations

141 The structure of the membrane-based parallel-plate dehumidifier is depicted in Fig. 1(a), and
 142 its air and solution flows are in a cross-flow arrangement. The air and solution channels are
 143 separated by semi-permeable membranes, thus heat and vapour can be transferred through
 144 membranes while the desiccant solution is prevented from going through them. The coordinate
 145 system used in numerical modelling is given in Fig. 1(b). As can be seen, the air and solution
 146 flow in x and y directions respectively, while heat and mass are exchanged in z direction. One
 147 air channel and one neighbouring solution channel are selected as the calculating domain.

148



149

150 **Fig. 1.** Structure of membrane-based parallel-plate dehumidifier (a), and coordinate system
 151 used for numerical modelling (b).

152

153 Heat and mass transfer phenomena of the dehumidifier are complicated, many factors have the
 154 influences on heat and mass transfer characteristics, such as the fluid thermal properties, vapour
 155 condensation, fluid flow rate, etc. In order to develop the numerical model, the following
 156 assumptions for simplification in this study are made:

- 157 1) The dehumidifier is well-insulated, which means heat transfer between the
 158 dehumidifier and environment is not considered.
- 159 2) Heat and mass transfer through membrane is normal to the membrane in z direction.

- 160 3) Axial conductions in both air and solution channels are neglected since Peclet numbers
 161 (pe) in the air and solution channels are much larger than 20 [33, 34].
 162 4) Condensation heat is released to solution side only since the solution side mass transfer
 163 coefficient is much higher than that in the air side.
 164 5) Both the air and solution flows are treated as laminar flows since their Reynolds
 165 numbers (Re) are much lower than 2300 in most cases [12].
 166 6) Both the air and solution flows are fully developed, while their temperature and
 167 concentration vary along channel length only.

168

169 2.1.1. Solution side governing equations

170 Heat and mass balance equations in the solution side are given as:

$$171 \left(\frac{\dot{m}_{sol}}{L} \cdot \frac{\partial T_{sol}}{\partial y} \cdot C_{p,sol} \right) \cdot dx dy = [U(T_{air} - T_{sol}) + h_{fg} \cdot U_m(W_{air} - W_{sol,mem})] dx dy \quad (1)$$

$$172 \frac{\dot{m}_{desi}}{L} \cdot \frac{\partial X_{sol}}{\partial y} \cdot dx dy = U_m \cdot (W_{air} - W_{sol,men}) dx dy \quad (2)$$

173 Where in equations, \dot{m}_{sol} is solution mass flow rate (kg/s); \dot{m}_{desi} is desiccant mass flow rate
 174 (kg/s); L is the length of dehumidifier (m) as illustrated in Fig. 1(a); T_{sol} is solution
 175 temperature ($^{\circ}C$); T_{air} is air temperature ($^{\circ}C$); W_{air} is air humidity ratio (kg/kg dry air);
 176 $W_{sol,men}$ is humidity ratio of membrane surface on solution side (kg/kg dry air); X_{sol} is
 177 solution mass fraction, which is calculated as:

$$178 X_{sol} = \frac{m_{water}}{m_{desi}} = \frac{1 - C_{sol}}{C_{sol}} \quad (3)$$

179 Where C_{sol} is solution mass concentration:

$$180 C_{sol} = \frac{m_{desi}}{m_{sol}} \quad (4)$$

181 h_{fg} is water condensation heat (J/kg); $C_{p,sol}$ is solution specific heat capacity (J/kgK);
 182 U (W/m^2K) and U_m (kg/m^2s) are heat transfer and mass transfer coefficients respectively,
 183 which are given by:

$$184 U = \left(\frac{1}{h_{air}} + \frac{\delta}{k_{mem}} + \frac{1}{h_{sol}} \right)^{-1} \quad (5)$$

$$185 U_m = \left(\frac{1}{h_{m,air}} + \frac{\delta}{k_{m,mem}} \right)^{-1} \quad (6)$$

186 Where h_{air} and h_{sol} are convective heat transfer coefficients in air and solution sides
 187 respectively (W/m^2K); $h_{m,air}$ is air side mass transfer coefficient (kg/m^2s); δ is membrane
 188 thickness (m); k_{mem} (W/mK) and $k_{m,mem}$ (kg/ms) are membrane thermal conductivity and
 189 mass transfer conductivity respectively.

190 2.1.2. Air side governing equations

191 Similarly, heat and mass balance equations in the air side are given below:

$$192 \frac{\dot{m}_{air}}{H} \cdot C_{p,air} \cdot \frac{\partial T_{air}}{\partial x} + U(T_{air} - T_{sol}) = 0 \quad (7)$$

$$193 \quad \frac{\dot{m}_{air}}{H} \cdot \frac{\partial W_{air}}{\partial x} dx + U_m (W_{air} - W_{sol,mem}) dx dy = 0 \quad (8)$$

194 Where H is height of the dehumidifier (m), as shown in Fig. 1(a); $C_{p,air}$ is air specific heat
195 capacity (J/kgK).

196

197 2.2. Normalization of governing equations

198 Governing equations (1)(2)(7)(8) are normalized as:

$$199 \quad \frac{\partial T_{sol}^*}{\partial y^*} - NTU_m h^* \frac{1}{Cr^*} (W_{air}^* - W_{sol,mem}^*) - NTU \frac{1}{Cr^*} (T_{air}^* - T_{sol}^*) = 0 \quad (9)$$

$$200 \quad \frac{\partial X_{sol}}{\partial y^*} - NTU_m \frac{1}{m^*} W_0 (1 + X_{sol}) (W_{air}^* - W_{sol,mem}^*) = 0 \quad (10)$$

$$201 \quad \frac{\partial T_{air}^*}{\partial x^*} + NTU (T_{air}^* - T_{sol}^*) = 0 \quad (11)$$

$$202 \quad \frac{\partial W_{air}^*}{\partial x^*} + NTU_m (W_{air}^* - W_{sol,mem}^*) = 0 \quad (12)$$

203 Where in the above equations, the following dimensionless properties have been defined.

204 Dimensionless length is defined by:

$$205 \quad x^* = \frac{x}{L} \quad (13)$$

206 Dimensionless height is defined by:

$$207 \quad y^* = \frac{y}{H} \quad (14)$$

208 Dimensionless temperature is defined by:

$$209 \quad T^* = \frac{T - T_{air,in}}{T_0} \quad (15)$$

210 Where T_0 is equal to $(T_{sol,in} - T_{air,in})$.

211 Dimensionless humidity ratio is defined by:

$$212 \quad W^* = \frac{W - W_{air,in}}{W_0} \quad (16)$$

213 Where W_0 is equal to $(W_{sol,in} - W_{air,in})$.

214 m^* is mass flow rate ratio, which is defined by:

$$215 \quad m^* = \frac{\dot{m}_{sol}}{\dot{m}_{air}} \quad (17)$$

216 Cr^* is thermal capacity ratio, which is defined by:

$$217 \quad Cr^* = \frac{(\dot{m}c_p)_{sol}}{(\dot{m}c_p)_{air}} \quad (18)$$

218 h^* is operating factor, which is a dimensionless number defined by:

$$219 \quad h^* = \frac{W_0 h_{fg}}{T_0 c_{p,air}} \quad (19)$$

220 NTU and NTU_m are numbers of heat and mass transfer respectively, which are defined by:

$$221 \quad NTU = \frac{UA}{(\dot{m}c_p)_{air}} \quad (20)$$

$$222 \quad NTU_m = \frac{U_m A}{\dot{m}_{air}} \quad (21)$$

223 Where A is total membrane area (m^2).

224

225 2.3. Boundary conditions

226 Boundary conditions for the solution side are:

$$227 T_{sol}^* = 1, \text{ at } y^*=0 \quad (22)$$

$$228 X_{sol} = X_{sol,in}, \text{ at } y^*=0 \quad (23)$$

229 While the air side boundary conditions are:

$$230 T_{air}^* = 0, \text{ at } x^*=0 \quad (24)$$

$$231 W_{air}^* = 0, \text{ at } x^*=0 \quad (25)$$

232

233 2.3.1. Heat transfer boundary conditions on membrane surfaces

234 To solve the governing equations, heat and mass transfer boundary equations on membrane

235 surfaces need to be established. Heat transfer boundary conditions are based on thermal energy

236 balance through the membrane:

$$237 h_{sol}(T_{sol,mem} - T_{sol}) = U(T_{air} - T_{sol,mem}) + h_{fg}U_m(W_{air} - W_{sol,mem}) \quad (26)$$

238 Eq. (26) can be normalized as:

$$239 NTU_{sol}(T_{sol,mem}^* - T_{sol}^*) = NTU(T_{air}^* - T_{sol,mem}^*) + NTU_m h^*(W_{air}^* - W_{sol,mem}^*) \quad (27)$$

240 Where NTU_{sol} is number of heat transfer unit in solution side and defined by:

$$241 NTU_{sol} = \frac{h_{sol}A}{(\dot{m}c_p)_{air}} \quad (28)$$

242

243 2.3.2. Mass transfer boundary conditions on membrane surfaces

244 Similarly, mass transfer boundary conditions are based on mass balance through the membrane:

$$245 U_m(W_{air} - W_{sol,mem}) = h_{m,sol}(C_{sol} - C_{sol,mem}) \quad (29)$$

246 Eq. (29) can be normalized as:

$$247 NTU_m W_0(W_{air}^* - W_{sol,mem}^*) = NTU_{m,sol}(C_{sol} - C_{sol,mem}) \quad (30)$$

248 Where $C_{sol,mem}$ is solution concentration in the interface between the solution and membrane

249 surface; $NTU_{m,sol}$ is number of mass transfer unit in the solution side, which is defined by:

$$250 NTU_{m,sol} = \frac{h_{m,sol}A}{\dot{m}_{air}} \quad (31)$$

251 Where $h_{m,sol}$ is solution side mass transfer coefficient (kg/m^2s).

252

253 2.4. Air and solution property equations

254 In numerical modelling, the air specific humidity or humidity ratio (kg/kg dry air) is derived

255 from its relative humidity by applying a correlation introduced in [35].

