Measuring Proton Shift Tensors with Ultrafast MAS NMR

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Abstract

A new proton anisotropic-isotropic shift correlation experiment is described which operates with ultrafast MAS, resulting in good resolution of isotropic proton shifts in the detection dimension. The new experiment makes use of a recoupling sequence designed using symmetry principles which reintroduces the proton chemical shift anisotropy in the indirect dimension. The experiment has been used to measure the proton shift tensor parameters for the OH hydrogen-bonded protons in tyrosine.HCl and citric acid at Larmor frequencies of up to 850 MHz.

Keywords: chemical shift anisotropy, ultrafast magic angle spinning, anisotropic-isotropic shift correlation, hydrogen bonding, symmetry-based recoupling sequence

Introduction

Hydrogen bonding plays a critical role in directing molecular self assembly, which is ubiquitous in biology and an important aspect of supramolecular chemistry, crystal engineering and nanotechnology. Solid-state 1 H NMR spectroscopy provides an excellent means to study hydrogen-bonded structures, because the 1 H chemical shift interaction contains information about the geometry of the hydrogen bond. For example, an early study [1] revealed a relationship between the 1 H isotropic shift δ_{iso} and the O...O distance in a broad range of crystalline solids forming O-H...O hydrogen bonds. By comparison with neutron diffraction data, which provides accurate positions for the hydrogen atoms, a linear correlation was later established between δ_{iso} and the H...O hydrogen bond length [2]. As confirmed by *ab initio* calculations [3], the main origin of this effect is the deshielding of the principal component of the 1 H chemical shift tensor perpendicular to the hydrogen bond that occurs as the bond length decreases. More recently, Wu *et al.* [4] showed for a series of crystalline hydrates that the span and the skew of the 1 H chemical shift tensor were linearly correlated to the

hydrogen bond length and the O-H...O bond angle, respectively. A similar correlation was identified between calculated values of the ¹H chemical shift anisotropy (CSA) and H...O distances in galactose [5]. These results suggest that variations in individual principal components are more sensitive indicators of changes in the hydrogen bond environment than the ¹H isotropic shift alone.

However, measurements of the ¹H shift tensor in solids are challenging, because of strong ¹H homonuclear dipolar couplings, which broaden the lines and reduce resolution, and the relatively small size of the ¹H chemical shift interaction. Until recently, experiments have been restricted to simple systems, usually in the form of single crystals [6-9] or perdeuterated powders [4], and the resulting lack of experimental data has precluded a full understanding of the relationship between ¹H shift tensors and hydrogen bond geometry. However, some progress has now been made towards more general methodologies for measuring the ¹H shift tensor based on two-dimensional NMR experiments which correlate the anisotropic and isotropic parts of the shift interaction. These make use of magic angle spinning (MAS) and multi-pulse homonuclear decoupling [10,11] to resolve different ¹H sites via their isotropic shifts in the detection dimension, so that a method of reintroducing or "recoupling" the MAS-averaged ¹H CSA is required during the evolution time. For example, Brouwer and Ripmeester [12] designed a recoupling sequence using symmetry principles [13,14], while Duma et al. [15] used rotary resonance [16-18] to reintroduce the ¹H CSA. In common with all methods based on rotary resonance, the latter suffers from substantial sensitivity to rf inhomogeneity, while the sequence symmetry chosen in the former restricts the experiment to relatively slow MAS rates. In order to improve the resolution of different sites in v₂, Hou et al. [19] recently exploited magnetization transfer to a neighbouring heteronucleus after recoupling the ${}^{1}H$ shift anisotropy during t_{1} . This approach was shown to be particularly powerful for measuring the ¹H shift tensor parameters for the amide protons in ¹⁵N-enriched proteins, but is less appropriate for hydrogen-bonded OH sites where a suitable directly bonded heteronucleus is not available.

