

1 **Full title:** Egocentric and Allocentric Representations in Auditory Cortex

2 **Short title:** Egocentric and Allocentric Representations in Auditory Cortex

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14

15 **Author Contributions**

16 S.M.T., W.O.B. and J.K.B. designed the experiment and wrote the paper; S.M.T. conducted the

17 experiments and analysed the data.

18 **Author Summary**

19 When we hear a sound, we can describe its location relative to ourselves (e.g. “the phone is on my  
20 right”) or relative to the world (e.g. “the phone is in the corner”). These descriptions of space are  
21 known as egocentric and allocentric respectively and illustrate the representation of sound location  
22 in coordinate frames defined by the observer or the world in which the observer can move. In the  
23 brain, we know that neurons in static subjects can represent sound locations. However because  
24 sound location relative to the subject and the world are always fixed when the subject is static, it is  
25 impossible to tell if neurons represent egocentric or allocentric sound location. Here we recorded  
26 neurons in auditory cortex of freely moving ferrets and showed that most cells represent egocentric  
27 sound location. We also recorded a smaller number of allocentric cells that represented sound  
28 location in the world across movement. Additionally we used the movement of subjects to  
29 investigate the neural encoding of sound source distance and the modulation of auditory processing  
30 by the speed of head movement.

31

32 **Abstract**

33 A key function of the brain is to provide a stable representation of an object's location in the world.  
34 In hearing, sound azimuth and elevation are encoded by neurons throughout the auditory system  
35 and auditory cortex is necessary for sound localization. However the coordinate frame in which  
36 neurons represent sound space remains undefined: classical spatial receptive fields in head-fixed  
37 subjects can be explained either by sensitivity to sound source location relative to the head  
38 (egocentric) or relative to the world (allocentric encoding). This coordinate frame ambiguity can be  
39 resolved by studying freely moving subjects and here we recorded spatial receptive fields in the  
40 auditory cortex of freely moving ferrets. We found that most spatially tuned neurons represented  
41 sound source location relative to the head across changes in head position and direction. In addition,  
42 we also recorded a small number of neurons in which sound location was represented in a world-  
43 centered coordinate frame. We used measurements of spatial tuning across changes in head  
44 position and direction to explore the influence of sound source distance and speed of head  
45 movement on auditory cortical activity and spatial tuning. Modulation depth of spatial tuning  
46 increased with distance for egocentric but not allocentric units, whereas for both populations  
47 modulation was stronger at faster movement speeds. Our findings suggest that early auditory cortex  
48 primarily represents sound source location relative to ourselves but that a minority of cells can  
49 represent sound location in the world independent of our own position.

## 50 **Introduction**

51           A central role of the brain is to build a model of the world and objects within it that remains  
52 stable across changes in sensory input when we move. In hearing, this requires an observer  
53 maintains the identification of an auditory object as they move through an environment. Movement  
54 is a critical aspect of sensing [1] that contributes to sound localization and other auditory behaviors  
55 [2-7], however the neural basis underpinning active hearing and how the brain constructs world-  
56 centered sound location remains unknown.

57           For a moving observer, it is possible to represent sound location either relative to oneself  
58 (egocentric representation) or relative to the world through which one moves (allocentric  
59 representation). Allocentric representations provide a consistent report of object location across  
60 movement of an observer [8], as well as a common reference frame for mapping information across  
61 several observers or multiple sensory systems [9, 10]. Despite the computational value and  
62 perceptual relevance of allocentric representations to hearing, studies of auditory processing have  
63 only recently considered the coordinate frames in which sound location is represented [11-13]. Both  
64 electroencephalography (EEG) and modelling studies hint that sound location might be represented  
65 in cortex in both head-centered and head-independent spaces. However EEG has not yet revealed  
66 the precise location of these representations and cannot determine how individual neurons in  
67 tonotopic auditory cortex define space.

68           In static subjects, auditory cortical neurons encode sound azimuth and elevation [14-18] and  
69 localization of sound sources requires an intact auditory cortex [19-21]. However, in static subjects  
70 with a fixed head position, neural tuning to sound location is ambiguous, as the head and world  
71 coordinate frames are fixed in alignment and so allocentric and egocentric sound location are always  
72 equivalent. While it has been largely assumed cortical neurons represent sound location relative to  
73 the head, the spatial coordinate frame in which location is encoded remains to be demonstrated.

74 Furthermore, though the acoustic cues to sound localisation are explicitly head-centered,  
75 information about head direction necessary to form a world-centered representation is present at  
76 early levels of the ascending auditory system [22]. Thus it may be possible for neurons in the  
77 auditory system to represent space in an allocentric, world-centered coordinate frame that would  
78 preserve sound location across changes in head position and direction.

79 Here we resolve the coordinate frame ambiguity of spatial tuning in auditory cortex by  
80 recording from neurons in freely moving subjects. In moving conditions, the head and world  
81 coordinate frames are no longer fixed and so we can determine in which coordinate frame a given  
82 cell is most sensitive. Our approach reveals head-centered and world-centered units that suggest the  
83 coexistence of egocentric and allocentric representations in auditory cortex. We also explore the  
84 impact of distance from a sound source and the speed of subject's movement on spatial tuning in  
85 auditory cortex.

## 86 **Results**

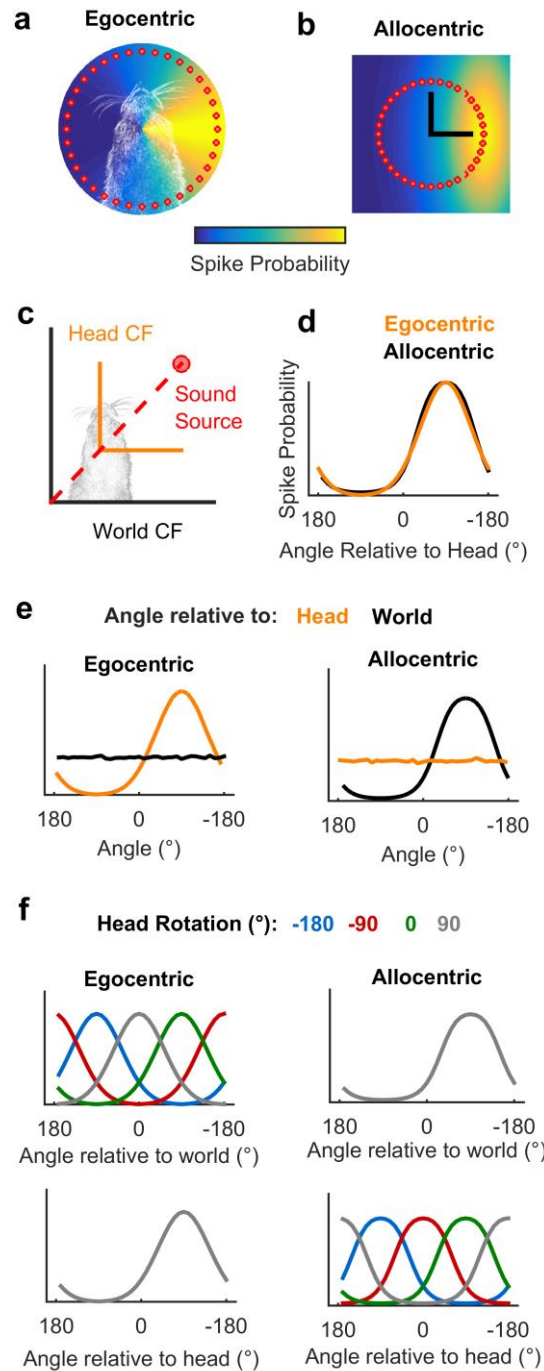
87 We hypothesised that measuring spatial tuning in moving subjects would allow us to  
88 distinguish between egocentric (head-centered) and allocentric (world-centered) representations of  
89 sound location (Fig 1). To formalize this theory and develop quantitative predictions about the  
90 effects of observer movement on spatial tuning, we first simulated egocentric and allocentric  
91 neurons that were tuned to sound locations defined relative to the head (Fig 1a) and world  
92 (independent of the subject) respectively (Fig 1b). We simulated allocentric and egocentric units  
93 using parameters fitted to produce identical spatial receptive fields when tested in the classical  
94 condition in which the head is in a fixed location at the center of a speaker ring (Fig 1c-d), illustrating  
95 the coordinate frame ambiguity. However our simulation confirmed that when the observer moved  
96 freely with a uniform distribution of head directions, spatial tuning would only be apparent in the  
97 coordinate frame relevant for neural output (Fig 1e). Additionally, changes in head direction would

98 produce systematic shifts in tuning curves in the coordinate frame that was irrelevant for neural  
99 output while tuning in the relevant coordinate frame would be invariant across head direction (Fig  
100 1f). We subsequently demonstrated that tuning curves of many shapes and preferred locations can  
101 theoretically be explained by spatial receptive fields based within an allocentric coordinate frame  
102 (Supplementary Fig. 1). With simulations providing a foundation, we then made recordings in freely  
103 moving animals to determine whether the spatial tuning of auditory cortical neurons followed  
104 egocentric or allocentric predictions.

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105 **Fig 1 Simulated receptive fields show that observer movement resolves coordinate frame**  
106 **ambiguity**

107 **a-b**, Simulated neurons with receptive fields tuned to sound location relative to the head (a,  
108 Egocentric) or in the world (b, Allocentric). Circles show hypothetical sound sources in a classical  
109 speaker ring; black lines indicate axes and origin of the simulated world. **c**, Schematic of world and  
110 head coordinate frames (CF). **d**, Sound-evoked tuning curves according to allocentric and egocentric  
111 hypotheses when head and world coordinate frames were aligned. **e-f**, Predictions of allocentric and  
112 egocentric hypotheses showing mean spike probability averaged across uniform distributions of head  
113 rotation and position (e) and at specific head directions (f).



114

115 To measure spatial tuning in moving subjects, we implanted ferrets ( $n = 5$ ) with multi-  
 116 channel tungsten electrode arrays allowing the recording of single and multi-unit activity during  
 117 behavior. During neural recording each ferret was placed in an arena, which the animal explored for  
 118 water rewards while the surrounding speakers played click sounds (Fig 2a). To measure the animal's  
 119 head position, direction and speed in the world during exploration (Fig. 2b-f) we tracked LEDs placed

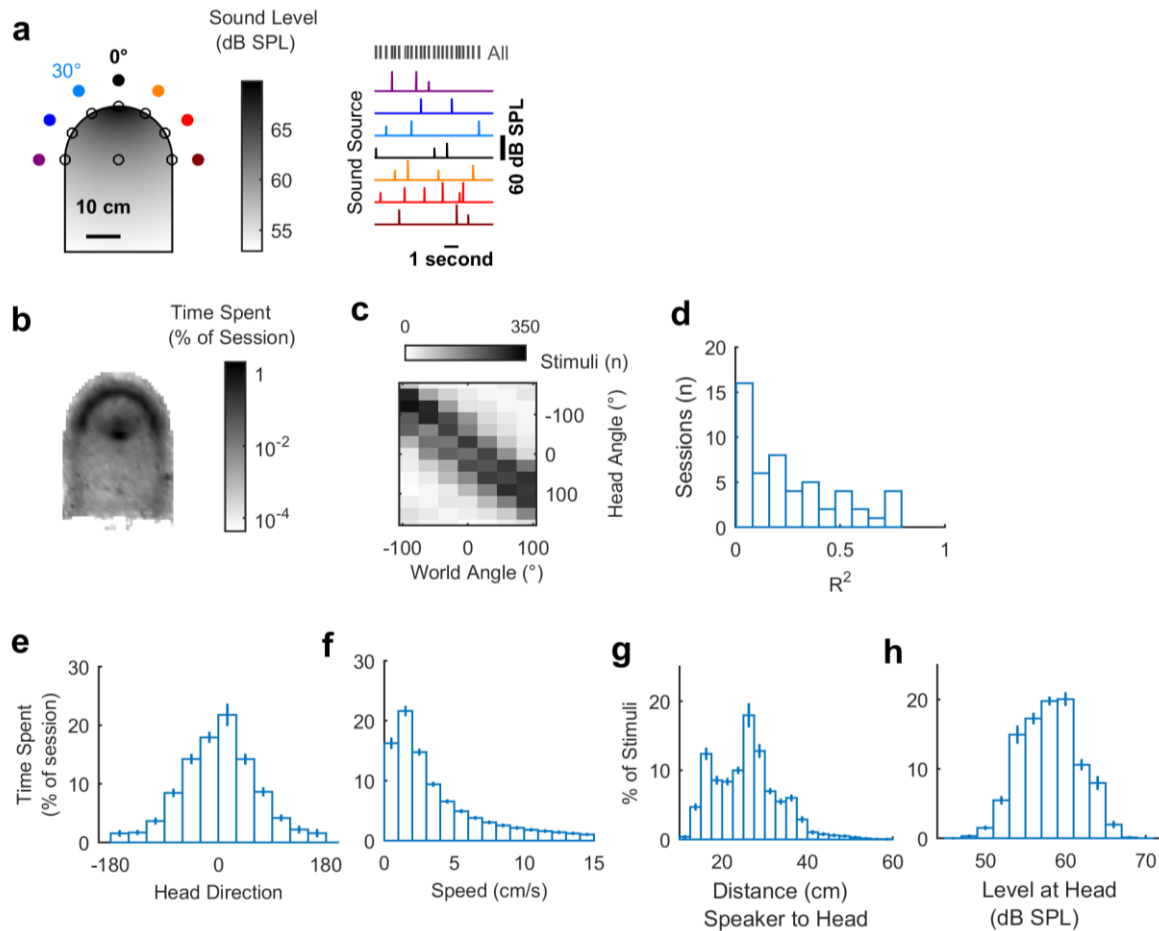
120 on the midline of the head (Supplementary Video 1). During exploration, click sounds were  
121 presented from speakers arranged at 30° intervals between ± 90° relative to the arena center with  
122 speaker order and inter-click interval (250 – 500 ms) varied pseudo-randomly. We also varied the  
123 level of clicks between 54 and 60 dB SPL such that absolute sound level varied both as a function of  
124 sound source level and distance between head and speaker, to reduce cues about sound location  
125 provided by absolute sound level (Fig 2g-h). Clicks were used as they provided instantaneous energy  
126 and thus ensured minimal movement of the animal during stimulus presentation (Supplementary  
127 Fig. 3c-d). The locations (speaker angle) from which the clicks originated were used alone to  
128 estimate *allocentric* receptive fields and were used in conjunction with the animal's head direction  
129 and position to measure *egocentric* spatial receptive fields.

