

Improved melting of latent heat storage via porous medium and uniform Joule heat generation

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Abstract

To enhance the rate of heat transfer in phase change materials (PCM), high conductivity porous materials have been widely used recently as a promising method. This study introduces a novel approach for improving melting of PCM by incorporating uniform Joule heat generation with the porous structure compared to central heat generation. Different cases based on the heater-in foam configuration under the same heat generation rate are numerically verified and compared with the case of using the central heating element, which the heat transfer in the domain enhances by the porous medium. The effects of pore density and rate of heat generation are explored using the thermal non-equilibrium model to better deal with the interstitial heat transfer between the internal heat-generated-in-foam and the PCM. For the case with the central heating element, the effects of heater dimensions as well as the rate of heat generation are also investigated. The results show that the uniform heat generation from the porous structure can

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24 substantially reduce the melting time. Applying 100 kW/m^3 for the rate of heat generation
 25 reduces the melting time by 21% compared with the best case of the localised heater.
 26 Meanwhile, applying higher pore-density foam does not bring any significant effect due to the
 27 uniform distribution of the heat generation. The results also show a small effect of localized
 28 heater size on the melting time with the same rate of heat generation density from the porous
 29 structure. However, for an identical volumetric heat source power of the localised heater, the
 30 rate of heat generation per volume is more effective compared with the heating element size
 31 due to the presence of the porous medium.

32 **Keywords:** Internal heat generation; Joule heating; Latent heat storage; Porous medium;
 33 Central heating element; Thermal non-equilibrium model.

34

Nomenclature

A_m	Mushy zone	t_m	Charging/Discharging time (s)
C	Inertial coefficient	T	Temperature (K)
C_p	PCM Specific heat (J/kg.K)	V	Velocity (m/s)
g	Gravity acceleration (m/s^2)	Greek symbols	
h_{sf}	Local heat transfer coefficient ($\text{W/m}^2.\text{K}$)	β	Expansion coefficient (1/K)
k_f	PCM thermal conductivity (W/m.K)		
k_{fe}	Effective thermal conductivity of PCM (W/m.K)		
k_s	solid porous medium thermal conductivity (W/m.K)	ε	Porosity
k_{se}	Effective thermal conductivity of porous medium (W/m.K)	λ	PCM Liquid fraction
K	Permeability (m^2)	μ	PCM Dynamic viscosity (kg/ms)
L	Fusion Latent heat of PCM (J/kg)	ρ	PCM Density (kg/m^3)
\dot{Q}	Heat generation rate (W/m^3)	ΔH	Latent heat (J/kg)
P	Pressure (Pa)	ΔP	Pressure drop (Pa)

35

36 1. Introduction

37 Globally, fossil fuel still provides about 80 % of the world's energy demand [1]. However,
 38 there are considerable release of greenhouse gases and pollutants (i.e.: CO, CO₂ and SO₂) to

39 the environment due to fossil fuel usages results in global warming and environmental pollution
40 [2]. Furthermore, high waste of energy in the form of heat due to the low efficiency arising
41 from thermodynamic limits and mishandlings is another disadvantage [3]. In this regard,
42 energy storage is a solution because of their ability to correct the gap between the energy
43 supplied and the energy demand, especially for intermittent energy sources such as solar and
44 wind [4, 5].

45 Many materials are available for use in thermal energy storage systems. However, the selection
46 of suitable material is very much dependent on the specific operating temperature range, the
47 stability of the material for long operation, and the target storage capacity of the system in use
48 [6]. Phase-change materials (PCMs) are one of the most widely used group due to their
49 attractive thermal energy-storage characteristics. They own high energy storage-to-mass ratio
50 as large amounts of latent heat could be stored or released during their solid-liquid phase
51 transitions within almost constant-temperature operating conditions [7-10]. PCMs have been
52 used in different applications including construction, energy recovery, solar energy storage,
53 electronic cooling and domestic buildings [11-13]. Due to the low thermal conductivity of most
54 PCM materials, some investigations have investigated the thermo-physical properties of PCMs
55 [14, 15]; others were interested in improving the efficiency of the related heat exchangers [16-
56 19]. The effort in improving the heat-transfer performance of PCM-based storage systems is
57 seen increasingly advances in recent years. Sadeghi et al. [20] numerically investigated multi-
58 layer PCMs in a circular heat exchanger with periodic thermal boundary conditions. They
59 found that for the single-layer unit, using a PCM with high latent heat capacity leads to
60 fluctuating average temperature with low amplitude. Likewise, they found that the multi-layers
61 system in storing latent energy is more applicable. Ghalambaz et al. [21] studied the thermal
62 flow and performance of Nano-Encapsulated Phase Change Materials (NEPCMs) in a cavity.
63 They found that the thermal improvement is extremely based on the non-dimensional fusion

64 temperature, and the relative improvement is 10% compared to the base-fluid. Chamkha et al.
65 [22] Studied the charging process of a nano PCM in a square cavity with a warm cylinder
66 placed in the centre of the cavity with the existence of both single and hybrid nanoparticles.
67 They stated that the solid-liquid interface and the charging rate are mainly influenced by the
68 nanoparticles loading and the thermal conductivity. Moreover, they found that the charging
69 rate is greater when the Fourier number vary between 0 and 0.5.

70 Metal foams are one of the superlative techniques in the field of heat transfer enhancement in
71 PCM-based systems [23-27]. Mahdi and Nsofor [9] studied numerically the potential for heat-
72 transfer rate enhancement in PCM-based shell-and-tube storage component using multi-
73 segment metal foam. They suggested that cascading the pore density in the heat flow direction
74 provides better uniform temperature distribution. Zhu et al. [28] studied the performance of a
75 storage system with CH_3COONa PCM using various porosities of metal foam and metal fins.
76 It was found that the combination accelerates the melting rate and improves PCM storage
77 performance. Zhang et al. [29] studied the behaviour of the PCM experimentally and
78 numerically. They stated that the composite of paraffin-copper foam improves heat transfer
79 over paraffin wax only due to the high thermal conductivity of the metal foam. Using the metal
80 foam also produces uniform temperature distribution. The numerical model of Zhao et al. [30]
81 improved the efficiency of a high-temperature energy storage system (LHTES) using graphite
82 foam. Using graphite foam reduces the required surface area of heat transfer in the system.
83 Krishnan et al. [31] numerically performed a two-temperature model to assess the efficiency
84 of combining porous medium-PCM using the Darcy-Brinkman equation to study the porous
85 medium effect.

86 Different heating modes have been used to charge the PCM and store thermal energy which is
87 selected based on the type of application, available source of energy, required charging time
88 and capacity, the melting point of the employed PCM, etc [32]. Different methods have been

89 used to charge the PCMs such as heating element, hot fluid flow, heat pipes, heat pumps and
90 renewable energies [33-35]. Moreno et al. [36] experimentally studied on the use of heat pump
91 integrated with a cold TES tank for space cooling application. They compared the use of PCM
92 with water as the storage material and showed that 14.5% higher capacity of PCM which
93 maintain the indoor temperature 20.65% longer. However, the charging time for the PCM is
94 4.55 times higher than water. As a heat storage heater for domestic space heating, Talebizadeh
95 Sardari et al. [37, 38] studied the effects of metal foam added to the PCM in a composite porous
96 / PCM to air heat exchanger compared with the PCM-only unit when the PCM was charged by
97 an electrical heating element. They showed the significant advantages of high conductivity
98 porous medium and presented that a uniform output temperature can be gained using a heat
99 transfer enhancement technique by the presence of metal foam inside the PCM. Mettawee and
100 Assassa [39] investigated experimentally the thermal performance of a compact PCM solar
101 collector. Solar energy was stored in the PCM which was then discharged by cold water. They
102 showed a higher rate of heat transfer for a higher thickness of the PCM layer due to the higher
103 effect of natural convection in the domain as the main parameter in spreading the heat in all the
104 domain. Sardari et al. [3] presented a study on heat recovery form domestic radiators using
105 compact PCM unit when the PCM is charged by the hot surface of the radiator. The system was
106 designed to store the excess energy of the radiator for the usage in peak hours.

