

Optical Spin-Transfer-Torque-Driven Domain-Wall Motion in a Ferromagnetic Semiconductor

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We demonstrate optical manipulation of the position of a domain wall in a dilute magnetic semiconductor, GaMnAsP. Two main contributions are identified. First, photocarrier spin exerts a spin-transfer torque on the magnetization via the exchange interaction. The direction of the domain-wall motion can be controlled using the helicity of the laser. Second, the domain wall is attracted to the hot spot generated by the focused laser. Unlike magnetic-field-driven domain-wall depinning, these mechanisms directly drive domain-wall motion, providing an optical tweezerlike ability to position and locally probe domain walls.

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Recent work advocating for the use of mobile magnetic domains for memory [1] and logic [2] applications has sparked renewed interest in the physics of domain-wall motion. A key element in these research efforts is the controlled propagation of domain walls driven by electric currents [3–7]. This occurs via spin-transfer torque, where, because of an exchange interaction with the magnetization, a noncollinear injected carrier spin can exert a torque on the magnetization. Recently, it has been demonstrated that a spin-transfer torque can also be applied optically [8]. In that experiment, the optical spin-transfer torque was used to induce precession [9,10] of the magnetization in a thin film of GaMn_{<0.09}As with an in-plane easy axis.

Here we consider a similar material, Ga_{0.94}Mn_{0.06}As_{0.91}P_{0.09}, with an out-of-plane easy axis. In this case, the optical spin-transfer torque induced by a circularly polarized laser at normal incidence is not expected to act within the magnetic domain. However, at a domain boundary, the magnetization has an in-plane component, allowing a local torque that results in an optical polarization dependent domain-wall (DW) motion. We demonstrate this helicity dependent optically induced DW motion by exposing a single DW to a train of above band gap picosecond laser pulses, and we identify the optical spin-transfer torque as the dominant helicity dependent mechanism driving the DW motion. In addition, we observe a second helicity independent effect that attracts the DW to the center of the focused Gaussian laser spot due to local heating of the magnetic material. During laser exposure the DW moves towards a final position where the effects of the optical spin-transfer torque and the thermal gradient are balanced. This interpretation is confirmed by

numerical simulations based on the Landau-Lifshitz-Bloch equations.

The wafer consists of a 25-nm-thick film of Ga_{0.94}Mn_{0.06}As_{0.91}P_{0.09} on a GaAs substrate. The annealed sample has a Curie temperature of 106 K. The addition of P results in an out-of-plane easy axis via a tensile growth strain [11]. To study domains constrained to one spatial dimension, the wafer is fabricated into 4 × 60 μm bars. Further details of the sample can be found in Ref. [12].

The sample is mounted in a cold-finger cryostat at 92 K. An out-of-plane magnetic field can be applied using an electromagnet. The magnetic domains are imaged using a Kerr microscope. A mode-locked Ti:sapphire laser provides a source of 140 fs optical pulses at an 80 MHz repetition rate. A bar aligned along the [110] direction, with a Neel wall [12], is excited with an exposure time of > 4 ms using a mechanical shutter. After a 10 m single-mode fiber, dispersion stretches the pulses to approximately 4 ps. The laser is focused to a spot with a Gaussian intensity profile with a full width at half maximum of $w = 5 \mu\text{m}$.

To prepare a magnetic domain we use thermally assisted magnetization reversal by laser excitation. First the magnetization is saturated using a negative magnetic field, $B_s = -15 \text{ G}$, large compared to the coercive field, $B_c = 4 \text{ G}$. The field is then ramped to a slightly positive value, $B_n = +0.9 \text{ G}$. The bar is illuminated for $\tau_n = 200\text{--}400 \text{ ms}$ at a high power of 94 mW, at a wavelength of 800 nm to generate a single reversed magnetic domain, as shown in Figs. 1(a)(i)–1(c)(i). The experiments are performed at 92 K, where it is relatively easy to reproducibly nucleate a single magnetic domain of a similar size.