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130 **Fig 2 Experimental design and exploratory behavior in a sound field**

131 **a**, Arena with speakers (filled circles) and water ports (unfilled circles). Shading indicates the sound  
132 field generated by a click from the speaker at 0° calibrated to be 60 dB SPL at the center of the  
133 chamber. Stimuli were presented with a pseudorandom interval and order across speakers. **b**, Mean  
134 proportion of time in each recording session spent within the arena. **c**, Stimulus angles relative to the  
135 head and world for one session that was representative of behavior in all sessions (n = 57). **d**,  
136 Correlation coefficients ( $R^2$ ) between sound angles in head and world coordinate frames across all  
137 behavioral sessions. **e-h**, Distributions of head direction, head speed, distance between head and  
138 sound source and the sound level at the animal's head during behavior. Bars indicate mean ± s.e.m.  
139 across sessions.





140

141 We observed that animals moved throughout the arena to collect water (Fig 2b) and used a  
 142 range of head directions during exploration (Fig 2e). In contrast to our initial simulations, the  
 143 distribution of the animal's head direction was notably non-uniform, leading to correlations between  
 144 sound source angle relative to the head and the world (e.g. Fig 2c; mean  $\pm$  s.e.m.  $R^2 = 0.247 \pm$   
 145  $0.0311$ ). This correlation between sound source angles resulted because the animal preferred to  
 146 orient towards the front of the arena ( $0^\circ$ ) and thus sounds that were to the right of the animal were  
 147 more often on the right of the arena than would result from random behavior. The preference of the  
 148 animal was likely a consequence of the shape of the arena, and the location of the water spouts  
 149 within it. Although the correlation between sound source locations relative to the head and within  
 150 the world was relatively small, we sought to determine how the animal's head direction preference  
 151 affected our experimental predictions.

152 To assess the influence of real animal behavior on our ability to distinguish coordinate  
153 frames, we combined our simulated egocentric and allocentric receptive fields (Fig 1) with the  
154 animal's head position and direction across each single behavioural testing session (Fig 3a). This  
155 allowed us to calculate the spatial tuning for known allocentric and egocentric receptive fields in  
156 both head and world coordinate frames. Our simulation predictions (Fig.1) demonstrated that for a  
157 uniform distribution of head angles the tuning function of allocentric or egocentric units should be  
158 flat when considered in the irrelevant coordinate frame. However, a bias in head location over time  
159 would produce spatial modulation in firing rate with location in the irrelevant coordinate frame (Fig  
160 3a). In order to account for this we therefore measured residual modulation as the ratio of  
161 modulation depth in each coordinate frame (Fig. 3;  $MD_{\text{Irrelevant}} / MD_{\text{Relevant}}$ ). Residual modulation thus  
162 represents the degree of indirect spatial tuning in one coordinate frame observed as a by-product of  
163 the animal's behavior combined with spatial tuning in another coordinate frame.

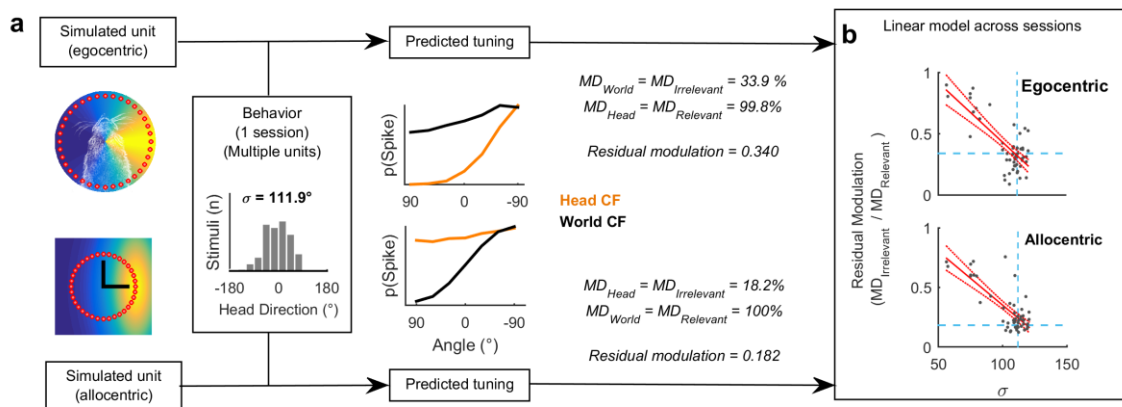
164 Across all behavioral sessions, residual modulation was inversely correlated with variation in  
165 the animal's head direction (expressed as standard deviation) for both egocentric ( $R^2 = 0.562$ ,  $p =$   
166  $1.07 \times 10^{-10}$ ) and allocentric simulated units ( $R^2 = 0.615$ ,  $p = 3.73 \times 10^{-12}$ ) (Fig 3b). This indicated that  
167 for real animal behavior, we would not expect to see the complete abolition of tuning but rather  
168 spatial tuning in both coordinate frames, with the weaker tuning potentially attributable to the  
169 animal's bias in head direction. In our neural analysis, we thus used the relationship between  
170 behavior and residual modulation to provide a statistical framework in which to assess the  
171 significance of spatial tuning of real neurons.

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### 172 **Fig 3 Estimating residual modulation**

173 **a**, Example workflow for estimating residual modulation in coordinate frames irrelevant for neural  
174 output that result from biases in head direction. Residual modulation was defined as: ( $MD_{\text{Irrelevant}} /$   
175  $MD_{\text{Relevant}}$ ). Estimations performed separately using simulated units for each behavioral session. **b**  
176 Residual modulation was inversely correlated with standard deviation of head directions ( $\sigma$ ). Red

177 filled lines indicate regression fit and confidence intervals. Dashed lines indicate data point for the  
 178 single session in (a).



179

## 180 Egocentric and allocentric tuning in auditory cortex

181 During exploration we recorded the activity of 186 sound-responsive units (50 single units,  
 182 136 multi-units) in auditory cortex (Supplementary Fig. 2). Electrode arrays were targeted to span  
 183 the low frequency areas where the middle and posterior ectosylvian gyral regions meet and thus  
 184 units were sampled from primary auditory cortex and two tonotopically organised secondary fields:  
 185 the posterior pseudosylvian and posterior suprasylvian fields. We analysed the firing rates of units in  
 186 the 50 milliseconds after the onset of each click; this window was wide enough to capture the neural  
 187 response while being sufficiently short that the animal's head moved less than 1 cm (median 4 mm,  
 188 Supplementary Fig. 3) and less than  $30^\circ$  (median  $12.6^\circ$ ) – the interval between speakers. The time  
 189 interval between stimuli always exceeded 250 ms.

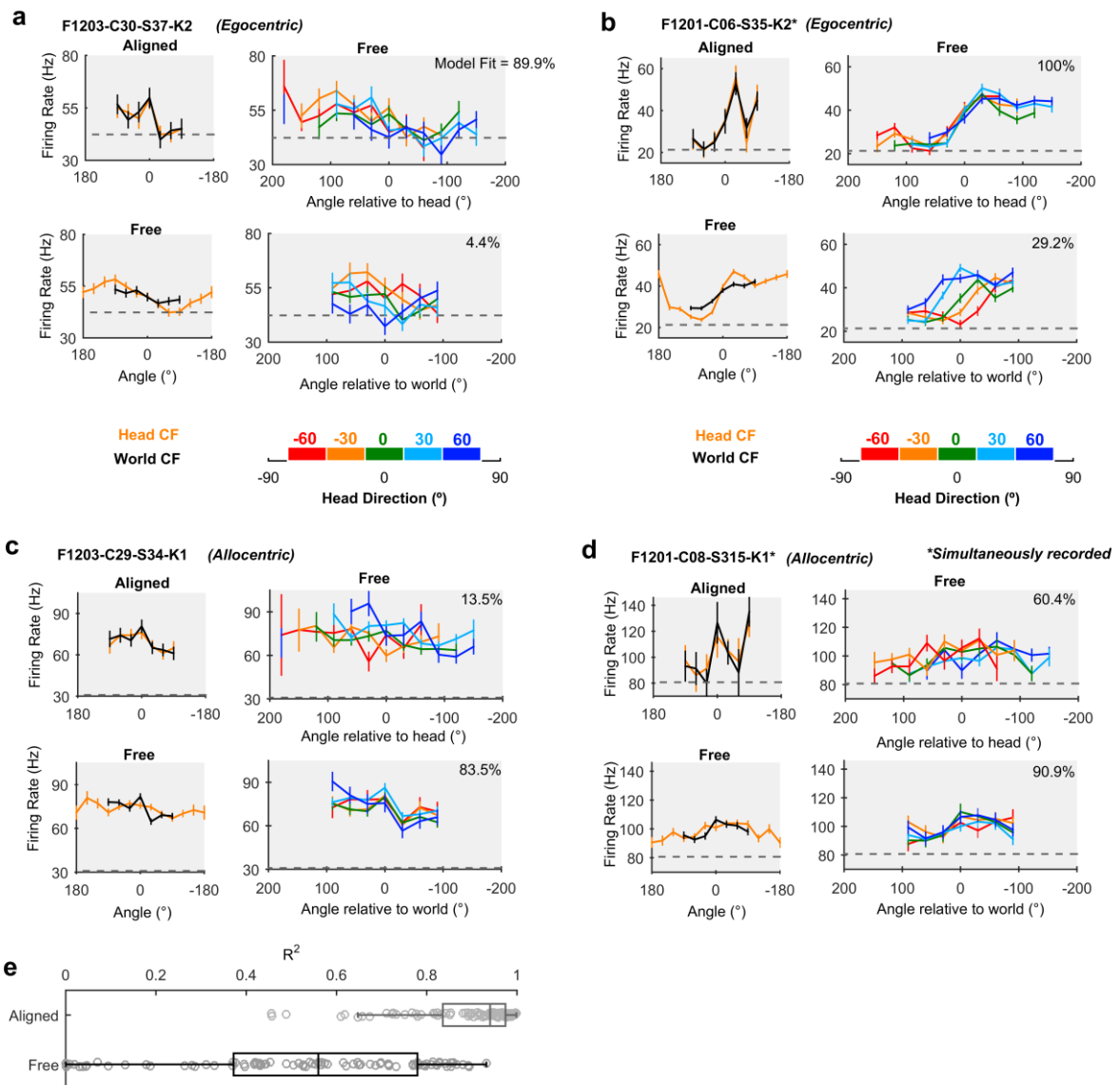
190 We identified periods of time when the animal was facing forwards ( $\pm 15^\circ$  of the arena  
 191 midline) at the center of the speaker ring (Supplementary Fig. 4): in this situation we mimic classic  
 192 neurophysiological investigations of spatial tuning in which head and world coordinate frames are  
 193 aligned. In the aligned case, we recorded 92 units that were significantly modulated by sound source  
 194 location (Fig 4a-d: *Top left*, GLM analysis of deviance,  $p \leq 0.05$ ) and for which spatial tuning curves  
 195 computed in head and world coordinate frames were highly correlated (mean  $\pm$  s.e.m:  $R^2 = 0.889 \pm$

196 0.0131). We then compared the aligned control condition with all data when the head and world  
197 coordinate frames were free to vary. Compared to the aligned condition, correlation between  
198 egocentric and allocentric tuning curves when coordinate frames were free to vary was significantly  
199 reduced (Fig 4e,  $R^2 = 0.522 \pm 0.0294$ ) (paired t-test: free vs. aligned  $t_{91} = 8.76$ ,  $p < 0.001$ ) and  
200 differences in spatial tuning in head and world coordinate frames became visible (Fig 4a-d: *Bottom*  
201 *left*).

---

202 **Fig 4 Spatial tuning of egocentric and allocentric units**

203 **a-d**, Spatial tuning of four example units that were classified as egocentric (a-b) or allocentric (c-d).  
204 In each panel, *top left*: Tuning curves calculated for sound angle in head and world coordinate frames  
205 (CF) when both frames were aligned. *Bottom left*: Tuning curve when head and world CFs were free  
206 to vary. *Top and bottom right*: Tuning curves plotted at specific head rotations. Model fit refers to  
207 percentage of explainable deviance calculated according to Figure 6 across all data in which  
208 coordinate frames were free to vary. Data for all tuning curves are shown as mean  $\pm$  s.e.m. firing  
209 rates. Dotted lines show the mean background activity measured in the 50 ms before stimulus  
210 presentation. **e**, Correlation coefficients between tuning curves in head and world CFs when aligned  
211 or free to vary as the animal foraged around the arena. Boxplots show median and inter-quartile range;  
212 symbols show coefficients for individual units.