In this communication, we demonstrate a ¹H anisotropic-isotropic shift correlation experiment which employs a symmetry-based recoupling sequence which is suitable for use when the MAS rate exceeds 50 kHz. The combination of MAS in this "ultrafast" regime and high B₀ field allows the majority of hydrogen-bonded sites in simple crystalline solids to be resolved in v_2 without the need for multi-pulse homonuclear decoupling. The usefulness of the new experiment is demonstrated by measurements of the ¹H shift tensors for all the hydrogen-bonded OH sites in tyrosine.HCl and citric acid.

Pulse Sequence Design

Levitt and co-workers [13,14] have used symmetry principles to design recoupling sequences which can reintroduce specific nuclear spin interactions averaged by MAS. The current work employs the most flexible class of symmetry-based recoupling sequence which is designated RN_n . These consist of N composite inversion pulses R, timed to occupy n rotor periods, where each R element of the overall sequence has duration $n\tau_r/N$ and alternate elements have phases $\pm \pi nv/N$. It has been demonstrated that the symmetry numbers N, n and v determine which interactions are retained in the first-order effective Hamiltonian for the sequence according to:

$$H^{(1)} \propto A_m^l T_\mu^\lambda \quad if \left(nm - \nu\mu\right) = \frac{N}{2} k_\lambda \tag{1}$$

where A is a rank-l irreducible spherical tensor operator describing the spatial part of the interaction Hamiltonian, and T is a rank- λ irreducible spherical tensor operator describing the spin part. The rotational components of the spatial and spin tensors m and μ take values m = l, l - 1, ... -l and $\mu = \lambda$, $\lambda - 1$, ... - λ , respectively, and k is any integer with the same parity as λ .

Recoupling sequences suitable for measuring the ¹H shift tensor recouple a single-quantum Hamiltonian which takes the form

$$H^{(1)} = \sum_{i} \left(\omega_{j} T_{-1}^{1} + \omega_{j}^{*} T_{1}^{1} \right)$$
 (2)

to first order, where the index j runs over all the ¹H shift interactions. The coefficient ω_j depends on the anisotropic part of the chemical shift interaction and determines the appearance of the recoupled powder pattern observed in the evolution dimension. Suitable symmetries must also avoid inadvertently recoupling the strong ¹H dipolar interactions, as well as isotropic ¹H shifts. Of the many symmetries which satisfy these conditions, R18 $_2^5$ [12] and R12 $_1^4$ [19] have been used successfully to measure ¹H shift tensor parameters. However, since the pulse sequence is synchronized with the spinning, the required rf amplitude increases with ω_r , so that these symmetries become impractical at ultrafast MAS rates. For R18 $_2^5$ and R12 $_1^4$ rf amplitudes in excess of 180 kHz and 240 kHz, respectively, would be required for MAS rates above 40 kHz, and in Refs. [12] and [19] experiments were carried out below 20 kHz. A different choice of sequence symmetry allows similar experiments to be carried out at higher MAS rates at which a well-resolved isotropic ¹H spectrum can be acquired without the need for homonuclear decoupling as in Ref. [12]. Note

that in the case of OH protons, resolution of different sites cannot be improved by magnetization transfer to a directly bonded heteronucleus as in Ref. [19].

The pulse sequence used to record 1 H anisotropic-isotropic shift correlation spectra in this work is shown in Figure 1. The preparation period consists only of a suitable relaxation delay, which is followed immediately by a R16 $_{3}^{2}$ recoupling sequence of duration t_{1} . This choice of R sequence symmetry allows MAS rates up to 67.5 kHz to be used before the required rf amplitude exceeds 180 kHz. During the evolution period, longitudinal 1 H magnetization decays under the action of the Hamiltonian in Eq. (2), and subsequently a $\pi/2$ pulse transfers any remaining longitudinal 1 H magnetization to the transverse plane where it is acquired during t_{2} . In practice, the experiment is initiated with a saturation sequence followed by a recovery delay to ensure constant initial magnetization and to avoid long recycle delays.