107 Heat generation in phase-change materials finds a wide range of applications such as thermal
108 control of electronic components, freezing of biological tissues, and solar thermal energy
109 storage systems. However, few studies have investigated the phase change process inside
110 practical systems with a heat source that is embedded in the PCM [40-42]. Bechiri and
111 Mansouri [43] analytically studied the volumetric heat generation influences on charging and
112 discharging heat transfer of nano-enhanced PCM inside a horizontal cylindrical enclosure.
113 They found that the storage efficiencies are higher and lower than 1 for positive and negative

114 heat generation, respectively, and the heat generation influence reduces as liquid fraction
115 increases. Jiji and Gaye [40] analytically analysed charging and discharging heat transfer in a
116 PCM with volumetric energy generation by using a one-dimensional quasi-steady
117 approximation. They developed simple correlations to estimate solidification and melting times
118 based on the heat generation parameter. They presented that the enhanced quasi-steady model
119 is valid for small Stefan numbers.

120 Even though extensive research has been carried out investigating the role of porous foam on
121 improving the functionality of PCMs as storage materials, no previous study adequately
122 investigates the applicability of internal heat-generated porous foam for an improved thermal
123 response of PCM-based latent-heat storage systems. Therefore, the aim of the present work is
124 to fill this gap by numerically investigating the effect of internal uniform heat generation from
125 the porous foam structure during the charging mode of a PCM-in-metal foam latent-heat
126 storage LHS unit. A rectangular container is considered for the heat storage material with the
127 porous medium subjected to Joule heating for uniform internal heat generation. Charging time,
128 heat transfer rate and average temperature are calculated and compared in different cases based
129 on the pore size and the rate of heat generation. Two approaches for internal heat generation
130 are considered. In the first approach, the heat is being uniformly generated inside the domain
131 which can be done by Joule heating of the porous medium and homogeneously propagates to
132 the PCM. The second approach is that the heat is generated from a localized heater in the centre
133 of the system, which is also rarely discussed in the literature. The presence of high conductivity
134 porous medium is commonly used to improve the heat transfer rate in the domain which
135 extremely enhances the heat diffusion inside the domain; however, the opportunity to achieve
136 an efficient thermal energy storage device must rise.

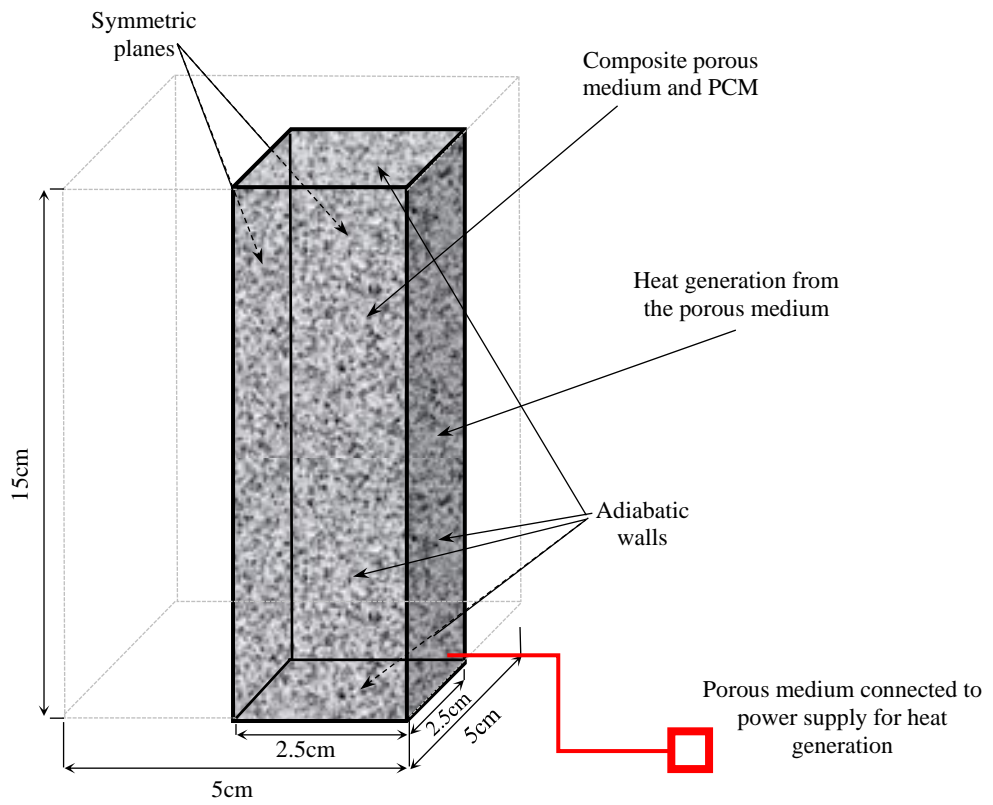
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138 **2. Problem description:**

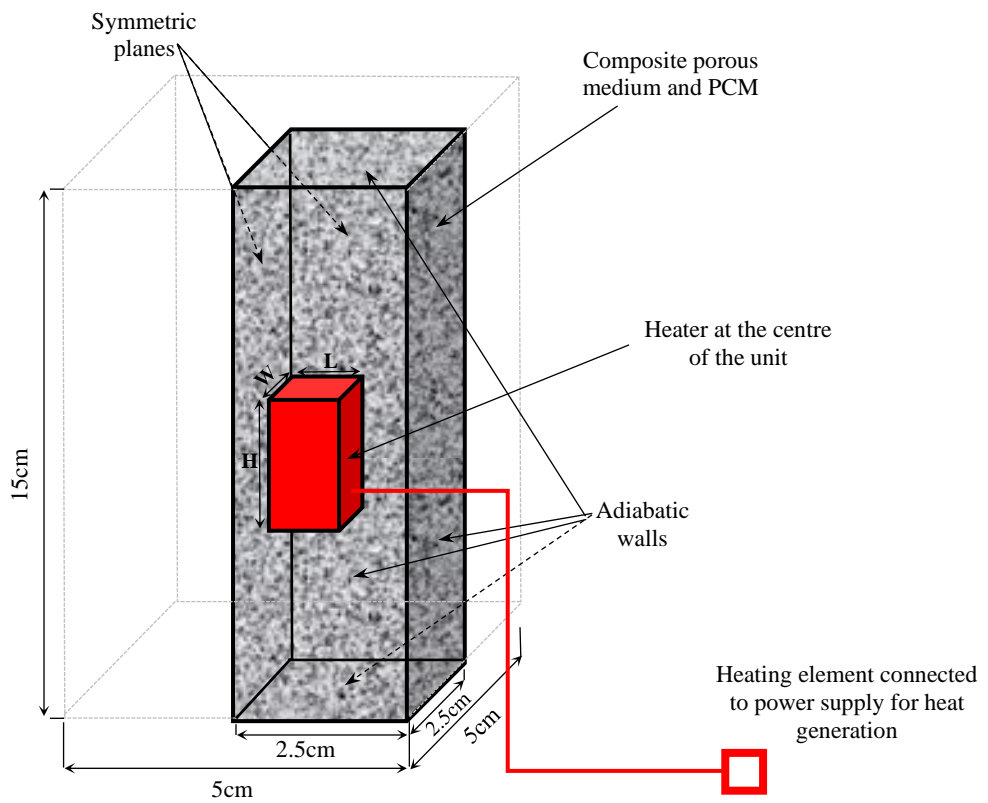
139 The core of this study is to propose well-performing heater-in-foam latent heat storage (LHS)
140 system by employing the porous structure with volumetric heat generation for superior
141 performance during the energy charging mode. The aim of applying Joule heating is to generate
142 uniform internal heat generation inside the PCM/porous medium composite. This novel method
143 is performed by passing a current through an electrical porous conductor to generate thermal
144 energy. Carbon foam is such a kind of material which can generate heat by Joule heating in
145 addition to the advantage of high thermal conductivity. Therefore, in one hand, due to the
146 presence of the porous medium, the problem of low thermal conductivity of the PCMs is solved
147 and in the other hand, due to the existence of porous medium uniformly in the domain, the heat
148 is generated uniformly and so there is no need to employ many heating elements inside the
149 domain.

150 Similar to the regular electrical heating elements, the heat is generated by passing an electric
151 current through a conductor known as Joule heating. The conductor is considered a porous
152 medium in this study. Therefore, by connecting the porous medium to the electricity, the matrix
153 can generate heat directly. In this study, the volumetric heat generation from the porous
154 structure is studied compared with a localised heater at the centre of the unit. Note that the
155 porosity of porous material is considered 95% in this study. Therefore, for the volumetric heat
156 generation from the porous medium, the volumetric heat generation is 5% of the realistic wire
157 volumetric heating rate in the energy equation.