213

214 When animals moved freely through the arena, and head and world coordinate frames were  
 215 thus dissociated, we observed units consistent with egocentric (Fig 4a-b and Supplementary Fig. 5)  
 216 and allocentric hypotheses (Fig 4c-d and Supplementary Fig. 6). For units consistent with the  
 217 egocentric hypothesis, spatial receptive fields were more strongly modulated by sound angle in the  
 218 head than world coordinate frame. For the unit shown in figure 4a, modulation depth values in the  
 219 head and world coordinate frames were 28.3% and 10.1% respectively. In figure 4b, modulation  
 220 depth was 49.0% in the head coordinate frame and 30.3% in the world coordinate frame.  
 221 Furthermore tuning curves for sounds plotted relative to the head remained consistent across head

222 rotation but shifted systematically when plotted relative to the world (Fig 4a-b: *Right columns*). Both  
223 outcomes are highly consistent with our simulation predictions (Fig 1).

224 In addition to identifying head-centered spatial tuning across movement, we also found  
225 units with spatial tuning that realized the predictions generated by the allocentric hypothesis. These  
226 units showed greater modulation depth to sound angle in the world coordinate frame than head  
227 coordinate frame (Fig 4c-d and Supplementary Fig. 6): For putative allocentric units, modulation  
228 depths for tuning curves were 21.2% and 13.4% in the world and head coordinate frames  
229 respectively for the unit shown in Fig. 4c, and 12.7% and 10.1% respectively for the unit shown in  
230 Fig. 4d. While these modulation depth values for these units were relatively low (possibly due to the  
231 high background activity), their tuning curves were consistent with representations of world-  
232 centered sound location. Specifically for allocentric units, spatial tuning in the world coordinate  
233 frame was robust to head rotation whereas tuning curves expressed relative to the head were  
234 systematically shifted when mapped according to head direction (Fig 4c-d: *Right column*).

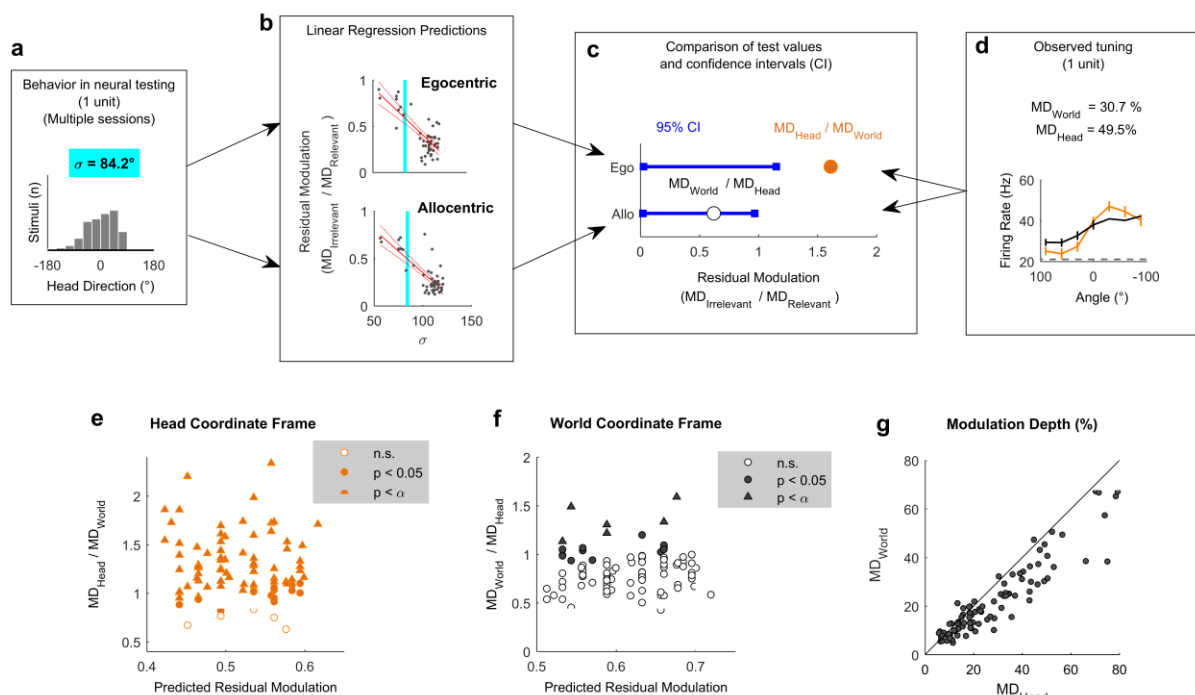
### 235 **Modulation depth across coordinate frames**

236 To quantify the observations we made above and systematically compare spatial tuning in  
237 world and head coordinate frames, we calculated modulation depth for both tuning curves for each  
238 unit. We next asked if modulation depth observed in either head or world coordinate frames was  
239 greater than the residual modulation predicted by our earlier simulations (Fig.3b). A linear  
240 regression model developed using simulated receptive fields was used to predict the magnitude of  
241 residual tuning for each coordinate frame from the animal's behavior during the recording of each  
242 unit (Fig 5a-d). To describe the animal's behavior across the relevant testing sessions for each neural  
243 recording, we calculated the standard deviation of head directions (Fig. 5a). A smaller standard  
244 deviation indicates a less uniform range of head-directions and when combined with our regression  
245 model (Fig 5b) would predict higher residual modulation in both coordinate frames. Thus for a given  
246 standard deviation, we could use linear regression to obtain a predicted confidence interval for the

247 residual modulation in head and world coordinate frames arising from allocentric or egocentric  
 248 tuning respectively (Fig. 5c). The observed modulation values were calculated for each unit as the  
 249 ratio of modulation depth in one coordinate frame divided by the other coordinate frame (Fig. 5d)  
 250 and significance was attributed when test values exceeded the confidence interval of residual  
 251 modulation.

252 **Fig 5 Modulation depth across coordinate frames**

253 **a-d** Workflow illustrating the use of animal behavior (a: summarized using the standard deviation of  
 254 head directions during neural testing,  $\sigma$ ) and linear regression models (b – see also Fig 3) to generate  
 255 confidence intervals for residual modulation (c) that were compared to observed modulation depth  
 256 values (d) normalized relative to the alternative coordinate frame. Blue vertical lines in b show the  $\sigma$   
 257 value in a. **e-f**, Normalized modulation depth observed for each spatially tuned unit compared against  
 258 the mean residual modulation predicted from behavior in head (e) or world (f) coordinate frames.  
 259 Bonferroni-corrected statistical criterion ( $p = 5.43 \times 10^{-4}$ ) is denoted by  $\alpha$ . **g**, Modulation depth for all  
 260 spatially modulated units ( $n = 92$ ) compared in world ( $MD_{World}$ ) and head coordinate frames ( $MD_{Head}$ )  
 261 during exploration.



262

263           Across all spatially tuned units, modulation in the head coordinate frame was significantly  
264 greater than predicted for 87 / 92 units (94.6%)( $p < 0.05$ , Fig 5e); modulation in the world coordinate  
265 frame was significant for 19 / 92 units (20.7%, Fig 5f). For 14 / 92 units (15.2%), modulation depth  
266 was significantly greater than expected in both coordinate frames. When Bonferroni corrected for  
267 multiple ( $n = 92$ ,  $\alpha = 5.43 \times 10^{-4}$ ) comparisons these numbers dropped to 69 / 92 units (75%) for  
268 modulation in the head coordinate frame, none of which were additionally modulated in a world  
269 coordinate frame, and 6 / 92 units (6.5%) for modulation in the world coordinate frame – none of  
270 which showed significant head-centered modulation. With this more conservative statistical  
271 threshold, modulation depths were not significantly greater than expected in either coordinate  
272 frame for the remaining 17 / 92 units (18.5%). Together these observations suggest that response  
273 types occupy a continuum from purely egocentric to purely allocentric. The existence of units with  
274 significant modulation in both coordinate frames with a less conservative statistical cut-off, or no  
275 significant modulation with corrected threshold may indicate mixed spatial sensitivity comparable  
276 with other reports in auditory cortex [23].

277           A key prediction from our simulations with both uniform head-directions (Fig.1) and actual  
278 head-directions (Fig 3a) was that modulation depth would be greater in the coordinate frame that  
279 was relevant for neural activity than the irrelevant coordinate frame (i.e. Head > World for  
280 egocentric; World > Head for allocentric). Having demonstrated that modulation within both co-  
281 ordinate frames was greater than expected based on the non-uniform sampling of head direction,  
282 we compared the modulation depth across coordinate frames for all spatially tuned units (Fig 5g).  
283 For 76 / 92 units (82.6%), we observed greater modulation depth in the head than world coordinate  
284 frame indicating a predominance of egocentric tuning and a minority of units (16 / 92, 17.4%) in  
285 which allocentric tuning was strongest.



## 286 **General Linear Modelling to define egocentric and allocentric populations**

287 Our analysis of modulation depth indicated the presence of both egocentric and allocentric  
288 representations in auditory cortex but also highlighted that the analysis of modulation depth alone  
289 was sometimes unable to resolve the coordinate frame in which units encoded sound location. To  
290 calculate modulation depth requires we discretize sound location into distinct angular bins, average  
291 neural responses across trials and thus ignore single trial variation in firing rates. General linear  
292 models (GLMs) potentially offer a more sensitive method as they permit the analysis of single trial  
293 data and allow us to treat sound angle as a continuous variable. We considered two models which  
294 either characterized neural activity as a function of sound source angle relative to the head  
295 (GLM<sub>HEAD</sub>) or in the world (GLM<sub>WORLD</sub>). For all units for which at least one GLM provided a statistically  
296 significant fit (relative to a constant model, analysis of deviance;  $p < 0.05$ , 91 / 92 units), we  
297 compared model performance using the Akaike information criterion (AIC)[24] for model selection.  
298 In accordance with the modulation depth analysis, the majority of units were better modelled by  
299 sound angle relative to the head than world (72/91 units; 79.1%; four animals) consistent with  
300 egocentric tuning. However, we also observed a smaller number of units (19/91 units; 20.9%; three  
301 animals) whose responses were better modelled by sound angle in the world and thus showed  
302 stronger representation of allocentric sound location.

303 To visualize GLM performance and explore egocentric and allocentric tuning further, we  
304 plotted a normalized metric of the deviance value usually used to assess model fit. Here we defined  
305 *model fit* as the proportion of explainable deviance (Fig 6a) where a test model (e.g. GLM<sub>WORLD</sub>) is  
306 considered in the context of GLMs that have no variable predictors of neural activity (a constant  
307 model) or use sound angle in both coordinate frames as predictors (a full model). This normalization  
308 step is critical in comparing model fit across units as deviance values alone are unbounded. In  
309 contrast, model fit is limited from 0 (indicating the sound angle provides little information about the  
310 neuron's response) to 100% (indicating the sound angle in one coordinate frame accounts for the

311 neuron's response as well as sound angles in both frames). While the units we recorded formed a  
312 continuum in this space, for the purpose of further analysis we defined egocentric and allocentric  
313 units according to the coordinate frame (head / world) that provided the best model fit as  
314 determined by the AIC above.

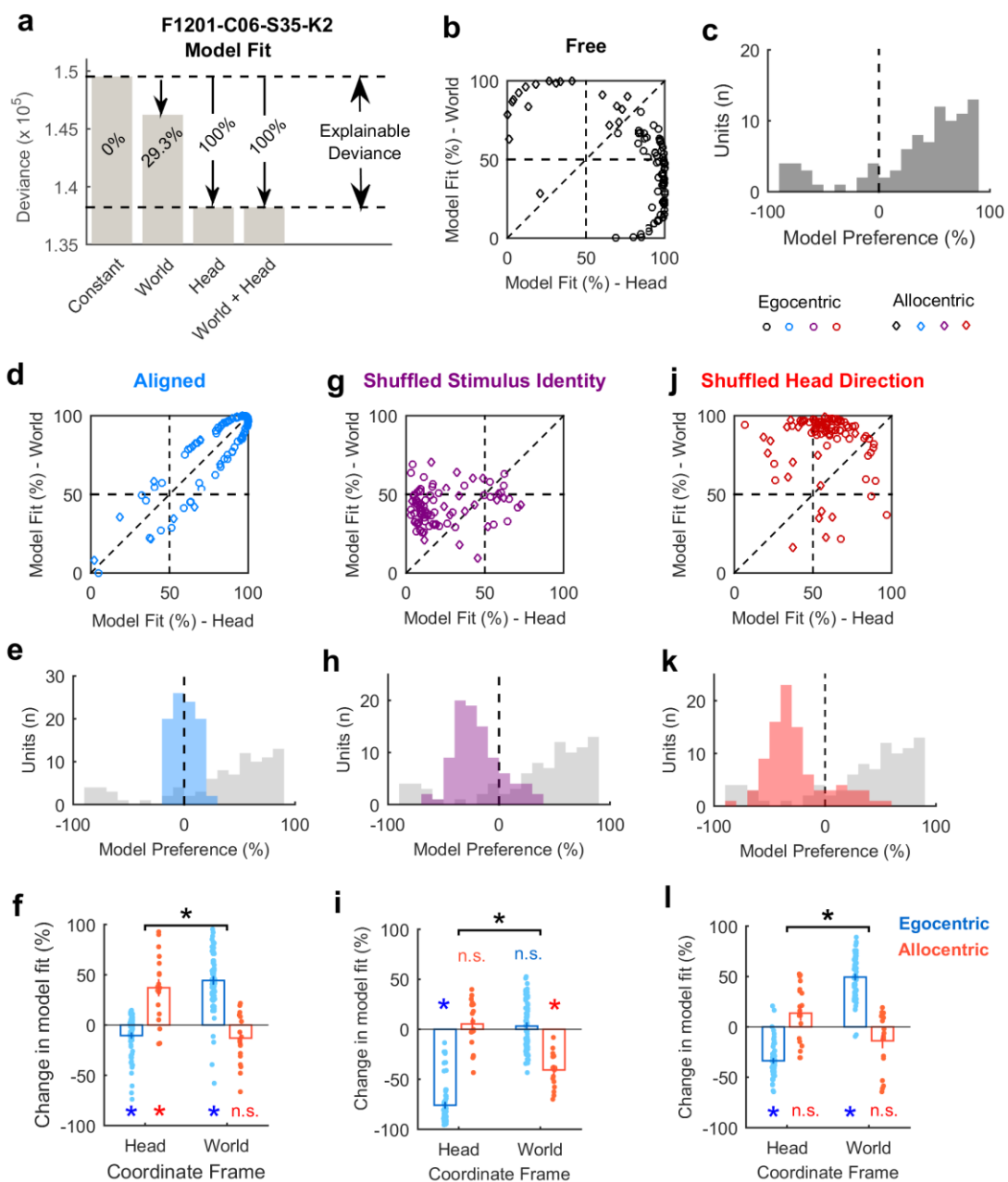
315         Using a GLM based analysis, we predicted that egocentric units would have a high  
316 percentage of the full model fit by sound angles relative to the head, and a low model fit for sound  
317 angles relative to the world, and that allocentric units would show the reciprocal relationship. To  
318 test these predictions we generated a *model preference* score; the model fit for sound angles  
319 relative to the head minus the model fit for sound angles in the world. Accordingly, negative values  
320 of model preference should identify allocentric units while positive values should indicate egocentric  
321 units. Neurons in which both sound angles relative to the world and head provide high model fit  
322 values may represent sounds in intermediary or mixed coordinate frames and would have model  
323 preference scores close to zero, as would neurons in which we were unable to disambiguate  
324 coordinate frame preference due to non-uniform head angle distributions.