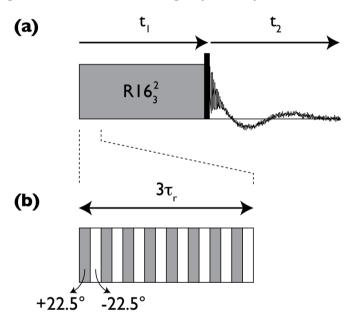


Figure 1. Experiment used to record ¹H anisotropic-isotropic shift correlation spectra at ultrafast MAS rates, as described in the text: (a) overall pulse sequence. The black bar represents a $\pi/2$ pulse. (b) R16²₃ sequence which operates during the evolution period, t_1 . Each bar represents a π pulse.

Experimental

¹H anisotropic-isotropic shift correlation spectra were recorded using the pulse sequence shown in Figure 1 on two spectrometers operating at Larmor frequencies of 600.13 and 850.13 MHz, both equipped with a 1.3 mm MAS probe. MAS rates of between 58.6 and 62.5 kHz were selected, so that the R16²₃ recoupling sequence required a ¹H rf amplitude of either 156.3 or 166.6 kHz. Note that the small coil diameter means that these amplitudes are well inside the manufacturer's specifications for the ultrafast MAS probes used

here. Further experimental details are given in the relevant figure captions. The two-dimensional FID was Fourier transformed with respect to t_2 , and the resulting spectrum was baseline corrected to remove the broad ¹H background signal. Since t_1 samples the decay of longitudinal ¹H magnetization quadrature detection is not appropriate, and a real Fourier transform was applied in the indirect dimension, resulting in ¹H CSA lineshapes in v_1 which are symmetrical about the origin. For anisotropic interactions, such as the CSA, the magnitude of the recoupled Hamiltonian always depends on the orientation of the molecular frame with respect to the rotor. This means that not all orientations are fully recoupled, and in this case there is some longitudinal ¹H magnetization which does not decay, resulting in a dc offset in the t_1 signal and a corresponding zero-frequency line in v_1 . This was removed by subtracting the average of the final 8 points of each interferogram prior to Fourier transform in v_1 . A schematic describing all the processing steps is included in the Supplementary Information (Figure S1). The t_1 dwell time must correspond to an even number of π pulses, but if sampling does not coincide with a complete R cycle, cycling sidebands appear in the v_1 dimension. Hence, a careful choice of sampling rate in the indirect dimension is necessary to ensure that these appear outside the ¹H CSA lineshape.

The anisotropy and asymmetry parameters for the chemical shift are defined according to $\zeta = \delta_{zz} - \delta_{iso}$ and $\eta = (\delta_{yy} - \delta_{xx})/\zeta$, respectively, with the principal components ordered according to $|\delta_{zz} - \delta_{iso}| \ge |\delta_{xx} - \delta_{iso}| \ge |\delta_{yx} - \delta_{iso}| > |\delta_{yy} - \delta_{iso}|$. Numerical simulations of the recoupled ¹H CSA lineshapes were performed using SIMPSON [20]. Powder averaging was achieved using 615 (α,β) orientations chosen according to the scheme of Zaremba [21] and 40 uniformly distributed values of γ . B_1 inhomogeneity was included by summing 17 simulations carried out using rf amplitudes weighted according to the experimentally determined B_1 distribution. The experimental distribution is skewed with its maximum on the high B_1 side and a long tail extending on the low side with significant intensity limited to $\pm 5\%$ of the nominal value. A Gaussian line broadening function was applied and the result processed in an identical fashion to the experimental data in order to obtain a simulated ¹H CSA lineshape. An array of these simulated lineshapes were generated for ζ up to 25 ppm and η in the range 0.0 to 1.0, and the ¹H shift tensor parameters were extracted by comparing these with the experimental data, using a similar method to that described in Ref. [12]. For each simulated lineshape the optimal scaling factor was found by fitting to the experimental data, and the corresponding χ^2 parameter was plotted as a function of ζ and η . The resulting error surface allows the best-fit values of ζ and η to be obtained, as well as their confidence limits, assuming χ^2 is suitably normalized [22].

