

Automatic Generation of Statistical Pose and Shape Models for Articulated Joints

Xin Chen, Jim Graham, *Member, IEEE*, Charles Hutchinson, and Lindsay Muir

Abstract—Statistical analysis of motion patterns of body joints is potentially useful for detecting and quantifying pathologies. However, building a statistical motion model across different subjects remains a challenging task, especially for a complex joint like the wrist. We present a novel framework for simultaneous registration and segmentation of multiple 3D (CT or MR) volumes of different subjects at various articulated positions. The framework starts with a pose model generated from 3D volumes captured at different articulated positions of a single subject (template). This initial pose model is used to register the template volume to image volumes from new subjects. During this process, the Grow-Cut algorithm [1] is used in an iterative refinement of the segmentation of the bone along with the pose parameters. As each new subject is registered and segmented, the pose model is updated, improving the accuracy of successive registrations. We applied the algorithm to CT images of the wrist from 25 subjects, each at five different wrist positions and demonstrated that it performed robustly and accurately. More importantly, the resulting segmentations allowed a statistical pose model of the carpal bones to be generated automatically without interaction. The evaluation results show that our proposed framework achieved accurate registration with an average mean target registration error of 0.34 ± 0.27 mm. The automatic segmentation results also show high consistency with the ground truth obtained semi-automatically. Furthermore, we demonstrated the capability of the resulting statistical pose and shape models by using them to generate a measurement tool for scaphoid-lunate dissociation diagnosis, which achieved 90% sensitivity and specificity.

Index Terms—Wrist, Carpal bones, 3D image registration, segmentation, statistical pose model, statistical shape model, articulated joint.

I. INTRODUCTION

A Number of recent studies have made use of statistical models for determining and quantifying abnormal articulated motion of anatomical joints (e.g. in the spine [2], [3], the femur [4] and inferring 3D motion from 2D video sequences in the wrist [5]). The principal underlying problem in building such statistical models is to establish correspondences representing important features across populations.

Davies et al [6] have shown how such correspondences can be achieved automatically, given a segmented training set.

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X. Chen and J. Graham are with the Centre for Imaging Sciences, Institute of Population Health, The University of Manchester, U.K. (e-mail: xin.chen@manchester.ac.uk)

C. Hutchinson is with the Division of Healthsciences, University of Warwick, U.K.

L. Muir is with the Department of Hand Surgery, Salford Royal NHS Foundation Trust, Salford, U.K.

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However, for a complex joint like the wrist, segmentation of the wrist bones from CT volumes is a challenging task. They suffer from variation in intensity due to the nature of the trabecular bone and indistinct boundaries due to partial volume effects and the narrow gap between adjacent surfaces ([7]–[10]). It is a common experience, which we share, that ‘automatic’ segmentation methods do not produce sufficiently accurate results and that ‘semi-automatic’ methods such as those based on Graph-cuts often require complex interactions for every training example. The problem is frequently solved by tedious manual segmentation. Furthermore, once segmentation is achieved further registration is required to align different articulated positions of different subjects [11]. This is complicated in articulated joints as the relative poses of different components vary throughout the motion of the joint. The wrist is a particularly challenging example as it comprises 8 carpal bones, the radius and the ulna (see figure 2) moving in a complex 3D pattern. Recently, Cootes et al. [12] introduced a framework to compute dense correspondences across groups of images based on groupwise image registration, which has been successfully applied to face and brain images. However, for the registration of bones, the features mainly lie on the surface of the bone and the pose variation involves significant articulation of rigid parts. This is not accommodated well in [12].

In this paper, we present a method for automatic segmentation and registration of bones in an articulated joint (specifically the wrist) in a range of articulated positions across a group of individuals for the purpose of building a statistical pose model (SPM). There is a small body of research addressing this question. van deGiessen et al. [11] introduced a constrained registration of the wrist joint based on segmented 3D surfaces using the iterative closest point (ICP) method, resulting in a 4D statistical model of wrist bone motion patterns [13]. The model represents local statistical properties between adjacent carpal bones by a set of pre-determined point correspondences, and is used for detecting abnormal bone spaces. Boisvert et al. [2] studied spine variation using 3D articulated pose models. The relative rigid transformation parameters of each vertebra with respect to the vertebra of the upper level were used to construct the articulated pose model. The spine variations between the same set of patients before and after treatment were compared using the model. Marai et al. [14] proposed a cost function based on distance fields for carpal bone registration, which is validated by aligning different poses for the same subject. In these studies, bone segmentations are performed either manually or semi-automatically prior to the registration. Here we describe a

method that exploits the fact that identical bones from the same individual occur in different poses in the same data set. The different examples of these bones adopt different poses relative to the other bones as the joint moves. Examples of similar bones in similar poses are observed for different individuals. We have previously presented a framework for combined segmentation and registration [15]. That work is extended here by removal of the requirement for initial manual alignment prior to registration and incorporating the SPM building process into the framework.

The main contributions of this paper, distinguishing it from the aforementioned studies, are: (1) it is an automatic framework where a statistical pose model (SPM) and a statistical shape model (SSM) can be generated via integrated segmentation and registration methods. (2) A consistent global scale factor is estimated by simultaneous registration performed on all articulated positions of the same subject, which leads to an accurate and compact SPM. (3) In contrast to [13], a statistical description of the *global* motion pattern of all carpal bones is calculated, from which the local pattern of motion between adjacent bones can also be described directly. Additionally, the SPM parameters can be used to align different wrist positions from different subjects, without the requirement (as in [13]) for a set of predefined positions. (4) The segmentation results are produced by a combination of data from all the wrist positions, which produces more reliable and consistent results than only using one wrist position for segmentation (e.g. [15]). (5) We avoid the requirement for interactive alignment (as in [15]) by basing the registration and segmentation on the pose model. This model, initially based on a single subject, grows incrementally as further subjects are registered and segmented. This results in fully automatic registration and segmentation. (6) The use of SPM and SSM as a measurement tool for pathology detection is demonstrated based on the Scaphoid-lunate dissociation condition.

The proposed framework, illustrated in outline in Fig. 1, is designed to align a template volume V_S to N target subjects, each with a number of different wrist positions. In our training datasets, CT data from 25 subjects, each at five different wrist positions were used (neutral position and four extreme positions in radial-ulnar and flexion-extension movement). The process consists of four steps. Step 1 is a pre-processing step that only needs to be done once. We randomly select one subject from the training data sets as the template, and segment a CT volume from one of the wrist positions (e.g. neutral position) using the grow-cut interactive segmentation method [1]. The segmented position is then registered to other positions within the template subject using the method described in [15] (see section IV(A,B)). The registration result is used to derive a pose model (described in section III). In steps 2 to 4, the template is propagated to all the positions of the k^{th} target subject simultaneously, providing estimates of the global rigid parameters, pose model parameters and local rigid parameters of each bone. In step 4, the Grow-Cut multi-label segmentation method is integrated with the registration process, which improves the robustness of the registration [15] and also generates a final segmentation. The successful registration result is then used together with the previously

available ($k-1$) registration results to produce an updated pose model for the next iteration. An outlier rejection strategy is used for pose model updating. The whole process is terminated when all subjects in the training data set are registered to the template. Detailed descriptions of each step are given in the following sections.