---

325 **Fig 6 General linear modelling of spatial sensitivity**

326 **a**, Calculation of model fit for sound angle relative to the head or world. Raw deviance values are  
327 normalized as a proportion of explainable deviance; the change in deviance between a constant and a  
328 full model. **b**, Model fit comparisons for all units when the animal was free to move through the  
329 arena. **c**, Model preference that indicates the distribution of units across the diagonal line of equality  
330 in (b). **d-e**, Model fit and model preference for data when the head and world coordinate frames were  
331 aligned. Grey background in (e) shows the distribution of model preference in the freely varying  
332 condition for reference. **f**, Change in *model fit* between freely moving and aligned states for egocentric  
333 and allocentric units in head and world coordinate frames. **g-h**, Model fit and model preference for  
334 freely moving data when speaker identity was shuffled. Data points in (g) show for each unit the  
335 median model fit averaged across 1000 shuffles. **i**, Change in model fit between unshuffled and

336 shuffled data. **j-k**, Model fit and model preference for freely moving data when the animal's head  
 337 direction was shuffled. Data points in (j) show for each unit median model fit averaged across 1000  
 338 shuffles. **l**, Change in model fit between unshuffled and shuffled data. Asterisks with horizontal bars  
 339 in (f), (i) and (l) indicate significant interactions (two-way anova on change in model fit with shuffle)  
 340 between coordinate frame (head / world) and unit type (egocentric / allocentric) ( $p < 0.001$ ). Asterisks  
 341 / n.s. for each bar represent significant / non-significant effects of shuffle on model fit in specific  
 342 coordinate frames and for specific unity types (red/blue; t-test,  $p < 0.05$ ).



343

344 In the space defined by model fit for sound angles relative to the head and world (Fig 6b),  
345 units clustered in opposite areas supporting the existence of both egocentric and allocentric  
346 representations. This clustering was also evident in the model preference scores, which showed a  
347 bimodal distribution (Fig 6c). Repeating this analysis on data in which the head and world coordinate  
348 frames were aligned (due to the animals position at the center of the speaker ring) demonstrated  
349 that model fit values for head and world coordinate frames became more similar and model  
350 preference scores were centered around zero (Fig 6d-e). When we compared the change in model fit  
351 with alignment (two-way anova), this was reflected as a significant interaction between coordinate  
352 frame (head or world) and unit type (egocentric or allocentric, determined by the coordinate frame  
353 that provided best model fit using the AIC)( $F_{1,178} = 130.1, p = 5.71 \times 10^{-23}$ ). Post-hoc comparison  
354 confirmed that model fit in the head coordinate frame decreased significantly for egocentric units  
355 (Bonferroni corrected for multiple comparisons,  $p = 5.04 \times 10^{-5}$ ) and increased significantly for  
356 allocentric units ( $p = 4.36 \times 10^{-4}$ ). In contrast in the world coordinate frame, alignment led to a  
357 significant increase in model fit for egocentric units ( $p = 2.22 \times 10^{-20}$ ) and a non-significant decrease  
358 in model fit for allocentric units ( $p = 0.155$ ).

359 We performed two additional control analyses on the freely moving dataset: firstly, we  
360 randomly shuffled the speaker identity while maintaining the same information about the animal's  
361 head direction. Randomising the speaker identity should affect the ability to model both egocentric  
362 and allocentric neurons and we would therefore predict that model fits for spatially relevant  
363 coordinate frames would be worse and model preference scores would tend to zero. (i.e. shuffling  
364 would shift model preference scores in the negative direction for egocentric units and the positive  
365 direction for allocentric units). As predicted, shuffling speaker identity eliminated clustering of  
366 egocentric and allocentric units in the space defined by model fit (Fig 6g) and lead to opposing  
367 effects on model preference (Fig. 6h-i): Model fit scores for egocentric and allocentric units were  
368 both affected by shuffling speaker identity but in opposite directions (unit x coordinate frame  
369 interaction,  $F_{1,178} = 227.4, p = 1.22 \times 10^{-33}$ ): For egocentric units, the model fit for sound angle

370 relative to the head declined significantly with shuffling ( $p = 7.44 \times 10^{-41}$ ) while fit for sound angle in  
371 the world did not change significantly ( $p = 0.271$ ). For allocentric units, model fit for sound angle in  
372 the world declined significantly ( $p = 1.29 \times 10^{-8}$ ) but was not significantly different in the head  
373 coordinate frame ( $p = 0.35$ ). When shuffling stimulus angle (averaging across 1000 shuffles), we  
374 identified 12 / 19 (63.2%) allocentric and 63 / 72 (87.5%) egocentric units with model preference  
375 scores beyond the 97.5% percentile limits of the shuffled distribution.

376           Secondly, we shuffled information about the animal's head direction while maintaining  
377 information about speaker identity. This should cause model fit values to decline for sound angle  
378 relative to the head for egocentric units and should therefore result in egocentric units shifting their  
379 model preference scores towards zero. For allocentric units the model fit for sound location in the  
380 world should be maintained, and we would not predict a systematic change in model preference.  
381 This was indeed the case (Fig 6j-l; interaction between coordinate frame and unit type:  $F_{1, 178} = 216.7$ ,  
382  $p = 1.35 \times 10^{-32}$ ): For egocentric units shuffling head direction significantly reduced model fit in the  
383 head coordinate frame ( $p = 1.40 \times 10^{-27}$ ) and increased model fit in the world coordinate frame ( $p =$   
384  $2.20 \times 10^{-31}$ ). For allocentric units, shuffling head direction did not significantly affect model fit in  
385 either head ( $p = 0.211$ ) or world coordinate frames ( $p = 0.178$ ).

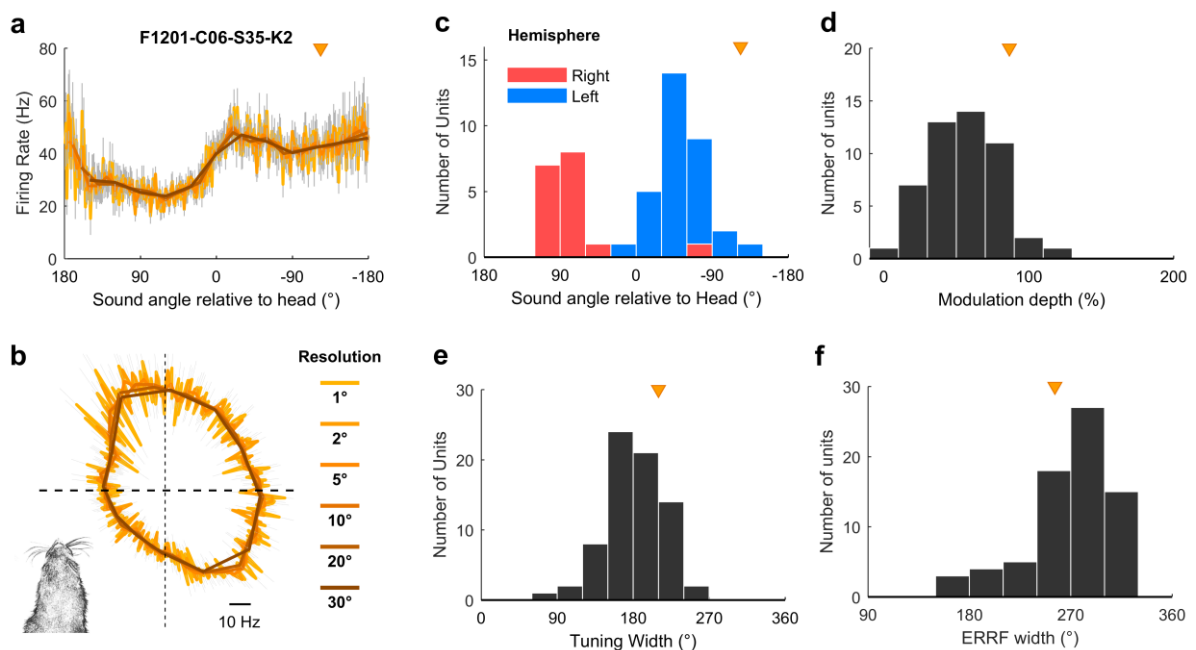
### 386 **Egocentric and allocentric units – population characteristics**

387           For egocentric units that encoded sound location in the head coordinate frame, it was  
388 possible to characterize the full extent of tuning curves in  $360^\circ$  around the head (Fig 5a-b) despite  
389 our speaker array only spanning  $180^\circ$ . This was possible because the animal's head direction varied  
390 continuously across  $360^\circ$  and so removed the constraints on measurement of spatial tuning imposed  
391 by the range of speaker angles used. Indeed, we were able to extend our approach further to  
392 characterize super-resolution tuning functions with an angular resolution more precise than the  
393 interval between speakers (Fig 7a-b and Supplementary Fig 7). Together these findings show it is  
394 possible to use changes in head direction to recover the spatial tuning of individual units with

395 greater detail than would be possible if the subject's head position and direction remained constant  
 396 relative to the sound sources. Egocentric units shared spatial receptive field properties typical of  
 397 previous studies [15, 16, 18, 25]: units predominantly responded most strongly to contralateral  
 398 space (Fig 7c) with broad tuning width (Fig 7e-f) that typifies auditory cortical neurons. We also  
 399 found similar, if slightly weaker spatial modulation when calculating modulation depth according to  
 400 Ref. [18] (Fig 7d).

401 **Fig 7 Egocentric unit characteristics**

402 **a-b**, Spatial tuning of example egocentric unit at multiple angular resolutions. Data shown as mean  $\pm$   
 403 s.e.m. firing rate plotted in Cartesian (a) or polar (b) coordinates. Triangle indicates preferred location  
 404 of unit. Inset (b) illustrates the corresponding head direction onto which spatial tuning can be super-  
 405 imposed. **c**, Preferred location of all egocentric units ( $n = 72$ ) in left and right auditory cortex. **d**,  
 406 Modulation depth calculated according to [18] across 360° for units in both hemispheres. **e-f**, Tuning  
 407 width (e) and equivalent rectangular receptive field width (ERRF)(f) for all units. Triangle indicates  
 408 the preferred location, modulation depth, tuning width and ERRF of the example unit in (a).



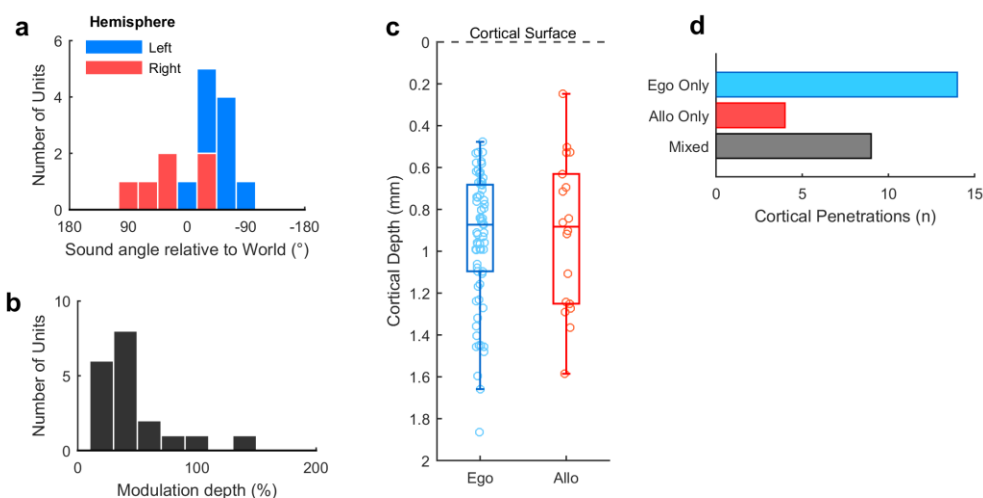
409

410 For allocentric units, we observed a similar contralateral tuning bias in preferred location  
 411 (Fig 8a) to egocentric units and that allocentric units had relatively low modulation depths (Fig 8b).  
 412 These tuning features may not be surprising as an allocentric receptive field could presumably fall  
 413 anywhere within or beyond the arena, and might therefore be poorly sampled by circular speaker  
 414 arrangements. If the tuning curves measured here were in fact sampling a more complex receptive  
 415 field that related to a world-centered coordinate frame (Fig 1b) we would predict that the receptive  
 416 fields would be correspondingly noisier. Allocentric and egocentric units were recorded at similar  
 417 cortical depths (Fig 8c) and on the same cortical penetrations as egocentric units were recorded on 9  
 418 of 13 electrodes (69.2%) on which we also identified allocentric units (Fig 8d).