Optically assisted magnetization reversal has previously been reported in highly resistive GaMnAs using relatively

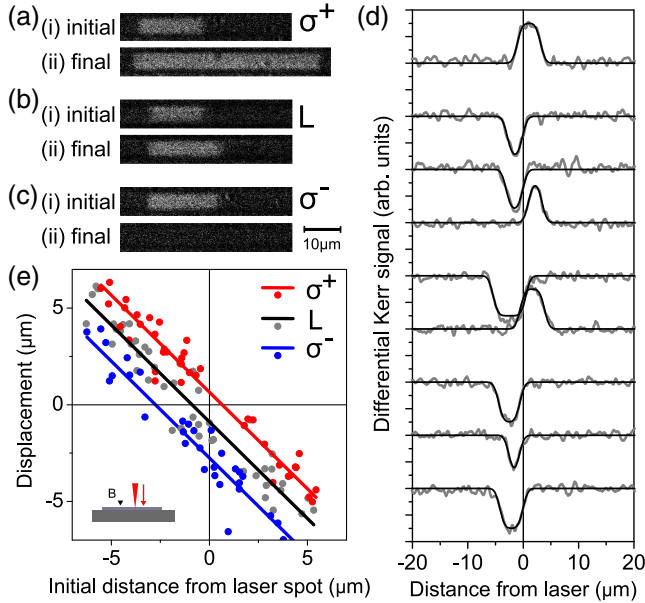


FIG. 1 (color online). (a), (b), (c) Images of the initial domain nucleated by the nucleation pulse (94 mW, $\tau_n = 300$ ms, 800 nm, $\nu_{\text{rep}} = 80$ MHz, $B_n = +0.9$ G), and the final domain after illumination by many trains of low power pulses, as described in the main text. Following nucleation, many measurements of the laser induced displacement of the right-hand DW are made. For each measurement, the laser is randomly repositioned within $4 \mu\text{m}$ of the DW and illuminated by a train of ps pulses (34 mW, $\tau_p = 10$ ms, 780 nm, $\nu_{\text{rep}} = 80$ MHz, $B_{\text{ext}} = 0$), below the threshold for domain nucleation. Following the application of many (> 50) pulse trains, the DW has moved to the right (left) for σ^\pm polarization and remains relatively unchanged for linear polarization. (d) Examples of the change in the magnetic domain following excitation with a linearly polarized pulse for different initial positions of the DW with respect to the laser. A cross section of the difference between the Kerr images taken before and after the laser exposure is plotted against the position relative to the center of the laser spot. Positive (negative) signal indicates a shrinking (growing) domain. In most cases, the final position indicated by the positive gradient is close to the center of the laser spot, regardless of initial position. (e) Plot of the DW displacement, $\Delta x = x_f - x_i$ vs initial position x_i . The effect of the pulse train is to move the DW to a stationary position, x_0 , that is shifted to the right (left) for σ^\pm polarizations, respectively. (Inset) A positive B field is defined parallel to the optical axis.

low power HeNe laser excitation [13,14] or a single 80 pJ, 100 fs laser pulse [15]. There, the polarization independent magnetization reversal was attributed to a reduction in the coercive field due to the photocarrier related suppression of the DW pinning potential in material of low ($< 1\%$) Mn concentration. We attribute the laser induced domain nucleation at small applied reversal fields to thermally assisted magnetization reversal and note a helicity dependent threshold. The helicity dependence of magnetization reversal has not yet been reported in a magnetic semiconductor, but it has been studied intensively in ferrimetallic materials such as GdFeCo [16–18]. We now focus on laser induced

motion of domain walls at laser powers and exposure times well below the threshold for domain nucleation.