II. PROBLEM PARAMETERISATION

A coordinate system is defined (see figure 2) across all the subjects, in order to represent a consistent wrist motion. The origin of the coordinate system is defined with respect to the centroid of the radius bone. The X and Y coordinates are the corresponding coordinates of the centroid. As the length of the radius present in the image varies from subject to subject, the Z-coordinate (along the length of the radius) is defined, arbitrarily, to be 30 voxels above the lowest point in the radius of the template subject. The orientations of the X, Y and Z axis are defined by the original CT volume coordinate system. All bone motions are represented relative to the origin. Three sets of parameters need to be estimated during image registration in order to interpret the true 3D pose of each carpal bone: (1) Global wrist pose which is estimated by aligning the radius. It includes rigid transformation parameters and a global scale factor, denoted by $\theta = \{tx, ty, tz, r1, r2, r3, s\}$. $t = [tx, ty, tz]^T$ denotes the global translations, and $r = [r1, r2, r3]^T$ is the Rodrigues parameter [13], [16] representing the global orientations. s controls the distance from the centroid of each bone to the origin in the radius, and the global size of the bones. (2) Poses of the carpal bones that are controlled by the statistical pose model parameters b^m (Eqn.(6), m is a notation indicating the model parameters), which provides a rough alignment of the carpal bones. (3) Local rigid transformation parameters and a local scale factor for each bone $\beta_i = \{tx_i^l, ty_i^l, tz_i^l, r1_i^l, r2_i^l, r3_i^l, s_i^l\}$ (i is an index identifying each of the carpal bones, the radius and ulna), which provide refined alignment of bones based on the results from (2).

Using homogenous coordinates, the i^{th} bone in the template volume coordinate system can be transformed to the target volume coordinate system by,

$$A_i = PD_i \begin{bmatrix} ss_i^l Q_i \\ 1 \end{bmatrix} \quad (1)$$

where Q_i indicates the coordinates for the region of the i^{th} bone in the template volume with respect to its own centroid. A_i is the transformed coordinates of the i^{th} bone in the target volume. s_i^l is the local scale factor that controls the size of the i^{th} bone. D_i is the pose matrix of the i^{th} bone estimated using the pose model and the local pose refinement. P is the global rigid transformation matrix defined by equation (2).

$$P = \begin{bmatrix} R & t \\ 0 & 1 \end{bmatrix} \quad (2)$$

where t is the translation vector $[tx, ty, tz]^T$. R is the 3×3 rotation matrix represented by Rodrigues parameters [13], [16], calculated as

$$R = I + K \sin |r| + K^2(1 - \cos |r|) \quad (3)$$

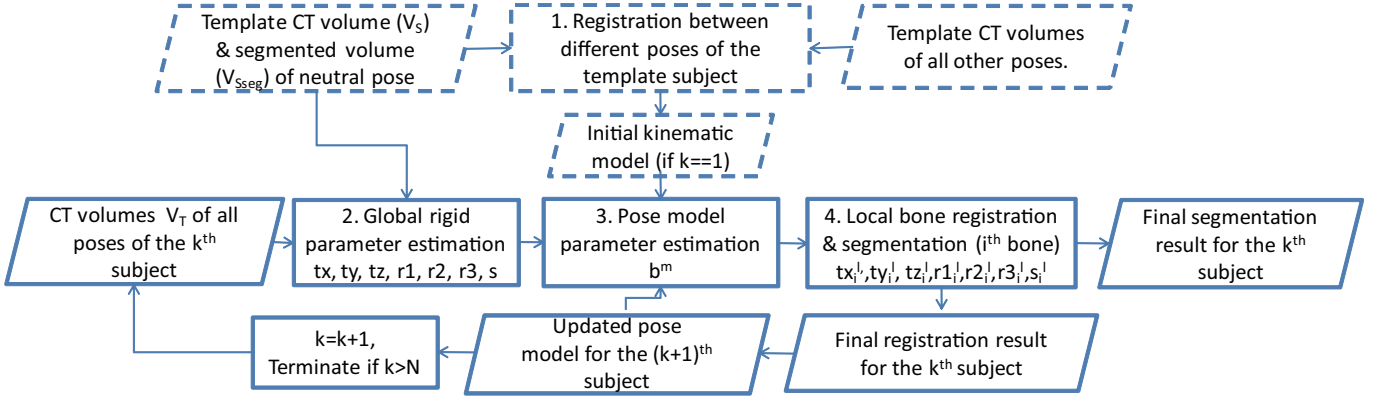


Fig. 1. Overview of the proposed system. The dashed boxes represent the initial registration and segmentation of the randomly selected template volume. The solid boxes represent the iterative registration and segmentation of the remaining examples.

where $|r|$ is the magnitude of the rotation vector $[r1, r2, r3]^T$. I is the identity matrix, and K is the skew-symmetric matrix normalised by $|r|$, expressed as

$$K = \begin{bmatrix} 0 & r3 & -r2 \\ -r3 & 0 & r1 \\ r2 & -r1 & 0 \end{bmatrix} / |r| \quad (4)$$

In equation (1), D_i is calculated as,

$$D_i = \begin{bmatrix} R_i^g & t_i^g \\ 0 & 1 \end{bmatrix} \quad (5)$$

where $t_i^g = s[tx_i^m, ty_i^m, tz_i^m]^T + [tx_i^l, ty_i^l, tz_i^l]^T$ is the summation of translation vectors estimated from the pose model and local bone refinement. $R_i^g = R_i^m R_i^l$ is the 3×3 rotation matrix that combines the rotations estimated from the pose model and local bone refinement respectively. R_i^m and R_i^l can be calculated individually by equation (3) using their corresponding Rodrigues parameters.

The use of Rodrigues parameters to represent bone orientations is convenient for pose model building and parameter optimisation. More importantly, unlike the quaternion representation, it does not require vector normalisation. Nor does it suffer from the singularity problem raised by the Euler angle rotations.

In the first step illustrated in figure 1, the template volume (V_S) is randomly selected from the training data sets. V_S is then segmented semi-automatically using the multi-label grow-cut method [1]. By using V_S and its corresponding segmentation result V_{Sseg} , each bone in V_S can be registered to other volumes at different wrist positions within the same subject using the method described in [15]. First, we manually adjust the transformation parameters of each bone in V_{Sseg} to roughly align with the target volume, and then automatically refine the transformation parameters via intensity based registration [17]. The refinement is iterated until an acceptable alignment is achieved. The bones to be registered belong to the same subject, so there are no significant shape differences. While the bone poses may be very different in different wrist positions, the initial rough interactive alignment makes it easy to achieve accurate registration. The interaction for each wrist position is also quick and efficient. This interactive step is carried out only

once for a given template volume. The result is an initial pose model, which is used for subsequent automatic registration.

III. STATISTICAL POSE MODEL GENERATION

The kinematics of the carpal bones is complex and significant pose difference can be introduced as the joint adopts different positions. In this section, we introduce a method for constructing the pose model of the carpal bones that enables the reproduction of valid poses with a small number of parameters. When carpal bones from different wrist positions of the same and different subjects are aligned, the pose model can be constructed from the transformation parameters of each bone with respect to a common reference coordinate system. The method of registration is described in sections IV and V. After the registration, we use the six rigid transformation parameters for each bone to train the SPM. The common coordinate system for all bone poses has an origin in the radius of the template volume (section II). Hence, for the SPM building, the transformation parameters for radius are always zero. The sizes of all the wrists are normalised to the template volume scale by using the estimated global scale factor. The pose of one subject is described by $(tx_1, ty_1, tz_1, r1_1, r2_1, r3_1, \dots, tx_{10}, ty_{10}, tz_{10}, r1_{10}, r2_{10}, r3_{10})^t$. (8 carpal bones, 1 radius and 1 ulna). Based on a set of training subjects, the pose model can be parametrised as,

$$h = \mu^m + \nu^m b^m \quad (6)$$

where the mean pose μ^m (m is a notation indicating the model parameters) and the principal subspace matrix ν^m are computed using PCA. The vector b^m represents the pose parameters that describe the pose of h along each principal direction. For the initial pose model, only the volumes at different positions of the template subject are used. The first two significant components are shown in figure 2, which represent 99% of the variation. As more subjects are aligned with the template, the pose model is updated by including more training samples, and is used for subsequent registrations.