256 The solution equilibrium specific humidity (W_{sol}) is used to calculate both the sensible and
 257 latent effectiveness, the relationship between the specific humidity and vapour pressure is given
 258 by [36]:

$$259 \quad W_{sol} = 0.62198 \frac{P_v}{P - P_v} \quad (32)$$

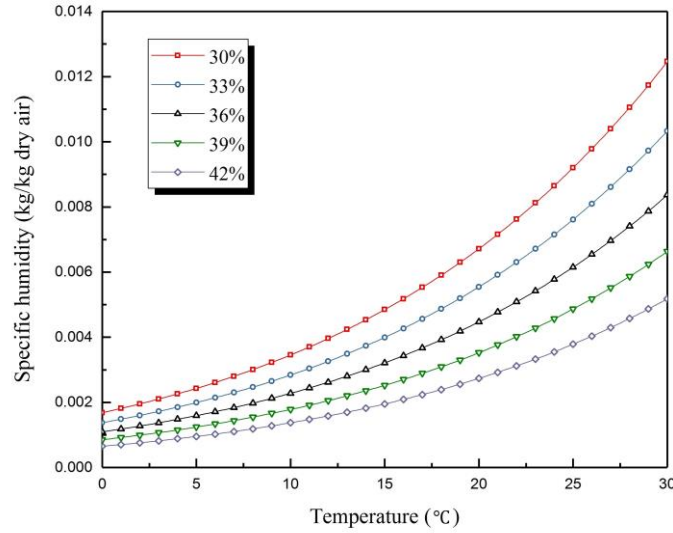
260 Where P is atmospheric pressure (Pa) and P_v is vapour pressure of desiccant solution (Pa).

261 The equilibrium vapour pressure of desiccant solution is a function of T_{sol} and C_{sol} ($P_v =$
 262 $f(T_{sol}, C_{sol})$), the correlation is given by [37]:

$$263 \quad \text{Log } P_v = KI \left[A - \frac{B}{T - E_s} \right] + \left[C - \frac{D}{T - E_s} \right] \quad (33)$$

264 Where P_v is solution equilibrium vapour pressure (kPa), K is an electrolyte parameter relating
 265 to solute; A, B, C, D and E_s are parameters regarding to solvent. A psychrometric chart of LiCl
 266 solution is plotted and shown in Fig. 2.

267



268

269

270

Fig. 2. Psychrometric chart of LiCl.

271 2.5. Performance evaluation

272 Effectiveness is the most important parameter used to evaluate the performance of a heat and
 273 mass exchanger [38]. Three types of effectiveness have been defined in this study: sensible
 274 effectiveness (ϵ_{sen}), latent effectiveness (ϵ_{lat}) and total effectiveness (ϵ_{tot}). ϵ_{sen} is the ratio
 275 between the actual and maximum possible rates of sensible heat transfer in a heat exchanger.
 276 ϵ_{lat} is the ratio between the actual and maximum possible moisture transfer rates in a mass
 277 exchanger. ϵ_{tot} is the ratio between the actual and maximum possible energy (enthalpy)
 278 transfer rates in a heat and mass exchanger. The capacity rate of desiccant solution is higher
 279 than that of the air, which means $Cr^* \geq 1$, then the sensible, latent and total effectiveness are
 280 defined by Eqs. (34) - (36) [39].

$$281 \quad \varepsilon_{sen} = \frac{T_{air,in} - T_{air,out}}{T_{air,in} - T_{sol,in}} \quad (34)$$

$$282 \quad \varepsilon_{lat} = \frac{W_{air,in} - W_{air,out}}{W_{air,in} - W_{sol,in}} \quad (35)$$

$$283 \quad \varepsilon_{tol} = \frac{\varepsilon_{sen} + H^* \varepsilon_{lat}}{1 + h^*} \quad (36)$$

284 Where $T_{air,out}$ is air temperature at the outlet (°C) and $W_{air,out}$ is air humidity ratio at the
285 outlet (kg/kg dry air).

286

287 **3. Simulation procedure**

288 *3.1. Discretization of governing equations*

289 Governing equations in section 2.1 are solved by finite difference method, and discretized by a
290 forward difference scheme. Discretization equations are given below:

$$291 \quad T_{sol(m+1,n)}^* - T_{sol(m,n)}^* - dy^* NTU_m h^* Cr [W_{air(m+1,n)}^* - W_{sol,mem(m+1,n)}^*] -$$

$$292 \quad dy^* NTU Cr [T_{air(m+1,n)}^* - T_{sol(m+1,n)}^*] = 0 \quad (37)$$

$$293 \quad X_{sol(m+1,n)} - X_{sol(m,n)} - dy^* m^* W_0 NTU_m [1 + X_{sol(m+1,n)}] [W_{air(m+1,n)}^* -$$

$$294 \quad W_{sol,mem(m+1,n)}^*] = 0 \quad (38)$$

$$295 \quad T_{air(m,n+1)}^* - T_{air(m,n)}^* + dx^* NTU [T_{air(m,n+1)}^* - W_{sol(m,n+1)}^*] = 0 \quad (39)$$

$$296 \quad W_{air(m,n+1)}^* - W_{air(m,n)}^* + dx^* NTU_m [W_{air(m,n+1)}^* - W_{sol,mem(m,n+1)}^*] = 0 \quad (40)$$

297 Where m is number of grids in x direction, and n is number of grids in y direction.

298 Since the air and desiccant solution are closely interacted with each other, the governing
299 equations are solved in Matlab iteratively until converged. In order to guarantee the accuracy
300 of numerical results, numerical tests have been conducted to determine the grid size. It has been
301 found that 30×60 grids are adequate in this study, the result difference is less than 1.0%
302 compared with 50×100 grids. The numerical uncertainty is 1.0%.

303

304 *3.2. Numerical solving scheme*

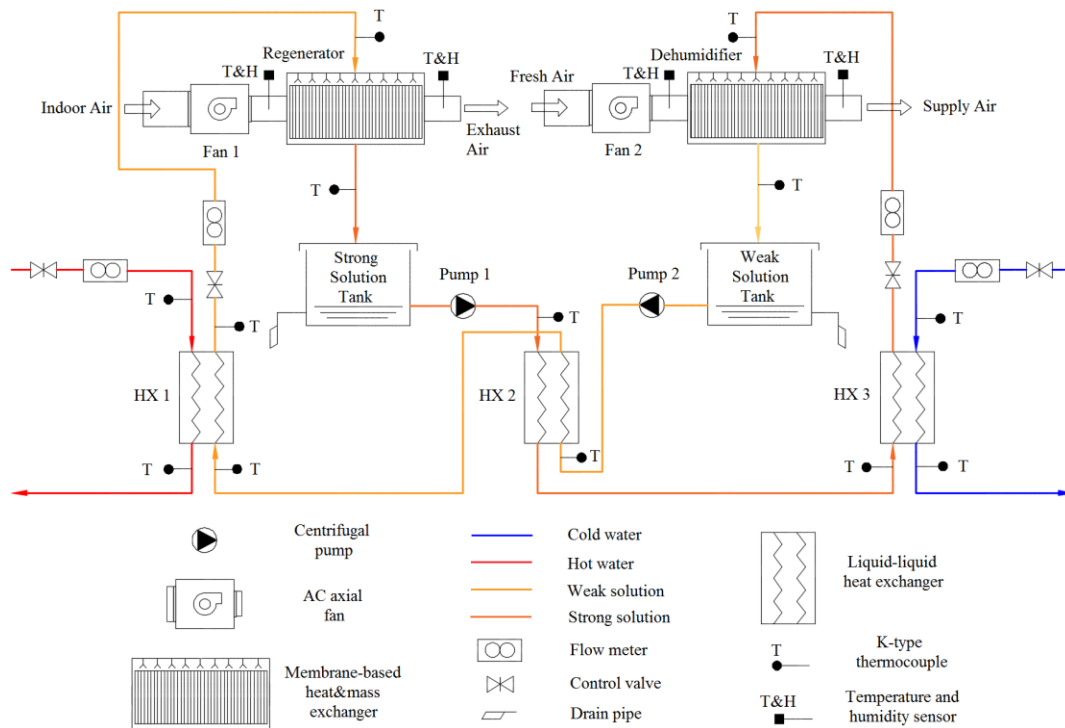
305 The numerical solution scheme used to solve interacted governing equations are given below:

- 306 1) Set the initial temperature and concentration fields for air and solution as boundary
307 conditions.
- 308 2) Assume the initial humidity ratio on the membrane surface as the solution inlet
309 equilibrium specific humidity.
- 310 3) Solve the energy equation (9) to get the solution temperature field (T_{sol}^*).
- 311 4) Figure out the mass equation (10) to obtain the solution concentration field (X_{sol}).
- 312 5) Deal with the energy equation (11) to acquire the air temperature field (T_{air}^*).
- 313 6) Solve the mass equation (12) to get the air humidity field (W_{air}^*).

