# Multivariable Control for a Three-Phase Rectifier Based on Deadbeat Algorithm

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Abstract—This paper presents a deadbeat control technique applied in a voltage source rectifier to regulate both the dc voltage (active power) and reactive power injected to the grid. As the deadbeat control is based on the system model, it leads to a faster response, without overshoot and no need to tune the controller parameters. Hence, it is used to fully control the voltage source rectifier, achieving a fast dynamic response for both the dc voltage and the power factor at the point of connection. However, there are some issues related to the high amount of power required to reach the references -especially in the dc voltage- in a few control steps. The proposed technique also protects the equipment by limiting the maximum power drained to/from the source. The mathematical development is made as a function of the converter power in order to limit it, but at the same time tracking the references with high dynamics, characteristic typical of deadbeat control.

#### Keywords—Deadbeat Control; Voltage Source Rectifier.

#### I. INTRODUCTION

Power converters have given significant solutions to the actual industry, providing accurate control of power, voltage and current, in low, medium and high power applications [1], [2]. However, power converters –voltage and current source-exhibit a nonlinear behavior, which complicates the mathematical analysis and their control. Therefore, many control techniques have been developed in order to manage the currents and voltages of power electronic devices [3] – [6]. Despite linear control fits better for these nonlinear systems [7] – [12].

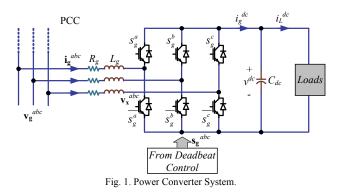
Among recently introduced control techniques, model based predictive control has been successfully applied to power converters, because the model and –consequently- its behavior can be easily found by using the Kirchhoff laws. Finite Control Set-Model Predictive Control (FS-MPC), for example, is based on predicting the system behavior using all possible converter available states and applying at the next sampling time the one that minimizes a specific cost function [8], [9]. However, there are other techniques -also based on predictive control- that do not use all possible cases to reach the references [7], [10], among them, the deadbeat control [13]-[16].

This paper proposes a novel deadbeat method applied to active rectifiers based on the voltage source converter. Deadbeat control is a technique with significant advantages as fast dynamic response, because it tries to track the references as soon as the model allows, *i.e.* the reference will be reached depending on the systems order. Traditionally, deadbeat controller is implemented only for current control [9], [11], [12]. This work however suggests a deadbeat approach for the control of whole system in a multivariable configuration, replacing the conventional linear control for the *dc* voltage.

The employed topology uses a three-phase converter with an RL input filter, which allows to boost the voltage from the *ac* side to the *dc* side, which in turn contributes with a second order dynamic in the current behavior. In addition, a *dc* capacitor is included to storage the power taken from the *ac* side and to maintain a desired *dc* voltage level, giving an additional dynamic. Thus, it can be seen that the whole system has a third order response; then, theoretically, the reference can be reached in three sampling steps at most.

Regardless the deadbeat control theory, there are some concerns related to nonlinear power converters, one of them is related with the saturation due to the maximum voltage that can be injected by the power converter, limited by the dc voltage. On the other hand, the maximum power that can be requested by the rectifier is limited by the maximum current that the RL input filter and the switches may bear. Therefore, a power control is also recommended if a deadbeat controller is implemented [9].

Thus, a deadbeat strategy is introduced, based on the power control in order to attain the advantages of quick response and minimum overshoot provided by the deadbeat technique, but at the same time protecting the system from overpower. The aforementioned issues entail a control algorithm based on the system model, with the aim to control the *dc* voltage and the power factor using the active and reactive power, respectively, which in turn gives the current references.



Once the current references are established –by the power control and the supply voltage- the converter voltage is selected –based on the model- and synthetized by a space vector modulation technique. The results show the fast dynamic and the minimum overshoot obtained with this technique. Furthermore, the resulting algorithm is easy to implement in a digital environment; thus, the whole analysis is performed in the discrete domain in order to facilitate the digital implementation.

