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Pro-Consumer Price Ceilings under Regulatory Uncertainty*

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Abstract

We examine optimal price ceilings when the regulator is uncertain about demand and maximizes expected consumer surplus. With perfect competition, if regulatory uncertainty is large enough, then softer intervention is called for, with the price ceiling set at a relatively high level compared with a full information scenario. In an imperfectly competitive setting where symmetric firms compete in supply functions, with large enough uncertainty, the optimal ceiling increases with the degree of competition, so greater competitive pressure justifies less restrictive regulation. Under perfect competition, we also determine a cut-off level of rationing efficiency below which a price ceiling should not be used.

Keywords: Competition; consumer surplus; price caps; rationing *JEL classification*: D41; D45; D80; L13; L50

I. Introduction

Although controversial, price ceilings have been used in a wide range of markets, including those for rental accommodation, gas, electricity, telecommunications, pay-day lending, and basic consumption goods. One rationale for price ceiling regulation is to correct inefficiency stemming from insufficient competition, while another is the protection of consumers. The latter rationale can explain the use of price controls in nearly competitive markets, including those for rental accommodation in developed economies (see Glaeser and Luttmer, 2003, on US rent controls) and those

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for basic food products in developing economies (see Mbaye *et al.*, 2015, on price caps in Senegal).¹

Price ceilings have been used extensively in utility markets, where competition is typically restricted, to secure low prices for consumers. Sappington and Weisman (2010) discuss the use of price ceilings in telecommunications, while Davis and Kilian (2011) examine price caps empirically in the US residential market for natural gas. A survey of regulators in transition and developing economies by Kirkpatrick *et al.* (2005) found that price controls had been used in 40 percent of the countries, most commonly in telecommunications (76 percent).

To correct market inefficiency, price regulation would aim to maximize total welfare. However, in recent years, there has been an increase in the focus of policy-makers and regulators on consumer welfare and a greater involvement of consumer groups in policy debate.² Following the 2002 Enterprise Act, approved UK bodies were designated super-complainants at the Office of Fair Trading to "strengthen the voice of consumers" and to protect their interests.³ Moreover, in markets where the suppliers are foreign-owned, consumer surplus might be an appropriate measure of domestic welfare. So the realities of regulation are more complex and call for a better understanding of a consumer-surplus standard in economic analysis.

In this paper, we explore how market conditions affect the level of a price ceiling that maximizes expected consumer surplus in a setting where the regulator is uncertain about demand. Our framework allows for varying degrees of competition, so it fits a gamut of market structures. We investigate first the impact of regulatory uncertainty on the optimal ceiling for perfect competition, and then the relationship between competitive pressure and the optimal level of intervention. We also examine the effect of arbitrary levels of rationing inefficiency on the optimal ceiling.

¹Other developing economies with price caps include Kenya and Argentina. See the Reuters articles "Kenya Enacts Price Control Law" of 16 September 2011 (https://www.reuters.com/article/ozabs-kenya-prices-idAFJOE78F0FM20110916) and "Argentine Peso Hits New Lows as Food Price Controls Take Effect" of 7 January 2014 (https://uk.reuters.com/article/economy-argentina-peso/-peso-hits-new-argentine-lows-as-food-price-controls-take-effect-idUKL2N0K H16320140107).

 $^{^{2}}$ Empirical evidence suggests that lobby groups influence regulation, with small supplier groups being more effective than consumers (a large but fragmented group). See Viscusi *et al.* (2005, Chapter 10).

³See Office of Fair Trading (2003). The consumer organization *Which?* – one of the first supercomplainants – played a part in shaping tariff regulation in the UK energy sector in 2014. The changed role of consumers can relate to utility market deregulation, increased market complexity (e.g., banking and financial services), and growing evidence on demand-side biases.

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In our model, private agents have all relevant information. So, uncertainty is entirely on the part of the regulator, who is aware of this disadvantage.⁴ This information structure also covers the possibility that the price ceiling is a long-term regulatory decision, while short-run market conditions can change. We focus on a frictionless homogeneous product market where trade occurs at a uniform price. If the price ceiling binds, then this lowers the cost of purchase to consumers, but it results in a shortage. For tractability, we assume quadratic cost and benefit functions, but we argue that the qualitative results are more general.