158 The unit is a rectangular cube with the dimensions of 5cm×5cm×15cm filled with PCM
159 embedded in a porous medium. Two walls are considered symmetry (one-quarter of the domain
160 is solved numerically) and the other walls are considered insulated (shown in Fig. 1-a as Case
161 0 with heat generation from the matrix).



a)



b)

Fig. 1. The schematic of the studied geometry a) with porous heat generation and b) with a central heating element.

162

163 For the second studied geometry, a rectangular solid cubic heater is located at the centre of the
164 unit. The volume of the heater is calculated based on the total volume of the porous medium
165 related to the rate of heat generation to have a meaningful comparison. In other words, the
166 volume of the porous medium in the first case is calculated and then the volume of the heater
167 is chosen equal to the volume of the porous medium in the first case. Fig. 1-b shows a schematic
168 of the LHS unit with a localised heating element, and Table 1 presents the dimensions and rates
169 of heat generation of the alternative proposed systems. The dimensions of the heating element
170 in Table 1 is determined as follows: according to the dimensions of the unit, the volume of the
171 porous medium in case 0 is $(15\text{cm}\times 2.5\text{cm}\times 2.5\text{cm}\times 0.05)$ 4.6875 cm^3 for a quarter of the storage
172 unit. 0.05 denotes to the ratio of solid ligament within the porous medium. Therefore, for the
173 central heating element with the height of 2.5 cm named as case 1, the width (W) of the heating
174 element is 1.369cm which is considered equal to the length (L) of the element. The dimensions
175 of the heating elements for the other cases are determined with a similar procedure. Note that
176 in the case of central heater, the PCM domain is also filled with porous medium and the mass
177 of PCM is similar in all the studied cases to have similar storage capacity. Note that in the
178 localised heater cases, the surrounding PCM is embedded in a porous medium; however, the
179 heat is generated only from the central heating element. In Fig. 1-b, only one-quarter of the
180 heater is displayed, and symmetric boundary conditions are used for two surfaces similar to the
181 whole domain. Moreover, the amount of PCM in all the studied cases is constant to have a
182 similar storage capacity in all the proposed cases to have a meaningful comparison.

183 Note that, as presented in Table 1, Cases 1, 2 and 3 have the same heater volume equal to the
184 volume of the porous medium case which has a similar rate of heat generation. For Cases 4 and

185 5, the volumes of the heating elements are changed based on the rate of heat generation. Cases
 186 4 and 5 are compared with Case 2 with a similar width and length but different heights when
 187 the total heat generated by the heating element (volume \times heat generation rate) is constant.

188

Table 1 The characteristics of the proposed system with a centred heater

	H (cm)	W=L (cm)	Heat generation rate (kW/m ³)
Case 1	2.5	1.369	100
Case 2	5	0.968	100
Case 3	10	0.685	100
Case 4	2.5	0.968	200
Case 5	10	0.968	50

189

190 RT-35 (RUBITHERM) is considered as the PCM with the physical properties presented in
 191 Table 2.

192

Table 2 The properties of RT 35 [44].

Property	RT35
Liquidus/Solidus temperature (°C)	309/302
Latent heat of fusion (kJ/kg)	170
Specific heat (kJ/kgK)	2
Expansion coefficient (1/K)	0.001
Thermal Conductivity (W/mK)	0.2
Viscosity (Pas)	0.023
Density (kg/m ³)	815

193

194 Note that the initial temperature of the PCM is considered equal to 292K.

195

196

197 **3. Mathematical description**

198 During the PCM phase-transition, heat is typically transferred by conduction only when the
 199 PCM is in the solid phase. However, as the melting of PCM starts to develop, the liquid part of
 200 PCM gets larger leading to the appearance of natural convection as an additional heat transfer
 201 mechanism [21]. The presence of porous medium here could help more heat to be transferred
 202 to the PCM by conduction rather by convection due to the high flow-resistant effect of the
 203 porous foam structure [45]. Thermal non-equilibrium model is employed to model the effect
 204 of the foam structure inside the PCM with the aid of an enthalpy-porosity method to model the
 205 phase-change phenomenon [46].

$$\frac{\partial \rho}{\partial t} + \nabla \cdot \rho \vec{V} = 0 \quad (1)$$

$$\frac{\rho}{\varepsilon} \frac{\partial \vec{V}}{\partial t} + \frac{\rho}{\varepsilon^2} (\vec{V} \cdot \nabla) \vec{V} = -\nabla P + \frac{\mu}{\varepsilon} (\nabla^2 \vec{V}) - \rho_{ref} \beta \varepsilon (T - T_{ref}) \vec{g} - \vec{S} - \vec{F} \quad (2)$$

For the PCM

$$\frac{\partial \varepsilon \rho_f C_{p,f} T}{\partial t} + \nabla (\rho_f C_{p,f} \vec{V} T) = \nabla (k_{fe} \nabla T) - S_L - h_{sf} A_{sf} (T_f - T_s) \quad (3)$$

For the porous medium:

$$(1 - \varepsilon) \rho_s C_{p,s} \left(\frac{\partial T_s}{\partial t} \right) = \nabla (k_{se} \nabla T_f) - h_{sf} A_{sf} (T_s - T_f) - S_g \quad (4)$$

206 In the momentum equation, to consider the effect of natural convention and buoyant flow, the
 207 Boussinesq approximation is employed. Furthermore, in Eq. (4), for the case of heat generation
 208 of the porous medium, a source term is added to the energy equation related to the heat
 209 generated from the porous structure which is considered 100 kW/m³. In the case of heat
 210 generation from the heating element, the heat is generated from the volume of heating elements
 211 in a separate solid zone.

212 k_{fe} and k_{se} should be calculated for the PCM and porous medium separately which are
 213 calculated based on effective thermal conductivity as follows [46, 47]:

$$k_{eff} = \frac{1}{\sqrt{2}(R_A + R_B + R_C + R_D)} \quad (5)$$

214 where

$$R_A = \frac{4\sigma}{(2e^2 + \pi\sigma(1-e))k_s + (4 - 2e^2 - \pi\sigma(1-e))k_f} \quad (6)$$

$$R_B = \frac{(e - 2\sigma)^2}{(e - 2\sigma)e^2k_s + (2e - 4\sigma - (e - 2\sigma)e^2)k_f} \quad (7)$$

$$R_C = \frac{\sqrt{2} - 2e}{\sqrt{2}\pi\sigma^2k_s + (2 - \sqrt{2}\pi\sigma^2)k_f} \quad (8)$$

$$R_D = \frac{2e}{e^2k_s + (4 - e^2)k_f} \quad (9)$$

215 where $e = 0.16$ and

$$\sigma = \sqrt{\frac{\sqrt{2}(2 - \left(\frac{3\sqrt{2}}{4}\right)e^3 - 2\varepsilon)}{\pi(3 - 2\sqrt{2}e - e)}} \quad (10)$$

216 and

$$k_{fe} = k_{eff}|_{k_s=0} \quad (11)$$

$$k_{se} = k_{eff}|_{k_f=0} \quad (12)$$

217 The source term in the momentum equation is given as [48]:

$$\vec{S} = A_m \frac{(1 - \lambda)^2}{\lambda^3 + 0.001} \vec{V} \quad (13)$$

218 where A_m is 10^5 [49-51]. Additionally, λ is defined as [52]:

$$\lambda = \frac{\Delta H}{L} = \left\{ \begin{array}{ll} 0 & \text{if } T < T_{Solidus} \\ 1 & \text{if } T > T_{Liquidus} \\ \frac{T - T_{Solidus}}{T_{Liquidus} - T_{Solidus}} & \text{if } T_{Solidus} < T < T_{Liquidus} \end{array} \right\} \quad (14)$$

219 where ΔH varies between zero for the solid-state and L for the liquid state.