After domain preparation, the sample temperature equalizes to the base temperature of 92 K at zero magnetic field. To locate the right-hand DW, the laser spot is then positioned outside of the reversed domain and the sample is exposed to a train of 4 ps laser pulses, (34 mW, 780 nm, 80 MHz repetition frequency) for 10 ms. To probe a change in DW position, Kerr images before and after the laser illumination are compared. If no change is identified, the laser spot is shifted towards the reversed domain by a step of $0.5 \mu\text{m}$. This procedure is repeated until a first change in DW position is observed.

After identifying the DW location, the laser spot is moved to a randomized position within $4 \mu\text{m}$ of the DW and the sample is again illuminated by a train of ps pulses. This procedure is repeated until about 30 displacements have been detected or until the entire domain has been erased by the laser induced DW motion.

The final differential Kerr images shown in Figs. 1(a)(ii)–1(c)(ii) are obtained from single Kerr images taken at the final domain configuration and after the domain was erased by a saturation field. In Fig. 1(a), where σ^+ -polarized laser pulses are used, the final domain is larger than the initial domain, indicating that the DW moved to the right. By contrast, in Fig. 1(c), for σ^- excitation, the domain has been completely erased, indicating that the DW moves to the left. In Fig. 1(b), the DW position remains relatively unchanged in the case of linear polarization.

Figure 1(d) presents examples of the light induced DW motion with respect to the laser position for linear polarization. Cross sections of differential Kerr images along the bar identify DW displacements by the nonzero differential Kerr signals. A positive (negative) signal indicates that the right-hand DW moves to the left (right), resulting in a shrinking (growing) domain. The edge of the positive gradient, indicating the final DW position, is independent of the start position. If the laser spot does not overlap with the DW, no DW motion is observed. In Fig. 1(e) the displacement of the DW is plotted against the initial position of the DW with respect to the laser spot. The result is a straight line of gradient -1 , indicating that a domain at arbitrary initial position x_i moves to a position where the DW is stationary. For linear polarization, the DW is attracted to the hot spot at the center of the laser. A similar observation has recently been reported for DW in CoPt [19]. For σ^\pm circular polarization, the final position of the DW is shifted to the right (left) with respect to the final position measured for linear polarization. This demonstrates that the direction of the laser induced DW motion depends on the helicity of the laser.

In the next experiment, a magnetic domain is prepared and the DW is located as before. The laser position is then fixed, and the final position of the DW following excitation

by a train of low power pulses is measured as a function of external magnetic field B_{ext} . The data are presented in Fig. 2. For a σ^\pm -polarized laser the stationary position x_0 is shifted by $\pm 2 \mu\text{m}$ with respect to the case of linear polarization. The gradient is relatively independent of polarization. For small external magnetic fields, the final position of the DW can be described by $x_f = x_0 + aB_{\text{ext}}$, where x_0 is the stationary position at $B_{\text{ext}} = 0$. We note that for larger external B fields (> 1.5 G), the nonilluminated DW can also move as a result of the optical excitation of the illuminated DW.

Above band gap excitation with σ^\pm polarization creates photocarriers with a spin density $\mathbf{s} \propto \hat{n} = \pm \hat{z}$. Spin-transfer torque mediated by optically generated spin-polarized electrons therefore acts predominantly on the DW where the magnetization rotates into the sample plane. Because of the exchange interaction, the carrier spin experiences many sub-ps period precessions about the quasistationary magnetization vector (period ~ 10 ns) during the 10 ps of ps spin lifetime of the carriers. This results in a time-averaged carrier-spin density along $\mathbf{s}_0 \propto \hat{n} \times \hat{m}_{\text{DW}} = \pm \hat{y}(\mp \hat{x})$ [8], considering a Neel (Bloch)-type DW with magnetization at the center of the DW along the $\hat{x}(\hat{y})$ direction, respectively [12]. This kicks the magnetization vector at the boundary in a direction $\hat{m}_{\text{DW}} \propto \hat{m}_{\text{DW}} \times \hat{s}_0 = \pm \hat{z}$ moving the DW to the right (left), as observed. Hence, optical spin-transfer torque can explain the helicity dependence of the direction of DW motion.