#### II. POWER CONVERTER MODEL

# A. abc Reference Frame Model

The three-phase Active Front End (AFE) topology used in this work is shown in Fig. 1, where the RL input filter imposes the current dynamics and the dc capacitor the dc voltage dynamics. The voltage Kirchhoff law in the ac side leads to:

$$\mathbf{v}_{\mathbf{g}}^{\ abc} = L_g d\mathbf{i}_{\mathbf{g}}^{\ abc} / dt + R_g \mathbf{i}_{\mathbf{g}}^{\ abc} + \mathbf{v}_{\mathbf{x}}^{\ abc} , \qquad (1)$$

and formulating the current Kirchhoff law on the dc side:

$$C_{dc} dv^{dc} / dt = i_g^{\ dc} - i_L^{\ dc} .$$
 (2)

where the current and voltage through the power converter is:

$$\mathbf{v}_{\mathbf{x}}^{abc} = \mathbf{s}_{\mathbf{g}}^{abc} v^{dc}, \ \dot{i}_{g}^{dc} = \mathbf{s}_{\mathbf{g}}^{abc} \mathbf{i}^{gabc}$$
(3)

#### B. αβ Reference Frame Model

The model can be transformed to the  $\alpha\beta$  reference frame, in order to reduce the number of equations, for balanced systems. The transformation used is given by:

$$\mathbf{x}^{\alpha\beta} = \sqrt{\frac{2}{3}} \begin{bmatrix} 1 & -1/2 & -1/2 \\ 0 & \sqrt{3}/2 & -\sqrt{3}/2 \end{bmatrix} \mathbf{x}_{abc} , \qquad (4)$$

where  $\mathbf{x}^{abc}$  and  $\mathbf{x}^{\alpha\beta}$  represent the variable in *abc* and  $\alpha\beta$  reference frames, respectively. Therefore, the power converter model can be rewritten with the fobllowing equations:

$$\mathbf{v}_{\mathbf{g}}^{\alpha\beta} = L_g d\mathbf{i}_{\mathbf{g}}^{\alpha\beta} / dt + R_g \mathbf{i}_{\mathbf{g}}^{\alpha\beta} + \mathbf{v}_{\mathbf{x}}^{\alpha\beta} , \qquad (5)$$

$$C_{dc}dv^{dc} / dt = \mathbf{s}_{\mathbf{g}}^{\ \alpha\beta}\mathbf{i}_{\mathbf{g}}^{\ \alpha\beta} - i_{L}^{\ dc} . \tag{6}$$

# C. Discrete Time Modeling

For digital implementation, it is recommended to discretize the power converter model in order to use these equations on the control design. The most used discretization method is performed through the Euler approximation, and given by:

$$dx(t)/dt \approx \left(x(k+1) - x(k)\right)/T_s, \qquad (7)$$

where x represents the discretized derivate approximation, and  $T_s$  the sampling time. Therefore, the power converter model can be rewritten, using (7), in the discrete form as:

$$\mathbf{v}_{\mathbf{g}}^{\alpha\beta}(k) = L_{g} \frac{\mathbf{i}_{g}^{\alpha\beta}(k+1) - \mathbf{i}_{g}^{\alpha\beta}(k)}{T_{s}} + R_{g}\mathbf{i}_{g}^{\alpha\beta}(k) + \mathbf{v}_{x}^{\alpha\beta}(k), (8)$$

$$v_{g}^{dc}(k+1) - v_{g}^{dc}(k+1) - v_{g}^{dc}(k+1) - v_{g}^{dc}(k) + v_{g}^{\alpha\beta}(k) + v_{g}^{\alpha$$

$$C_{dc} \frac{v (\kappa+1) - v (}{T_s} = \mathbf{s}_{\mathbf{x}}^{\alpha\beta}(k) \mathbf{i}_{\mathbf{g}}^{\alpha\beta}(k) - i_L^{dc}(k).$$
(9)

# III. DEADBEAT CONTROL

The aim of the control study is to manage the dc voltage and the power factor at the Point of Common Coupling (PCC). Both of them are related to the power consumed by the converter which, in fact, tie the ac power to the dc power.