A preliminary analysis of perfect competition with efficient rationing shows that with no uncertainty the ceiling that maximizes consumer surplus always binds (i.e., it is strictly lower than the equilibrium price). Consider a price ceiling that is marginally below the market clearing price: this has both a negative effect on consumer surplus, as some consumers are excluded from the market, and a positive effect, as those who still purchase pay a lower price. As the marginal consumers excluded from the market have the lowest valuations, the negative effect is small and completely offset by the surplus gains of all those who still purchase. The optimal ceiling balances the gains and losses. We further show that this result is robust for relatively low levels of demand uncertainty.

Next, we introduce arbitrary levels of uncertainty, and we characterize the optimal price ceiling.⁵ We show that sufficient regulatory uncertainty calls for a price ceiling set at a relatively high level, and thus for softer intervention, compared with the no-uncertainty case. At this level, the ceiling might not bind ex post, and so it might not benefit consumers. However, it offers protection against potentially high free-market prices. To see the intuition, suppose the optimal price ceiling under no uncertainty were set. If the realized demand is low enough, then the market clearing price will be lower than this ceiling and the intervention will not bind. Then, a marginal increase in the price ceiling would not affect consumer surplus. In contrast, if the realized demand is large enough, this ceiling binds and a marginal increase brings it closer to the (higher) level that is optimal for that particular high demand, and thus increasing consumer surplus.

Our perfect competition model is relevant for interventions in fragmented markets, such as rent controls or price caps on basic

⁴For example, a regulator might be uncertain of the demand for new products.

⁵Although, in the main text, we focus on regulatory uncertainty regarding demand, in the Online Appendix we show that we obtain qualitatively similar results in a model with supply uncertainty only (e.g., the regulator might be uncertain about what innovations are in the pipeline). In the Online Appendix, we also outline the corresponding model with two-sided (demand and supply) uncertainty, and we explore its solution numerically.

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consumption goods. To analyze optimal ceilings in concentrated markets (e.g., telecommunications or utility markets), we employ an imperfectly competitive framework, which can be interpreted as the reduced form of a model where identical firms compete in linear supply functions. We draw on the fact that, in this setting, aggregate supply in equilibrium is a fraction of the perfectly competitive supply, which allows us to explore varying degrees of market power. The reduced-form model can also represent a monopoly, so our results apply to this limiting case.

If there is no regulatory uncertainty, then the optimal ceiling is the same for any degree of competition. As this ceiling lies below the perfectly competitive equilibrium price, it is also below the (higher) imperfect competition equilibrium prices. However, with sufficient regulatory uncertainty, we show that the appropriate level of the ceiling depends on the degree of competition, as this determines the unregulated market price. The more concentrated the market, the greater the expected consumer-surplus loss if there is no regulation. This creates a stronger incentive to lower the price ceiling, triggering a positive relationship between the optimal ceiling and the degree of competition. Thus, with enough uncertainty, a higher price ceiling (i.e., less restrictive intervention) is justified in an environment with greater competitive pressure.

We also explore the impact of rationing inefficiency on the optimal price ceiling under perfect competition.⁶ We determine a cut-off level of rationing efficiency below which a price ceiling should not be used, and we show that our previous findings are qualitatively robust when rationing efficiency exceeds this level. Rationing is fully efficient when the goods supplied are allocated to the consumers with the highest valuations amongst those willing to purchase. At a binding ceiling, all consumers who buy the product enjoy a higher surplus than in the absence of regulation. However, with inefficient rationing, some of these consumers displace others who value the product more. If rationing is sufficiently inefficient, then the loss in consumer surplus from such misallocations, together with lower supply, fully offsets the benefits for the consumers (who buy) at the lower price.

A vast body of economics literature has analyzed the rationales, design, and impact of price regulation (see Armstrong and Sappington, 2007, for a comprehensive review). In this context, our information structure was first formalized by Weitzman (1974) in order to analyze the choice of regulatory instrument. It was subsequently used in studies of optimal regulation (e.g., Baron and Myerson, 1982; Lewis and Sappington, 1988) that consider more sophisticated mechanisms. Lewis and Sappington (1988) show that, in a monopoly market, a regulator facing demand uncertainty could implement

⁶In our setting, the regulator cannot affect the extent of rationing efficiency in the market.