We now argue against the two other candidate mechanisms that could give rise to a helicity dependent shift of the DW position. First, the circular dichroism of the material can lead to a difference in photocarrier density and temperature across the DW. This would cause the DW to move towards the hot region, as observed for linearly polarized light. In the case of a negative saturation magnetic field, the

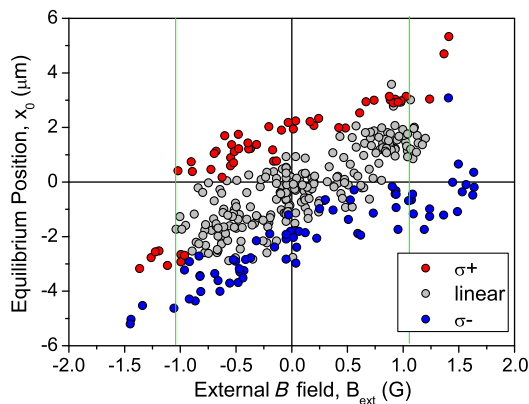


FIG. 2 (color online). Final DW position x_0 versus external magnetic field B_{ext} . For small magnetic fields, the equilibrium position varies linearly with the magnetic field. The helicity of the laser illumination acts similarly to an applied magnetic field that shifts the final position by $x_0 = \pm 2 \mu\text{m}$ for σ^\pm polarization, respectively.

magnetization \downarrow/\uparrow either side of the right-hand DW is $\downarrow\uparrow\uparrow\downarrow$, where \uparrow/\downarrow indicates the direction of the total angular momentum of the lowest energy heavy-hole state, responsible for the magnetic circular dichroism [20]. In the case of σ^\pm -polarized excitation, a photohole of angular momentum $\downarrow(\uparrow)$ is added, and the resulting thermal gradient is hot (cold) [cold (hot)] causing the DW to move left (right). This is the opposite of what is observed. Furthermore, the majority of the light, $> 95\%$, is absorbed below the 25 nm film of GaMnAs. Therefore, the heating of the sample should be relatively independent of the dichroism. Hence, the circular dichroism is not the dominant mechanism. Second, the laser can generate an effective magnetic field along the optical axis due to the inverse Faraday effect. However, recent studies have shown that compared to the optical spin-transfer torque, the inverse Faraday effect is weak in dilute magnetic semiconductors [8]. These conclusions were made on the basis of spectroscopic measurements showing that the peak in the Kerr rotation was not coincident with that in the measured torque.

To further test our understanding, we investigate the power and wavelength dependence of the final domain wall position, x_0 . The results are presented in Fig. 3. Figure 3(a) plots the power dependence of x_0 . Assuming the DW moves until reaching a position where the power density

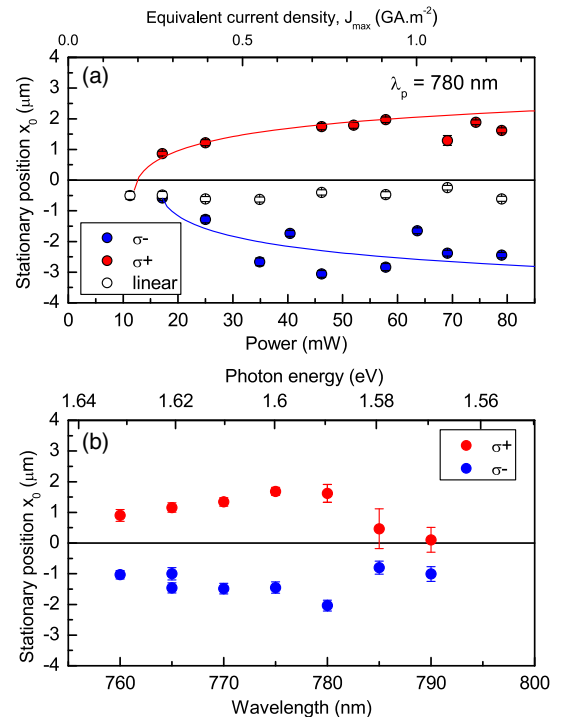


FIG. 3 (color online). Investigation of the stationary position relative to the laser position, x_0 . (a) x_0 vs power. The sign of x_0 changes with the helicity. There is a power threshold, followed by saturation. (b) x_0 vs wavelength ($P = 25$ mW, $\tau_p = 5$ ms). x_0 exhibits a broad peak centered at ~ 775 nm.