#### A. Desired Voltage Injected by the Converter

The voltage injected by the rectifier named  $v_x$  can be calculated from (8) as:

$$\mathbf{v}_{\mathbf{x}}^{\alpha\beta}(k) = \mathbf{v}_{\mathbf{g}}^{\alpha\beta}(k) - L_{g} \frac{\mathbf{i}_{g}^{\alpha\beta}(k+1) - \mathbf{i}_{g}^{\alpha\beta}(k)}{T_{s}} - R_{g} \mathbf{i}_{g}^{\alpha\beta}(k)$$
(10)

where  $\mathbf{i}_{g\alpha\beta}(k + 1)$  can be established as the current reference imposing a given  $\mathbf{v}_{\mathbf{x}\alpha\beta}(k)$  to reach this reference in one step ahead. However, due to the impossibility to apply the voltage  $\mathbf{v}_{\mathbf{x}\alpha\beta}(k)$  at time k, because of the intrinsic computing delay, the expression (10) must be one step forwarded leading to:

$$\mathbf{v}_{\mathbf{x}}^{\alpha\beta}(k+1) = \hat{\mathbf{v}}_{\mathbf{g}}^{\alpha\beta}(k+1) + \cdots \\ -L_{g}\frac{\mathbf{i}_{\mathbf{g}}^{\alpha\beta}(k+2) - \hat{\mathbf{i}}_{\mathbf{g}}^{\alpha\beta}(k+1)}{T_{s}} - R_{g}\hat{\mathbf{i}}_{\mathbf{g}}^{\alpha\beta}(k+1),$$
(11)

where the current reference is now given by  $i_{g\alpha\beta}(k+2)$ .

On the other hand, a couple of new variables are necessary to calculate  $\mathbf{v}_{\mathbf{x}}^{\alpha\beta}(k+1)$ . First, an estimation of the current  $\mathbf{i}_{\mathbf{g}\alpha\beta}(k+1)$  can be calculated from (8) as:

$$\hat{\mathbf{j}}_{\mathbf{g}}^{\alpha\beta}(k+1) = (1 - T_s R_g / L_g) \mathbf{i}_{\mathbf{g}}^{\alpha\beta}(k) + \cdots (T_s / L_g) (\mathbf{v}_{\mathbf{g}}^{\alpha\beta}(k) - \mathbf{s}_{\mathbf{g}}^{\alpha\beta}(k) v^{dc}(k)).$$
(12)

Second, an estimation of the grid voltage  $\mathbf{v}_{g^{\alpha\beta}}(k+1)$  can be calculated as  $\hat{\vec{v}}_g(k+1) = e^{j2\pi f_g T_s} \vec{v}_g(k)$ , leading to:

$$\hat{\mathbf{v}}_{\mathbf{g}}^{\alpha\beta}(k+1) = \begin{bmatrix} v_{g}^{\alpha}(k)\cos(\omega T_{s}) - v_{g}^{\beta}(k)\sin(\omega T_{s}) \\ v_{g}^{\alpha}(k)\sin(\omega T_{s}) + v_{g}^{\beta}(k)\cos(\omega T_{s}) \end{bmatrix}.$$
(13)

Voltage  $v_x(k + 1)$  is a function of the current reference  $i_g(k+2)$ , which in turn are imposed by (*i*) the active power that charges/discharges the *dc* capacitor, and (*ii*) the reactive power, which fixes the power factor at the PCC.

#### B. Current References

The power supplied by the grid can be separated in active and reactive components, expressed as:

$$p_{g}(k) = \operatorname{Re}\left\{\vec{v}_{g}(k)\vec{i}^{*}(k)_{g}\right\}$$
$$= v_{g}^{\alpha}(k) \cdot i_{g}^{\alpha}(k) + v_{g}^{\beta}(k) \cdot i_{g}^{\beta}(k), \qquad (14)$$

$$q_{g}(k) = \operatorname{Im}\left\{v_{g}(k)\tilde{i}_{g}^{*}(k)\right\}$$
$$= v_{g}^{\beta}(k) \cdot i_{g}^{\alpha}(k) - v_{g}^{\alpha}(k) \cdot i_{g}^{\beta}(k), \qquad (15)$$

where  $\vec{v}_g$  represents the voltage phasor and  $\vec{i}_g^*$  represents the current conjugate phasor as:

$$\vec{v}_{g}(k) = v_{g}^{\alpha}(k) + jv_{g}^{\beta}(k), \qquad \vec{i}_{g}^{*}(k) = i_{g}^{\alpha}(k) - ji_{g}^{\beta}(k)$$
(16)