- 314 7) Based on the temperature and humidity fields for air and solution flows, solve heat and
 315 mass transfer boundary conditions on the membrane surface (26) and (27) to obtain the
 316 membrane surface temperature and concentration fields in the solution side ($T_{sol,mem}^*$
 317 and $C_{sol,mem}$).
- 318 8) Calculate the membrane surface humidity field in the solution side ($W_{sol,mem}^*$) based
 319 on $T_{sol,mem}^*$ and $C_{sol,mem}$.
- 320 9) Adopt new $W_{sol,mem}^*$ as a default value and return to step 7 until $W_{sol,mem}^*$ is
 321 converged.
- 322 10) Return to step 3 with the new $W_{sol,mem}^*$ until T_{sol}^* , X_{sol} , T_{air}^* and W_{air}^* are
 323 converged.
- 324

325 4. Experimental work

326 In order to assess the performance of a membrane-based parallel-plate liquid desiccant
 327 dehumidification system, a test facility is designed and built in the laboratory, which is depicted
 328 in Fig. 3.



329
 330 **Fig. 3.** Schematic diagram of the laboratory test rig.

331

332 The test rig mainly consists of a dehumidifier, a regenerator, two solution tanks and three heat
 333 exchange units. The outdoor air with high temperature and relative humidity is generated in the
 334 environmental chamber, and it flows into the dehumidifier where both its moisture content and

335 temperature are reduced by cold desiccant solution, then it leaves the dehumidifier unit at a dry
 336 and cool state. Its flow rate is controlled by adjusting an AC axial fan rotation speed (ebm-papst
 337 Mulfingen GmbH & Co. KG). The dehumidifier has a dimension of 410mm (L) x 230mm (W)
 338 x 210mm (H) with 11 air channels and 11 solution channels. The regenerator has the same
 339 structure as the dehumidifier. Three gauze layers are paved on the top surface of the
 340 dehumidifier unit to ensure even solution distribution. The dehumidifier specifications and
 341 membrane physical properties are given in Table 1.

342 **Table 1**
 343 Dehumidifier specifications and membrane physical properties.

Symbol	Unit	Value
L	m	0.41
W	m	0.23
H	m	0.21
d_{air}	m	0.0077
d_{sol}	m	0.0043
δ_{mem}	m	0.5×10^{-3}
k_{mem}	W/mK	0.3
$k_{m,mem}$	kg/ms	3.87×10^{-6}

344
 345 Lithium chloride (LiCl) is used as the desiccant in the system. The desiccant solution is
 346 circulated in the system by two identical pumps (15W centrifugal magnetically driven type with
 347 flow rate range of 0-10L/min) and their flow rates are measured by two liquid flow indicators
 348 (Parker UCC PET 1-15 L/min). The desiccant solution and air transport properties are listed in
 349 Table 2.

350 **Table 2**
 351 Air and desiccant solution transport properties.

Symbol	Unit	Value
k_{air}	W/mK	0.03
k_{sol}	W/mK	0.53
D_{air}	m^2/s	2.46×10^{-5}
D_{sol}	m^2/s	0.892×10^{-2}
$c_{p,air}$	J/kgK	1020
$c_{p,sol}$	J/kgK	3200
ρ_{air}	kg/m^3	1.29
ρ_{sol}	kg/m^3	1247

352
 353 Air velocities through the dehumidifier and regenerator are measured at the air duct outlets by
 354 a thermo-anemometer (Testo 405) with a measuring range up to 10m/s. All fans at the inlets of
 355 the dehumidifier and regenerator are equipped with infinitely variable speed controllers to
 356 adjust air flow rates. All air inlets and outlets are instrumented with humidity and temperature
 357 sensors (Sensirion Evaluation KIT EK-H4). The desiccant solution and water temperatures are
 358 measured with K-type thermocouples, and all sensors are connected to a DT500 data logger.
 359 The dehumidifier, regenerator, heat exchangers, storage tanks and pipes are well insulated to

360 reduce the environment influence. All measurement devices and their accuracies are listed in
 361 Table 3. Uncertainty analysis has been conducted for all experimental data by applying a
 362 method of propagation introduced by Taylor [40] to estimate uncertainties for experimental
 363 data.

364 **Table 3**

365 Measurement devices and uncertainties.

Device	Measurement	Range	Uncertainty
Testo thermos-anemometer	Air velocity	0-10 <i>m/s</i>	±5%
Sensiron Evaluation KIT EK-H4	Temperature	-40-125 °C	±0.4%
	Relative humidity	0-100 %	±3%
K-type thermocouple probe	Temperature	0-1100 °C	±0.75%
DT500 Datalogger	Data acquisition	-	±0.15%
Parker UCC PET liquid flow indicator	Solution flow rate	1-15 <i>L/min</i>	±5%
Parker liquid flow indicator	Water flow rate	2-22 <i>L/min</i>	±2%

366

367 5. Results and discussion

368 5.1. Model validation

369 Analytical solutions and experimental data are used to validate the numerical results. 12 groups
 370 of experimental data under different operating conditions are used to validate numerical results.
 371 Under each operating condition, the numerical calculation and experimental results of sensible
 372 effectiveness (ϵ_{sen}) and latent effectiveness (ϵ_{lat}) are compared, as shown in Table 4. It can be
 373 seen that generally numerical modelling results of both ϵ_{sen} and ϵ_{lat} agree well with
 374 experimental data. The maximum discrepancy between numerical results and experimental data
 375 for ϵ_{sen} is 8.756%, while the maximum discrepancy for ϵ_{lat} is 9.822%.

376

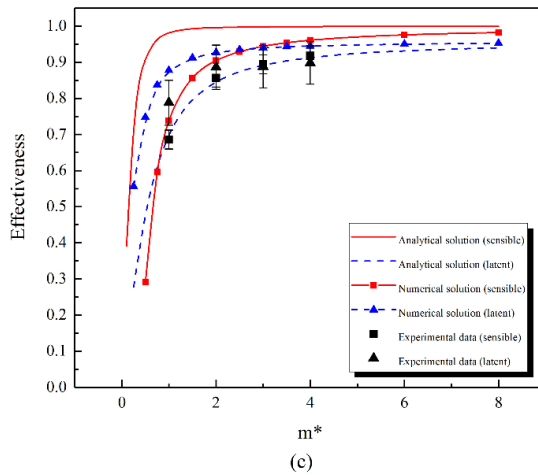
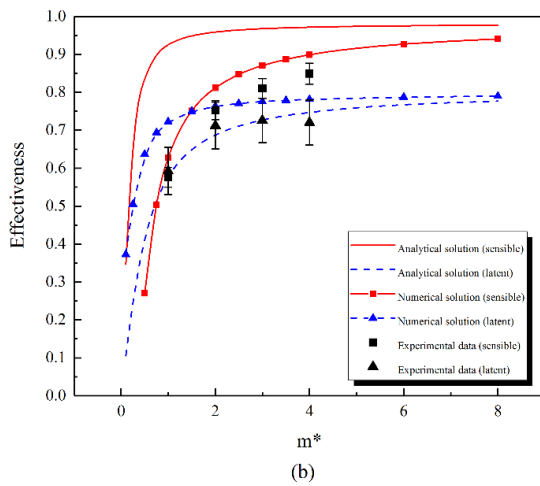
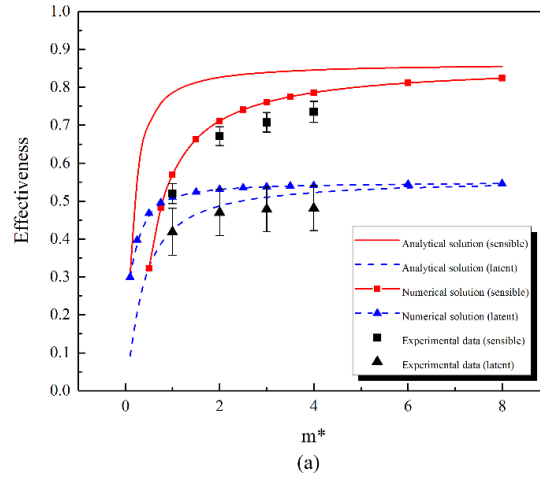
377 **Table 4**