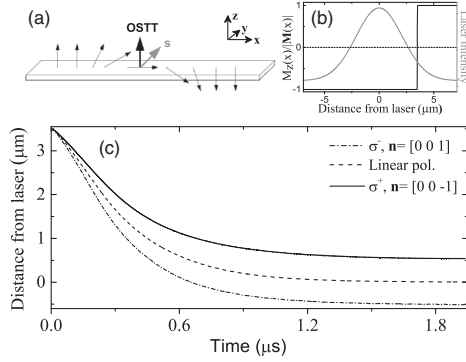


FIG. 4. (a) Schematic of magnetization at a Néel wall and direction of the optical spin-transfer torque. (b) Initial position of the DW and the laser spot intensity profile. (c) Subsequent DW motion following the application of 80 MHz train of laser pulses. For linear polarization, the DW moves to the center of the laser spot. For circular polarization (σ^\pm) the additional spin-transfer torque slows down (speeds up) the DW motion, shifting the final position by $\pm 0.5 \mu\text{m}$. The average speed over the first $0.25 \mu\text{s}$ is about $v_{\text{lin}} \approx 5 \text{ ms}^{-1}$ or 60 nm/pulse ; $v_- \approx 6 \text{ ms}^{-1}$ and $v_+ \approx 4 \text{ ms}^{-1}$.

$Pe^{-x^2/w_{\text{eff}}^2}$ is below the threshold P_{th} for DW motion, a manual fit to $x_0 \approx x_0^{(\text{lin})} \pm w_{\text{eff}} \sqrt{\ln(P/P_{\text{th}})}$ is made. The threshold power is $P_{\text{th}} = 12$ (17) mW for σ^\pm polarization, respectively [21]. This equates to an effective current density (photon flux $\times e$) of $J_{\text{max}}^{\text{th}} \approx 0.25 \text{ GA m}^{-2}$. We note that this is similar to the threshold current density measured for electrically driven DW motion in the same wafer [12]. The effective width of the Gaussian temperature profile is less than the laser spot size, $w_{\text{eff}} = 1.9 \mu\text{m} < w$. This is attributed to a power threshold that is lower at the hot spot. Because of the power threshold, we conclude that the DW is moving in a flow regime [12] driven by an optical spin-transfer torque.

Figure 3(b) presents the wavelength dependence of x_0 , which peaks at 785 nm. DW motion is only observed for above band gap excitation, verifying that the DW is driven by photogenerated carriers. The generation of spin may become less effective at higher photon energies due to increased spin relaxation. In this wavelength regime, the circular dichroism increases monotonically with wavelength [22], further ruling out circular dichroism as the dominant source of the helicity dependent term. The helicity dependent direction of DW motion is observed for the experimentally accessible temperatures of 85–98 K.

To estimate the expected shifts in the DW following laser excitation, simulations using a 1D micromagnetic Landau-Lifshitz-Bloch (LLB) model [23], including the demagnetizing field [24], were performed with parameters given in [25]. In the case of linear polarization, a temperature increase proportional to the time-averaged intensity is assumed with an amplitude $\Delta T = 13 \text{ K}$ [9] and a base temperature of 92 K. This modifies the magnitude of

the equilibrium magnetization $M_{\text{eq}}(T)$ [26] scaling the exchange stiffness and magnetic anisotropy coefficients of the internal fields, resulting in a free-energy well for the DW. As shown in Fig. 4(b), for the $[1\bar{1}0]$ bar, the Néel wall is initially at a position of $+3.5 \mu\text{m}$ from the center of the laser spot. When the temperature profile is switched on, the DW moves to the center of the hot spot on a microsecond time scale, as shown in Fig. 4(c).