Results and Discussion

Figure 2 shows SIMPSON simulations performed as described above of 1 H CSA lineshapes recoupled using a R16 $_{3}^{2}$ sequence operating at a MAS rate of 62.5 kHz for a Larmor frequency of 600 MHz. These simulations demonstrate that measurement of the chemical shift parameters ξ and η is possible using the anisotropic-isotropic correlation spectrum described here. In (a) the increasing ξ results in an increase in the width of the pattern, while the sensitivity of the lineshape to η is demonstrated in (b). The experimentally determined B_{1} distribution has been added to otherwise identical simulations which are shown in (c) and (d). Changing the R symmetry results in a different scaling factor, so the lineshapes observed with R16 $_{3}^{2}$ are similar but not identical to those for R18 $_{2}^{5}$ [12] or R12 $_{1}^{4}$ [19]. Even at the relatively low field of 600 MHz, values of ξ below 5 ppm can be determined as illustrated in (a). In practice the variation with η seen in (b) is obscured to some extent by effect of B_{1} inhomogeneity, as illustrated in (d). In common with R18 $_{2}^{5}$ [12] or R12 $_{1}^{4}$ [19], the sign of ξ cannot be determined because of the symmetry of the recoupled 1 H CSA lineshape. Furthermore, R sequences with this symmetry also reintroduce the heteronuclear dipolar interaction, so they are not suitable for measuring 1 H CSAs in the presence of abundant nuclei without additional decoupling [19].

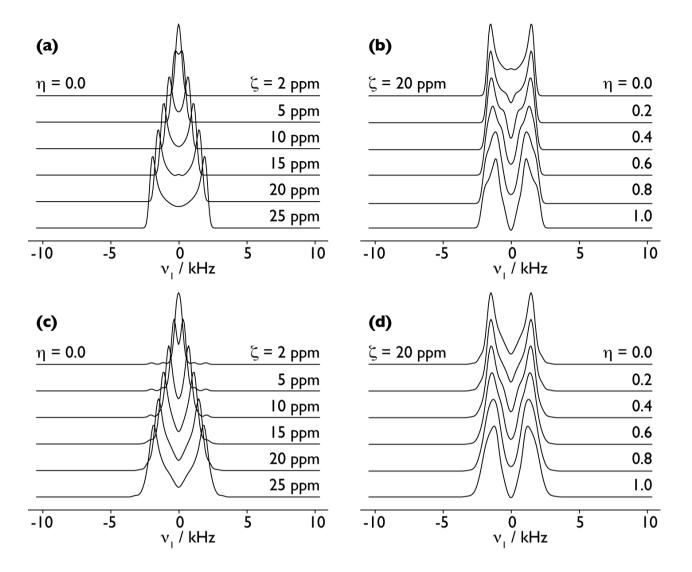


Figure 2. SIMPSON simulations of ¹H CSA lineshapes recoupled using a R16²₃ sequence for a Larmor frequency of 600 MHz and a MAS rate of 62.5 kHz, carried out as described in the text. The simulations in (a) and (c) show the variation of the recoupled lineshape with ζ for η = 0.0, while (b) and (d) show the variation with η for ζ = 20 ppm. The effects of B_1 inhomogeneity are neglected in (a) and (b), while the experimentally determined B_1 distribution is included in (c) and (d). Note the broadening of the singularities in the latter as a result of the B_1 inhomogeneity, and the consequent loss of sensitivity to η in particular.

As an illustration of the method Figure 3(a) shows a ¹H anisotropic-isotropic correlation spectrum of tyrosine.HCl recorded at a Larmor frequency of 850.13 MHz and a MAS rate of 58.6 kHz. Other experimental parameters are given in the caption. The high-field ultrafast MAS ¹H spectrum (top) exhibits two well-resolved peaks which have been assigned previously by measurement of ¹H-¹⁷O internuclear distances using heteronuclear recoupling experiments [23]. The neutron structure of tyrosine.HCl [24] contains two short hydrogen bonds both involving the phenolic OH (designated O¹H¹ in Ref. [24]) which acts