From (14) and (15), the currents are calculated as a function of the grid voltage and the desired active and reactive power as:

$$i_{g}^{\beta, ref}(k) = \frac{v_{g}^{\beta}(k)p^{ref}(k) - v_{g}^{\alpha}(k)q^{ref}(k)}{\left|\vec{v}_{g}(k)\right|^{2}}, \qquad (17)$$

$$i_{g}^{\alpha, ref}\left(k\right) = \frac{q^{ref}\left(k\right) + v_{g}^{\alpha}\left(k\right)i_{g}^{\beta, ref}\left(k\right)}{v_{e}^{\beta}\left(k\right)}.$$
 (18)

Equations (17) and (18) give the current as a function of the desired active and reactive power. However, (11) needs the current references at time k + 2; therefore, (17) and (18) must be two step forwarded to use them for the current references. On the other hand, when (17) and (18) are forwarded, it is required the voltage  $v_{ga\beta}(k + 2)$  which can be found as:

$$\hat{\vec{v}}_{g}(k+2) = e^{j2\cdot 2\pi f_{g}T_{s}} \vec{v}_{g}(k), \qquad (19)$$

and the power references should also be found at step k + 2, leading to:

$$i_{g}^{\beta, ref}(k+2) = \frac{v_{g}^{\beta}(k+2)p^{ref}(k+2) - v_{g}^{\alpha}(k+2)q^{ref}(k+2)}{\left|\vec{v}_{g}(k+2)\right|^{2}},$$

$$(20)$$

$$i_{g}^{\alpha, ref}(k+2) = \frac{q^{ref}(k+2) + v_{g}^{\alpha}(k+2)i_{g}^{\beta, ref}(k+2)}{v_{g}^{\beta}(k+2)}.$$

$$(21)$$

# C. Power References

The power references can be separated in (*i*) the active power reference, defined by the active power consumed by the AFE, and (*ii*) the injection of the reactive power, defined by the power factor. The active power consumed by the AFE is separated between (*a*) the *dc* power, to charge/discharge the *dc* capacitor and the power consumed by the load  $v^{dc}i_L^{dc}$ , and (*b*) the amount of power dissipated by the *RL* input filter. Thus, (*a*) the *dc* active power can be written as:

$$p^{dc}(t) = \frac{1}{2} C_{dc} \frac{d(v^{dc}(t))}{dt} + v^{dc}(t) \cdot i_L^{dc}(t).$$
(22)

or in the discrete form:

$$\frac{\left[ v^{dc}(k) + \frac{T_{s}}{C_{dc}} \left( \left( \mathbf{s}_{\mathbf{g}}^{a\beta}(k) \right)^{T} \mathbf{i}_{\mathbf{g}}^{a\beta}(k) - i_{L}^{dc}(k) \right) \right]}{\hat{v}^{dc}(k+1)} \right] \\ \frac{\left[ 2 \hat{\mathbf{i}}_{\mathbf{g}}^{a\beta}(k+1) - \mathbf{i}_{\mathbf{g}}^{a\beta}(k) \right]}{\left[ 2 \hat{v}^{dc}(k+2) - \mathbf{i}_{\mathbf{g}}^{dc}(k+2) - v^{dc}(k) \right]} \right] \\ \frac{\left[ 2 \hat{\mathbf{j}}_{\mathbf{g}}^{a\beta}(k+1) - \mathbf{i}_{\mathbf{g}}^{a\beta}(k) \right]}{\left[ 2 \hat{v}^{dc}(k+2) - \hat{v}^{dc}(k+2) + \hat{v}^{dc}(k+2) - i_{L}^{dc}(k) + \left| \hat{\mathbf{i}}_{\mathbf{g}}^{a\beta}(k+2) \right|^{2} R_{g}} \right] \\ \frac{\left[ \frac{1}{2} C_{dc} \frac{v^{dcref2}(k+3) - \hat{v}^{dc}(k+2)}{T_{s}} + \hat{v}^{dc}(k+2) + \hat{v}^{dc}(k+2) + \hat{\mathbf{i}}_{\mathbf{g}}^{a\beta}(k+2) \right]^{2} R_{g}}{\left[ \frac{1}{2} \sqrt{1/(pf^{2})^{ref} - 1} \cdot p_{s}^{ref}(k+2)} \right] \\ \frac{\left[ \frac{1}{2} \sqrt{1/(pf^{2})^{ref} - 1} \cdot p_{s}^{ref}(k+2)}{q_{g}^{ref}(k+2)} + \frac{p_{g}^{ref}(k+2)}{p_{g}^{ref}(k+2)} \right] \\ \frac{\left[ \frac{1}{2} \sqrt{1/(pf^{2})^{ref} - 1} \cdot p_{s}^{ref}(k+2) + p_{s}^{ref}(k+2) + q_{s}^{ref}(k+2) \right]}{q_{g}^{ref}(k+2)} \\ \frac{\left[ \frac{1}{2} \sqrt{1/(pf^{2})^{ref} - 1} \cdot p_{s}^{ref}(k+2) + q_{s}^{ref}(k+2) + q_{s}^{ref}(k+2) \right]}{q_{g}^{ref}(k+2)} \\ \frac{\left[ \frac{1}{2} \sqrt{1/(pf^{2})^{ref} - 1} \cdot p_{s}^{ref}(k+2) + q_{s}^{ref}(k+2) + q_{s}^{ref}(k+2) \right]}{q_{g}^{ref}(k+2)} \\ \frac{\left[ \frac{1}{2} \sqrt{1/(pf^{2})^{ref} - 1} \cdot p_{s}^{ref}(k+2) + q_{s}^{ref}(k+2) + q_{s}^{ref}(k+2) \right]}{q_{g}^{ref}(k+2)} \\ \frac{\left[ \frac{1}{2} \sqrt{1/(pf^{2})^{ref} - 1} \cdot p_{s}^{ref}(k+2) + q_{s}^{ref}(k+2) + q_{s}^{ref}(k+2) \right]}{q_{g}^{ref}(k+2)} \\ \frac{\left[ \frac{1}{2} \sqrt{1/(pf^{2})^{ref} - 1} \cdot p_{s}^{ref}(k+2) + q_{s}^{ref}(k+2) + q_{s}^{ref}(k+2) \right]}{q_{g}^{ref}(k+2)} \\ \frac{\left[ \frac{1}{2} \sqrt{1/(pf^{2})^{ref} - 1} + q_{s}^{ref}(k+2) + q_{s}^{ref}(k+2) + q_{s}^{ref}(k+2) \right]}{q_{g}^{ref}(k+2)} \\ \frac{\left[ \frac{1}{2} \sqrt{1/(pf^{2})^{ref} - 1} + q_{s}^{ref}(k+2) + q_{s}^{ref}(k+2) + q_{s}^{ref}(k+2) \right]}{q_{g}^{ref}(k+2)} \\ \frac{\left[ \frac{1}{2} \sqrt{1/(pf^{2})^{ref} - 1} + q_{s}^{ref}(k+2) + q_{s}^{ref}(k+2) + q_{s}^{ref}(k+2) \right]}{q_{g}^{ref}(k+2)} \\ \frac{\left[ \frac{1}{2} \sqrt{1/(pf^{2})^{ref} - 1} + q_{s}^{ref}(k+2) + q_{s}^{ref}(k+2) + q_{s}^{ref}(k+2) \right]}{q_{g}^{ref}(k+2)} \\ \frac{\left[ \frac{1}{2} \sqrt{1/(pf^{2})^{ref} - 1} + q_{s}^{ref}(k+2) + q_{s}^{ref}(k+2) + q_{s}^{ref}(k+2) \right]}{q_{s}^{ref}(k+2)$$

$$p^{dc}(k) = \frac{1}{2} C_{dc} \frac{v^{dc^2}(k+1) - v^{dc}}{T_s} + v^{dc}(k) \cdot i_L^{dc}(k), \quad (23)$$

and (b) the power used by the first order RL input filter is expressed as:

$$p_{RL}(k) = \operatorname{Re}\left\{\left(\vec{v}_{g}(k) - \vec{v}_{x}(k)\right)\vec{i}_{g}^{*}(k)\right\},$$
 (24)