378 Comparisons between numerical results and experimental data.

Operating conditions				Comparisons					
NTU	m^*	m_{air} (kg/s)	m_{sol} (kg/s)	$\epsilon_{sen,num}$	$\epsilon_{sen,exp}$	Error (%)	$\epsilon_{lat,num}$	$\epsilon_{lat,exp}$	Error (%)
2	1	0.1216	0.1216	0.5699	0.520	8.756	0.5101	0.460	9.822
2	2	0.1216	0.2431	0.7113	0.671	5.665	0.5311	0.500	5.856
2	3	0.1216	0.3647	0.7608	0.708	6.940	0.5380	0.508	5.576
2	4	0.1216	0.4862	0.7861	0.735	6.500	0.5413	0.511	5.597
4	1	0.0608	0.0608	0.6276	0.576	8.221	0.7226	0.653	9.632
4	2	0.0608	0.1216	0.8116	0.753	7.220	0.7632	0.742	2.778
4	3	0.0608	0.1823	0.8704	0.810	6.940	0.7756	0.756	2.527
4	4	0.0608	0.2432	0.8990	0.849	5.562	0.7816	0.750	4.043
8	1	0.0304	0.0304	0.7376	0.686	6.996	0.8778	0.818	6.812
8	2	0.0304	0.0608	0.9043	0.857	5.231	0.9270	0.916	1.187
8	3	0.0304	0.0912	0.9440	0.894	5.297	0.9396	0.918	2.299
8	4	0.0304	0.1216	0.9608	0.918	4.455	0.9452	0.928	1.820

379

380



381

382 **Fig. 4.** Comparisons among numerical modelling, experimental data and analytical solutions
 383 for sensible and latent effectiveness under different NTU values: NTU=2(a); NTU=4(b);
 384 NTU=8(c).

385

386 The numerical modelling results and experimental data are presented in Fig. 4, the numerical
 387 modelling results follow the same trends of experimental data for both the sensible and latent
 388 effectiveness under different *NTUs*. Based on the uncertainty analysis, which is shown as error

389 bars for experimental data, it can be seen that numerical modelling results are within the
 390 tolerance range of experimental data. So it can be concluded that the agreements between the
 391 numerical modelling and experimental data for both the sensible and latent effectiveness are
 392 satisfied. It should be emphasized that under each NTU , the discrepancy reduces with the
 393 solution mass flow rate. This is because that the lower of solution mass flow rate, the greater
 394 influence of solution mal-distribution on the effectiveness.

395 Analytical solutions to the model of an enthalpy exchanger with membrane core have been
 396 presented in several literatures. According to these literatures, the sensible effectiveness is a
 397 function of two dimensionless parameters (NTU and Cr^*) for an unmixed cross flow, and given
 398 as [41,42]:

$$399 \quad \varepsilon_s = 1 - \exp \left[\frac{\exp(-NTU^{0.78} Cr^{*-1}) - 1}{NTU^{-0.22} Cr^{*-1}} \right] \quad (41)$$

400 Similar to the sensible effectiveness, the latent effectiveness is calculated as [43]:

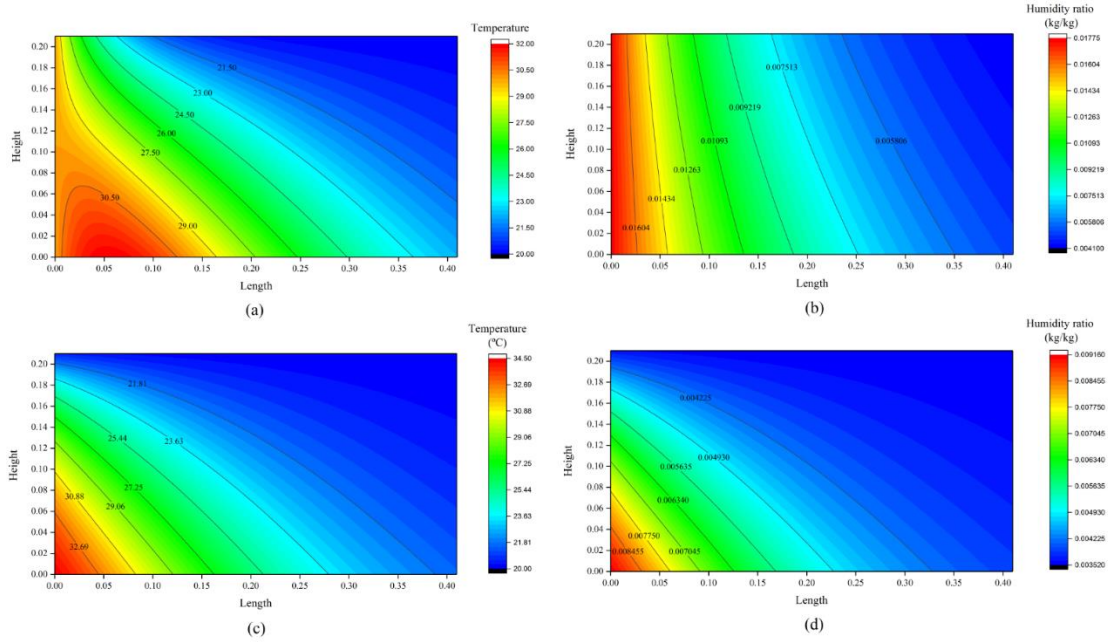
$$401 \quad \varepsilon_l = 1 - \exp \left\{ \frac{NTU_m^{0.22}}{m^{*-1}} [\exp(-m^{*-1} NTU_m^{0.78}) - 1] \right\} \quad (42)$$

402 Results of the analytical solution are also given in Fig. 4. The numerical modelling and
 403 analytical solution results have similar variation trends, an acceptable agreement between them
 404 is achieved. Based on the comparisons, it is valid to predict the performance of the membrane-
 405 based cross-flow dehumidifier by the numerical model.

406

407 *5.2. Temperature and humidity fields*

408 Temperature and humidity fields of the air and solution channels, and the membrane surface
 409 are obtained based on the numerical model. The distributions of temperature and humidity ratio
 410 in the air channel and membrane surface under $NTU = 8$ and $m^* = 2$ are plotted in Fig. 5. The
 411 inlet temperatures of the air and solution are 30°C and 20°C respectively, while the inlet air
 412 relative humidity and solution concentration are set as 70% and 39% respectively. It is observed
 413 that the air has the lowest temperature (20.00°C) and humidity ratio (0.0042 *kg/kg dry air*)
 414 at the right top corner of the air outlet. This is because the air at the top side of the dehumidifier
 415 interacts with stronger and cooler desiccant solution. Furthermore, the air becomes cooler and
 416 drier along the air channel length. It is noticed that the air temperature at left bottom corner of
 417 the dehumidifier is slightly higher than its inlet temperature. This is owing to the increase of
 418 the solution temperature during the dehumidification process.



419
 420 **Fig. 5.** Air temperature field (a); air humidity ratio field (b); temperature field on membrane
 421 surface (c); humidity ratio field on membrane surface (d).

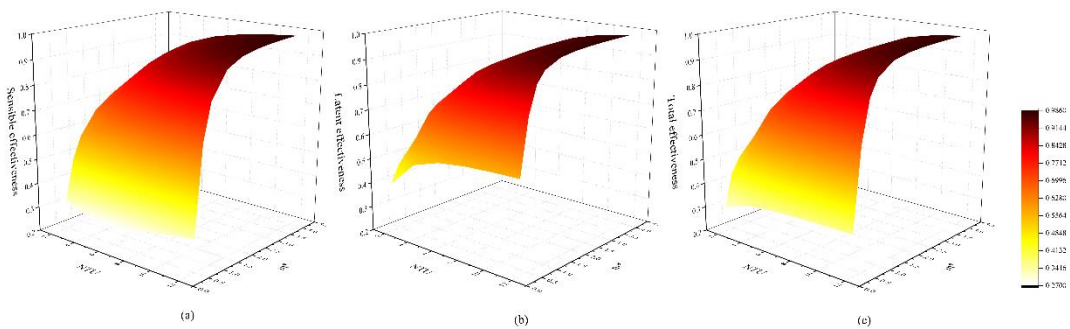
422

423 Furthermore, Fig. 5 (c) and (d) reflect the temperature and humidity boundary conditions on
 424 the membrane surface, it is clear that the boundary condition is neither uniform temperature nor
 425 uniform humidity ratio. They are both non-uniform and two-dimensional profiles, the
 426 temperature and humidity ratio decrease along the diagonal line of the membrane surface.