220 The body force in the momentum equation is defined as:

$$\vec{F} = \left(\frac{\mu}{K} + \frac{\rho C |\vec{V}|}{\sqrt{K}} \right) \vec{V} \quad (15)$$

221 In this equation, K is the permeability given as [53]:

$$K = 0.00073 d_p^2 (1 - \varepsilon)^{-0.224} \left(\frac{d_l}{d_p} \right)^{-1.11} \quad (16)$$

222 and C is the inertial coefficient given as [53]:

$$C = 0.00212 (1 - \varepsilon)^{-0.132} \left(\frac{d_l}{d_p} \right)^{-1.63} \quad (17)$$

223 where d_l is the ligament or cell diameter is given as:

$$d_l = 1.18 d_p \sqrt{\frac{1 - \varepsilon}{3\pi} \left(\frac{1}{1 - e^{-(1-\varepsilon)/0.04}} \right)} \quad (18)$$

224 d_p is the pore size given as:

$$d_p = 0.0254 (m) / \omega \quad (19)$$

225 Note that ω is the pore density with the unit of PPI means pores per inch.

226 In Eq. (3), S_L is given as [4]:

$$S_L = \frac{\partial \varepsilon \rho \lambda L}{\partial t} + \nabla (\rho \vec{V} \lambda L) \quad (20)$$

227 To calculate the local heat transfer between the porous medium and PCM, the porous structure

228 is usually considered as cylinders and the laminar flow of liquid PCM in porous structure is

229 considered similar to the flow around a cylinder [54]. Therefore, the interstitial heat transfer

230 coefficient is calculated, for the appropriate range of Reynolds number, as [37, 44]:

$$h_{sf} = 0.76 Re_d^{0.4} Pr^{0.37} k_f / d_l \quad \text{for} \quad 0 < Re_d \leq 40 \quad (21)$$

231 where

$$Re_d = \rho_{pcm} \left(\sqrt{\sum_{i=1}^3 u_i^2} \right) d_l / (\varepsilon \mu_f) \quad (22)$$

232 and A_{sf} is the specific surface area of the porous medium given as:

$$A_{sf} = \frac{3\pi d_l(1 - e^{-(1-\varepsilon)/0.04})}{0.59d_p^2} \quad (23)$$

233 Note that before the PCM starts to melt, there is no convection heat transfer inside the pores. It
234 can be found in Eq. (21) when h_{sf} is zero since Re_d is zero based on Eq. (22).

235

236 4. Numerical process and code verification

237 The equations governed on the problem are solved using ANSYS-FLUENT utilizing a UDF
238 (User-defined functions) to determine h_{sf} . A detailed discretion of the numerical process is
239 discussed in Ref. [46, 47]. For mesh analysis, different cases are studied considering a higher
240 mesh density in y-direction due to the presence of gravity as well as an equal number of nodes
241 for both x and z-directions. Table 3 presents the melting time for both cases of internal heat
242 generation from the porous medium and localised heater (Case 1 in Table 1) for the heat
243 generation rate of 100 kW/m³. The porosity and pore density of the porous medium are
244 considered 95% and 30 PPI, respectively. The results show that after the number of 37,500
245 nodes (60×25×25), there is no considerable variation in the results. As presented, the difference
246 between the melting times for different cell numbers for the case of heat generation from the
247 porous medium is negligible due to the uniform heat generation distribution in the domain.

248

Table 3 Mesh independence analysis for different number of cells

	Heat generation from the porous medium	Localised heat generation from the heating element
Number of cells	Melting time (min)	
25000	836.3	1004.2
37500	837.5	1015.4
50000	837.7	1016.3

249

250

251 The size of the time step is 0.5 s and there is no variation seen by reducing the time step size
252 down to 0.25 s. The schematic of the entire computational mesh, as well as the front and top
253 views, is shown in Fig. 2.

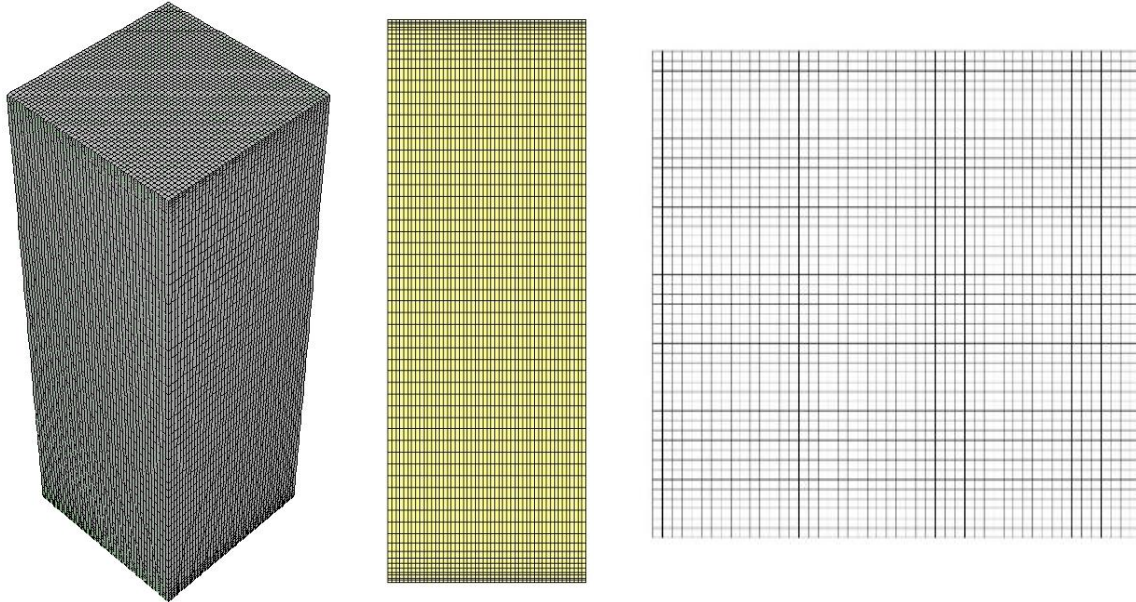


Fig. 2. The computational domain at different views.

254 To verify the method, a rectangle heat storage unit with the dimensions of 200×120×25 mm is
255 modelled which is studied experimentally by Zhao et al. [8, 55] and numerically using the
256 thermal non-equilibrium model by Liu et al. [56]. The LHS unit includes a combination of
257 PCM (RT-58) with metal foam with 95% porosity and 10 PPI pore density considering a heat
258 flux boundary condition of 1600 W/m² for the bottom surface and convection for the other
259 boundaries. The temperature located at the centre at the height of 8mm is presented in Fig. 3
260 shows an excellent agreement with both numerical and experimental analysis. The maximum
261 differences between the present work and the work of Liu et al. [56] and Zhao et al. [8] are 6%
262 and 3%, respectively.

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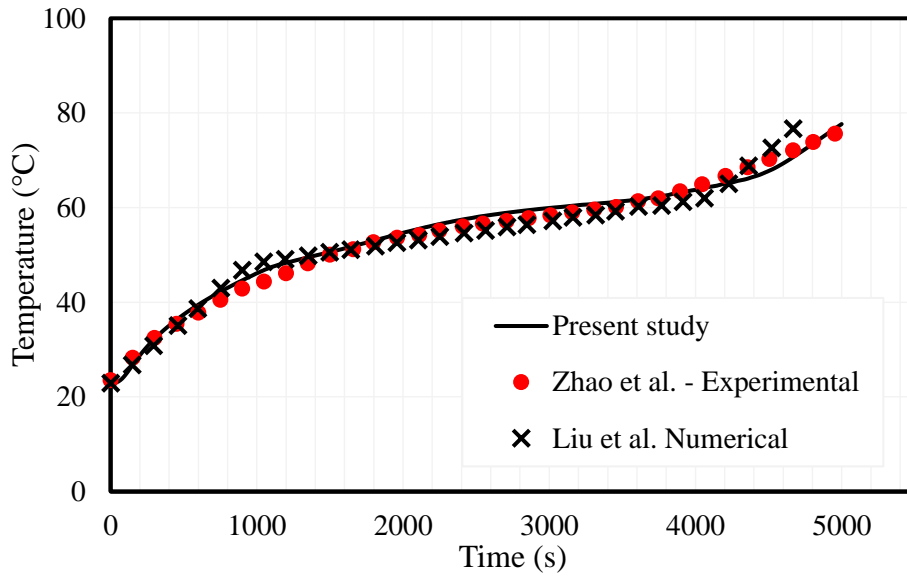


Fig. 3. The validation study of a rectangular MFLHS system compared with experimental data of Zhao et al. [55] and numerical study of Liu et al [56]

264

265 **5. Results and discussion**

266 In this section, the internal heat generation from the porous structure is firstly discussed, then
 267 the results of a localised heater are analysed after studying the effective parameters.