where the voltage  $\vec{v}_{g}(k) - \vec{v}_{x}(k)$  can be written as:

$$\vec{v}_g(k) - \vec{v}_x(k) = \vec{z}_g \vec{i}_g(k), \qquad (25)$$

with  $\vec{z}_g = R_g + jL_g$ . Therefore, the power  $p_{RL}$  is now defined as:

$$p_{RL}(k) = \operatorname{Re}\left\{\vec{z}_{g}\vec{i}_{g}(k)\vec{i}_{g}^{*}(k)\right\} = \operatorname{Re}\left\{\vec{z}_{g}\left|\vec{i}_{g}(k)\right|\right\}$$
$$= \left|\vec{i}_{g}(k)\right|^{2}\operatorname{Re}\left\{\vec{z}_{g}\right\} = \left|\vec{i}_{g}(k)\right|^{2}R_{g}$$
(26)

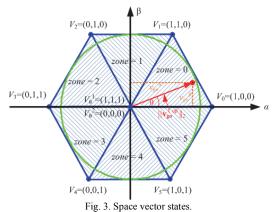
Consequently, the active power required by the AFE is:

$$p^{ref}(k+2) = p^{dc}(k+2) + p_{RL}(k+2), \qquad (27)$$

this equation is two step forwarded to achieve the desired reference required by (20) and (21). As (27), and therefore (23) is two step forwarded, the voltage  $v^{dc}(k+3)$  is defined as the *dc* voltage reference and the voltage  $\hat{v}^{dc}(k+2)$  needs to be estimated. A prediction of  $v^{dc}$  can be found using (9) as:

$$\hat{v}^{dc}(k+1) = v^{dc}(k) + \frac{T_s}{C_{dc}} \left( \left( \mathbf{s}_{\mathbf{g}}^{\alpha\beta}(k) \right)^T \mathbf{i}_{\mathbf{g}}^{\alpha\beta}(k) - i_L^{dc}(k) \right)$$
(28)

From (28) it is easy to note that if this equation is again one step forwarded –to obtain  $v^{dc}(k + 2)$ - it will be necessary to



include: (i)  $i_L(k+1)$  which normally is defined as a disturbance, being this prediction a difficult task, then it is considered the following approximation  $\hat{i}_L(k+2) \approx \hat{i}_L(k+1) = i_L(k)$ , (ii) the switching state at step k + 1, which is not feasible because this variable is the controller output, (11). Consequently, to overcome this problem,  $\hat{v}^{dc}(k+2)$  is estimated as:

$$\hat{v}^{dc}(k+2) = \hat{v}^{dc}(k+1) + \Delta v^{dc}(k+1).$$
(29)

where  $\Delta v^{dc} (k+1) = \hat{v}^{dc} (k+1) - v^{dc} ($ 

On the other hand, the reactive power reference is set as a function of the power factor *pf* and the desired active power, then, the equation is defined as:

$$q_{g}^{ref}(k+2) = \pm \sqrt{1/(pf^{2})^{ref} - 1} \cdot p_{g}^{ref}(k+2).$$
(30)

#### D. Effects of the Fast Imposed Dynamic

Deadbeat Control has important advantages as the fast response, and the minimum overshoot. Furthermore, the desired voltage can be achieved in three steps and the power factor in two steps from (20), (21) and (27). However, three steps for the dc link voltage controller is too fast to be accomplished, because the amount of energy to charge/discharge the dc capacitor may be significant. Therefore, it is important to limit this amount of power to protect the rectifier of high currents, which may damage the components. On the other hand, the power converter has a natural saturation point given by the maximum  $v_x$  voltage which is related to the dc link voltage.