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the first-best solution by using a menu of price-transfer pairs, when marginal cost is increasing. In contrast to these studies, we focus on a price ceiling, a simple but commonly used instrument, which is particularly relevant in markets where the intervention is fixed over a period in which demand can fluctuate.⁷

Recent work has examined the regulation of price caps in oligopoly markets with homogeneous products, where both the firms and the regulator face demand uncertainty. Earle *et al.* (2007) point out that an increase in a price ceiling near marginal cost might raise welfare. Grimm and Zöttl (2010) show that there is always a range of ceilings that increase production and welfare from the unregulated market levels and, for non-degenerate uncertainty, this range is strictly above marginal cost.⁸ In contrast to their analyses, our analysis focuses on a consumer-surplus standard with only the regulator facing uncertainty.

Consumer welfare has sometimes been used in regulation in conjunction with a welfare standard (e.g., for merger policy in Europe and the US). The consumer-surplus standard has been regarded as a way to redress the regulatory and policy-making balance in favor of consumers, a less-represented group. Besanko and Spulber (1993) show that this standard can offset some of the informational advantage that firms have over the regulator.⁹ Nevertheless, to be sure, a consumer-surplus standard has various caveats, including adverse dynamic consequences on the innovation and investment incentives of firms and their long-run survival.¹⁰

Our work is also related to an emerging body of literature that explores inefficient rationing under price regulation. Bulow and Klemperer (2012) examine the impact of price regulation on consumers in a model with general demand and supply and random rationing, but with no uncertainty. They show that if supply is locally more elastic than demand, then a price ceiling always hurts consumers when demand is convex. By considering arbitrary levels of rationing inefficiency and regulatory uncertainty, our findings complement their findings. Glaeser and Luttmer

⁷Furthermore, some of the instruments required for optimal regulation (e.g., transfers) might not be available in practice. See Armstrong and Sappington (2007) for discussion of practical regulatory policies, and see Crew and Kleindorfer (2002) for more on the limitations of optimal regulation models.

⁸In related models, Reynolds and Rietzke (2018) consider endogenous entry and identify conditions under which a price cap is welfare improving, while Lemus and Moreno (2017) explore the optimal ceiling when a monopolist pre-commits to a capacity level before the demand is realized.

⁹Neven and Röller (2005) analyze how institutional settings, such as transparency and accountability, interact with the choice of an appropriate standard.

¹⁰Moreover, to the extent to which consumers own the firms (e.g., through pension funds), this standard might also be detrimental to consumers (see Motta, 2004).

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(2003) and Davis and Kilian (2011) analyze price regulation empirically, and the welfare loss associated with inefficient rationing in competitive markets.¹¹ We contribute to this literature by exploring the interplay between rationing inefficiency and regulatory uncertainty. By parametrizing rationing efficiency, we propose a flexible theoretical framework that allows for a range of outcomes and extends previous work.

We explore how market characteristics affect a pro-consumer price ceiling in a static framework. However, the introduction of a price ceiling is likely to have long-term consequences, most notably by affecting the investment incentives of firms. Dobbs (2004) finds that under uncertainty regarding technological change, a price cap reduces a monopolist's incentive to invest in capacity expansion. Also, Biglaiser and Riordan (2000) show that dynamic adjustments of the price ceiling can distort incentives for capital replacement. Nonetheless, as argued by Joskow (2014), a price ceiling gives a strong incentive for cost reduction, although consumers could only benefit later, when the ceiling is revised.¹² A fuller analysis of proconsumer price ceilings would need to investigate the dynamic effects of both the instrument and the consumer-surplus standard, and to assess the relative performance of different regulatory interventions in this context.

After formulating the model in Section II, we present a preliminary analysis of perfect competition with little or no regulatory uncertainty in Section III. In Section IV, we introduce arbitrary levels of demand uncertainty, and in Section V we analyze the imperfect competition case. In Section VI, we explore the implications of rationing inefficiency. We present our conclusions in Section VII. All proofs missing from the text are relegated to the Appendix or the Online Appendix.

II. The Model

Consider a market in which the regulator might be uncertain about the demand for a homogeneous product. There is no uncertainty on the part of private agents. On this basis, the regulator chooses a price ceiling that maximizes expected consumer surplus. The regulatory intervention is announced to all private agents (producers and consumers).