268

269 *5.1. Heat generation from the porous structure*

270 By volumetric heat generation from the porous medium, the temperature and liquid fraction
 271 field distribution are uniform and in an identical time, all the field has an almost constant
 272 temperature and liquid fraction. Fig. 4 displays the variation of PCM mean temperature and
 273 liquid fraction as well as the mean temperature of the porous medium in terms of time for the
 274 PCM-in- foam LHS unit. Note that the porosity and pore density is selected equal to 95% and
 275 30 PPI, respectively, with the heat generation rate of 100 kW/m³. When the temperature rises
 276 from 302K, the melting process starts after almost 115 minutes. At the time of 837.5 minutes,
 277 when the temperature is almost 309, the liquid fraction reaches to one and the PCM melts

278 completely. During the phase change, the PCM temperature rises with a low rate due to placing
 279 PCM in the latent heat section after the beginning sharp increase. The temperature of the porous
 280 medium is virtually equal to the PCM since the foam generates heat directly and the number
 281 of pores is high (30 PPI). A negligible temperature difference exists between the PCM and
 282 porous temperatures. The reason is due to the uniform heat generation in the domain which
 283 lessens the difference between the temperature of PCM and porous medium. As shown in Fig.
 284 1, the heat is generated uniformly in the entire domain from the surface of the pores in the
 285 porous medium and due to the small volume of the pores, the temperatures of the PCM and
 286 porous medium are almost the same. It should be noted that due to the uniform distribution of
 287 liquid fraction and temperature, the contour plots are uniform and at an identical time, all the
 288 domain has an almost constant liquid fraction and temperature due to the uniform heat
 289 generation inside the domain.
 290

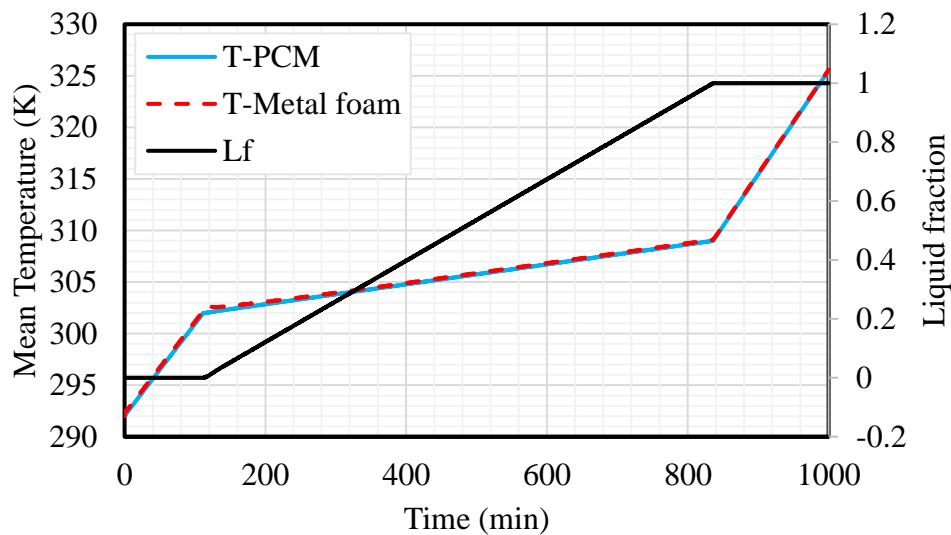


Fig. 4. The variation of PCM mean temperature and liquid fraction as well as porous temperature for the LHS unit with $\epsilon=0.95\%$, $\omega=30\text{PPI}$ and $\dot{q}=100\text{kW/m}^3$

291

292 Fig. 5 illustrates the variation of temperature at three different points with various heights at
 293 the centre of the system. As shown, the temperatures at different heights are similar. The main

294 reason is the proposed charging method which is uniform heat generation from the porous
 295 medium in the system. Thus, because of uniform internal heat generation, the temperatures are
 296 almost similar in the domain. Furthermore, due to the presence of high conductivity porous
 297 medium and thus high rate of heat transfer, the temperature is uniform in all the domain.
 298 Consequently, all point has equal temperatures. These are also the reasons for the equilibrium
 299 condition between the PCM and porous medium shown in Fig. 4. After a sharp temperature
 300 enhancement, during the phase change process, the temperature rises to a lower rate and then
 301 increases sharply.
 302

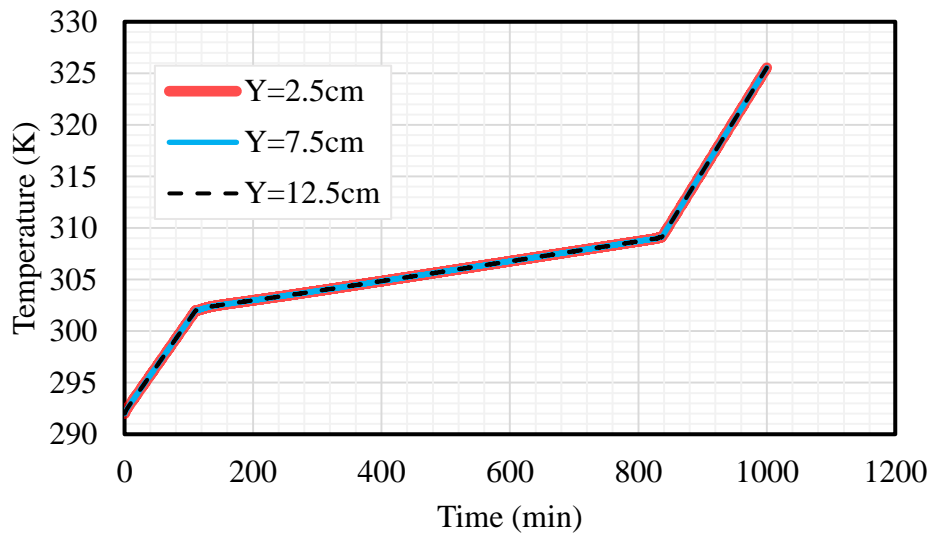


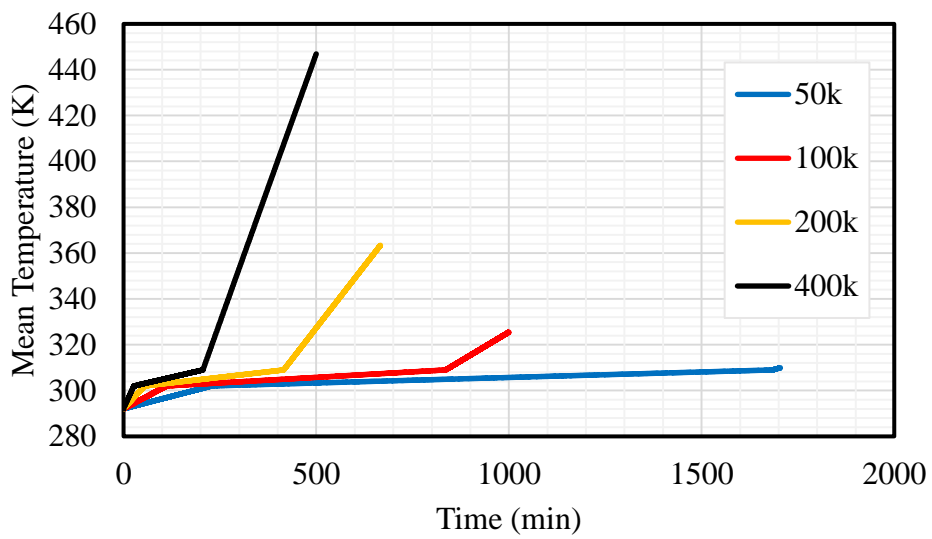
Fig. 5. The variation of PCM temperature at different points for the LHS unit with $\epsilon=0.95\%$,
 $\omega=30\text{PPI}$ and $\dot{q}=100\text{kW/m}^3$