427

428 *5.3. Effects of dimensionless parameters*

429



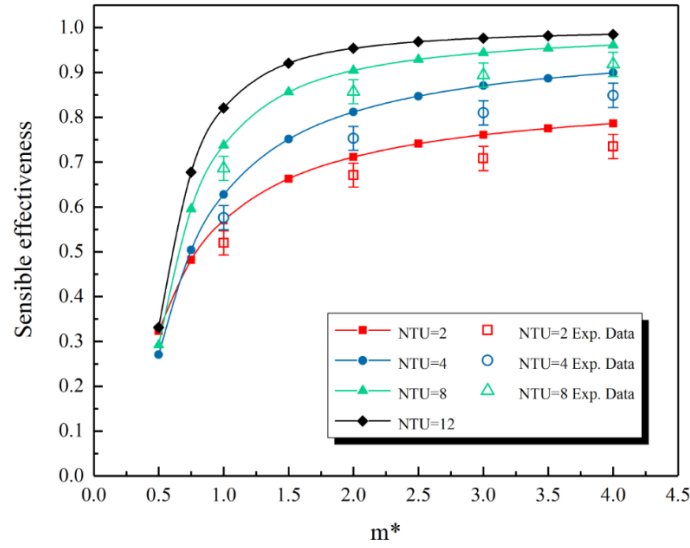
430
 431 **Fig. 6.** Variations of effectiveness: (a) sensible effectiveness; (b) latent effectiveness; (c) total
 432 effectiveness with m^* and NTU .

433

434 The variations of sensible, latent and total effectiveness with m^* and NTU are given in Fig. 6.
 435 The maximum values of sensible, latent and total effectiveness are 0.9849, 0.9845 and 0.9846
 436 respectively when $m^* = 4$ and $NTU = 12$. The minimum values of sensible, latent and total

437 effectiveness are 0.3232, 0.4682 and 0.4353 when $m^* = 0.5$ and $NTU = 2$. Separate effects of
 438 m^* and NTU are discussed then.

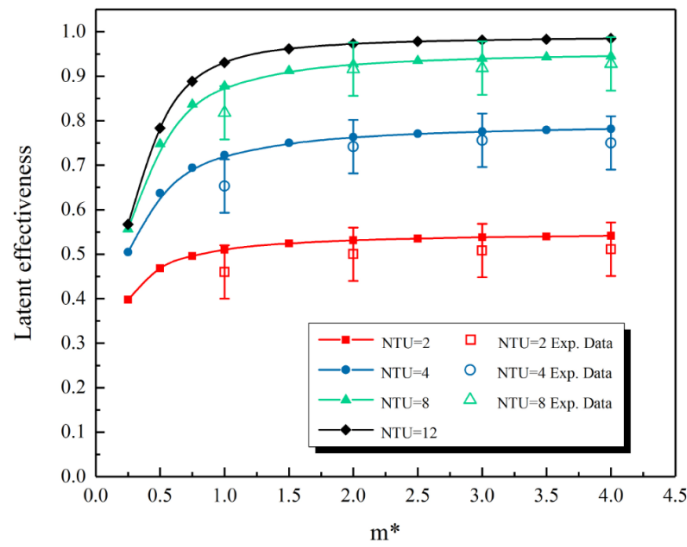
439 m^* is the relative mass flow rate of two fluids in the dehumidifier, and changed by adjusting
 440 solution mass flow rate while keeping air mass flow rate under each NTU . The variations of
 441 sensible, latent and total effectiveness with m^* at different $NTUs$ are depicted in Figs. 7-9.



442

443 **Fig. 7.** Sensible effectiveness variations with m^* under different $NTUs$.

444



445

446 **Fig. 8.** Latent effectiveness variations with m^* under different $NTUs$.

447

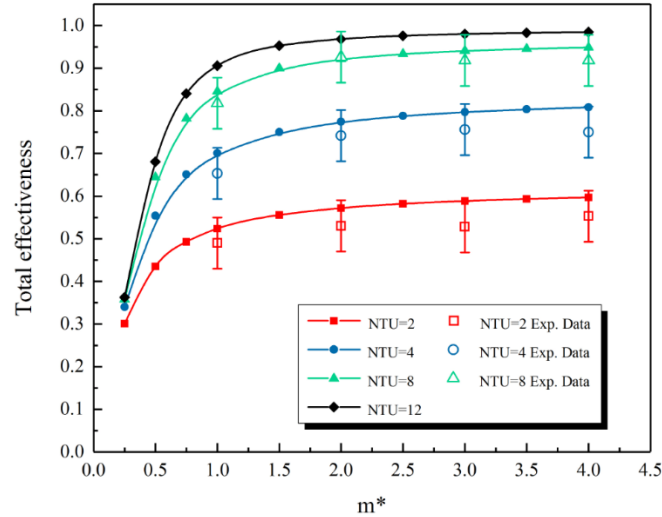


Fig. 9. Total effectiveness variations with m^* under different $NTUs$.

448

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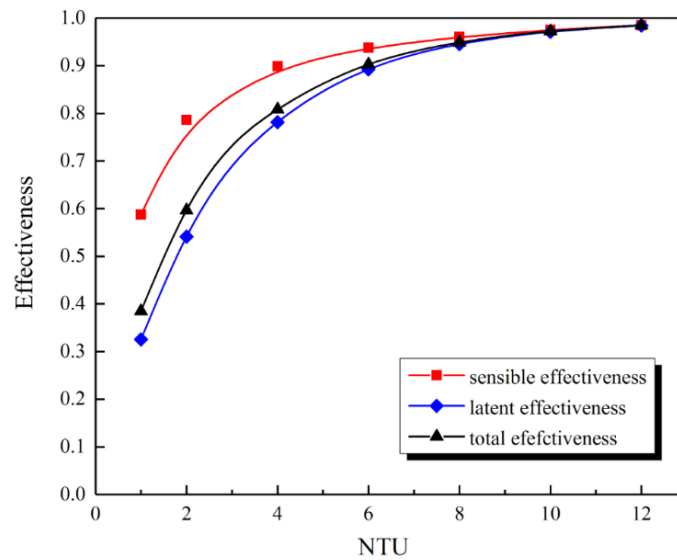
450

451 It is evident that m^* has significant influences on sensible, latent and total effectiveness, which
452 all increase with m^* . The gradient of change for the sensible effectiveness is more considerable
453 than that for latent and total effectiveness. For instance, at $NTU = 8$, the sensible effectiveness
454 rises from 0.2917 to 0.9608 as m^* increases from 0.5 to 4. In the meanwhile, the latent and total
455 effectiveness vary from 0.7476 to 0.9452 and from 0.6441 to 0.9487 respectively. However,
456 the gradients of their changes become moderate gradually and only a slight variation is observed
457 once m^* exceeds 1. Take the latent effectiveness as an example, under $NTU = 4$, the
458 effectiveness increases by 43.15% as m^* rises from 0.25 to 1.0, while the effectiveness only
459 increases by 8.16% when m^* rises from 1.0 to 4.0. Therefore a critical value of m^* can be
460 defined as m_{crit}^* , and the effectiveness are more sensitive to m^* when m^* is lower than m_{crit}^* .
461 Once m^* exceeds m_{crit}^* , there is not much significant change any more. Similar trends can be
462 found in literatures [43, 44], in which their results show that both sensible and latent
463 effectiveness increase with m^* when $m^* < 1$, and they are nearly constant when $m^* \geq 1$.
464 Similar to m_{crit}^* , another important indicator Cr_{crit}^* has been introduced in literatures [45, 46],
465 as all effectiveness increase with Cr^* and are more sensitive before Cr^* reaching a critical
466 value. This is easily explainable since Cr^* is proportional to m^* . Compared to Cr^* , m^* is a
467 more straightforward parameter for the system. As a result, it is desirable to maintain the
468 dehumidification system operating at a condition where m^* is close to m_{crit}^* . It is also worth
469 mentioning that the gradient of change with m^* gets smoothly at low NTU . This is more
470 obvious for the latent and total effectiveness. For example, the latent effectiveness increases by
471 36.21% (i.e. from 0.3974 to 0.5413) when m^* varies from 0.25 to 4 under $NTU = 2$, while
472 under $NTU = 12$, an growth of 73.63% (i.e. from 0.5670 to 0.9845) is observed for the same

473 m^* range. This means there is hardly benefit by increasing m^* at low NTU to improve the
 474 system performance.

475 On the other hand, NTU is another important dimensionless parameter affecting the
 476 effectiveness. In literature [46], NTU is treated as the most important parameter with the most
 477 significant impact on the dehumidification system. Compared to the flow rate, the non-
 478 dimensional group NTU is a comprehensive indicating parameter because it eliminates the
 479 impact of channel geometric properties. In numerical modelling, NTU is changed by adjusting
 480 air mass flow rate, while the solution mass flow rate is changed proportionally to maintain a
 481 constant m^* accordingly. Variations of effectiveness with NTU under $m^* = 4$ are shown in Fig.
 482 10.

483



484

485 **Fig. 10.** Variations of effectiveness with NTU under $m^* = 4$.