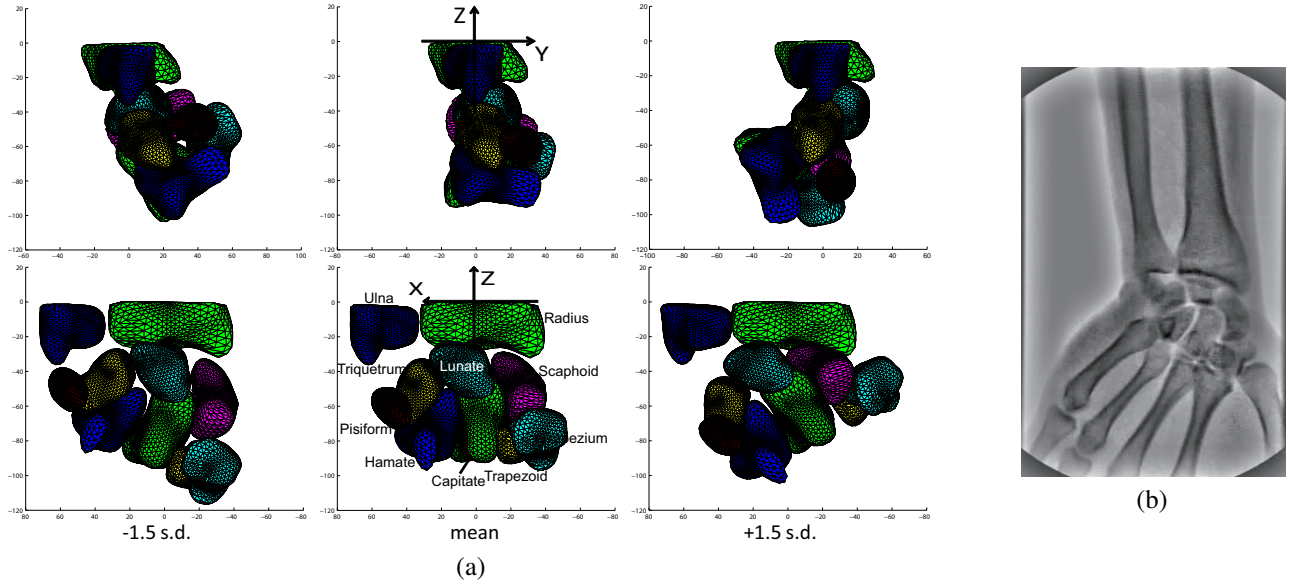


Fig. 2. (a) The poses of the first component (top row, lateral view) and the second component (bottom row, AP view) of the simple pose model. In each case the mean ± 1.5 s.d. are shown. (b) X-ray image showing the anatomical context of the carpal bones

IV. GLOBAL RIGID PARAMETER AND POSE MODEL PARAMETER ESTIMATION

As illustrated in figure 1, by using V_S , V_{Sseg} and the pose model, the global rigid pose and poses of the individual carpal bones can be estimated in sequence, aligning the corresponding bones in V_S and V_T (target volumes). The registration process is to find the pose parameters that best align the corresponding bones in V_S and V_T by producing an optimum similarity value. The cost function that measures the similarity, and optimisation method for estimating the pose parameters are described in the following subsections.

A. Similarity Measurement

To evaluate the similarity between the corresponding bone regions in V_S and V_T , we investigated several forms of the cost function (normalised correlation coefficient, sum of squared differences and mutual information based on intensities), achieving the best results from the one shown in equation (7), based on the difference of the normalised gradient magnitude of the two images. We define the Normalised Sum of Squared Difference (NSSD) between two images G_S and G_T as:

$$E = \left(\frac{\sum_{j \in C} (G_S(T(j)) - G_T(j))^2}{w} \right)^{0.5} \quad (7)$$

where C represents the region of interest (ROI) corresponding to each specific bone and j indexes the voxels of C in G_T . The ROI is a region slightly larger than the bone volume, obtained by a dilation of 10 voxels along the three axis. w is the total number of voxels in C . $G_S(T(j))$ and $G_T(j)$ are the normalised values derived from the image gradient in the transformed template ROI image and the corresponding target image respectively, which are generated by equation (8).

$$G_S(T(j)) = \frac{1}{(1 + \mu M_S(T(j)))}, G_T(j) = \frac{1}{(1 + \mu M_T(j))} \quad (8)$$

where T is the transformation (inverse to our estimated pose transformations) applied to C from target volume to template volume. M_S and M_T represent the gradient magnitude of the smoothed V_S and V_T respectively. V_S and V_T are smoothed by a $7 \times 7 \times 7$ Gaussian kernel with variance equal to 1 voxel (0.5 mm). μ was experimentally set to 0.1. Example images of the original CT slice and corresponding normalised gradient magnitude images are shown in figure 3.

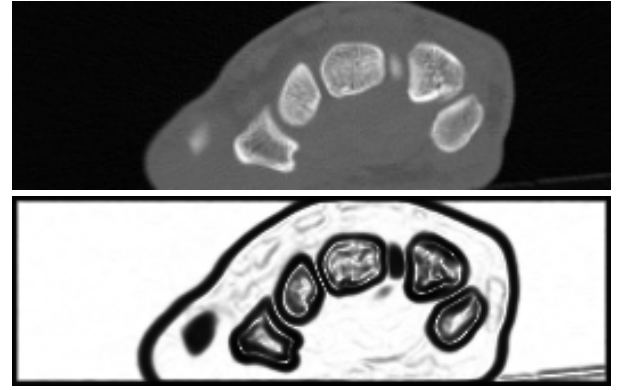


Fig. 3. top: CT slice, bottom: corresponding normalised gradient magnitude.

B. Optimisation

The global rigid pose parameter θ can be estimated by registration of the radius bone, since a point (defined in section II) in the radius of the mesh model is used as the origin of the coordinate system for all motions. Other carpal bones and ulna are registered by estimating their individual pose parameters. We have target volumes captured at different positions (5 wrist positions in our case) that belong to the same subject. They have different translation and rotation parameters, but should have a consistent scale factor s with respect to the template. Hence, we register the template bones to those target volumes

simultaneously at each iteration (Step 3 in figure 1) When the translation and rotation parameters are estimated, only the volume with corresponding wrist position is used to evaluate the cost function. In estimating the scale factor, s , on the other hand, volumes from all wrist positions are used to evaluate the cost function (summation of the cost function values). At the end of the registration, a set of translation and rotation parameters are obtained that correspond to the poses of the individual bones, and a single global scale factor is calculated for all wrist positions of the same subject. Individual scale factors for each bone are calculated in the local refinement stage (section V). Scale invariance is important for pose model generation.

The optimization method we use is a simplified version of the Brent-Powell method [18], requiring a smaller number of optimisation steps. We use parabola fitting to replace the Brent line search in the Brent-Powell method. The multi-dimensional search space ($\theta = \{tx, ty, tz, r1, r2, r3, s\}$ and b^m) is explored by iterative individual 1D line searches. For each parameter search, the cost function is evaluated at the current position, positive and negative neighbour positions (defined by a search range), then an optimum is found by fitting a parabola to the 3 evaluated positions. The optimum is iteratively refined by reducing the search range until convergence. More details can be found in [19].