303

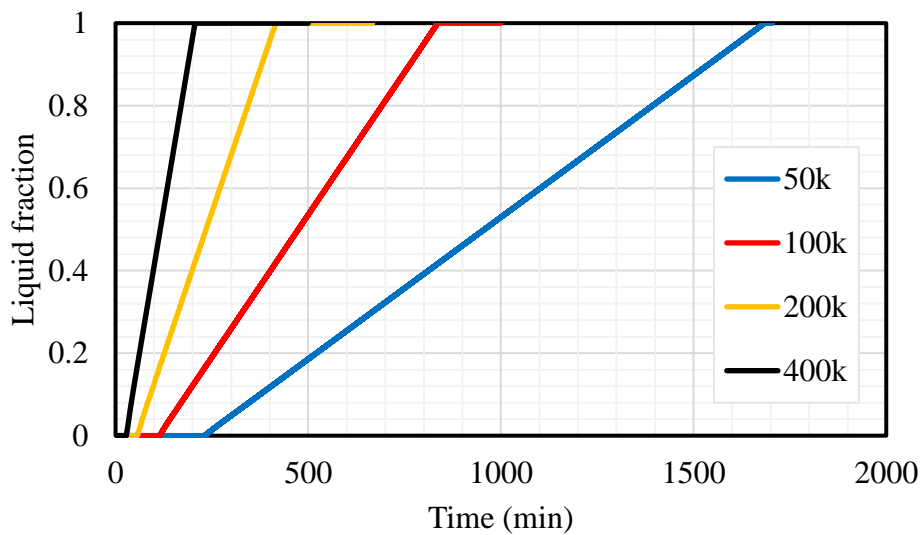
304 5.1.1. Influence of volumetric heat generation rate

305 The influence of the volumetric heat generation rate on the PCM mean temperature and liquid
 306 fraction are illustrated in Figs. 6-a and 6-b, respectively. By applying a higher heat generation
 307 rate, the PCM melts in a shorter time expectedly. During the charging process, the temperature
 308 is almost constant (vary between solidus and liquidus temperatures) and then rises sharply. For
 309 a higher heat generation rate, a higher slope of the temperature rising line is achieved during

310 the phase change. At the time when the PCM melts entirely for the heat generation rate of 200
311 kW/m³, the mean PCM temperature is almost 400 K for the case of 400 kW/m³. Note that since
312 the heat generations are different for various cases, as mentioned, the melting times are also
313 varied, and the simulations are terminated when the PCM melts completely. Therefore, in Fig.
314 6-a, the times of the simulations are varied.
315



a)



b)

Fig. 6. The variation of a) PCM mean temperature and b) liquid fraction Case 0 for different heat generations rates

316

317 Table 4 presents the melting time and the time-saving percentage compared with the heat
 318 generation rate of 100 kW/m³ for different rates of heat generation. By enhancing the rate of
 319 heat generation, the melting time reduces with a constant rate approximately. By doubling the
 320 heat generation rate, the melting time reduces by almost 50%. The reason is due to the uniform
 321 distribution of heat generation inside the domain as a result of a homogeneous porous medium.

322 This is also can be seen in Fig. 6-b. This can be also explained according to the dimensionless

323 numbers of Fourier number $(\frac{\alpha t}{H^2})$ and Stefan number $(\frac{c_p q_w H}{kL})$ and Rayleigh number

324 $(\frac{\rho^2 g \beta c_p q_w H^4}{k^2 \mu})$ where q_w is defined as the heat flux of the heat source. The non-dimensional

325 analysis was performed in the literature for different cases and the results have shown that the
 326 liquid fraction is varied as a function of Fourier, Stefan and Rayleigh numbers [4, 46, 51, 57-

327 60]. Since natural convection is negligible in the existence of metal foam, the Rayleigh number

328 variation does not affect the liquid fraction significantly [46]. In the proposed system in this

329 study, by doubling the heat generation rate and considering all the other parameters constant,

330 Stefan number also doubles results in a lower melting time by almost 50% as presented in

331 Table 4. Note that the liquid fraction and melting time is proportional directly with the Stephan

332 number [4, 46, 51, 57, 60].

333

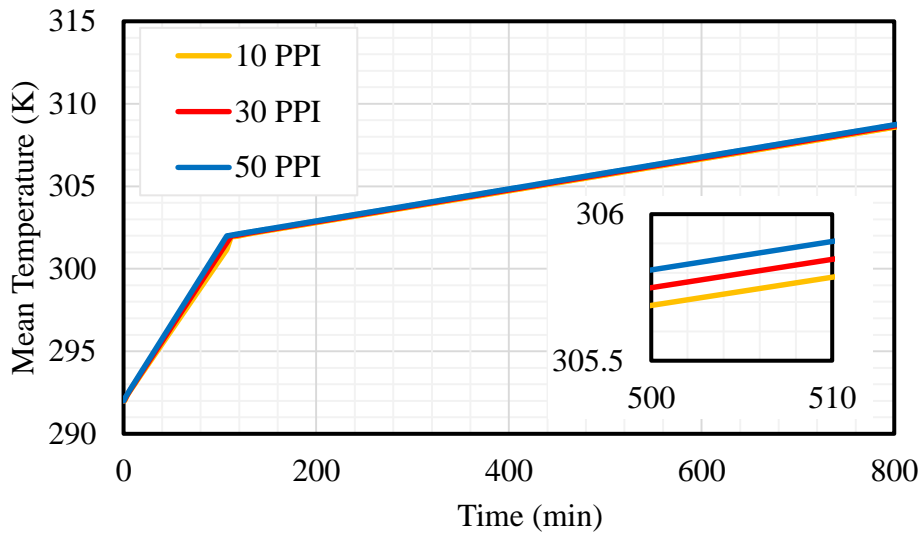
Table 4 The melting time and the time-saving percentage for Case 0 for different heat generation rates compared with the heat generation rate of 100 kW/m³

Heat generation rate (kW/m ³)	Melting time (min)	Timesaving
50	1685.92	-101.30
100	837.50	0.00
200	417.00	50.20

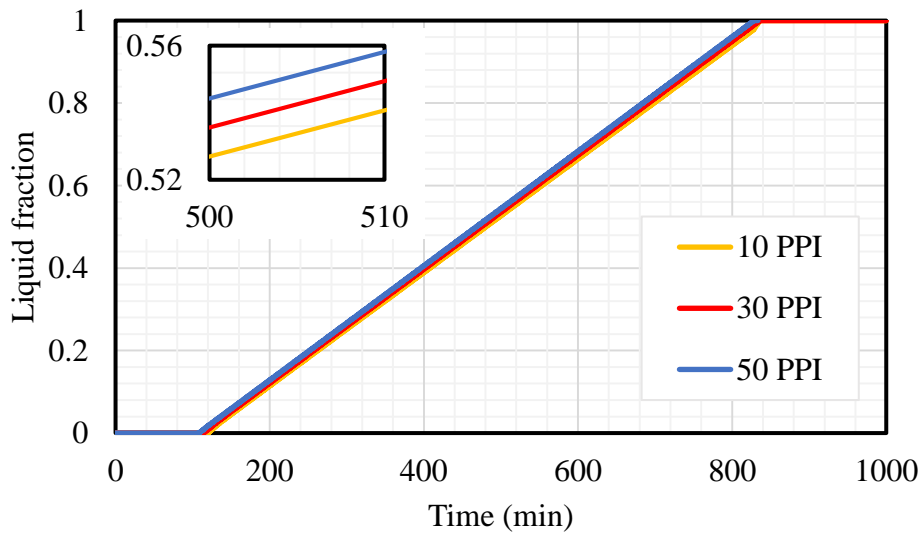
334

335 5.1.2. Effect of pore density

336 Fig. 7 displays the transient effect of pore density on the PCM mean temperature (Fig. 7-a) and
337 the liquid fraction (7-b) for Case 0 with $\dot{Q}=100\text{kW/m}^3$. By changing the pore density of the
338 porous medium, the size of pores changes results in a different inertial coefficient and
339 permeability of the porous medium in the momentum equation. As shown in Fig. 7-a, a
340 negligibly higher temperature is achieved using a higher pore density resulting in a negligibly
341 lower melting time (Fig. 7-b). The larger pore density enhances the solid-liquid interfacial
342 surface area results in a higher effective thermal conductivity. However, increasing the pore
343 density reduces the permeability which results in the lower natural convection effect.
344 Therefore, it is a trade-off process of PCM melting in different pore densities [61]. In the
345 proposed system, the main reason for the negligible effect of pore density is the heat generated
346 from the porous medium for the charging process. Due to the equal amount of uniform heat
347 generation from the porous medium for different pore densities and due to the high effect of
348 heat generation in the proposed system, the effect of pore density is negligible. However, as
349 shown, by using a higher pore density, the distribution of the heat generated in the domain is
350 more uniform helping the melting process.



a)