486

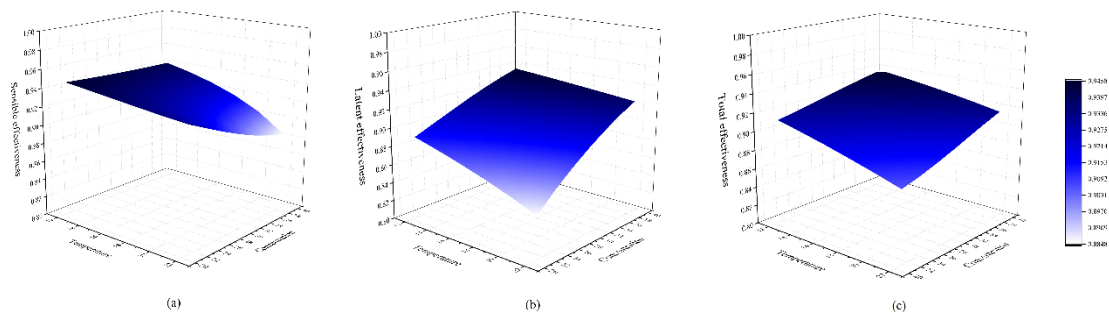
487 All effectiveness are seriously affected by NTU as indicated in Fig. 10. Under the same m^* , the
 488 sensible effectiveness is the highest while the latent effectiveness is the lowest among the three
 489 effectiveness. Similar to the influences of m^* , the three effectiveness vary more remarkably
 490 when NTU is in the range of 1 to 4. Once NTU exceeds 4, variations of these effectiveness tend
 491 to level off. For instance, under $m^* = 4$, the sensible effectiveness increases by 53.02% (i.e.
 492 from 0.5875 to 0.899) when NTU changes from 1 to 4, conversely it only increases by 9.56%
 493 (i.e. from 0.899 to 0.9849) when NTU varies from 4 to 14. Cases are similar for the latent and
 494 total effectiveness. Thus similar to m^*_{crit} or Cr^*_{crit} , a critical value of NTU exists and is defined
 495 as NTU_{crit} . Increasing NTU beyond NTU_{crit} would not enhance the system efficiency.
 496 Furthermore, it is observed from Figs. 7-9 that when m^* is low, there is hardly benefit to
 497 improve these effectiveness by increasing NTU . This is more obvious for the sensible
 498 effectiveness. For instance, under $m^* = 0.5$, increasing NTU from 2 to 12 will only slightly

499 enhance the sensible effectiveness from 0.3232 to 0.3311. However, under $m^* = 4$, the sensible
 500 effectiveness improves from 0.7861 to 0.9849 when NTU increases from 2 to 12. Therefore
 501 there is hardly significance to increase NTU at low m^* for performance improvement.
 502 To sum up, these effectiveness increase with m^* and NTU , but their increase gradients are
 503 limited as $m^* > m^*_{crit}$ (i.e. 1 in this study) and $NTU > NTU_{crit}$ (i.e. 4 in this case). Effects of
 504 m^* and NTU are interacted on each other. Under a relatively low NTU there is hardly benefit
 505 to increase m^* , especially for the latent effectiveness. By contrast, with low m^* , no obvious
 506 performance improvement could be achieved by increasing NTU , especially for the sensible
 507 effectiveness.

508

509 5.4. Effects of solution properties

510 Solution temperature (T_{sol}) and concentration (C_{sol}) affect the system performance, variations
 511 of sensible, latent and total effectiveness with T_{sol} and C_{sol} are presented in Fig. 11, while NTU
 512 and m^* are set as 8 and 2 respectively.



513

514 **Fig. 11.** Variations of effectiveness: (a) sensible effectiveness; (b) latent effectiveness; (c)
 515 total effectiveness with T_{sol} and C_{sol} .

516

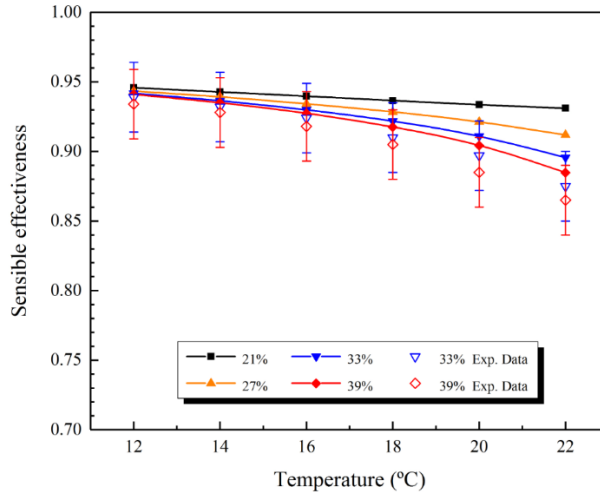
517 The sensible effectiveness reaches the maximum value of 0.9458 when $T_{sol} = 12^\circ\text{C}$ and $C_{sol} =$
 518 21%, while its minimum value is 0.8848 when $T_{sol} = 22^\circ\text{C}$ and $C_{sol} = 39\%$. The maximum
 519 latent effectiveness is 0.9366 when $T_{sol} = 12^\circ\text{C}$ and $C_{sol} = 39\%$, and its minimum value is
 520 0.8449 when $T_{sol} = 22^\circ\text{C}$ and $C_{sol} = 21\%$. For the total effectiveness, it reaches the maximum
 521 value of 0.9380 when $T_{sol} = 12^\circ\text{C}$ and $C_{sol} = 39\%$, while the minimum value is 0.8757 when
 522 $T_{sol} = 22^\circ\text{C}$ and $C_{sol} = 21\%$. Effects of T_{sol} and C_{sol} on the system performance are
 523 discussed separately then.

524 Solution temperature has a great influence on the system performance since it is closely related
 525 to the solution surface vapour pressure. The variations of the effectiveness with T_{sol} under
 526 different C_{sol} are shown in Figs. 12-14.

527

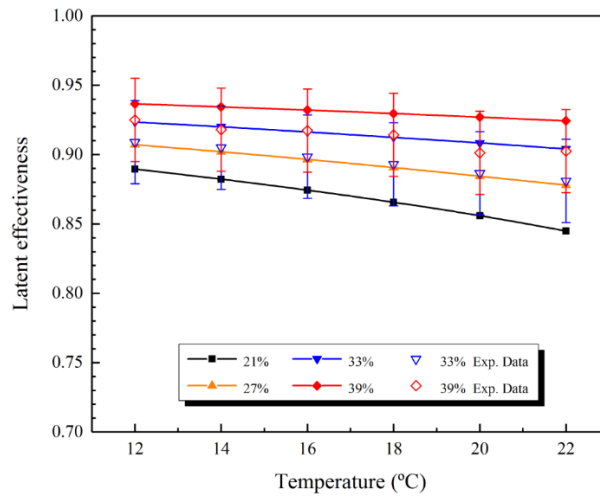
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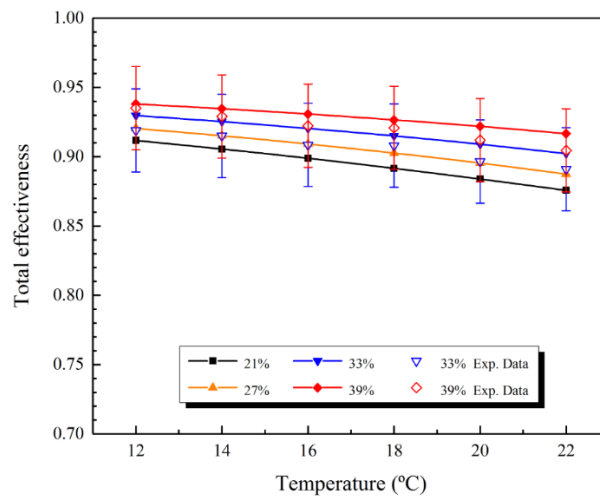
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Fig. 12. Sensible effectiveness variations with T_{sol} under different C_{sol} .



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Fig. 13. Latent effectiveness variations with T_{sol} under different C_{sol} .

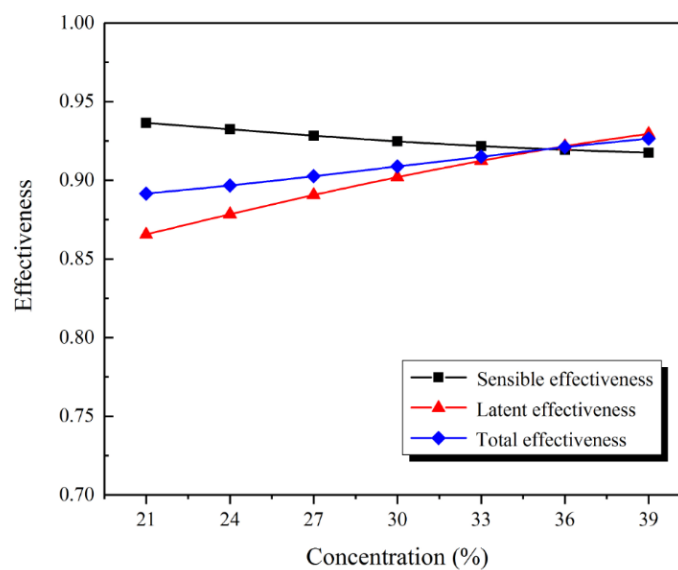


536
537

Fig. 14. Total effectiveness variations with T_{sol} under different C_{sol} .