V. SIMULTANEOUS REGISTRATION AND SEGMENTATION FOR LOCAL POSE REFINEMENT

After performing the global rigid and pose model transformation, the template bones are approximately aligned with the bones in the target volume. Some local misalignment may still remain requiring a further step to refine the local pose of each bone. In this section, we introduce an integrated segmentation and registration method, which combines the multi-label Grow-Cut segmentation [1] and intensity-based registration. This method, illustrated in Fig. 4, is developed from that described in our previous paper [15], improved in several respects. To make this paper self contained, the following description includes details of the previously published version.

The main objective of the method is to estimate $\beta_i = \{tx_i^l, ty_i^l, tz_i^l, r1_i^l, r2_i^l, r3_i^l, s_i^l\}$ for the i^{th} bone, improving its registration accuracy. The use of combined segmentation and rigid registration is preferred over non-rigid registration methods for this application. Finding the accurate pose parameters to align the bones is important for the SPM building. Non-rigid registration tends to deform the shape rather than finding the optimum pose. If rigid registration is performed individually, the topology of the bones may not be preserved and the bone volumes may overlap. This is overcome by combining the registration with multi-label Grow-Cut segmentation. In Grow-Cut, multiple labels are calculated simultaneously at each iteration and region overlapping is forbidden. It helps to make the registration more robust to the initial starting pose, and also acts as a soft constraint to preserve the topology of the bones. Subsequently, the segmentation results V_{Tlabel} can be used to build the statistical shape model of each bone. The

overview of the framework is illustrated in figure 4; each of the key steps is described in the following subsections.

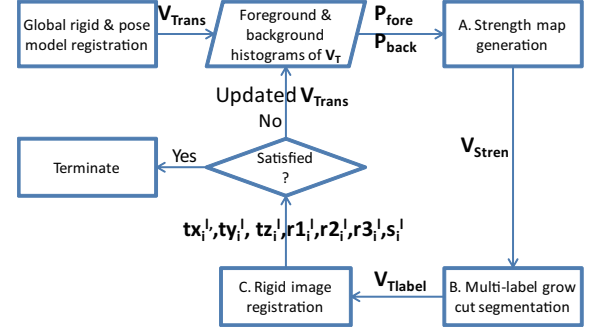


Fig. 4. Overview of the integrated segmentation and registration system corresponding to box 4 in figure 1.

A. Strength Map Generation

There are two key elements in Grow-Cut segmentation [1]. They are the current label at each voxel and a strength map associated with the image. The strength map indicates the ‘energy’ of the corresponding voxel, which is used to determine if the corresponding label can be propagated to its neighbours at each iteration. Since each labeled bone from V_{Sseg} (segmentation of V_S) has been roughly aligned with the target volume V_T through previous registrations, the labels for V_T can be therefore initialised using the transformed V_{Sseg} , denoted as V_{Ttrans} . In V_{Ttrans} , all overlapped bone areas are set to zero, as new labels shouldn’t be introduced. The initial label V_{Ttrans} will be evolved according to the associated strength map.

Here we present a novel method for initialising the strength map V_{Stren} for Grow Cut. The objective is to initialise this map with values of 1 (high certainty) and 0 (low certainty) of being either bone or non-bone. To obtain the V_{Stren} , an initial binary volume, $V_{bwTrans}$ (bone=1, non-bone=0) is generated from V_{Ttrans} . The normalised foreground and background histograms calculated from the overlap of $V_{bwTrans}$ and the target volume V_T allow us to calculate the probability that a voxel belongs to the foreground (P_{fore}) or background (P_{back}). Using Eqn. (9), we calculate the likelihood (V_L) of classifying each voxel as bone (positive) or non-bone (negative), from which Eqn. (10) and (11) generate new binary volumes (V_{bwL1} , V_{bwL2}) representing high certainty regions of bone and non-bone respectively. The thresholds of 0.9 and -0.5 were determined empirically. V_{bwL3} (Eqn. (12)) represents the region of V_T that is not classified as bone either in $V_{bwTrans}$ or V_{bwL1} . Equation (13) identifies the regions that are identified with certainty to be bone or non-bone, based on the histograms (P_{fore} and P_{back}), constrained to be within the respective bone and non-bone regions defined by $V_{bwTrans}$. Following Grow Cut relabelling, $V_{bwTrans}$ and V_{Stren} are calculated for each iteration step.

$$V_L = \frac{(P_{fore}(V_T) - P_{back}(V_T))}{\max(P_{fore}(V_T), P_{back}(V_T))} \quad (9)$$

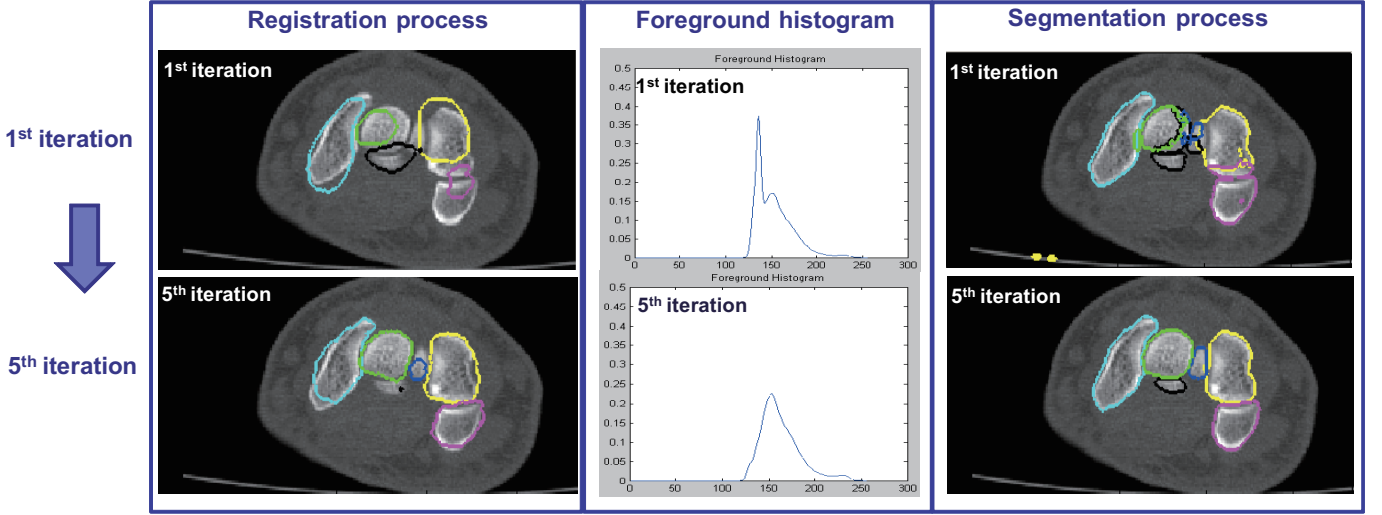


Fig. 5. Process of integrated segmentation-registration iteration for registering the template volume (coloured contours) to a target volume of a different subject. At first (global) registration the correspondence between the template and target volumes is poor resulting in the inclusion of a significant region of background in the foreground histogram. The segmentation step improves the correspondence of the bones. At a later iteration the registration and the foreground histogram are improved. The resulting segmentation step results in good agreement between the segmentation and the target volume.

$$V_{bwL1} = \begin{cases} 1 & \text{if } V_L > 0.9 \\ 0 & \text{otherwise} \end{cases} \quad (10)$$

$$V_{bwL2} = \begin{cases} 1 & \text{if } V_L < -0.5 \\ 0 & \text{otherwise} \end{cases} \quad (11)$$

$$V_{bwL3} = 1 - (V_{bwTrans} \cup V_{bwL1}) \quad (12)$$

$$V_{Stren} = (V_{bwL2} \cap V_{bwL3}) \cup (V_{bwTrans} \cap V_{bwL1}) \quad (13)$$

B. Multi-class Grow Cut Segmentation

The advantages of Grow Cut in this application are its ability to obtain a multi-label solution in simultaneous iteration, and the capacity for fast parallel implementation. The segmentation labels of ten bones (carpal bones plus radius and ulna) need to be updated simultaneously, helping to preserve bone topology. For efficiency the Grow Cut code was parallelised using NVidia Quadro FX 3800 Graphic Card via the CUDA API [20].