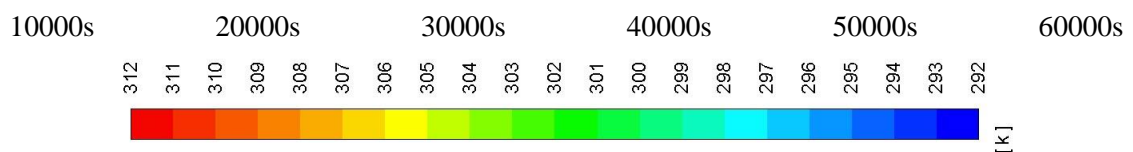
b)

Fig. 7. The variation of a) PCM mean temperature and b) liquid fraction for Case 0 with $\dot{Q}=100\text{kW/m}^3$ for different pore densities

353 *5.2. Heat generation from the localised heater*

354 To show the advantages of the internal heat generation, a PCM-in-metal foam LHS unit with a
 355 heater (the heater was designed as a solid block (without porous medium and PCM) and defined

356 to give a constant heat flux) at the centre with a similar rate of heat generation is simulated. As
 357 mentioned, the dimensions of the heater are selected based on the volume of porous structure
 358 in Case 0. Fig. 8 shows the contour plot of PCM temperature (Fig. 8-a) and the liquid fraction
 359 (Fig. 8-b) at 10000s time intervals for the Case 1 in Table 1 at the middle section of the unit. It
 360 should be noted that in the liquid fraction contours, the liquid fraction is varied between 0 and
 361 1. When the liquid fraction is 1, it means that the PCM is completely in the liquid state and
 362 when it is 0, the PCM is in the solid-state. Between 0 and 1, the PCM is placed in the mushy
 363 zone.
 364 In Fig. 8, the height and length of the heater are 2.5 cm and 1.369 cm, respectively. The heat
 365 transfers out in the domain from the central heating element toward the walls. The temperature
 366 of the heater increases with time and when it reaches the solidus PCM temperature, melting
 367 starts. Due to the presence of metal foam inside the domain, a uniform temperature distribution
 368 can be seen as discussed in [47]. As shown in Fig. 8-b, a higher liquid fraction occurs around
 369 the heater due to the higher temperature of the heater compared with the other parts of the unit;
 370 however, due to the effect of surrounding metal foam, the liquid fraction enhances in all the
 371 domain but with a higher rate around the heater.
 372



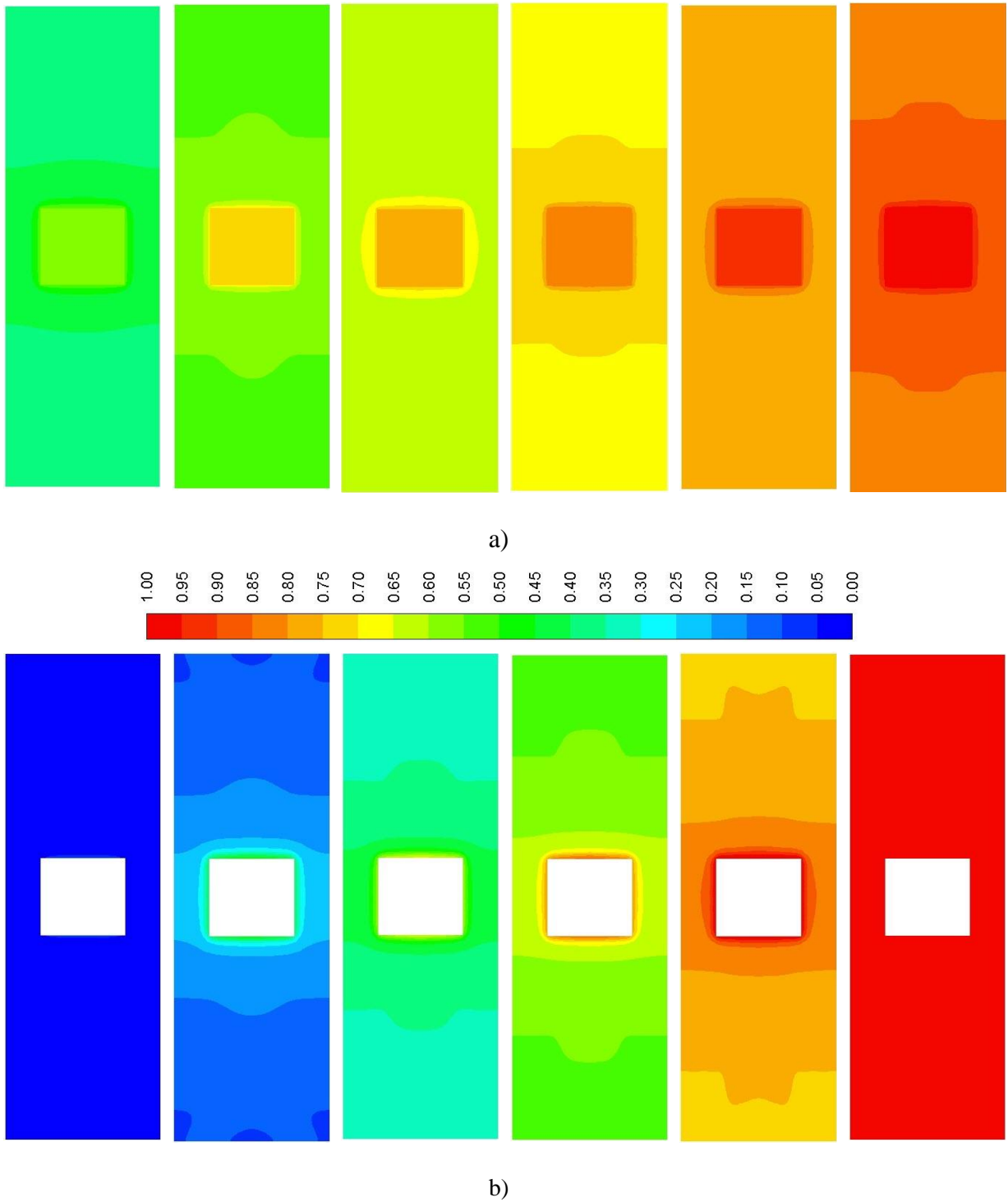


Fig. 8. The distribution of a) temperature and b) liquid fraction at various times for the system using a centred heater with $\varepsilon=0.95\%$, $\omega=30$ PPI and $\dot{Q}=100$ kW/m³

373

374 The total melting time is 1015.4 minutes for Case 1, which is 17.5% higher than that compared

375 with the case of an internal heat generation even with the presence of a high conductivity porous

376 medium. Note that it is expected that by using a higher area of the heat exchanger with constant

377 heat generation rate, the heat is transferred quicker from the heating element to the PCM and
378 therefore it has a high impact on the melting rate. In the case of internal heat generation from
379 the porous medium, a heat source with a higher surface area is employed results in a shorter
380 melting time. Therefore, the novel introduced method of uniform heat generation using Joule
381 heating is proven as a more advantageous method for reducing the charging time compared
382 with using metal foam with a separate heater.

383

384 5.2.1. Influence of heating element dimension at a constant heat generation rate

385 As mentioned in Table 1, for a constant heat generation rate of 100 kW/m^3 , three different sizes
386 for the heating element are studied with the same volume compared with the case of internal
387 heat generation from the porous medium. Fig. 9 shows the effect of the central heating element
388 on the mean temperature of the PCM, respectively. For all units with a central heating element,
389 lower mean temperature of the PCM can be seen compared with the case of Joule heating from
390 the porous medium. For a lower height, a higher mean temperature is achieved results in a
391 lower melting time. The relatively high flow-resistant forces due to the existence of the porous
392 medium largely affect the convective flow of liquid PCM and make the role of natural
393 convection to be almost negligible. Therefore, the reason for the advantage of case 1 over other
394 cases is only related to the dimensions of the unit. It means that due to the effect of the porous
395 medium which results in suppressing the effect of natural convection, conduction is the main
396 mechanism for heat transfer and therefore the direction of the heating element is not important.
397 In other words, it is not important that which edge of the heating element is in the gravity
398 direction. Therefore, the heating element with a more uniform distribution in the domain related
399 to the dimensions of the storage unit can be more effective for heat generation. Therefore, case
400 1, which the heating element is more uniform in all directions according to Table 1, has the
401 best performance higher temperature and a higher melting rate compared with other studied

402 cases with central heating elements. The melting time of case 1 is almost 2% and 3% less than
 403 cases 2 and 3, respectively. It should be noted that although the differences are small but have
 404 an effect on improving the performance of the LHS systems. Furthermore, considering the
 405 studied effect in a larger size of an LHS system, the effect can be more pronounced results in
 406 a higher energy saving. Note that, in general, due to the presence of metal foam in the system,
 407 the temperature difference in the systems with a central heating element with different
 408 dimensions is very small.
 409