---

419 **Fig 8 Allocentric unit characteristics**

420 **a**, Preferred location of all allocentric units ( $n = 19$ ) in left and right auditory cortex. **b**, Modulation  
 421 depth calculated across  $180^\circ$  for units in both hemispheres. **c**, Comparison of cortical depth at which  
 422 egocentric and allocentric units were recorded. Ferret auditory cortex varies in thickness between 1.5  
 423 and 2 mm and electrode depths were confirmed histologically (Supplementary Fig. 2). **d**, Number of  
 424 cortical penetrations on which we recorded only egocentric units, only allocentric units or a  
 425 combination of both (mixed). All 92 spatially tuned units were recorded on 27 unique electrodes, with  
 426 recorded units being distributed throughout cortex as the electrodes were descended.



427

## 428 **Timing of spatial information**

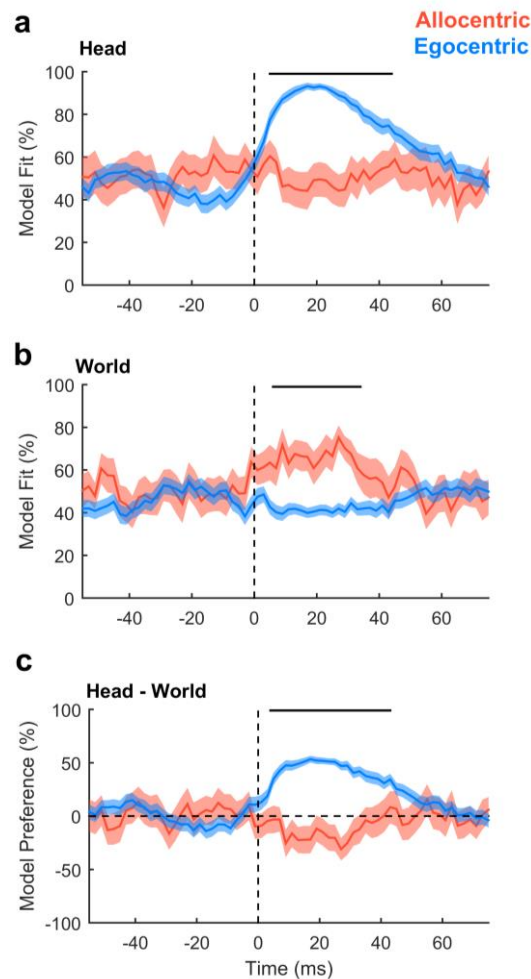
429           Our findings suggested the existence of egocentric and allocentric tuning in auditory cortex.  
430   As these descriptions were functionally defined, we hypothesized that differences between  
431   allocentric and egocentric tuning should only arise after stimulus presentation. To test this, we  
432   analyzed the time course of unit activity in a moving 20 ms window and compared model fit and  
433   model preference of egocentric and allocentric units (defined based on the AIC analysis above) using  
434   cluster-based statistics to assess significance [26]. Model fit for sound angles relative to the head  
435   was greater for egocentric than allocentric units only between 5 and 44 ms after stimulus onset (Fig  
436   9a,  $p = 0.001996$ ). Model fit for sound angles in the world was greater for allocentric than egocentric  
437   units only between 6 and 34 ms after stimulus (Fig 9b,  $p = 0.001996$ ). Model preference diverged  
438   only in the window between 4 and 43 ms after stimulus onset (Fig 9c,  $p = 0.001996$ ). We observed  
439   no differences between egocentric and allocentric units before stimulus onset or when coordinate  
440   frames were aligned (Supplementary Figure 8). Thus the differences between egocentric and  
441   allocentric units reflected a stimulus-evoked effect that was only observed when head and world  
442   coordinate frames were free to vary.

---

### 443 **Fig 9 Egocentric and allocentric tuning over time**

444   **a**, Model fit for predicting neural activity from sound angles relative to the head. **b**, Model fit for  
445   predicting neural activity from sound angles in the world. **c**, Model preference. Data shown as mean  $\pm$   
446   s.e.m. for egocentric and allocentric unit populations. Black lines indicate periods of statistical  
447   significance (cluster based unpaired t-test,  $p < 0.05$ ).





448

449 **Population representations of space**

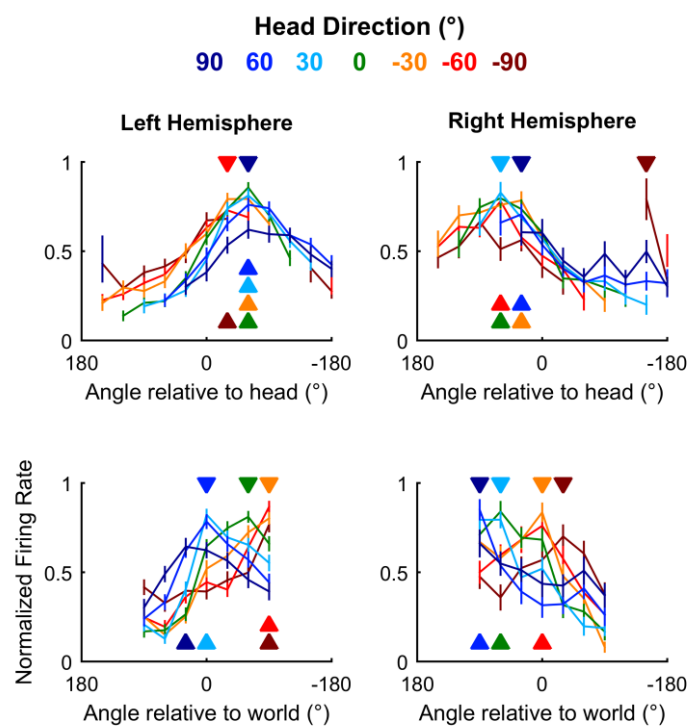
450 We next asked how auditory cortical neurons behaved as a population when spatial tuning  
 451 was compared across head directions. In contrast to individual units, population activity more closely  
 452 reflects the large-scale signals observed in human studies using electroencephalography (EEG) to  
 453 distinguish coordinate frame representations [11, 12]. To form populations, we took the unweighted  
 454 mean of normalized firing rates from all units recorded from left ( $n = 64$ ) or right ( $n = 28$ )  
 455 hemispheres and compared tuning curves measured at different head directions. As would be  
 456 expected from the predominance of egocentric units, we found that tuning curves for both left and  
 457 right auditory cortical populations were consistent within the head but not world coordinate frame  
 458 (Fig 10). Thus the allocentric units we find here are sufficiently rare as to be masked in overall

459 population readouts of spatial tuning, potentially accounting for conflicting findings of coordinate  
460 frame representations from EEG recordings.

---

461 **Fig 10 Auditory cortical tuning**

462 Population tuning curves plotted across head direction for mean ( $\pm$  s.e.m.) normalized response of all  
463 units in left and right auditory cortex; filled triangles indicate sound angle of maximum response at  
464 each head direction.



465

---

466 **Distance modulation of cortical neurons and spatial tuning**

467 Studying auditory processing in moving subjects allowed us to resolve coordinate frame  
468 ambiguity so that we could determine the spaces in which neurons represent sound location.  
469 However recording in freely moving subjects also made it possible to go beyond angular  
470 measurements of the source location and address how neurons represented the distance of sound  
471 sources. Though often overlooked, distance is a critical component of egocentric models of neural  
472 tuning as the acoustic cues indicating sound location such as inter-aural level differences (ILDs)

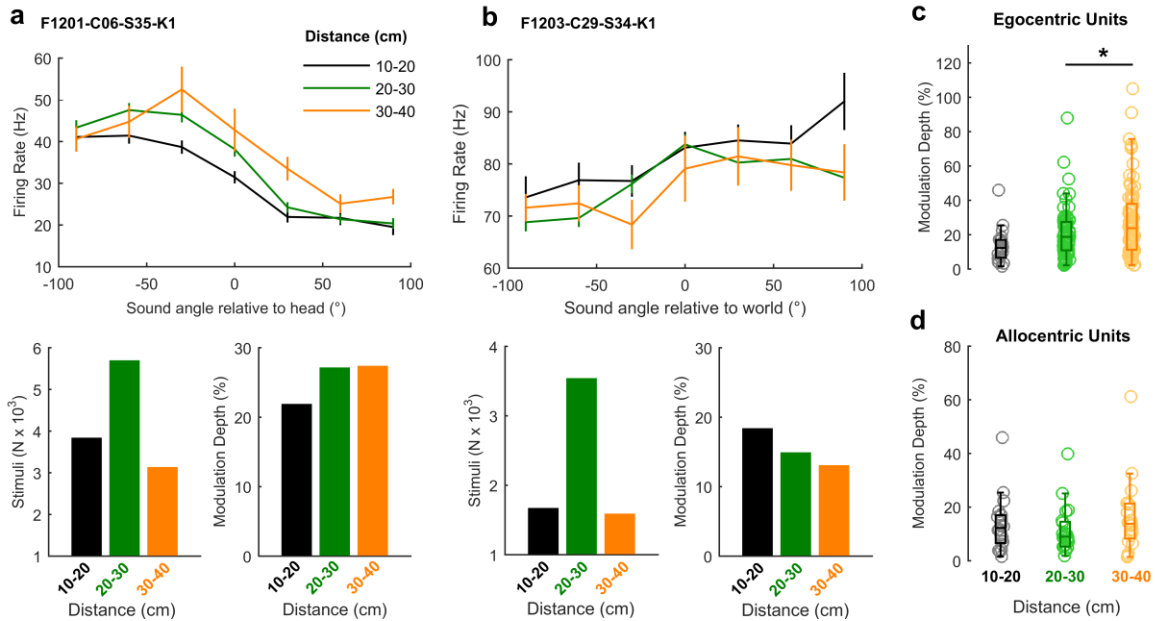
473 change as sound sources approach the head. For distant sound sources (typically > 1 m) ILDs are  
474 small relative to distance-related attenuation of sound; however ILDs become much larger as sounds  
475 approach the head and source-receiver distance decreases [27, 28]. Neurons must therefore  
476 accommodate for distance dependent cues to accurately represent sound location across changes in  
477 head position. In our study, the distance between head and sound source ranged from 10 cm (the  
478 minimum distance imposed by the arena walls) to 40 centimetres, with only 3.37% of stimuli (mean  
479 across 57 test sessions) presented at greater distances (Fig. 2g) and thus all stimuli were likely to  
480 produce large ILDs [27, 28].

481           Spatial tuning was observed at all distances studied in both egocentric (Fig 11a) and  
482 allocentric units (Fig 11b) however modulation depth increased with distance for egocentric units  
483 (ANOVA,  $F_{2,216} = 3.45$ ,  $p = 0.0334$ ). Pairwise post-hoc comparisons showed that modulation depth  
484 was largest for sounds at greatest distances (Fig 11c) though the only significant difference was  
485 found for sounds presented 20 to 30 cm and 30 to 40 cm away ( $t_{72} = -3.54$ ,  $p = 0.0279$ ). In contrast,  
486 modulation depth did not change significantly with distance for allocentric units (Fig 11d,  $F_{2,57} =$   
487  $0.962$ ,  $p > 0.1$ ).

---

488 **Fig 11 Spatial tuning across distance**

489 **a-b**, Tuning curves of an egocentric (**a**) and allocentric (**b**) unit obtained with sound sources at  
490 varying distances from the animal's head. Bar plots show the number of stimuli and modulation depth  
491 for each tuning curve. **c-d** Distributions of modulation depth measured across distance for egocentric  
492 and allocentric units. Asterisk indicates significant pair-wise comparison (Tukey-Kramer corrected,  $p$   
493  $< 0.05$ ).



494

495 **Speed modulation of cortical neurons and spatial tuning**

496 Changes in head position and direction also allowed us to investigate how speed of head  
 497 movement (Fig. 2f) affected neural activity. Movement is known to affect auditory processing in  
 498 rodents [29-31] but its effects on spatial representations of sound location and also on auditory  
 499 cortical processing in other phyla such as carnivores remain unknown. Here we presented click  
 500 sounds for which dynamic acoustic cues would be negligible and thus we could isolate the effects of  
 501 head movement on neural activity.