For circular polarization, the optical spin-transfer torque is described by an additional effective field in the LLB equation, $\mathbf{H}_{\text{eff}}^{\text{OSTT}} = [J_{\text{eff}}/\mu_0 M_{\text{eq}}(T)]\mathbf{s}$, due to the exchange field exerted by the carrier-spin density \mathbf{s} on the magnetization. An additional rate equation [8] is used to describe the time evolution of the spin: $\dot{\mathbf{s}} = (J_{\text{eff}}(T)/m_{\text{eq}}\hbar)\mathbf{m} \times \mathbf{s} + R(t)\hat{\mathbf{n}} - \mathbf{s}/\tau$, where $R(t)\hat{\mathbf{n}}$ describes the spin pumping rate due to laser excitation, and $\tau \approx 30 \text{ ps}$ is the carrier-spin lifetime [8]. The spin pump rate is treated as a $\nu_{\text{rep}} = 80 \text{ MHz}$ train of square pulses of duration $\tau_L = 4 \text{ ps}$, proportional to the intensity profile of the laser, and an effective pump rate $e\nu_{\text{rep}}\tau_L R_{\text{max}} = 0.8 \text{ GA m}^{-2} \mu\text{m}^{-1}$, which assumes an absorption length of $\sim 1 \mu\text{m}$ in GaAs [27]. The different polarization cases σ^\pm are controlled by the direction of the carrier spin $\hat{\mathbf{n}} = (0, 0, \mp 1)$, respectively. In the simulations shown in Fig. 4(a), the DW moves to a stationary position x_0 shifted by $\pm 0.6 \mu\text{m}$ with respect to the center of the laser spot, reproducing the observed helicity dependence of the sign of the shift. Calculations with no temperature gradient and uniform illumination have also been performed. There, the DW moves by $\pm 35 \text{ ms}^{-1}$ in the steady state. Hence the temperature gradient limits the displacement, and the calculation represents a lower limit on the displacement. The effect of the optical spin-transfer torque (OSTT) on the DW is illustrated in Fig. 4(a). Initially, the injected carrier spin is aligned along the z axis. The precession around the exchange field due to the magnetization is fast compared to the carrier lifetime 0.4 ps vs 30 ps, and the time-averaged carrier spin aligns along the $\hat{\mathbf{y}} \propto \hat{\mathbf{n}} \times \mathbf{m}$ axis. For the example of a Néel wall, the carrier spin applies a torque on the magnetization, kicking the magnetization in the $\pm \hat{\mathbf{z}}$ direction. Following the kick, the magnetization precesses around the internal fields moving the DW. For the case of the 80 MHz repetition rate considered here, the DW is still moving when the next laser pulse strikes, leading to a steady-state motion where the magnetization precesses around an equilibrium state that is intermediate between a Néel and a Bloch wall. We note that similar DW motion is observed and calculated for the Bloch wall of the $[110]$ bar.

To summarize, we observe shifts in a magnetic DW position following above band gap excitation with a train of picosecond laser pulses. Two main driving terms are identified and reproduced in micromagnetic simulations. The first helicity dependent term results from spin-polarized photocarriers exerting a spin-transfer torque on the DW. The second helicity independent term attracts the DW to the

laser hot spot due to a free-energy well resulting from a reduction in the local magnetic moment. Laser manipulation of the DW position provides a tool for local rather than global control of DW motion. It provides an experimental route to investigate DW motion following ultrafast, rather than nanosecond, kicks to the spin-transfer torque. By isolating laser induced magnetization reversal from DW propagation, these techniques should provide insights into magnetization reversal.

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