First, we consider a perfectly competitive market. Let consumers' gross benefit (or utility) from the consumption of q units of the product be given

¹¹Focusing on misallocations due to rent control, Glaeser and Luttmer show that under conservative assumptions, 20 percent of rented apartments in New York City were in the wrong hands. Davis and Kilian (2011) find substantial allocative costs in the US residential market for natural gas over the 1950–2000 period.

¹²Price ceilings also have dynamic effects in the presence of search frictions. For related work, see Armstrong *et al.* (2009), Fershtman and Fishman (1994), and Rauh (2004).

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by $\mathfrak{B}(q,\eta) = (B + \eta)q - bq^2/2$, where b > 0 and $B + \eta > 0$. From the regulator's point of view, η is a random variable with zero mean, $E(\eta) = 0$, distributed according to a twice continuous and differentiable cumulative distribution function $\mathcal{F}(\eta)$ defined on a closed interval $[n_{\min}, n_{\max}]$. We assume that the hazard rate $\mathcal{F}'(\eta)/[1 - \mathcal{F}(\eta)]$ is strictly increasing. The suppliers' cost of producing q units is given by $\mathfrak{C}(q) = Cq + cq^2/2$, where c > 0 and C > 0. Then, inverse demand and supply are $P_d(q, \eta) = \partial \mathfrak{B}(q, \eta)/\partial q = B + \eta - bq$ and $P_s(q) = \partial \mathfrak{C}(q)/\partial q = C + cq$, respectively.

Writing p for unit price, it follows that direct demand and supply are given, respectively, by

$$q^{d}(p) = \frac{B + \eta - p}{b} \quad \text{and} \quad q^{s}(p) = \frac{p - C}{c}.$$
 (1)

We assume that consumers and producers can observe η , while the regulator cannot. This captures the informational advantage that producers might have over the regulator, regarding demand.¹³

We use p^* to denote the expost market clearing price (where $q^d(p^*) = q^s(p^*)$), and q^* to denote the corresponding output level. Then,

$$p^* = \frac{c(B+\eta) + bC}{b+c}$$
 and $q^* = \frac{B+\eta - C}{b+c}$. (2)

We assume that $B + \eta > C$ for any η . This guarantees a well-defined equilibrium output ex post. Note that ex ante (before the demand shock η is realized), the regulator views $p^*(\eta)$ as a random variable with expected value

$$p_e^* = \frac{cB + bC}{b + c}.$$
(3)

We explore the regulatory intervention that takes the form of a price ceiling \bar{p} , assuming that resale of rationed goods is not possible. A price ceiling stipulates a maximal trade price and only binds if the unregulated market price lies above the regulated level. If it lies at or below the ceiling, then the outcome coincides with the unregulated market equilibrium; that is, for a given price ceiling \bar{p} , if $p^* \leq \bar{p}$, then $q(p) = q^*$ (as given by equation (2)), and if $p^* > \bar{p}$, then $q(p) = q^s(\bar{p})$ (as given by equation (1)). The cumulative distribution function of $p^*(\eta)$ is determined by the cumulative distribution function of $p(\mathcal{F}(\eta))$. Because η is defined on a closed interval, so is the cumulative distribution function of $p^*(\eta)$.

Then, we examine price ceilings in a model of imperfect competition, maintaining our assumptions regarding the demand side of the market and

¹³Note that η might be unknown when the regulator sets a price ceiling, but it might be revealed before the producers make supply decisions, or producers might be able to adjust their behavior as information about η is revealed by the market.

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the quadratic cost presented above. We assume that there are N identical suppliers and each firm *i*'s cost of producing q_i units is given by $\mathfrak{C}(q) = Cq_i + Ncq_i^2/2$.¹⁴ We interpret our model as one where the firms compete by choosing linear supply functions. Building on Klemperer and Meyer (1989), we assume that each firm chooses a supply function $S_i(p-C) = d_i(p-C)$, where the slope $d_i > 0$.¹⁵ In the linear supply function equilibrium, a firm's supply is only a fraction of its supply in the perfect competition model (i.e., where the firms are price takers).¹⁶ Thus, with imperfect competitive market. It then follows that the aggregate quantity supplied in the symmetric supply function equilibrium at price p can be written as

$$q^s(p,\delta) = \delta \frac{p-C}{c},$$

where $\delta < 1$ captures the restriction in output below the competitive level. Note that δ increases with the degree of competition, captured by the number of firms, N. As the market becomes nearly competitive $(N \rightarrow \infty)$, δ converges to 1. Alternatively, $q^s(p, \delta)$ can be regarded as an ad hoc way of capturing the restriction in aggregate supply in a market where the firms have market power.