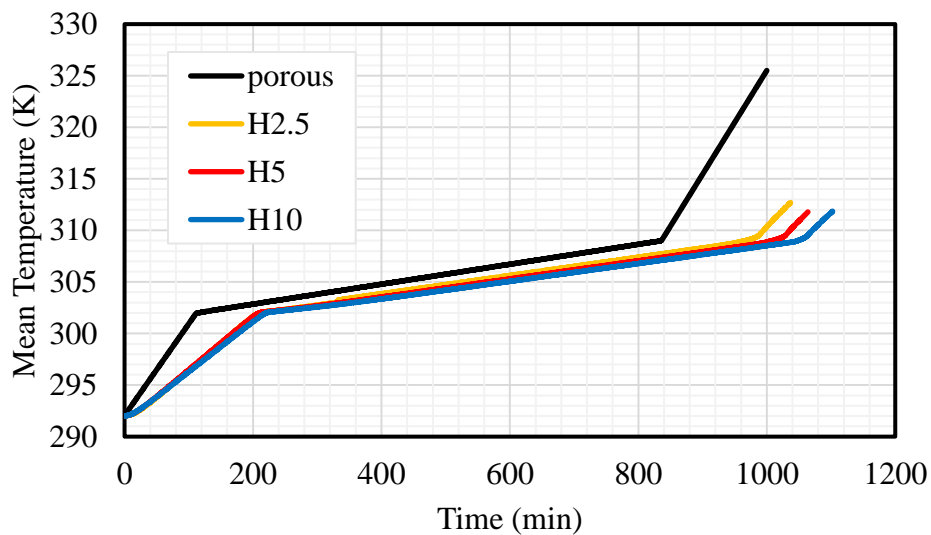


Fig. 9. The variation of the mean PCM temperature in terms of time for the system with a central heating element with different sizes with $\epsilon=0.95\%$, $\omega=30$ PPI and $\dot{Q}=100$ kW/m³

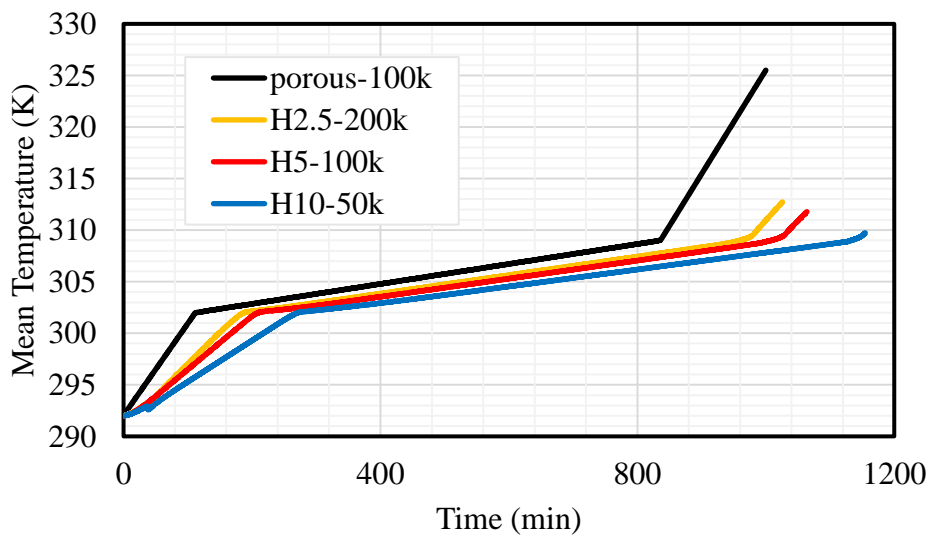
410

411

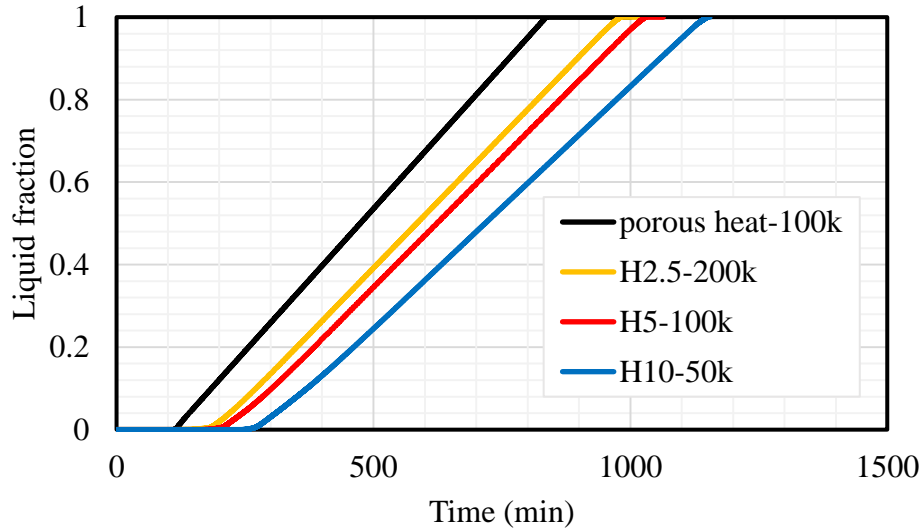
412 5.2.2. Influence of the dimension of heating element related to the rate of heat generation

413 To understand the effect of heating element size more clearly, Figs. 10-a and 10-b illustrate the
 414 mean temperature and liquid fraction of PCM for Case 2 in Table 2 compared with Cases 4 and
 415 5 where the horizontal area of the heating element is considered constant and the height is
 416 changed based of the rate of heat generation. Note that in all cases, the amount of heat

417 generation from the heat source is the same. As shown, the unit with a lower height and higher
 418 heat generation rate shows a higher mean temperature and results in a lower melting time.
 419 Because of the high conductivity porous medium in the domain, as mentioned, the effect of
 420 heating element dimensions is suppressed. Therefore, a case with a higher heat generation rate
 421 shows better results. According to the hear generation rate, the volumetric heat source power
 422 is identical for all cases of 2, 4 and 5; however, for the case with higher heat generation rate
 423 per volume, the heat transfers faster inside the porous medium to due to a higher heat generation
 424 rate and as a result penetrates faster in all the domain. Thus, in an identical time, the temperature
 425 in the case with higher heat generation rate (case 4) is higher as shown in Fig. 10. The melting
 426 time for case 4 is 4.7% and 14.7% higher than that for cases 2 and 5, respectively. The results
 427 of this section show that, for an identical volumetric heat source power, the rate of heat
 428 generation per volume is more pronounced than the surface area of the heating elements due to
 429 the presence of the porous medium.
 430



a)



b)

Fig. 10. The variation of a) mean temperature and b) liquid fraction in terms of time for the system with a central heating element related to the heat generation rate with different sizes and heat generation rates with $\varepsilon=0.95\%$, $\omega=30$ PPI

431

432 6. Conclusion

433 Effects of uniform internal heat generation based on Joule heating to porous foams embedded
 434 in PCM-based heat storage system were numerically investigated. The melting time was
 435 compared with the case of a localised central heating element considering the same PCM
 436 volume and the same heat generation rate. The results show an almost 21% reduction in the
 437 total melting time with the application of internal heat generation rate from the porous medium
 438 compared with the case of a central heating element for heat generation rate of 100 kW/m^3 .
 439 Meanwhile, the melting time is not affected significantly by increasing the pore density of the
 440 metal foam. It is also observed that doubling the rate of heat generation could reduce the
 441 melting time up to 50% due to the uniformity of temperature distribution with the application
 442 of internal heat generation. For the analysis of central heating element with the same heat
 443 generation rate, the results reveal a superior effect of the heat generation rate than the heating
 444 element dimensions on the melting time. For an identical volumetric heat source power of the

445 localised heater, the rate of heat generation per volume is more effective compared with the
446 heating element size due to the presence of the porous medium. Results from the study would
447 serve as guidelines for the application of internal heat generation in broad PCM-based
448 applications including thermal control of electronic components, freezing of biological
449 tissues, and solar thermal energy storage systems. Furthermore, the study on the dimensions of
450 the central heating element provides effective approaches for a more efficient energy storage
451 system.

452

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