as the acceptor group in a hydrogen bond with the carboxylic OH (designated O²H²) and simultaneously as the donor in a hydrogen bond with the chloride ion. Figure 3(b) shows (red lines) cross-sections parallel to v_1 taken at v_2 frequencies corresponding to the isotropic ¹H shifts of H² and H³. These are compared with SIMPSON simulations (dashed lines) for the best-fit ζ and η obtained as described above. The results of the fits are given in Table 1, and the error surfaces with respect to ζ and η are shown in the Supplementary Information (Figure S2). The sensitivity to η evident in Figure 2(b) is substantially reduced in experimental v_1 cross-sections due to rf inhomogeneity which broadens the ¹H CSA lineshape. Omitting rf inhomogeneity from the simulations used to extract the ¹H shift parameters reduces the quality of the fit and results in the overestimation of η .

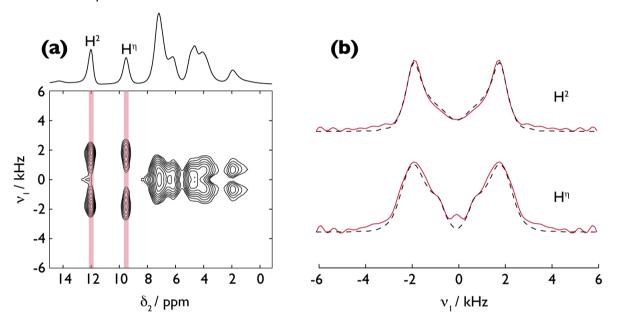


Figure 3. (a) shows a 1 H anisotropic-isotropic correlation spectrum of tyrosine.HCl recorded at a Larmor frequency of 850.13 MHz. The MAS rate was 58.6 kHz, so that the R16 ${}^{2}_{3}$ recoupling sequence required a 1 H rf amplitude of 156.3 kHz, corresponding to a π pulse duration of 3.2 μs. There were 48 t_{1} increments with data points sampled every 12 R elements, resulting in a dwell time in the indirect dimension of 38.4 μs. In t_{2} 2048 complex points were acquired with a spectral width of 150 kHz. Saturation was achieved using a train of 200 π /2 pulses separated by intervals of 10 ms with a recovery delay of 4 s. 1 H chemical shifts were referenced to Me₄Si, and the assignments of the 1 H sites are taken from Ref. [23] using the labelling scheme from Ref. [24]. (b) shows (red lines) cross-sections parallel to v_{1} taken at v_{2} frequencies corresponding to the isotropic 1 H shifts of the hydrogen-bonded OH protons H² and H³, along with SIMPSON simulations (dashed lines) for the best-fit chemical shift parameters.

As a further test Figure 4(a) shows a ¹H anisotropic-isotropic correlation spectrum of anhydrous citric acid recorded at a lower Larmor frequency of 600.13 MHz and a MAS rate of 62.5 kHz. Other experimental parameters are given in the caption. The ultrafast MAS ¹H spectrum (top) exhibits four well-resolved peaks which have been partially assigned in Ref. [12] by comparison with the single-crystal X-ray structure [25]. Figure 4(b) shows (red lines) cross-sections parallel to ν_1 taken at ν_2 frequencies corresponding to the isotropic ¹H shifts of the four hydrogen-bonded sites. These are compared with SIMPSON simulations (dashed lines) for the best-fit ζ and η parameters. The results of the fits are given in Table 1, and the error surfaces are shown in the Supplementary Information (Figure S3). There is generally good agreement with the ζ values measured by Brouwer and Ripmeester at higher B₀ field and lower MAS rate [12]. Ultrafast MAS causes sample heating which might cause partial averaging of the ¹H CSA, but there is no systematic difference between the values obtained at different MAS rates which would suggest this is a problem here. Finally, the effect of rf inhomogeneity results in a fairly significant uncertainty for η , but once again this is comparable to that obtained at lower MAS rates.