Using $q^s(p, \delta)$, we can derive the equilibrium outcome in the unregulated imperfectly competitive market. We use p^{δ} to denote the expost unregulated market price – where $q^d(p^{\delta}) = q^s(p^{\delta}, \delta)$ – and q^{δ} to denote the corresponding output level. Then,

$$p^{\delta} = \frac{c(B+\eta) + \delta bC}{\delta b + c}$$
 and $q^{\delta} = \frac{\delta (B+\eta - C)}{\delta b + c}$

As in the competitive framework, the regulator views the unregulated market price $p^{\delta}(\eta)$ with imperfect competition as a random variable.

In general, price ceiling regulation can result in excess demand, in which case the scarce output will be rationed. However, if there is some degree of rationing inefficiency, this will limit the scope for pro-consumer price regulation. Therefore, we adapt our perfect competition model by introducing a parameter that captures rationing inefficiency. Specifically,

¹⁴This individual cost function guarantees that when the total cost of producing q using N-plants in the industry is minimized, the total cost is the same as under perfect competition, $\mathfrak{C}(q) = Cq + cq^2/2$. Then, the marginal cost curve coincides with $P^s(q)$.

¹⁵Klemperer and Meyer (1989) show that with unbounded demand uncertainty and a symmetric industry, there is a unique equilibrium where firms choose linear supply functions of the form we consider. This result holds for any distribution of uncertainty (even if it degenerates into a mass point), so long as the support is unbounded.

¹⁶Akgün (2004) employs a related framework. We present a supply function competition microfoundation for our model in the Online Appendix.

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we write the regulator's objective function as a linear combination of the expected consumer surplus for both efficient rationing and extremely inefficient rationing. With efficient rationing, the goods supplied are allocated to the consumers with the highest valuations among those willing to buy. With extremely inefficient rationing, the available supply is allocated to the consumers whose valuations are the lowest. Our objective function puts weight α on expected consumer surplus with efficient rationing, and $1 - \alpha$ on expected consumer surplus with inefficient rationing, where $\alpha \in [0, 1]$. This covers fully efficient rationing ($\alpha = 1$), extremely inefficient rationing ($\alpha = 0$), and all intermediate cases, including random rationing that corresponds to $\alpha = 1/2$.

In our model, the extent of rationing inefficiency is determined by market conditions and is independent of regulatory uncertainty.¹⁷ For expositional simplicity, our initial analysis assumes efficient rationing. We then allow for arbitrary levels of rationing efficiency, and we show that the optimal ceiling that is obtained under efficient rationing carries over for α above a critical level, which depends on the slopes of demand and supply. This critical level can lie above or below $\alpha = 1/2$.¹⁸

III. Preliminary Analysis

In this section, we introduce some of our results in a "textbook" framework of perfect competition and efficient rationing (i.e., we assume that $\delta = 1$ and $\alpha = 1$). We start with a situation where demand (as well as supply) is deterministic, and we show that consumer surplus can be increased from the free-market benchmark by setting an appropriate binding price ceiling. We then discuss why this result still holds when there is a limited amount of demand uncertainty. In the following section, we provide a formal analysis, allowing for arbitrary degrees of uncertainty.¹⁹

Using the model introduced in Section II, let us initially assume that $\eta = 0$. Demand becomes $q^d(p) = (B - p)/b$, and the equilibrium price in the unregulated market is $p^* = (cB + bC)/(b + c)$. For any price ceiling $\bar{p} \ge p^*$, the market price is p^* and consumer surplus is given by $CS(q^d(p^*)) = b(B - C)^2/2(b + c)^2$.

¹⁷Note that α can instead be interpreted also as the probability, for the regulator, that rationing will be efficient, if this is independent of demand uncertainty.