In our proposed framework, the strength map V_{Stren} is initialised automatically in step A (Fig. 4), and V_{Trans} (from step A or updated from step C) is used as the labeled volume. Since, there is only a small number of uncertain voxels with $V_{Stren} = 0$ at each iteration, it takes less than 2 seconds to complete the segmentation of a $141 \times 268 \times 169$ volume. The segmentation volume is denoted as V_{Tlabel} .

C. Rigid Image Registration

Following the segmentation, rigid image registration is performed. The cost function expressed in equation (14) is used as the similarity measurement in which a new term is added to the cost function described in equation (7). Since each bone has a unique label, the new cost function term tends to ‘drag’ the template bones to the corresponding segmented regions, which preserves the topology of the bones.

$$E_{local} = E + \left(\frac{\sum_{j \in C} (B_S(T(j)) - B_T(j))^2}{w} \right)^{0.5} \quad (14)$$

E is the gradient-based cost function in equation (7). B_S and B_T are the ROI binary image obtained from V_{Sseg} and the corresponding binary image obtained from V_{Tlabel} respectively. Other notations are the same as in equation (7). The optimisation method is the same as described in section IV-B. A new V_{Trans} is then obtained by using the updated transformation parameters.

D. Iteration and Termination

Step A to C are repeated; the segmentation volume, registration parameters and the intensity histograms coherently improve each other until the termination conditions are satisfied (the difference of the segmented volume V_{Tlabel} between adjacent iterations stops decreasing). The iteration process is illustrated in figure 5. The foreground histogram, registration and segmentation result at the 1st and 5th (final) iterations are shown, where the coloured contours from the template are superimposed on the target volume. The method described here differs from that described in [15] in that the transformation parameters and segmentations for all wrist positions are estimated in the same framework, and a consistent scale factor for each bone is calculated across all wrist positions. The final segmentation result is derived from all wrist positions. The labelled volumes at different positions are transformed to the template volume coordinate system. The overlapping area that is greater than 60% is used for the final label. Then the final label is transformed back to the volume at each position. The combination of segmentations in different wrist positions, and hence with different orientations relative to the sampling grid, reduces segmentation errors arising from partial volume effects. Combining the segmentation with the registration method makes the registration more robust than

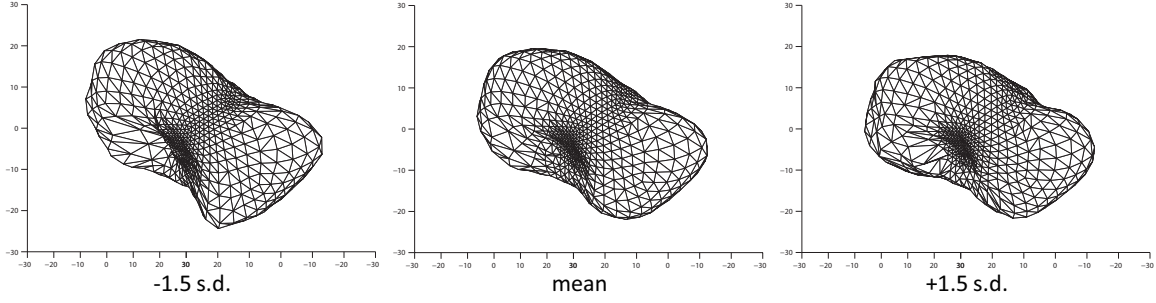


Fig. 6. The first component of the shape model of the scaphoid. The mean ± 1.5 s.d. are shown.

the registration only method, in terms of the sensitivity to the initial bone pose. This was evaluated in [15].

VI. STATISTICAL SHAPE MODEL GENERATION

The shape of the bones varies among different subjects. A SSM of each bone in the wrist is also important for pathology diagnosis. The key step of generating a SSM is to establish correspondences across subjects. In some approaches this has been achieved using deformable registration (e.g. [12], [21], [22]). However, in these studies the principal aim is to establish shape, rather than pose correspondence. In the context of our framework, it is important to determine the correct relative bone poses, and deformable registration would tend to change the shape of the bones rather than finding the correct pose. This would result in a less accurate SPM, so rigid registration is preferred. It would be possible to apply deformable registration after rigid alignment. In this case the computational cost depends on the selected deformable model. The final result is highly dependent on the regularisation method applied, and may be difficult to correct if increased accuracy is required. In our proposed framework, the shape differences between the corresponding bones of different individuals are accommodated by the segmentation process. Following the automatic registration and segmentation framework, the segmentation result can be directly used for the SSM construction. Our SSM is based on the Point Distribution Model (PDM- for example [23]). This requires the establishment of point correspondences between bones of different subjects, for which we use the well-known minimum description length (MDL) algorithm [6]. One training example is described by $(x_1, y_1, z_1, \dots, x_{1002}, y_{1002}, z_{1002})^t$ (1002 points on each bone). The coordinates of the shape points of each bone are expressed with respect to its own centroid. The statistical shape model, o_i , is then described as,

$$o_i = \mu_i^q + \nu_i^q b_i^q \quad (15)$$

where μ_i^q and ν_i^q (q is a notation indicating the shape parameters) are the mean shape and the principal subspace matrix for the i^{th} bone. b_i^q is the shape model parameter for generating new valid bone shapes. Figure 6 shows the shapes that arise by varying the first component of SSM of the scaphoid.

VII. FRAMEWORK INTEGRATION

Each part of the framework (figure 1) has been described in previous sections. Two important issues need to be further explained to complete the framework.

Firstly, in order to increase the robustness of the framework, the CT volumes are pre-processed to construct a multi-scale pyramid (downsampled by a factor of 2 at each level). In the optimisation procedure, the same set of initial search ranges is used at each level for both the global and local registrations (described in section VIII). The search ranges are divided by 2 each time the criteria are met, and the whole process is terminated when the maximum value of the search ranges is smaller than a pre-set threshold. To avoid the optimisation becoming trapped in local minima, a stochastic optimisation procedure is used for global parameter (wrist pose and scale factor) and pose model parameter (carpal bone pose) estimation, as follows:

- 1) Starting from zero transformation and orientation, optimise the poses of the bones of all input wrist volumes.
- 2) Record the best cost function value for each pose.
- 3) Randomly alter the starting value of the parameters for unsatisfied poses (defined in step 4) within the possible parameter space, and optimise again.
- 4) Repeat steps 2 and 3. Terminate the random process for the pose if the best function value of that pose remains unchanged for 5 times or the number of iterations exceeds 20.

This stochastic process is only performed on the lowest pyramid level for computational efficiency and robustness.