Thus, two equations are adapted in order to ensure a slower dynamic response. First, the equation that gives the dc active power is rewritten as:

$$p^{dc}(k) = \frac{1}{2} C_{dc} \frac{v^{dc2}(k+1) - v^{dc2}(k)}{T_s} k_1 + v^{dc}(k) \cdot i_L^{dc}(k)$$
(31)

where  $k_1$  is placed to reduce the amount of power required by the first term in (31). This constant also allows to smooth the dynamic response, because it reduces the noise influence on the power reference. This harmful effect is amplified because the voltage is squared and divided by  $T_s$ . Then, it is important to include  $k_1$  for noisy variables. The second equation given by (27) needs to be limited in order to reduce the maximum reference current in (20) and (21). Therefore, the final algorithm states that if  $p^{ref} > p_{max}$ , then  $p^{ref} = p_{max}$ ; and if  $p^{ref} < -p_{max}$ , then  $p^{ref} = -p_{max}$ . The whole control algorithm is presented in Fig. 2.

# IV. VOLTAGE SYNTHETIZATION

Once the voltage  $\mathbf{v}_{\mathbf{x}}$  is defined by the deadbeat control, it must be synthetized by a modulation technique, [12]. Space Vector is chosen to achieve the requested voltage  $\mathbf{v}_{\mathbf{x}}$  provided by the deadbeat control. The range of voltages that the modulating strategy is capable to generate can be seen in Fig. 3, limited by the *dc* link voltage and the eight valid states. Thus, any voltage  $\mathbf{v}_{\mathbf{x}}$  inside the hatched region can be achieved with the three nearest voltages (one of them the zero state). Thus the voltage  $\mathbf{v}_{\mathbf{x}}$  is synthetized as,

$$T_{s}\mathbf{v}_{\mathbf{x}}^{\alpha\beta} = \mathbf{V}_{i}^{\alpha\beta}\boldsymbol{v}^{dc}T_{1} + \mathbf{V}_{i+1}^{\alpha\beta}\boldsymbol{v}^{dc}T_{2} + \mathbf{V}_{\theta}^{\alpha\beta}\left(T_{s} - T_{1} - T_{2}\right), \quad (32)$$

where  $V_{\theta}$  represents the zero state and *i* represents the zone where the vector  $v_x$  is, Fig. 3. Therefore, each state is applied during the following times:

$$T_{1} = \frac{\left(\nu^{dc} \mathbf{V}_{i+1}^{\alpha\beta}\right)^{\times} \mathbf{v}_{\mathbf{x}}^{\alpha\beta}}{\left(\nu^{dc} \mathbf{V}_{i+1}^{\alpha\beta}\right) \times \left(\nu^{dc} \mathbf{V}_{i}^{\alpha\beta}\right)} T_{s} , \qquad (33)$$

$$T_{2} = \frac{v_{x}^{\alpha}}{v^{dc}V_{i+1}^{\alpha}}T_{s} - \frac{v^{dc}V_{i}^{\alpha}}{v^{dc}V_{i+1}^{i}}T_{1}, \qquad (34)$$

where  $\mathbf{V}_i^{\alpha\beta}$  is defined as:

$$\mathbf{V}_{i}^{\alpha\beta} = \sqrt{\frac{2}{3}} \left[ \sin\left(i \cdot \pi/3\right) \quad \cos\left(i \cdot \pi/3\right) \right]^{T}, \qquad (35)$$

Now, in order to decide the zone where the voltage  $v_x$  is placed, Fig. 3, the angle  $\theta = \arg \{v_{x\alpha\beta}(k+1)\}$  is calculated as:

TABLE I

$$\theta = \operatorname{sign}\left(v_{x}^{\beta}\left(k+1\right)\right) \cdot \operatorname{arccos}\left(\frac{v_{x}^{\alpha}\left(k+1\right)}{\left\|\mathbf{v}_{x}^{\alpha\beta}\left(k+1\right)\right\|_{2}}\right), \quad (36)$$

PARAMETERS	
Parameters	Value
Vg	230 V, rms
Vdc	600 V
$R_g$	0.4 Ω
$L_g$	4.75 mH
$C_{dc}$	2.2 mF
$R_{dc}$	250 Ω
$f_{g}$	50 Hz
$f_s$	10kHz
$k_1$	0.06

V. RESULTS

To corroborate the mathematical analysis and the aforementioned algorithm, the topology shown in Fig. 1 is controlled by the presented deadbeat technique and tested under different conditions with the parameters listed in TABLE I.