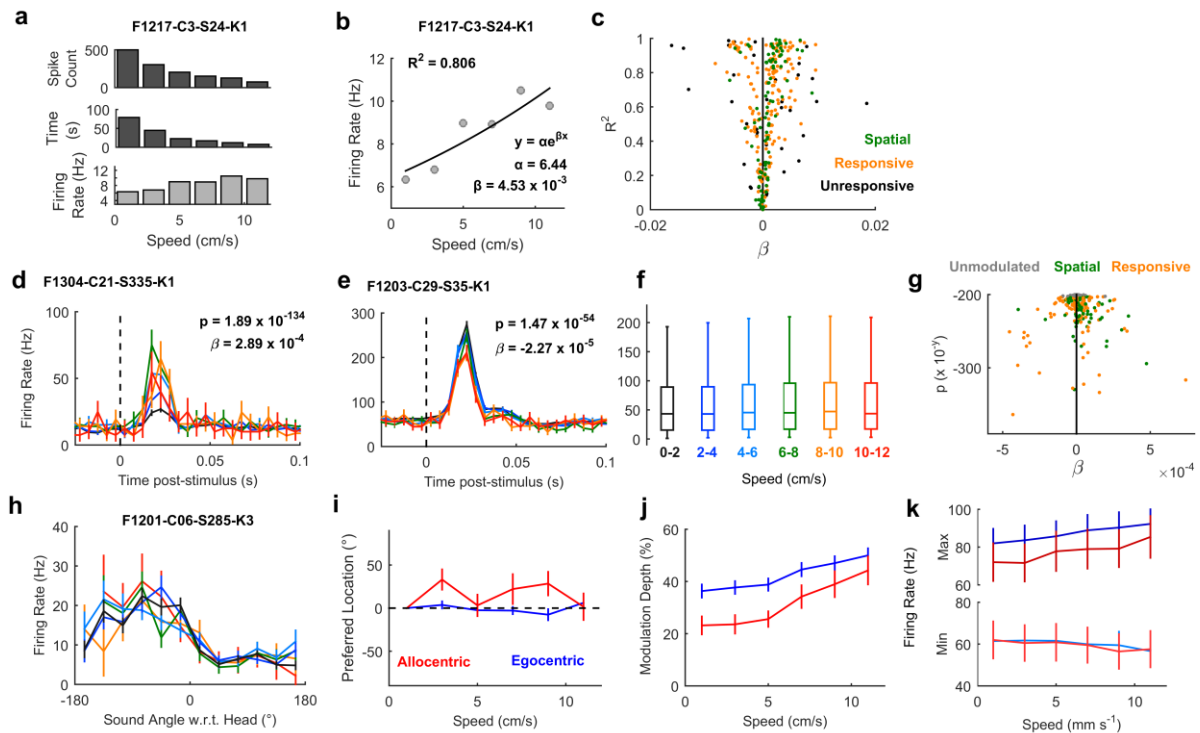
502 To address auditory cortical processing first, we asked how many of our recorded units  
 503 (regardless of auditory responsiveness or spatial modulation) showed baseline activity that varied  
 504 with speed. For each unit, we took all periods of exploration (excluding the 50 ms after each click  
 505 onset) and calculated the speed of the animal at the time of each action potential. We then  
 506 discretized the distribution of spike-triggered speeds to obtain spike counts as a function of speed  
 507 and normalized spike counts by the duration over which each speed range was measured. This  
 508 process yielded a speed-rate function for baseline activity (Fig 12a). We then fitted an exponential  
 509 regression curve to each function (Fig 12b) and plotted the correlation ( $R^2$ ) and regression

510 coefficients ( $\beta$ ) of each curve to map the magnitude and direction of association between speed and  
511 baseline activity (Fig 12c). Across the recorded population, we saw both positive and negative  
512 correlations representing units for which firing rate increased or decreased respectively with speed.  
513 However a significantly larger proportion of the population increased firing rate with speed across all  
514 units (t-test vs. 0;  $t_{308} = 3.77$ ,  $p = 1.97 \times 10^{-4}$ ). This was also true if we considered only sound  
515 responsive units ( $t_{267} = 5.15$ ,  $p = 5.17 \times 10^{-7}$ ) or only spatially tuned units ( $t_{91} = 4.12$ ,  $p = 8.41 \times 10^{-5}$ ).

---

516 **Fig 12 Speed related auditory cortical activity and sensory processing**

517 **a** Example calculation of speed-related modulation of baseline firing of one unit using reverse  
518 correlation. **b**, Example speed-firing rate function summarized using regression ( $\beta$ ) and correlation  
519 ( $R^2$ ) coefficients for the same unit as (a). **c**, Population distribution of regression and correlation  
520 coefficients showing the predominance of units with increasing speed-rate functions ( $\beta > 0$ ). **d-e**, Peri-  
521 stimulus time histogram of sound evoked responses for units that were modulated by speed: In (d)  
522 activity was enhanced as speed increased from 1 to 7 cm s<sup>-1</sup> and decreased thereafter. In (e) firing  
523 decreased with increasing speeds, although speed-related modulation was smaller relative to sound  
524 evoked activity than (d). **f**, Box plots showing distributions (median and inter-quartile range) of  
525 evoked firing rates in response to clicks across speed for all sound responsive units. **g**, Population  
526 distribution of regression coefficients ( $\beta$ ) and model fit (analysis of deviance p values) for all sound-  
527 responsive units. Units for which speed was not a significant predictor of neural activity ( $p > 0.001$ )  
528 denoted in grey. **h**, Spatial tuning curve for one unit for clicks presented at different head movement  
529 speeds. **i-k**, Change in preferred location (i), modulation depth (j) and min / max firing rates (k) of  
530 egocentric and allocentric units as a function of speed. Data for d-e and h-k shown as mean  $\pm$  s.e.m.



531

532

We also observed speed-related modulation of sound-evoked responses in individual units

533

(Fig. 12d-e). For each individual unit, we characterized the relationship between head speed and

534

single trial firing rates (averaged over the 50 ms post-stimulus onset) using a general linear model

535

that measured both the strength (analysis of deviance  $p$  value) and direction (model coefficient,  $\beta$ )

536

of association. Positive  $\beta$  values indicated an increase in firing rate with increasing speed whereas

537

negative  $\beta$  values indicated a fall in firing rate with increasing speed. Thus the direction of the

538

relationship between firing rate and speed was summarized by the model coefficient, allowing us to

539

map the effects of movement speed across the population (Fig. 12f). For 199/268 sound-responsive

540

units (74.3%), speed was a significant predictor of firing rate (analysis of deviance vs. a constant

541

model,  $p < 0.001$ ) however the mean coefficient value for movement sensitive units did not differ

542

significantly from zero ( $t_{199} = 0.643$ ,  $p = 0.521$ ). This suggests the sound-responsive population was

543

evenly split between units that increased or decreased firing with speed. We noted that a

544

significantly greater proportion of spatially modulated units (74/92, 80.4%) had sound evoked

545

responses that were sensitive to speed than units that were either not spatially modulated or for

546

which we had insufficient sample sizes to test spatial modulation (125/176, 71.0%)(Chi-squared test,

547  $\chi^2 = 3.96, p < 0.05$ ). For those 74 spatially modulated and speed sensitive units, coefficients were  
548 mostly larger than zero (mean  $\pm$  s.e.m. =  $2.73 \times 10^{-5} \pm 1.53 \times 10^{-5}$ ) however this effect was not  
549 statistically significant ( $t_{73} = 1.80, p = 0.076$ ). For the remaining speed sensitive units, the mean  
550 coefficients was closer to zero (mean  $\pm$  s.e.m. =  $-5.02 \times 10^{-6} \pm 1.49 \times 10^{-5}$ ).

551         Lastly, we asked if speed affected spatial tuning. Spatial tuning could be observed at all  
552 speeds of movement in spatially tuned units (Fig. 12h) and the preferred locations of units did not  
553 vary systematically with speed (Fig 12i). For neither egocentric nor allocentric units was there a  
554 significant effect of speed in an ANOVA on preferred locations (egocentric:  $F_{5, 432} = 0.53, p = 0.753$ ;  
555 allocentric:  $F_{5, 108} = 1.53, p = 0.188$ ). However we did observe significant changes in modulation  
556 depth (Fig 12j) both for egocentric ( $F_{5, 432} = 4.91, p = 0.0002$ ) and allocentric units ( $F_{5, 108} = 5.09, p =$   
557  $0.0003$ ), indicating that spatial modulation was greater when the head was moving fastest. Change  
558 in modulation depth resulted from both a gradual suppression in minimum and enhancement in  
559 maximum firing rates with speed (Fig 12k). However none of these changes in minimum or  
560 maximum firing rate were significant in comparisons across speed (ANOVA with speed as main  
561 factor,  $p > 0.5$ ) indicating that it was only through the aggregative change in responses to both  
562 preferred and non-preferred locations that modulation depth increased with speed.

## 563 **Discussion**

564         Here we have shown that by measuring spatial tuning curves in freely moving animals it is  
565 possible to demonstrate the coordinate frames in which neurons define sound location. For the  
566 majority of auditory cortical neurons, we found egocentric tuning that confirm the broadly held but  
567 untested assumption that within the central auditory pathway sound location is represented in  
568 head-centered coordinates. We also identified a small number of units with allocentric tuning,  
569 whose responses were spatially locked to sound location in the world, suggesting that multiple  
570 coordinate frames are represented at the auditory cortical level. These units were consistently

571 identified across different analyses, observed in several subjects and could be dissociated from  
572 egocentric receptive fields recorded in the same behavioral sessions. Finally we explored the  
573 dependence of neural activity and spatial tuning on sound source distance and the speed of head  
574 movements, demonstrating that both factors can modulate firing rates and spatial tuning in auditory  
575 cortex.

576 Our results show that an animal's movement can be successfully tracked to measure head-  
577 centered egocentric tuning during behavior. While we used speakers placed at 30° intervals across a  
578 range of 180°, we were nonetheless able to characterize spatial tuning of egocentric units around  
579 the full circumference of the head (i.e. Fig. 7b). This illustrates the practical benefit of using moving  
580 subjects to characterize head-centered spatial tuning as the animal's head rotation generates the  
581 additional variation in sound angle relative necessary to fully map azimuthal tuning with a reduced  
582 number of sound sources. Furthermore, as the animal's head direction was continuous, the stimulus  
583 angle was also continuous and thus it was possible to measure spatial tuning at finer resolutions  
584 than that of the speaker ring from which stimuli were presented. In contrast to egocentric tuning,  
585 our ability to map allocentric receptive fields was limited by the speaker arrangement that only  
586 sparsely sampled world coordinates (Fig 2a). This may in part explain the low number of allocentric  
587 units in our population and denser sampling of the world may reveal unseen allocentric tuning – for  
588 example in the 94 units we recorded that were not spatially modulated by sound locations in the  
589 world that we tested. While a full 360° speaker ring may offer a minor improvement in sampling  
590 density, the radial organization of the ring remains a suboptimal design for sampling rectangular or  
591 irregular environments. To fully explore the shape of allocentric receptive fields will require denser,  
592 uniform speaker grids or lattices in environments through which animals can move between sound  
593 sources.

594 A notable property of egocentric units was the relationship between modulation depth of  
595 spatial tuning and distance, which was absent in allocentric units. This distance sensitivity may



596 largely be driven by changes in inter-aural level differences, although other auditory and non-  
597 auditory cues can affect distance perception [32-36]. However modulation depth in our study was  
598 lowest for proximal sounds when ILDs would be larger, and when other cues such as inter-aural time  
599 differences remain relatively constant [27, 28]. Localization of nearby sound sources (< 1 m) is  
600 possible for ferrets and humans [37, 38], though within the range of distances we considered here,  
601 angular error of azimuthal localization in humans increases slightly as sounds approach the head  
602 [37]. Thus our findings are consistent with human psychophysical performance but suggest larger  
603 localization cues may not always produce better sound localization by neurons in auditory cortex. In  
604 future it will be critical to validate our findings for sound sources at greater distances where sound  
605 localization has been more widely studied.

606           In addition to recording many egocentric units, we also recorded a small number of  
607 allocentric units, supporting the idea that auditory cortex represents sound location in multiple  
608 coordinate frames [23] and parses an auditory scene into distinct objects [39, 40]. We believe this is  
609 the first study to look for world-centered encoding of sound locations at the cellular level and thus  
610 the units we recorded, while small in number, reflect a novel spatial representation in the auditory  
611 system.

612           A key question is where allocentric units reside in cortex: Egocentric and allocentric units  
613 were located on the same electrodes and cortical depths, in the primary and posterior regions of  
614 auditory cortex. However, the low density of electrodes in our arrays, and their placement over a  
615 low frequency border, prevented us from mapping the precise tonotopic boundaries necessary to  
616 attribute units to specific cortical subfields [41]. Future use of denser sampling arrays may enable  
617 cortical mapping in behaving animals and thus precise localization of allocentric units. We targeted  
618 the low-frequency reversal between primary and posterior auditory cortex as these areas are likely  
619 to be sensitive to inter-aural timing cues, and the animals involved in this work were also trained to  
620 discriminate non-spatial features of low frequency sounds in another study [42]. Posterior regions

621 may correspond to part of the ‘what’ pathway in auditory processing whereas the anterior  
622 ectosylvian gyrus may correspond to the ‘where’ pathway in which spatial tuning is more extensive  
623 [43, 44]. It is thus likely that the coordinate frames represented in our population (where only 49%  
624 of units were spatially sensitive) may be more ubiquitous in anterior regions of ferret auditory  
625 cortex. Indeed given sensorimotor and cross-modal coordinate frame transformations are a key  
626 feature of activity in parietal cortex [10], it is likely that allocentric representations exist beyond  
627 auditory cortex.

628         While the observation of allocentric receptive fields in tonotopic auditory cortex is novel, the  
629 existence of allocentric representations has been predicted by behavioural studies in humans [6, 13].  
630 Furthermore, coordinate transformations occur elsewhere in the auditory system [23, 45] and  
631 behavioral movements can influence auditory subcortical and cortical processing [29, 30]. Perhaps  
632 most importantly, vestibular signals are integrated into auditory processing already at the level of  
633 the cochlea nucleus [46] allowing the distinction between self and source motion [22]. Auditory-  
634 vestibular integration, together with visual, proprioceptive and motor corollary discharge systems,  
635 provides a mechanism through which changes in head direction can partially offset changes in  
636 acoustic input during movement to create allocentric representations. At present it is unclear  
637 whether allocentric representations require self-generated movement and it will be interesting to  
638 test if world-centered tuning is present if head direction is systematically varied in stationary  
639 animals.