Secondly, at each iteration of the SPM updating procedure (see Fig.1), an outlier rejection algorithm is applied to exclude inaccurate registrations. After the registration is finished for each subject, the cost function values for each bone across all wrist positions are compared. Since the data is in the same image modality and from the same subject, the cost function value for the corresponding bones should be similar, independent of bone poses. Only the wrist positions with the cost function value less than $1.2 \times$ the best (smallest) cost function value are considered as successful registration. After all of the subjects are visited, those excluded subjects are revisited and aligned again by using the SPM generated from the included subjects. If successful registration is achieved, the revisited subject will be included to update the SPM. The process is repeated until the number of included subjects is unchanged. The unregistered volumes do not contribute to the model.

VIII. EVALUATION

We evaluated our framework based on CT data from 25 subjects (10 female and 15 male, median age 51, age range 25 - 72 years), recruited from the hand clinic at Salford Royal Hospital, Greater Manchester, UK. Eight of these subjects were diagnosed radiologically as suffering from scaphoid-lunate dissociation (referred to as the ‘abnormal’ group in the following discussion), the remainder being assessed not to have this condition (referred to as the ‘normal’ group). Each subject was imaged at five different wrist positions: neutral, and four extreme positions in radial-ulnar and flexion-extension movement. The wrist positions were held on a specially designed foam. Each of the CT volumes is captured by a GE LightSpeed VCT machine with a very low-dose exposure. The exposure from all 5 scans was 20 mGy. The acquisition parameters were: tube voltage of 80 kV, focal spot of 0.7 mm, slice thickness of 0.625 mm, pixel spacing of $0.29 \times 0.29 \text{ mm}^2$. The volumes were re-sampled by tri-linear interpolation to iso-cubic volumes of $0.5 \times 0.5 \times 0.5 \text{ mm}^3$ prior to the registration and segmentation. We found that higher resolution (e.g. $0.25 \times 0.25 \times 0.25 \text{ mm}^3$) did not produce a much better accuracy of the segmentation and registration but required much larger memory and longer computational time.

Using the interactive method described in [15] we obtained the segmentation of each of these subjects in the neutral position and the transformation parameters that relate the neutral position to the extreme positions for that subject. The segmentations at each position were validated by an experienced clinician. These segmented and registered images were used as ground truth in the evaluation of the automated framework described here.

In our experiments, each of the 25 subjects was selected as the template and registered with the remaining 24 subjects in turn. The registration order to other subjects was randomly sequenced. In the optimisation procedure, the same set of fixed initial search ranges was used at each level for both the global and local registrations (4 voxels for translation, $4\pi/180$ for rotation, 0.2 for scale and one standard deviation for pose model parameters). The framework terminated when the largest search range was smaller than 0.1.

A. Registration Results

To evaluate the registration results, we transformed the mesh points of each bone in neutral position to other positions using the ground truth registration parameters and our estimated registration parameters respectively, for each subject. Then the 3D Euclidean distances of each corresponding mesh point between the two transformed meshes for each bone are measured (known as mean target registration error (mTRE) [24]). The registration errors are presented in table I, showing the measurements from 25 (different initial template) \times 24 (subjects) \times 5 (positions) tests. The errors were only calculated based on successful registrations, defined by the outlier rejection scheme (section VII). Specifically, for each bone, the successful registration rate is the total number of instances of that bone included by the outlier rejection algorithm divided by the total number of tested volumes. As shown in table I,

registration achieved sub-voxel accuracy (mean error of $0.34 \pm 0.27 \text{ mm}$). The successful registration rate of each bone across all tests are also presented in table I. The successful registration rate for most bones is very high. The main exception is the ulna which is much lower than the others. The shape of the ulna is highly symmetric and its movement varies greatly between individuals. In some individuals, there is relatively little movement, while in others there may be significant movement. Of the others, the lowest successful registration rate occurred in the trapezoid. This bone has a nearly spherical shape, making calculation of the orientation rather unstable. It is also the smallest of the carpal bones.

The standard deviation of the success rate indicates that the success rate and registration error are not very sensitive to the selection of initial template, as the SPM is updated each time a new subject is included, and the failed registrations are revisited in a larger loop. In our 25 independent tests, based on different initial template, 19 or 20 out of 25 subjects were consistently successfully registered (all positions successfully aligned) and used for final SPM generation. Subjects were excluded from model building if any of the positions for that subject were rejected by the automatic framework. In each rejected subject the failed positions arose because of misalignment of either the ulna or trapezoid (or both).

TABLE I
MEAN AND STANDARD DEVIATION REGISTRATION ERRORS (MEASURED BY MEAN TARGET REGISTRATION ERROR IN MM) AND THE SUCCESSFUL REGISTRATION RATE OF EACH BONE BASED ON USING EACH OF THE 25 SUBJECTS IN TURN AS THE INITIAL TEMPLATE.

Bones	Ulna	Radius	Triquetrum	Lunate	Scaphoid
mTRE (mm)	0.29 ± 0.24	0.22 ± 0.17	0.33 ± 0.26	0.42 ± 0.34	0.43 ± 0.33
SucRate (%)	80.2 ± 3.7	99.8 ± 0.5	95.6 ± 3.1	96.7 ± 2.0	97.3 ± 2.2
Bones	Pisiform	Hamate	Capitate	Trapezoid	Trapezium
mTRE (mm)	0.39 ± 0.30	0.28 ± 0.21	0.4 ± 0.34	0.38 ± 0.33	0.30 ± 0.25
SucRate (%)	95.3 ± 3.1	97.1 ± 1.0	93.1 ± 7.6	90.9 ± 3.1	97.1 ± 1.9

B. Statistical Pose Model Updating

Only the first two significant components of the SPM were used throughout the whole registration across all subjects. When the SPM is updated at each iteration, the percentage of variations captured by the first two significant components decreases. The percentage variation represented by the first two components in the evolving process of the SPM over the 25 independent tests is shown in figure 7. This converged to 92% to 93% variation, irrespective of the registration sequence and initial template selection. An animation of generating intermediate poses by varying the first two components of the final SPM can be found in the supplementary material. In our experiments, including more PCA components did not increase the registration accuracy. This also indicates that the integrated registration and segmentation local refinement step works very well based on the starting pose provided by the pose model.

C. Segmentation Result

We compared the segmentation results with ground-truth using the Tanimoto coefficient (TC) [25] (also known as

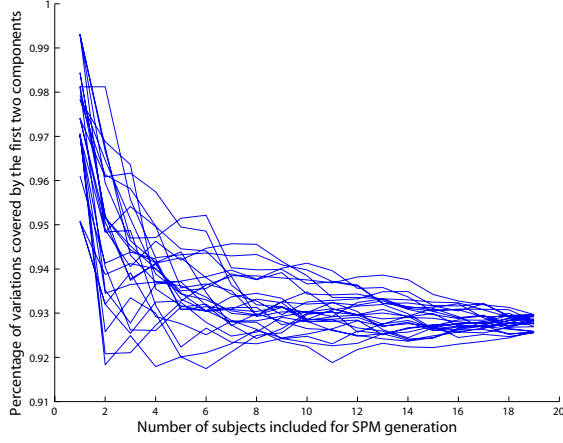


Fig. 7. The percentage of variation covered by the first two significant components in SPM updating process. Each line represents the use of a different subject as the template.

the Jaccard similarity coefficient [26]), presented in table II, showing the mean and standard deviation from 25 independent tests using different initial template subjects. The Tanimoto coefficient measures similarity between two sample sets, and is defined as the size of the intersection divided by the size of the union of the sample sets. The coefficient is between $[0, 1]$, where 1 indicates perfect overlap of the compared images. These segmentation results, arising entirely from the automated framework without further refinement, show a high level of segmentation accuracy and repeatability. An example of the automatically segmented carpal bones is presented in figure 8, showing the sagittal, axial and coronal view with the 3D mesh model.