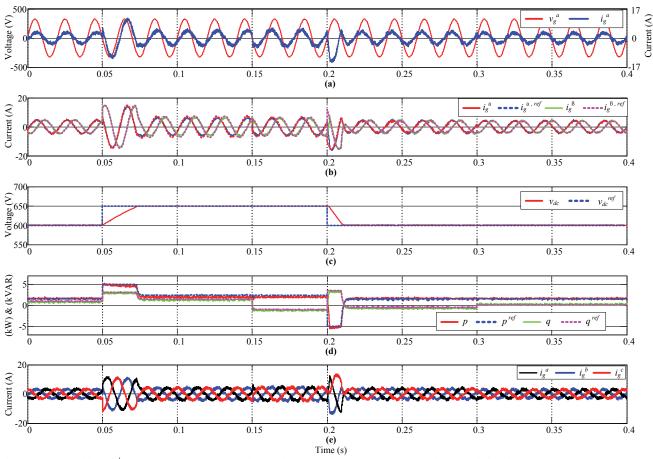


Fig. 4. Power control loops  $v^{dc}$  step and reactive power control (a) grid voltage and current, (b) reference and measured  $\alpha\beta$  grid current, (c) reference and measured dc voltage, (d) reference and measured active and reactive power, and (e) grid currents  $i_g^{abc}$ .

The designed controller is tested under dc voltage reference step change, Fig. 4. The dc voltage changes from 600V to 650 V in t = 0.05 s and then it goes back to 600V in t = 0.2 s. The results illustrated in Fig. 4 show that the reference is achieved in only 20 ms approximately for the step up, *i.e.* one grid cycle, for a 50 V step change. In addition, it is worth to highlight that no overshoot is presented, which is an advantage of the deadbeat control. On the other hand, the time to reach the reference when it goes down is less than when it goes up, which is mainly due to the losses presented in the inverter, making easier to reduce instead to increase the power stored in the dccapacitor.

Aiming to see the load impact behavior, Fig. 5 shows the system response when the *dc* current is incremented in a 100% from 2.4 A. This was obtained inserting a 250  $\Omega$  resistor in parallel to  $R_{dc} = 250 \Omega$ . The result shown in Fig. 5 describes that the *dc* voltage as well as the power factor is maintained in their reference value even with this significant step change, and the deadbeat control imposes higher currents in order to track its references given by the requested load power.

#### VI. CONCLUSIONS

Deadbeat control is a suitable alternative to control power converters. When this method is applied on this multivariable systems, the time response is significantly reduced, and without overshoot. On the other hand, and despite the fast response, the maximum amount of power is limited by the same algorithm protecting the equipment of potential damage due to extreme operating conditions. In addition, as the control algorithm is based on the model, it is intuitive once the variables and references are defined.

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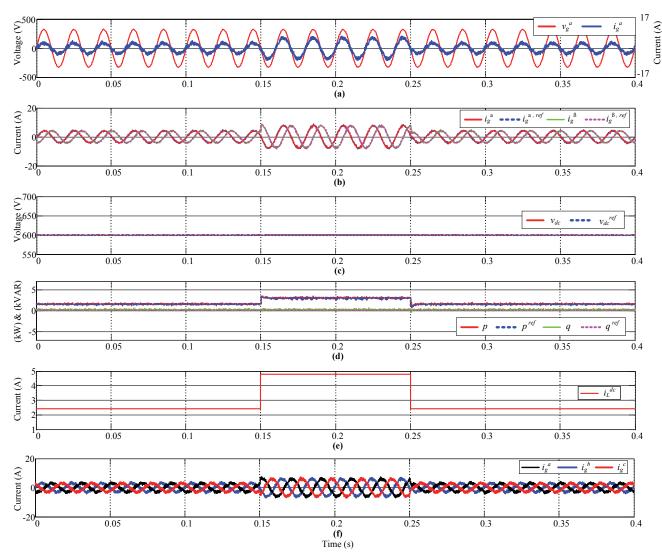


Fig. 5. Step load impact (a) grid voltage and current, (b) reference and measured  $\alpha\beta$  grid current, (c) reference and ameasured *dc* voltage, (d) reference and measured active and reactive power, (e) *dc* load current  $i_{a}^{abc}$ , and (f) grid currents  $\mathbf{i}_{g}^{abc}$ .

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