538 It is clearly reflected in Figs. 12-14 that all effectiveness decrease accordingly with the solution
539 temperature. The decrease of sensible effectiveness is easily understood since the increase of
540 solution temperature narrows the temperature difference between the solution and air. The
541 decrease of latent effectiveness is because vapour pressure in the solution side increases with
542 the solution temperature, which weakens the dehumidification potential. Although decreasing
543 the solution temperature can improve the sensible effectiveness, the improvement is not
544 significant. The sensible effectiveness is weakened by increasing dehumidification effect since
545 more latent heat released to the solution side would increase the solution temperature, which
546 would affect the sensible effectiveness negatively. It also should be mentioned that at a low
547 solution concentration, the sensible effectiveness variation is almost negligible. For instance,
548 the sensible effectiveness increases by only 1.58 % (i.e. from 0.9311 to 0.9458) when the
549 solution temperature decreases by 10 °C under $C_{sol} = 21\%$. Thus when the solution
550 concentration is low, decreasing solution temperature will not improve the sensible
551 effectiveness significantly. The case is opposite for the latent effectiveness as it is more
552 sensitive to T_{sol} when C_{sol} is low. For example, under $C_{sol} = 21\%$, the latent effectiveness
553 increases by 5.3% (i.e. from 0.8449 to 0.8896) when the solution temperature decreases from
554 22°C to 12°C. By contrast, it only increases by 1.33% (i.e. from 0.9243 to 0.9366) under $C_{sol} =$
555 39%. This indicates that the latent effectiveness is more sensitive to solution temperature at a
556 low solution concentration. Nevertheless, the effect of T_{sol} on the latent effectiveness is
557 insignificant compared to C_{sol} as discussed subsequently.

558 Solution concentration affects the system performance as it is directly related to surface vapour
559 pressure. However, increasing C_{sol} has different impacts on the sensible, latent and total
560 effectiveness, which can be observed from Fig. 15.



561
562

Fig. 15. Variations of effectiveness with C_{sol} under $T_{sol} = 18^{\circ}\text{C}$.

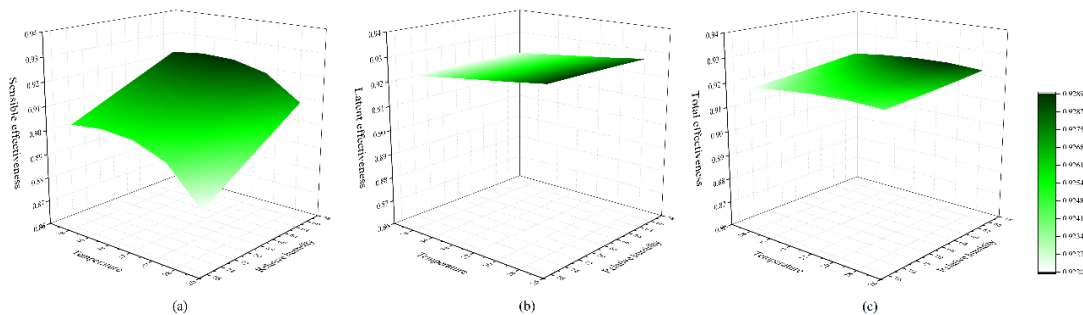
563 As presented in Fig. 15, increasing solution concentration from 21% to 39% would decrease
 564 the sensible effectiveness from 0.9366 to 0.9176, and increase the latent and total effectiveness
 565 from 0.8656 to 0.9296 and from 0.8916 to 0.9266 respectively. Similar to the effects of T_{sol} ,
 566 increasing solution concentration will decrease the solution surface vapour pressure, thus the
 567 solution absorption ability will be enhanced and the latent effectiveness will be increased. The
 568 increased dehumidification ability will negatively affect the sensible effectiveness since more
 569 latent heat will be released to the solution side. The total effectiveness is mainly dominated by
 570 the latent effectiveness since they have the same variation trends. It can be observed in Fig. 12
 571 that the sensible effectiveness is neither sensitive to T_{sol} nor C_{sol} . For the latent effectiveness,
 572 the effect of solution concentration is far more obvious than that on the sensible effectiveness.
 573 For instance, at $T_{sol} = 12^{\circ}\text{C}$, the sensible effectiveness decreases by 0.51% (i.e. from 0.9458
 574 to 0.941) when C_{sol} changes from 21% to 39%, while the latent effectiveness increases by 5.28%
 575 (i.e. from 0.8896 to 0.9366). The latent effectiveness improvement is more significant at a
 576 higher solution temperature. For example, at $T_{sol} = 22^{\circ}\text{C}$, the latent effectiveness increases by
 577 9.40% (i.e. from 0.8449 to 0.9243) when C_{sol} varies from 21% to 39%.

578 To sum up, the sensible effectiveness is insensitive to both T_{sol} and C_{sol} , while the latent
 579 effectiveness is comparatively more sensitive. Thus in practical applications, a low solution
 580 temperature is not necessary since it is energy consuming and no significant performance
 581 improvement could be achieved. In the meanwhile, at a relatively high solution temperature,
 582 increasing C_{sol} will improve dehumidification ability more considerably. It implies that
 583 increasing solution concentration is a better approach to improve the latent effectiveness
 584 without decreasing the sensible effectiveness.

585

586 5.5. Effects of inlet air condition

587 Inlet air condition (i.e. temperature $T_{air,in}$ and relative humidity $RH_{air,in}$) is of vital
 588 importance to evaluate the adaptivity of the system. Variations of the sensible, latent and total
 589 effectiveness with $T_{air,in}$ and $RH_{air,in}$ are presented in Fig. 16, while NTU and m^* are set as 8
 590 and 2 respectively.



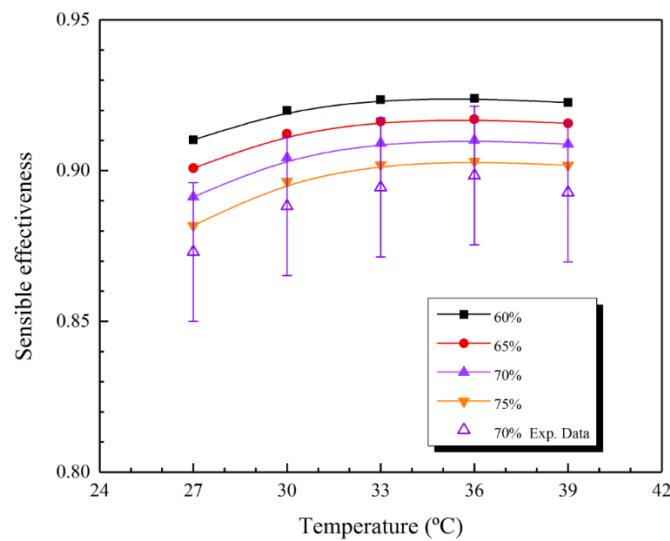
591

592 **Fig. 16.** Variations of effectiveness: (a) sensible effectiveness; (b) latent effectiveness; (c)

593

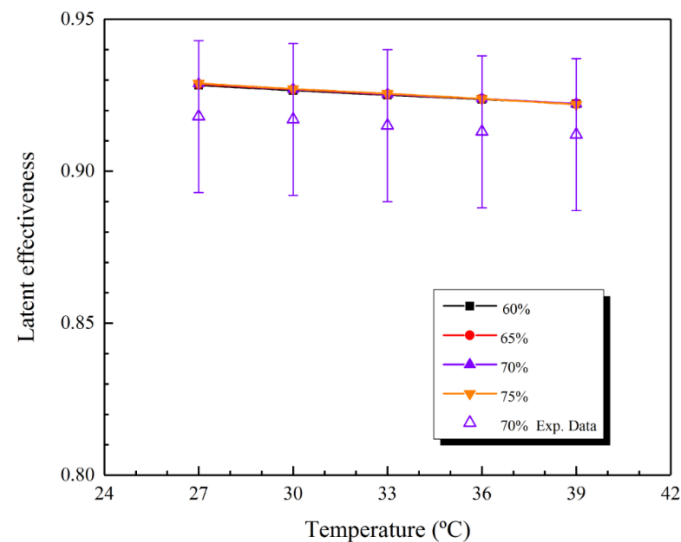
total effectiveness with $T_{air,in}$ and $RH_{air,in}$.