640         It is also unclear how head position is also integrated into auditory processing. Positional  
641 information within the medial temporal lobe (or its carnivore equivalent) is a leading candidate given  
642 the connections between entorhinal and auditory cortex [47, 48]; however the functional  
643 interactions between these areas and their potential contributions to allocentric processing remain  
644 to be addressed. Another critical question relates to the visual (or other sensory) cues that animals  
645 may use to orient in the world and define allocentric representations. Given that head and place

646 cells remap in different settings [49, 50] and that auditory cortex receives tactile and visual  
647 information through multiple pathways [48, 51], it will be interesting to determine if changes in  
648 visual / tactile environment affects tuning of allocentric receptive fields, and if so, what  
649 environmental features anchor auditory processing.

650         Variation in the animal's head position with movement also allowed us to study the effects  
651 of head movement speed on auditory processing and spatial tuning. In contrast to other studies in  
652 freely behaving animals that reported movement-related suppression of activity [29-31] we found  
653 that neurons tended to fire more strongly when the head moved faster (Fig 12). One reason for this  
654 difference may lie in the behavior measured: Other investigators have covered a diverse range of  
655 actions including locomotion in which both the head and body move and self-generated sounds are  
656 more likely. We only considered the head speed of an animal and did not track the body position  
657 that would distinguish head movements from locomotion (which was relatively limited given the size  
658 of the animal and the arena). It is thus likely that much of the variation in speed we observe is a  
659 product of head movement during foraging without locomotion and thus with relatively little self-  
660 generated sound. The behavior of our subjects may therefore present different requirements for  
661 auditory-motor integration that result in distinct neural effects.

662         We also observed that spatial modulation was also greater when the animal was moving  
663 faster, which may be consistent with the sharpening of tuning curves during behavioral engagement  
664 [15]. While sharpening of engagement-related spatial tuning was linked to a reduction in spiking  
665 responses at untuned locations, we observed non-significant decreases in peak and minimum firing  
666 rates (which together increased modulation depth) suggesting that the mechanisms underlying  
667 speed-related modulation of spatial tuning may be subtly different. At the acoustic level, faster  
668 movements provide larger dynamic cues [2, 3] that improve sound localization abilities in humans [3,  
669 52, 53] and may explain the increase in modulation depth of units at greater speeds observed here.

670            In summary, we recorded spatial tuning curves in auditory cortex of freely moving animals to  
671   resolve coordinate frame ambiguity. We demonstrated many egocentric units representing location  
672   relative to the head and a small number of allocentric units representing sound location relative to  
673   the world. We also studied the role of distance and speed in auditory cortical processing. Together  
674   our findings illustrate that auditory cortical processing of sound space may extend to multiple  
675   coordinate frames and spatial dimensions such as azimuth and distance, as well as non-auditory  
676   variables such as speed of movement.

677 **Methods**

678 **Ethics statement**

679 All experimental procedures were approved by a local ethical review committee (AWERB;  
680 University College London and The Royal Veterinary College, University of London) and performed  
681 under license from the UK Home Office (Project License 70/7267) and in accordance with the  
682 Animals (Scientific Procedures) Act 1986.

683 **Simulated spatial receptive fields**

684 Egocentric

685 Egocentric tuning described the relationship between spike probability ( $P$ ) and sound source  
686 angle relative to the midline of the subject's head ( $\theta_{HS}$ ) and was simulated in Matlab (MathWorks)  
687 using a Gaussian function:

$$P(\theta) = ae^{-\frac{(\theta_{HS}-b)^2}{2c^2}} \quad (1)$$

690 In the example shown in figure 1a, parameters ( $a = 1.044$ ,  $b = 0^\circ$  and  $c = 75.7^\circ$ ) were determined by  
691 manual fitting to find values for which egocentric and allocentric tuning matched qualitatively. The  
692 theta domain was between  $\pm 180^\circ$  binned at  $1^\circ$  intervals and distance of sound sources was not  
693 included in the simulation.

694 Allocentric

695 Allocentric tuning describes the relationship between neural output (reported here as spike  
696 probability;  $P$ ) and sound source position within the world measured in Cartesian ( $x, y$ ) coordinates.  
697 Spatial tuning was simulated as the dot product of spike probability vectors returned from functions  
698 defined separately for positions on the x- and y-axes:

699 
$$P(x, y) = f(x) \cdot f(y) \tag{2}$$

700 In figure 1b, logistic probability functions were used for both dimensions:

701 
$$f(x) = \frac{e^{-\frac{(x-\mu)}{s}}}{s \left(1 + e^{-\frac{(x-\mu)}{s}}\right)^2}$$

702 
$$\tag{3}$$

704 
$$f(y) = \frac{e^{-\frac{(y-\mu)}{s}}}{s \left(1 + e^{-\frac{(y-\mu)}{s}}\right)^2}$$

703 
$$\tag{4}$$

705 With  $\mu = 1000$  mm and  $s = 400$  mm for the x-axis, and  $\mu = 0$  mm and  $s = 1000$  mm for the y-axis. For  
706 both axes, spike probability vectors were generated for domains between  $\pm 1500$  mm binned at 2  
707 mm intervals.

708 Stimulus presentation, head pose and movement

709 The position and orientation of the subject's head within the world was described as a  
710 coordinate frame transform composed of a translation vector between origins (indicating the head  
711 position) and a rotation matrix between axes (indicating the head direction). Stimuli were presented  
712 on each time step of the simulation from each speaker in a ring at  $10^\circ$  intervals, 1000 mm from the  
713 origin of the world coordinate frame. As the simulation was deterministic, each stimulus was  
714 presented to static simulations only once to calculate the response. When simulating motion, a  
715 'pirouette' trajectory was constructed in which the subject's head translated on a circular trajectory  
716 (radius = 50 mm; angular speed =  $30^\circ$  per time-step) while simultaneously rotating (angular speed =  
717  $10^\circ$  per time-step) for 7200 stimulus presentations (Supplementary Video 2). For each stimulus  
718 presentation, the stimulus angle was calculated relative to both the midline of the head and the  
719 vertical axis of the arena (Supplementary Fig 9). Simulation responses were quantized in  $1^\circ$  bins.

## 720 **Animals**

721           Subjects were five pigmented female ferrets (1-5 years old) trained in a variety of  
722 psychophysical tasks that did not involve the stimuli presented or the experimental chamber used in  
723 the current study. Each ferret was chronically implanted with Warp-16 microdrives (Neuralynx, MT)  
724 housing sixteen independently moveable tungsten microelectrodes (WPI Inc., FL) positioned over  
725 middle and posterior fields of left or right auditory cortex. Details of the surgical procedures for  
726 implantation and confirmation of electrode position are described elsewhere[54]. The weight and  
727 water consumption of all animals was measured throughout the experiment. Regular otoscopic  
728 examinations were made to ensure the cleanliness and health of ferrets' ears.

729           Subjects were water-restricted prior to testing, during which they explored the experimental  
730 arena to find freely available sources of water. On each day of testing, subjects received a minimum  
731 of 60ml/kg of water either during testing or supplemented as a wet mash made from water and  
732 ground high-protein pellets. Subjects were tested in morning and afternoon sessions on each day for  
733 up to three days in a week (i.e. a maximum of six consecutive testing sessions); on the remaining  
734 weekdays subjects obtained water in performance of other psychophysical tasks. Test sessions  
735 lasted between 10 and 50 minutes and were ended when the animal lost interest in exploring the  
736 arena.

737

## 738 **Experimental Design and Stimuli**

739           In each test session, a ferret was placed within a D-shaped arena (Fig. 2a, rectangular  
740 section: 35 x 30 cm [width x length]; semi-circular section: 17.5 cm radius; 50 cm tall) with seven  
741 speakers positioned at 30° intervals, 26 cm away from a central pillar from which the animal could  
742 find water. The periphery of the circular half of the arena was also fitted with spouts from which  
743 water could be obtained. Animals were encouraged either to explore the arena by delivery of water

744 at all spouts, or to hold their head at the center spout by restricted water delivery at this location.  
745 The arena and speakers were housed within a sound-attenuating chamber lined with 45 mm sound-  
746 absorbing foam.

747 During exploration (n = 57 test sessions), clicks were presented from each speaker with  
748 random inter-stimulus intervals (250 – 500 ms). The instantaneous energy of clicks minimized  
749 dynamic cues, simplifying neural analysis and comparisons with other work on spatial encoding.  
750 Clicks were presented at 60 dB SPL when measured from the center of the arena using a measuring  
751 amplifier (Bruel & Kjaer 2636). However because sound level varied across the arena, we roved  
752 sound levels over a  $\pm 6$  dB range to reduce changes in level arising from differences in position of the  
753 head within the sound field. The frequency response of each speaker (Visaton SC 5.9) was measured  
754 using goly codes [55] and compensated for to produce a flat spectral output between 20 Hz and 20  
755 kHz. Stimulus location and water delivery were independent and subjects were not required to  
756 attend to stimuli in order to find water rewards. To avoid characterizing neural responses to the  
757 sound of solenoid control signals, stimulus presentation and water reward were delivered in  
758 separate alternating time windows; water was delivered in a short period of 1 to 2 seconds when  
759 each solenoid was rapidly opened (100 ms duration) with a 10 second interval between delivery  
760 windows in which click stimuli were presented. Sessions typically lasted approximately 15 - 20  
761 minutes (median = 16.5 minutes; range = 6.15 – 48.0 minutes) in which several thousand stimuli  
762 could be presented (median = 1984; range = 304 – 3937).

### 763 **Head Tracking**

764 During exploration of the experimental arena, the animal's head position and orientation  
765 were tracked using two LEDs (red and green) placed along the midline of the head and recorded  
766 using an RV2 video acquisition system (TDT) sampling at 30 frames per second and synchronized  
767 with the electrophysiology recording hardware. For each video frame, the red and green LED  
768 positions were identified in Matlab from a weighted image in which the channel color of the target



769 LED was positively weighted and all other channels negatively weighted. Each LED position was then  
770 taken as the center of the largest cluster of pixels containing the maximum weighted value. To  
771 maximize the frame rate of the camera, we recorded with a low exposure time (10-20 ms). Lower  
772 exposure also improved LED identification by reducing signal intensity in the background of each  
773 frame.

774 In cases where an LED went out of view of the camera (usually due to the roll or pitch of the  
775 head, or the recording cables obscuring the LED), the maximum weighted value identified as the LED  
776 would be a random point within the arena resulting either from a weak reflection or image noise. To  
777 remove such data, we set a minimum intensity threshold based on the distribution of maximum  
778 values in weighted images across all frames. In cases where the LED intensity failed to match the  
779 specified threshold, the LED position was noted as missing. To compensate for missing data, we  
780 estimated LED positions across runs of up to a maximum of ten frames (333 ms) using spline  
781 interpolation. Longer runs of missing data were discarded.

782 We then mapped each LED position in the image ( $M$ ) into the behavioral arena to give the  
783 new position  $N$  using the transformation:

$$784 \quad N = T + RM \quad (5)$$

785 Where  $T$  is the translation between the origin of the image coordinate frame (i.e. pixel [0,0]) and the  
786 origin of the arena coordinate frame (the center of the arena). And,  $R$  is the three-dimensional  
787 rotation matrix describing the rotation between the arena and image coordinate frames.  $T$  was  
788 obtained by manually identifying the pixel closest to center of the arena (i.e. the equidistant point  
789 between all speakers) in a calibration image captured at the start of each test session.  $R$  was  
790 estimated from singular value decomposition using the position and distance between known points  
791 in the arena (also identified manually from each calibration image). Here we estimated a 3D rotation  
792 matrix to take into account the position of the camera relative to the arena (i.e. above the arena

793 rather than below). All coordinate frames were represented using the right-hand rule (i.e. positive  
794 values for counter-clockwise rotation about the z-axis) to ensure consistency with the *atan2*  
795 function.

796 The animal's head position ( $\overline{AH}$ ) was then calculated as the mid-point between the LEDs  
797 within the arena and was used to define the origin of the head-centered coordinate frame  
798 (Supplementary Fig 9). The animal's head direction ( $\theta_{HA}$ ) was calculated from the two argument  
799 arctangent function (*atan2*) of the vector between LEDs that defined the midline (Y-axis) of the  
800 head-centered coordinate frame ( $\hat{H}$ ). The Z axis was undefined by the tracking system as we only  
801 measured two points (red and green LEDs) with a single camera; this leads to ambiguity about the  
802 pitch and roll of the head. To compensate for this deficiency we assumed that when LEDs were  
803 visible, the XY plane of the head always matched the plane of the arena floor and that the Z-axis of  
804 the head was orthogonal to this plane and oriented towards the camera. Such assumptions are  
805 justified by the properties of the tracking system – as the head rolls or pitches away from the  
806 assumed conditions, it becomes impossible to identify both LEDs within the image due to the limited  
807 angular range of the each diode. Therefore tracking was impossible (in which case data was  
808 discarded) in the same conditions in which our assumptions became untenable.

809 By using the frame times recorded on the device, it was possible to create a time series of  
810 head position and direction within the arena that could be compared to the spiking pattern of  
811 neurons. We used the inter-frame interval and change in position of the head origin, smoothed with  
812 a nine-point Hann window to calculate the speed of head movement.