TABLE II

THE TANIMOTO COEFFICIENT COMPARING THE GROUND TRUTH SEGMENTATION AND AUTOMATICALLY CALCULATED SEGMENTATION FOR EACH BONE. THE MEAN AND STANDARD DEVIATION ARE SHOWN, BASED ON 25 INDEPENDENT TESTS USING DIFFERENT INITIAL TEMPLATE SUBJECTS.

Bones	Ulna	Radius	Triquetrum	Lunate	Scaphoid
TC	0.86 ± 0.10	0.88 ± 0.06	0.90 ± 0.06	0.88 ± 0.10	0.87 ± 0.09
Bones	Pisiform	Hamate	Capitate	Trapezoid	Trapezium
TC	0.90 ± 0.10	0.91 ± 0.03	0.83 ± 0.10	0.82 ± 0.09	0.90 ± 0.10

D. Pathology Detection

In previous sections, we presented a complete framework for automatically generating a SPM and SSM across subjects at different positions. In this section, we demonstrate the effectiveness of the SPM and SSM by applying them to pathology detection and quantification. Using a ‘standard’ SPM and SSM, the relative poses of the carpal bones can be measured and recorded as ‘standard’. One condition that may be assessed using this measurement is bone dissociation, where the 3D distance between the bones is larger than normal. Scaphoid-Lunate dissociation is one of the most common of these and we use it as an example to demonstrate the method of using the SPM and SSM for diagnosis.

Since the bone spaces may vary at different wrist positions, the constructed ‘standard’ measurement tool needs to be position dependent. One major advantage of using the SPM is that the wrist from different positions can be aligned directly based on the SPM values. The first two components of our SPM cover more than 90% of the observed variation in the full range of flexion-extension and radial-ulnar movements. The combination of the two components is also able to generate interpolated positions within the motion range. To simplify the problem, here we only demonstrate the pathology detection tool based on radial-ulnar deviation movement, which is the most appropriate for diagnosing Scaphoid-Lunate dissociation.

1) *Building the ‘Standard’ Scaphoid/Lunate Model:* 14 subjects in the normal group, each at 3 different positions (neutral and extreme radial-ulnar deviation), were used to build the ‘standard’ measurement model. Each of the 14×3 target volumes is aligned with the final SPM (based on 25 subjects, each at 5 wrist positions) from the registration framework (section VII) to obtain the poses of the individual bones, and hence the scaphoid-lunate distance. Since there are not enough samples that cover the full range of continuous positions, we interpolated (cubic spline) the positions at integer intervals of the pose model parameter (Fig. 2) between the neutral position and two extreme positions of radial-ulnar deviation for each subject. This results in the training volumes being grouped at each integer interval of the 2nd component of the SPM parameter. (The second component of the SPM mainly represents radial-ulnar movement- see Fig. 2).

To diagnose the Scaphoid-Lunate dissociation conditions, the ‘standard’ range of distances between these two bones need to be calculated and recorded. The ‘standard’ SSM represents a range of shapes for each bone. To maintain consistency in the measurement of distances, each carpal bone is represented by its mean shape. The SSM has the same number of surface points (1002) on each bone. The point correspondences between different bones are established by using the index of the mesh points on the surface. Here we used evenly down-sampled number of surface points N ($N=100$ in our case) to reduce the memory usage and improve the computational efficiency. If each of the j^{th} selected surface points on the Lunate and Scaphoid of the k^{th} sample volume at position ϕ are represented as $l_{\phi,j}^k$ and $s_{\phi,j}^k$ respectively, the relative distance between the Scaphoid and Lunate was calculated as,

$$d_{\phi,j}^k = l_{\phi,j}^k - s_{\phi,j}^k \quad (16)$$

$d_{\phi,j}^k$ is a 3×1 vector (X,Y and Z axis). Then the mean differences $m_{\phi,j}$ and covariance matrix $C_{\phi,j}$ of the j^{th} point pair based on all k samples at position ϕ can be obtained. Equation 16 shows that we calculate and record the distances for each pair of points. Subsequently, the average Mahalanobis distance (MD) between the newly accessed data and the model is calculated using equation (17).

$$m_{\phi} = \frac{1}{N} \sum_{j=1}^N \sqrt{(d_{\phi,j}^{new} - m_{\phi,j})^T C_{\phi,j}^{-1} (d_{\phi,j}^{new} - m_{\phi,j})} \quad (17)$$

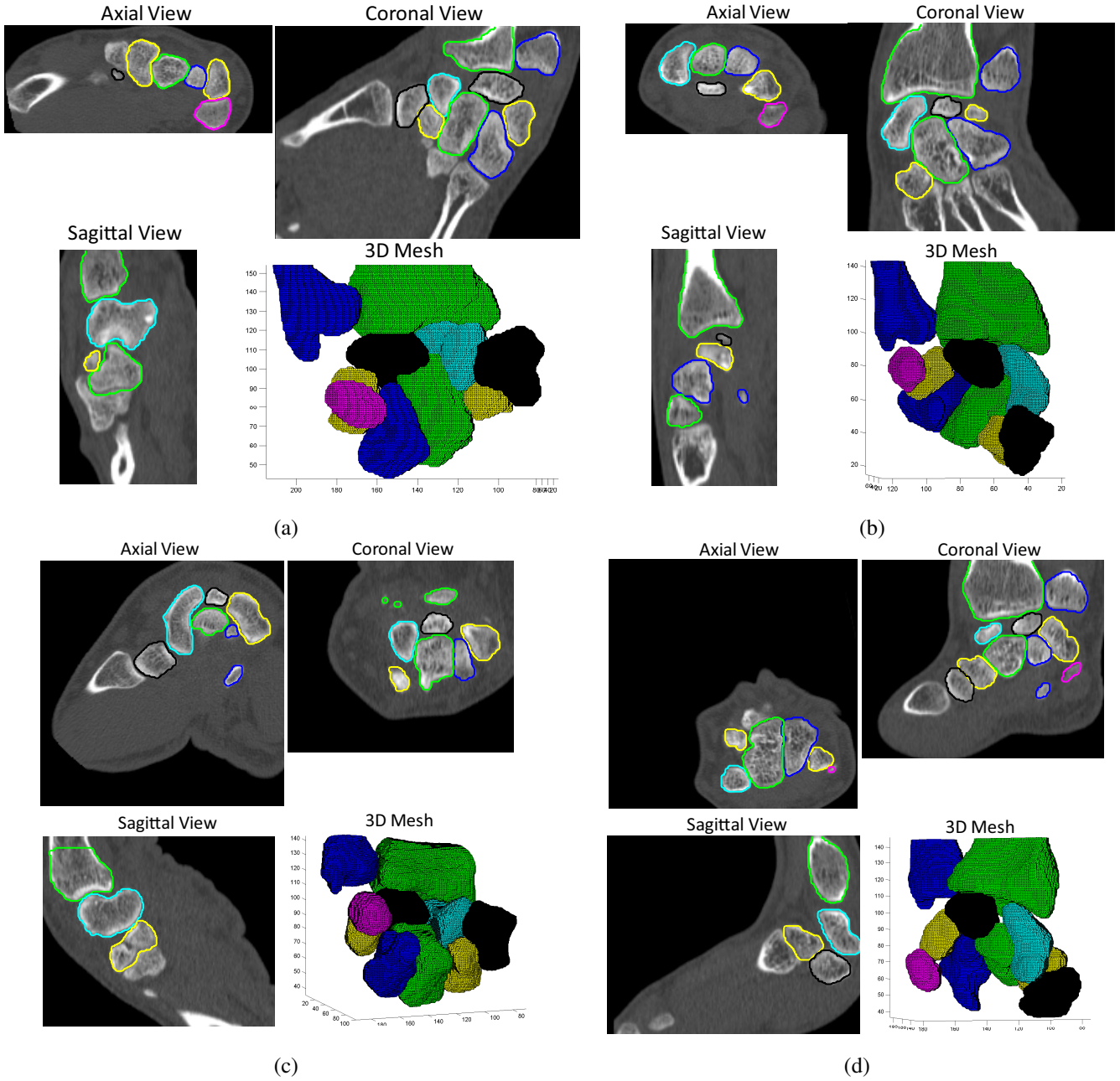


Fig. 8. The axial view, coronal view, sagittal view and 3D mesh model of automatically segmented wrists at (a) Radial deviation (b) Ulnar deviation (c) flexion (d) Extension positions of different subjects. The unlabelled bones that appear in some images are parts of the metacarpal bones which are not included in the segmented template. The coloured lines of the 2D-slices correspond to the colours in the 3D mesh models.