594 The maximum sensible effectiveness is 0.924 when $T_{air,in} = 36^{\circ}\text{C}$ and $RH_{air,in} = 60\%$, while
 595 the minimum value is 0.8818 when $T_{air,in} = 27^{\circ}\text{C}$ and $RH_{air,in} = 75\%$. Comparatively, the
 596 latent effectiveness reaches the maximum value of 0.9289 when $T_{air,in} = 27^{\circ}\text{C}$ and $RH_{air,in} =$
 597 75% , while the minimum value is 0.9222 when $T_{air,in} = 39^{\circ}\text{C}$ and $RH_{air,in} = 60\%$. For the
 598 total effectiveness, the maximum value is 0.9249 when $T_{air,in} = 33^{\circ}\text{C}$ and $RH_{air,in} = 60\%$,
 599 while its minimum value is 0.9174 when $T_{air,in} = 39^{\circ}\text{C}$ and $RH_{air,in} = 75\%$. Then effects of
 600 $T_{air,in}$ and $RH_{air,in}$ on the system performance are discussed separately.
 601



602
 603
 604

Fig. 17. Sensible effectiveness variations with $T_{air,in}$ under different $RH_{air,in}$.



605
 606
 607

Fig. 18. Latent effectiveness variations with $T_{air,in}$ under different $RH_{air,in}$.

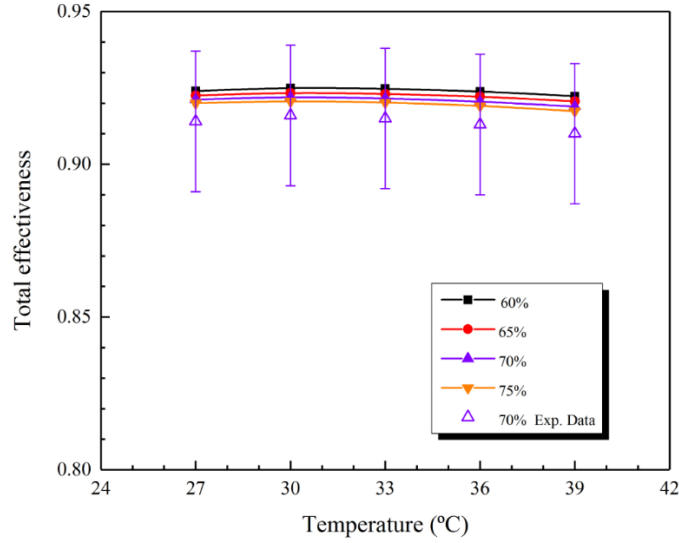


Fig. 19. Total effectiveness variations with $T_{air,in}$ under different $RH_{air,in}$.

608

609

610

611 The effectiveness variations with $T_{air,in}$ under different $RH_{air,in}$ are shown in Figs. 17-19, it

612 can be seen that the sensible effectiveness is more sensitive to $T_{air,in}$ and $RH_{air,in}$ compared

613 with the latent and total effectiveness. When $T_{air,in}$ increases from 27°C to 36°C, the sensible

614 effectiveness gradually rises and reaches the peak value at 36°C. This is because that increasing

615 $T_{air,in}$ at a constant $RH_{air,in}$ will enhance the heat transfer potential [16]. However the sensible

616 effectiveness starts to decrease slightly when $T_{air,in}$ is higher than 36°C. For instance, under

617 $RH_{air,in} = 75\%$, the sensible effectiveness rises by 2.42% (i.e. from 0.8818 to 0.9031) when

618 $T_{air,in}$ increases from 27°C to 36°C. From 36°C to 39°C, the sensible effectiveness decreases

619 slightly (i.e. from 0.9031 to 0.9018). For the latent effectiveness, the effect of $T_{air,in}$ is

620 negligible, for example, under $RH_{air,in} = 75\%$, the latent effectiveness decreases by 0.74%

621 (i.e. from 0.9289 to 0.9220) when $T_{air,in}$ rises from 27°C to 39°C. This is attributed to the

622 increased membrane moisture resistance [46]. The case is similar for the total effectiveness, an

623 obvious relationship between the total effectiveness and $T_{air,in}$ can hardly be found. Effect of

624 $RH_{air,in}$ on the sensible effectiveness is clear, the lower $RH_{air,in}$, the higher sensible

625 effectiveness. Furthermore, the improvements of the sensible effectiveness by decreasing

626 $RH_{air,in}$ at different inlet air temperatures are basically similar. For example, by decreasing

627 $RH_{air,in}$ from 75% to 60%, the sensible effectiveness improvements are 3.22%, 2.63%, 2.39%,

628 2.31% and 2.31% respectively at $T_{air,in}$ of 27°C, 30°C, 33°C, 36°C and 39°C. For the latent and

629 total effectiveness, similar to the effects of $T_{air,in}$, they can barely be affected by $RH_{air,in}$ as

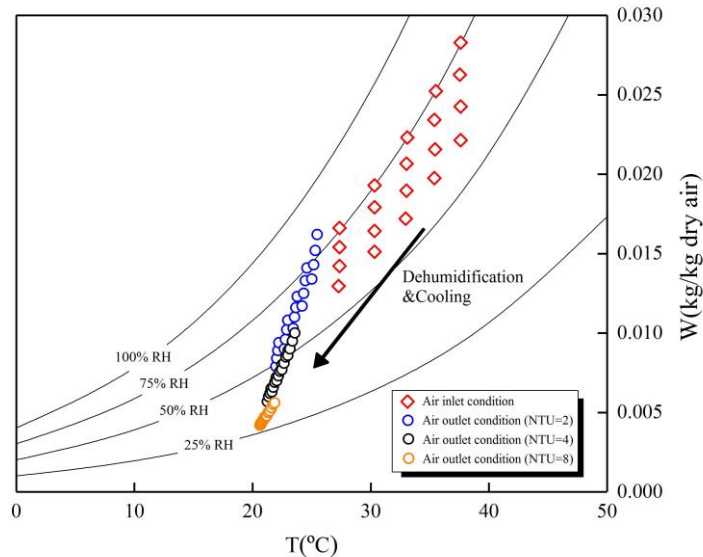
630 well. In other words, the latent and total effectiveness are insensitive to both $T_{air,in}$ and

631 $RH_{air,in}$.

632 In fact, the inlet air state depends on the local weather condition, thus $T_{air,in}$ and $RH_{air,in}$ are
633 input parameters for the system rather than controllable ones. Fig. 20 illustrates inlet and outlet
634 air conditions on the psychrometric chart.

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637

638 **Fig. 20.** Inlet and outlet air conditions on the psychrometric chart for numerical modelling.

639

640 In traditional cooling coil air-conditioning system, the inlet air is dehumidified by reducing its
641 temperature below its dew point temperature, afterwards the air relative humidity is normally
642 high, which means its temperature is too low for the supply air requirement, and subsequently
643 re-heating is required and more energy is consumed. As seen in Fig. 20, both inlet air
644 temperature and humidity content are reduced after passing through the dehumidifier, and the
645 system outlet air has relatively low temperature and relative humidity. Furthermore, the outlet
646 air is at the very similar condition in spite of different inlet conditions with the same NTU , and
647 this is more obvious at high NTU . This means this system has broad adaptability in different
648 weather conditions, and can produce relative stable state supply air.

649 To sum up, the influences of $T_{air,in}$ and $RH_{air,in}$ on the latent and total effectiveness are
650 negligible, while their effects on the sensible effectiveness are weak as well but evident. The
651 cross-flow membrane-based parallel-plate liquid desiccant dehumidification system has better
652 air-conditioning ability to provide the supply air with relatively stable condition despite diverse
653 outdoor conditions.

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657 **6. Conclusions**

658 A numerical model is developed to investigate the performance of a cross-flow membrane-
659 based parallel-plate liquid desiccant dehumidification system, the interaction between the
660 solution and air through membranes is studied by solving heat and mass governing equations
661 in Matlab. The influences of main parameters on dehumidification effectiveness (sensible,
662 latent and total effectiveness) are assessed respectively, which include: number of heat transfer
663 units (NTU), solution to air mass flow rate ratio (m^*), solution temperature (T_{sol}), solution
664 concentration (C_{sol}), inlet air temperature ($T_{air,in}$) and relative humidity ($RH_{air,in}$). The
665 conclusions can be drawn as follows:

- 666 • m^* and NTU are two of the most important parameters influencing the system
667 effectiveness. Although all effectiveness increase with m^* and NTU , their increasing
668 gradients hardly change when m^* and NTU exceed m^*_{crit} and NTU_{crit} respectively.
- 669 • It is desirable to operate the system at the critical condition where m^*_{crit} and NTU_{crit}
670 are 1 and 4 respectively in this study.
- 671 • Effects of m^* and NTU on the system performance are interacted with each other.
672 There is hardly benefit to the system performance improvement by increasing m^* at
673 low NTU , especially for the latent effectiveness. By contrast, no obvious performance
674 enhancement is achieved by increasing NTU at low m^* , especially for the sensible
675 effectiveness.
- 676 • There is no obvious improvement in the sensible effectiveness with low temperature
677 and high concentration solution, which is insensitive to both T_{sol} and C_{sol} .
- 678 • The latent effectiveness increases significantly with C_{sol} at a high solution temperature,
679 while the system sensitive effectiveness does not decrease observably.
- 680 • The system has broad adaptability in different weather conditions by providing relative
681 stable state supply air, in particular at high NTU .

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