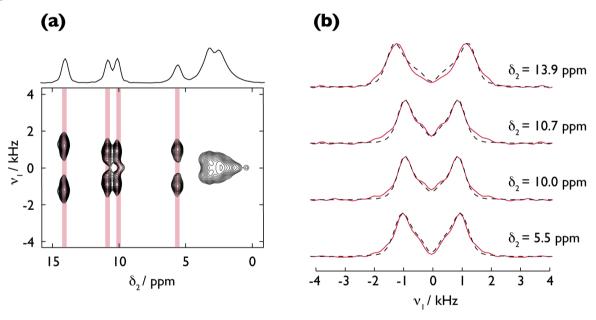


Figure 4. (a) shows a 1 H anisotropic-isotropic correlation spectrum of anhydrous citric acid recorded at a Larmor frequency of 600.13 MHz. The MAS rate was 62.5 kHz, so that the R16 $_{3}^{2}$ recoupling sequence required a 1 H rf amplitude of 166.6 kHz, corresponding to a π pulse duration of 3.0 μs and a dwell time in t $_{1}$ of 36.0 μs. Other parameters were identical to those given in the caption to Figure 3, except that the recovery delay was 120 s. (b) shows (red lines) cross-sections parallel to v_{1} taken at v_{2} frequencies corresponding to the isotropic 1 H shifts of the hydrogen-bonded OH protons, along with SIMPSON simulations (dashed lines) for the best-fit chemical shift parameters.

Table 1. Values of ¹H chemical shift parameters (with 95% confidence limits) measured in this work from fitting to simulated spectra as described in the text.

| Site | δ_{iso} | ۲ | η |
|--------------------------|----------------|-------------------|----------------|
| Tyrosine.HCla | | | |
| H^2 | 12.0 | 17.5 (17.3, 17.7) | 0.0 (0.0, 0.1) |
| H $^{\eta}$ | 9.6 | 18.5 (18.0, 19.0) | 0.5 (0.4, 0.7) |
| Citric acid ^b | | | |
| H ⁵ | 13.9 | 16.9 (16.5, 17.3) | 0.3 (0.0, 0.5) |
| Н6,7 с | 10.7 | 12.5 (12.2, 12.8) | 0.3 (0.0, 0.4) |
| H ^{6,7} c | 10.0 | 12.5 (12.2, 13.8) | 0.2 (0.0, 0.4) |
| H^8 | 5.5 | 13.6 (13.5, 14.2) | 0.4 (0.0, 0.7) |

- a. ¹H sites labelled according to Ref. [24]
- b. ¹H sites labelled according to Ref. [25]
- c. sites H⁶ and H⁷ cannot be assigned.

Conclusion

A new ¹H anisotropic-isotropic shift correlation experiment has been described which operates with ultrafast MAS, resulting in good resolution of isotropic ¹H shifts in the detection dimension, especially in combination with high B_0 fields. A recoupling sequence is required to reintroduce the ¹H CSA in the indirect dimension, but the symmetry numbers must be carefully chosen in order to avoid high rf amplitudes, and the R16²₃ sequence was found to be an appropriate choice for MAS rates over 60 kHz. The new experiment has been used to measure the ¹H shift tensor for all the hydrogen-bonded OH sites in tyrosine.HCl and citric acid. Good agreement was found between the resulting values of ζ and η and those obtained previously. A number of possible improvements to the experiment can be envisioned. The ¹H CSA could be recoupled using a modified version of the ROCSA experiment due to Chan and Tycko which has been used to measure ¹²C shift parameters in uniformly labelled amyloid fibrils [26]. This approach has the advantage that the resulting undistorted ¹H CSA lineshapes allow measurement of the sign of ζ . The effect of B_1 inhomogeneity could be reduced by employing amplitude- or phase-modulated R elements after the fashion of Nishiyama *et al.* [27] Alternatively, the signal which results from the extremes of the B_1 distribution could be filtered out by extending the duration of the $\pi/2$ magnetization transfer pulse, as described in a different context by Lu *et al.* [28] These modifications are currently under investigation in our laboratory.

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