### 813 **Neural Recording**

814 Neural activity in auditory cortex was recorded continuously throughout exploration. On  
815 each electrode, voltage traces were recorded using TDT System III hardware (RX8 and RZ2) and  
816 OpenEx software (Tucker-Davis Technologies, Alachua, FL) with a sample rate of 25 kHz. For

817 extraction of action potentials, data were band-pass filtered between 300 and 5000 Hz and motion  
818 artefacts were removed using a decorrelation procedure applied to all voltage traces recorded from  
819 the same microdrive in a given session [56]. For each channel within the array, we identified  
820 candidate events as those with amplitudes between -2.5 and -6 times the RMS value of the voltage  
821 trace and defined waveforms of events using a 32-sample window centered on threshold crossings.  
822 Waveforms were then interpolated (128 points) and candidate events combined across sessions  
823 within a test run for spike sorting. Waveforms were sorted using MClust (A.D. Redish, University of  
824 Minnesota, <http://redishlab.neuroscience.umn.edu/MClust/>) so that candidate events were  
825 assigned to either single-unit, multi-unit clusters or residual hash clusters. Single units were defined  
826 as those with less than 1% of inter-spike intervals shorter than 1 millisecond. In total 331 units were  
827 recorded, including 116 single units (35.1%).

#### 828 **Tracking unit identity across recording sessions**

829 Through the experiment, electrodes were descended progressively deeper into cortex at  
830 intervals of 50 – 100  $\mu\text{m}$  to ensure sampling of different neural populations. At most recording sites,  
831 we tested animals on multiple sessions (1-6 sessions) across several (1-3) consecutive days.  
832 Conducting test sessions over multiple days makes possible the recording of different units at a  
833 single recording site over time (i.e. through electrode drift, gliosis etc.). To constrain our analysis to  
834 units with a consistent identity we tracked the waveform of recorded units across sessions within a  
835 test run. Our rationale was that a unit should have a constant waveform shape across test sessions  
836 and any differences in waveform shape should be small relative to differences in the waveforms of  
837 units measured on other electrodes or at other depths by the same electrode. Thus for one test  
838 session at a given recording site, we calculated the Euclidean distance matrix between the mean  
839 waveform recorded on that session ( $W_{\text{Test}}$ ) and the mean waveform recorded on each additional  
840 session at the same recording site ( $D_{\text{Test}}$ ). We also calculated the distances between  $W_{\text{Test}}$  and the  
841 mean waveform recorded for every session at different recording sites ( $D_{\text{Control}}$ ).  $D_{\text{Control}}$  provided null

842 distributions for waveform distances between pairs of neurons known to have separate identities  
843 (due to the spatial separation between electrodes at recording sites [ $>50\ \mu\text{m}$  in depth,  $>500\ \mu\text{m}$   
844 laterally]). For a given waveform, we then calculated the statistical probability of observing distances  
845 between test waveform and waveforms *at the same recording site* given the distribution of distances  
846 between test waveforms and waveforms *at other recording sites*. For waveforms exceeding  
847 statistical significance (t-test;  $p < 0.05$ , Bonferroni corrected for the number of sessions conducted at  
848 the recording site), we concluded that the same neuron or neuronal population was recorded.

849 For runs of test sessions, we took the longest continuous run for which waveform distances  
850 were significantly smaller than expected by chance. The majority of units tested more than once  
851 could be tracked over all sessions tested (72.4%: 126 / 174 units) although the number of neurons  
852 tracked fell off with time.

### 853 **Data Analysis**

854 During exploration we characterized sound evoked responses from auditory cortical units.  
855 Each click stimulus and the concomitant neural response could be related to controlled variables  
856 determined by the experimental design and measured variables observed from head tracking.  
857 Controlled variables were the position of the sound source relative to the arena and sound source  
858 level in dB SPL whereas measured variables were the position and direction of the head relative to  
859 the arena, as well as head speed. Controlled and measured variables were combined to determine  
860 several experimental parameters: Stimulus position relative to the head was calculated as the vector  
861  $\overrightarrow{HS}$ :

$$862 \qquad \qquad \qquad \overrightarrow{HS} = \overrightarrow{AS} - \overrightarrow{AH} \qquad \qquad \qquad (6)$$

864 Where  $\overrightarrow{AH}$  is the vector from arena origin to head origin and  $\overrightarrow{AS}$  is the vector from arena origin to  
865 the sound source. Stimulus angle relative to the head ( $\theta_{HS}$ ) was calculated by subtracting head

866 direction in the arena ( $\theta_{HA}$ ) from the stimulus angle relative to the origin of the head coordinate  
867 frame:

$$\theta_{HS} = \text{atan2}(\overrightarrow{HS}_y, \overrightarrow{HS}_x) - \theta_{HA} \quad (7)$$

870 The distance between head and stimulus was calculated as the magnitude of  $\overrightarrow{HS}$  and expressed as a  
871 ratio relative to the distance between arena and stimulus to calculate sound level at the head:

$$p_H = p_A \cdot \frac{|\overrightarrow{AS}|}{|\overrightarrow{HS}|} \quad (8)$$

874 Where  $P_H$  and  $P_A$  are sound pressures at the head and center of the arena expressed in pascals and  
875 sound level is expressed in dB SPL:

$$L = 20 \cdot \log_{10} \left( \frac{\tilde{p}}{2 \times 10^{-5}} \right) \quad (9)$$

878 Sound level was calibrated to 60 dB SPL (0.02 Pa) at the center of the arena.

879 For each variable we calculated the value at the time of stimulus presentation (i.e. with a lag  
880 of 0 ms) and contrasted these values with the spiking responses of neurons. To study encoding of  
881 stimulus features (both measured and control variables) by neurons, single trial responses of  
882 individual units were summarized as the mean firing rate 0 – 50 ms after stimulus onset. This  
883 window was sufficiently long to characterize the response of units (Supplementary Fig. 5a and 6a)  
884 but also short enough that changes in head direction and position during the analysis window were  
885 small (Supplementary Fig 3). Sound-responsive units (268/336) were first identified as those with  
886 evoked firing rates that differed significantly from background activity measured in the 50 ms before

887 stimulus presentation (GLM analysis of deviance using Poisson distributions and log link function;  $p \leq$   
888 0.05).

889         Spatially tuned units were then identified using sound-evoked responses collected with the  
890 animal at the center of the arena with the head and world coordinate frames in approximate  
891 alignment. For a stimulus presentation to be included in this analysis, the animal's head origin was  
892 required to be within 5 cm of a point 2.5 cm behind the arena center (Supplementary Fig. 4a). The  
893 2.5 cm offset was applied to provide an approximate account for the distance between the animal's  
894 snout and head center. Head direction was also required to be within  $\pm 15^\circ$  of the midline of the  
895 arena (i.e. the line of symmetry of the arena, so that the animal was facing forward). Sound-evoked  
896 responses under these constraints were then fitted with a GLM (Poisson distribution; log link  
897 function) with sound source angle relative to the head binned in  $30^\circ$  intervals as predictor. To ensure  
898 adequate data for statistical testing, units were only assessed if responses were recorded for  $\geq 5$   
899 stimulus presentations in each angular bin (186/268 units). Units for which sound source angle  
900 significantly reduced model deviance ( $\chi^2$  distribution,  $p \leq 0.05$ ) were classed as spatially tuned  
901 (92/186 units). While this approach may not identify all spatially informative neurons (some of which  
902 may signal sound location by spike timing rather than rate [18, 57] or that may be tuned only to  
903 sounds behind the head that were not sampled by speakers in the aligned condition) it identified a  
904 sub-population of spatially sensitive units on which further analysis could be performed.

905         To calculate spatial tuning curves, analysis was expanded to include all head positions and  
906 directions recorded. To calculate world-based tuning curves, mean firing rate across trials (0 - 50 ms)  
907 was plotted for each sound source angle relative to the arena. For head-based tuning curves, sound  
908 source angle relative to the head was binned at  $30^\circ$  intervals and mean spike rate plotted as a  
909 function of the bin center angle. To study super-resolution tuning of egocentric units (Fig 5a-b), the  
910 bin width used to calculate curves was reduced to  $20^\circ$ ,  $10^\circ$ ,  $5^\circ$ ,  $2^\circ$ , or  $1^\circ$ . To compare spatial tuning of  
911 egocentric units with other studies, we also calculated preferred location, modulation depth and

912 tuning width and equivalent rectangular receptive field width for spatial tuning curves calculated  
913 relative to the head across 360° according to the methods used for awake cats [15, 18]. For  
914 allocentric units, we calculated preferred location and modulation depth for across sound location in  
915 the world.

### 916 **Modulation depth analysis**

917 For each unit we calculated the depth of spatial modulation for tuning curves in each  
918 coordinate frame. Unless otherwise stated, modulation depth (MD) was calculated as:

$$920 \quad MD = \frac{\max(x) - \min(x)}{\max(x)} \times 100$$

919 ( 10 )

921 Where  $x$  is the vector of firing rates in response to sounds located in each 30° bin between ±90°  
922 either of the world or head coordinate frame.

923 Modulation depth could also be calculated for simulated neurons using the same equation  
924 but with  $x$  being a vector of spike probabilities. This approach allowed us to calculate modulation  
925 depth for simulated allocentric and egocentric units when presented with sounds during observed  
926 animal movement (Fig 3). In simulations, modulation depth could be calculated in head and world  
927 coordinate frames that were either relevant or irrelevant for neural activity depending on whether  
928 the simulation was allocentric or egocentric. We termed modulation depth in the irrelevant  
929 coordinate frame *residual modulation* when expressed as a ratio of modulation in the represented  
930 coordinate frame:

$$932 \quad \text{Residual Modulation} = \frac{MD_{Irrelevant}}{MD_{Relevant}}$$

931 ( 11 )

933 For allocentric simulations, the world was relevant and the head was irrelevant; whereas for  
934 egocentric simulations, the head was relevant and the world was irrelevant.

935 For each test session in which we observed animal behavior, we compared the relationship  
936 between the residual modulation calculated during simulations of both allocentric and egocentric  
937 units, with the standard deviation of the head directions ( $\sigma$ , Fig 3). We fitted a linear regression  
938 model to this relationship that was subsequently used to test if observed modulation depth values of  
939 real units were significantly greater than the residual modulation expected from the animal's  
940 behavior. The linear regression model was fitted using the *fitlm* function in Matlab (R2015a). For  
941 each observed unit we measured the standard deviation of head angles during neural testing ( $\sigma$ )  
942 and, together with the regression models, predicted the 95% or 99.95% (post-Bonferroni correction  
943 for 92 units) confidence interval of residual modulation values in the head and in the world  
944 coordinate frame. Prediction was performed in Matlab using the *predict* function with the most  
945 conservative options selected (simultaneous confidence bounds and prediction for new observations  
946 rather than fitted mean values) to give the widest confidence intervals and thus minimize the  
947 probability of false positives. If the observed modulation depth of a unit in a particular coordinate  
948 frame exceeded the upper bound of the confidence interval for that frame, we identified it as  
949 significantly modulated.

## 950 **General Linear Models (GLMs)**

951 To compare the relationship between single trial firing rates and sound source angles in the  
952 head and world coordinate frames, we fitted the average firing rate on each trial (0-50 ms) with a  
953 generalized linear regression model (Matlab, *fitglm* function: Poisson distribution, log link function).  
954 For both sound source angles relative to the head and relative to the world, we measured the  
955 deviance of models fitted separately with each parameter ( $D_{\text{Test}}$ ). The Akaike information criterion  
956 [24] was used to compare test models and distinguish allocentric and egocentric units as those for  
957 which sound source angle relative to the world or head respectively provided the best model. For all



958 but one unit that was excluded from further analysis, either sound source angle relative to the world  
959 or head improved model fit compared to a constant model (analysis of deviance; Bonferroni  
960 correction for two comparisons;  $p < 0.05$ ).

961 To visualize GLM performance (Fig 6), we calculated *model fit* for each unit and coordinate  
962 frame as:

$$964 \quad \text{Model Fit} = \frac{D_{Const} - D_{Test}}{D_{Const} - D_{Full}} \quad (12)$$

965 Where  $D_{const}$  was the deviance resulting from a constant model, and  $D_{Full}$  was the deviance resulting  
966 from a full linear model that included both sound source angle relative to the head and relative to  
967 the world. We compared the model fit for data obtained when the head and world coordinate  
968 frames were free to vary, and when we restricted data to cases when the head and world coordinate  
969 frames were aligned (see above). We also repeated our analysis but with speaker identity or head  
970 direction information randomly shuffled between stimulus presentations prior to calculation of  
971 spatial tuning curves. Shuffling was repeated 1000 times and, across shuffles, we calculated the  
972 median model fit in head and world coordinate frames. Here we used the median rather than mean  
973 of the permuted values across shuffles were not always normally distribution. To test the effect of  
974 shuffle on model fit of all units, we performed a two-way anova on change in model fit with shuffle,  
975 with coordinate frame (head / world) and unit class (egocentric / allocentric). Post-hoc tests were  
976 conducted on change in model fit vs zero (t-test) with Bonferroni correction for multiple  
977 comparisons.

978 For each analysis in which we calculated model fit, we also calculated *model preference* as:

$$980 \quad \text{Model Preference} = \text{Model Fit}_{Head} - \text{Model Fit}_{World} \quad (13)$$

981 Model preference could thus vary between -100% (better fit for neural data based on sound angle in  
982 the world) and +100% (better fit for neural data based on sound angle relative to the head).

983 For time-based comparison of model performance, we reduced the time over which firing  
984 rates were considered (from 50 to 20 ms) and repeated the analysis with a window offset by -60 ms  
985 to 90 ms after stimulus presentation that moved with a 2 ms interval. Model fit and preference  
986 values for allocentric and egocentric units were compared across time using a non-parametric  
987 cluster-based statistical test [26] implemented in Matlab through the FieldTrip toolbox [58].

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991

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