2) *Wrist Diagnosis*: To assess a new wrist, the image is firstly registered to the template volume using the proposed framework. After the SPM parameters are estimated, the measurement of the input image can be compared with the ‘standard’ model at the corresponding wrist positions. Additionally, the mean shape of the SSM is used to represent each of the assessed carpal bones, where the point correspondences between Scaphoid and Lunate were already established. The MD (Eqn. (17)) is then calculated to indicate the degree of abnormality of the subject. Seventy-five volumes (three wrist positions from each of the 25 subjects) were registered by the proposed framework. The MDs of 64 automatically and successfully registered volumes are presented in figure 9. The

11 unsuccessfully registered volumes (see section VIII(A)) came from 3 normal subjects and 1 abnormal subject. The MDs for the remaining 14 successfully registered normal wrists were calculated using leave-one-out experiments (13 subjects were used for ‘standard’ model building). In this figure, the red squares represent abnormal subjects and the black crosses represent normal subjects. The accuracy of classifying individual volumes as abnormal is indicated in the Receiver Operating Characteristics (ROC) curve shown in figure 10, obtained by varying the threshold of MD (the same threshold for all positions). The area under curve is 0.94. The MD threshold that produces the best classification is 2.04, which results in a 92% true positive rate (TPR) and 12% false

positive rate (FPR) in identifying individual abnormal wrist position.

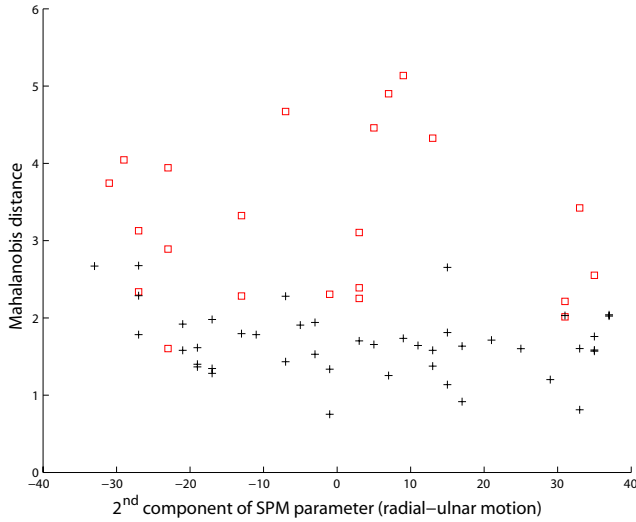


Fig. 9. The Mahalanobis distances of 22 subjects at a range of wrist positions for Scaphoid-Lunate measurement. Red squares represent abnormal subjects; black crosses are normal subjects.

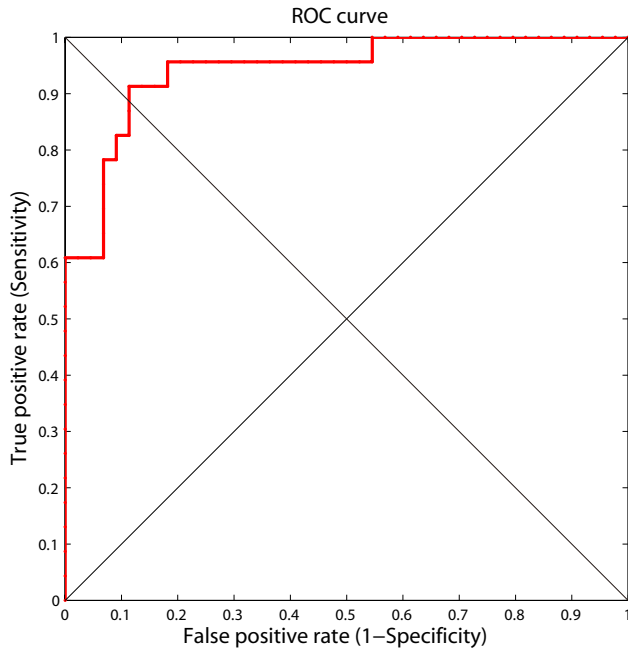


Fig. 10. ROC curve for individual wrist position diagnosis.

IX. DISCUSSION

Statistical pose models of articulated joints in 3D are potentially highly useful in imaging studies aimed at assessing abnormal kinematics [4], [13], [27]. We have previously described [27] the use of models built in this way for inference of 3D kinematics based on 2D image sequences, and demonstrated that this can be achieved with sufficient accuracy to allow meaningful clinical measurements to be

made. However, the task of building such a model, requiring accurate segmentation of each bone in a complex joint in several articulated positions, is a daunting one. We argue that the model needs to incorporate the position variation arising from the articulation (kinematics) and the variation in shape of bones between individuals. In this study we have demonstrated a method for building such models, which exploits the facts that identical bones from the same individual are represented in different positions, and that the positions are similar between individuals. The method learns a statistical pose model, while simultaneously generating accurate segmentations. The use of rigid registration integrated with segmentation has allowed us to decouple the issues of pose and shape, as it is only the latter that is relevant for segmentation. Convergence of the iterative framework is assisted by using the evolving model to constrain the registration. This approach has something in common with combined group-wise registration and model building [12], where the registration avoids the selection of an arbitrary template. In this case the number of articulated components adds several degrees of freedom to the problem, and we have based the registration on a single template example. However, we have demonstrated that the combined registration and segmentation is insensitive to the template selection. The variation in pose of the bones at different joint positions results in a requirement for interactive initiation of the registration in the template example. The segmentation step works by having an initial approximate segmentation from the registration of the bones across different positions, which suggests the use of methods developed for semi-interactive segmentation (e.g. Graph-Cut [28], Grow-Cut [1] and Random Walker [29]). We evaluated some such methods; the efficient multi-label propagation of segmentation provided by grow-cut made it ideal for this purpose. The iterative refinement of the grow-cut strength map means that, should further interactive segmentation prove necessary after the final convergence, this can easily be accommodated within the framework. Our observed segmentations were sufficiently good to make this step unnecessary in this case. The segmentation showed high consistency with ground-truth and sub-voxel registration accuracy was achieved.

We demonstrate the effectiveness of the statistical pose and shape model built using our automatic framework by using it to identify scaphoid-lunate dissociation. Scaphoid-lunate dissociation is most apparent in wrist positions along the radial-ulnar movement. The model was able to represent the kinematics with sufficient precision to allow the abnormal cases to be identified with high sensitivity and specificity. The use of a SPM for this purpose allows images from different sets of articulated positions to be aligned directly with the model using the SPM values. This confers an advantage over, for example, the method described in [11], where comparisons are made by aligning the wrists at a limited number of pre-defined positions.

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