 $^{^{18}}$ Random rationing could be used as an alternative benchmark, but then we would have to cover two cases (with the critical level of efficiency above or below 1/2), which would complicate the exposition.

¹⁹Under perfect competition, a price ceiling cannot improve (expected) total surplus. However, our analysis focuses on intervention that aims to maximize consumer surplus.

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However, any price ceiling $\bar{p} < p^*$ is binding so that output is $\min[q^d(\bar{p}), q^s(\bar{p})] = q^s(\bar{p}) = (\bar{p} - C)/c$. With efficient rationing, consumer surplus is

$$CS(q^{s}(\bar{p})) = Bq^{s}(\bar{p}) - \frac{1}{2}b(q^{s}(\bar{p}))^{2} - \bar{p}q^{s}(\bar{p})$$

$$= \frac{(\bar{p} - C)[2c(B - \bar{p}) - b(\bar{p} - C)]}{2c^{2}} \equiv CS_{d}^{L}.$$
(4)

Using $CS(q^d(p^*))$ and CS_d^L , we obtain the following result.

Lemma 1. With no uncertainty, the price ceiling \hat{p} that maximizes consumer surplus under perfect competition with efficient rationing is given by

$$\hat{p} = \frac{cB + (b+c)C}{b+2c} < p^*.$$
(5)

If a price ceiling were set marginally below the market clearing price p^* , there would be not only a first-order gain in consumer surplus, because the lower price would be paid by all consumers who still buy the good, but also a second-order loss of consumer surplus from the marginal reduction in quantity supplied. With further marginal reductions in the price ceiling, the gain is made over steadily smaller quantities supplied, while the loss is steadily greater because consumers with higher marginal willingness to pay are excluded. Thus, the optimal pro-consumer price ceiling \hat{p} is strictly lower than the free-market equilibrium price p^* , and this balances the trade-off. The left panel of Figure 1 illustrates this trade-off at the optimal price ceiling \hat{p} . The consumer-surplus gain is captured by the dotted rectangle, and the loss by the dotted triangle.²⁰

Before introducing uncertainty, we briefly discuss how the analysis above would be affected by nonlinearity of demand and supply. It can be seen that, for a given demand-supply intersection and for given slopes of demand and supply at this intersection, the same qualitative conclusion holds if there is strict convexity or strict concavity of either curve. However, strict convexity results in a higher optimal ceiling, while strict concavity results in a lower optimal ceiling than in the linear case. Consider the strictly convex demand tangent to the straight line $P_d(q)$ in the left panel of Figure 1 at the intersection with $P_s(q)$. The consumer-surplus loss from the ceiling \hat{p} is then larger than in the figure, but the gain is the same. Still, there are binding ceilings for which the net gain is positive (e.g., a ceiling marginally below p^*). A similar argument holds

²⁰Equation (1) can be written as $\hat{p}[1 - (b - c)/c\varepsilon_s(\hat{p})] = MR(\hat{p})$, where $\varepsilon_s(\hat{p})$ is supply elasticity and $MR(\hat{p})$ is the market marginal revenue at price $p = \hat{p}$. This gives a parallel with the Lerner index, but with an additional relative slope term.

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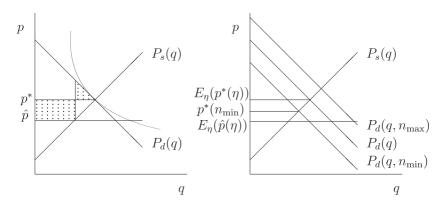


Fig. 1. Optimal pro-consumer price ceiling with efficient rationing

if supply is strictly convex. Then the loss is the same and the gain is smaller than in the linear case. These conclusions are reversed for strict concavity.

We now introduce a small amount of demand uncertainty. The right panel of Figure 1 illustrates the highest and lowest demand functions, $P_d(q, n_{\text{max}})$ and $P_d(q, n_{\text{min}})$, respectively. In this case, $P_d(q)$ is the expected demand, and it captures a situation where the realized value of η is equal to the expectation of η , $E(\eta) = 0$. For any realization of η , consumer surplus is maximized at a price ceiling

$$\hat{p}(\eta) = \frac{c(B+\eta) + (b+c)C}{b+2c} < p^*(\eta).$$
(6)

This follows immediately from replacing *B* with $B + \eta$ in Lemma 1. The expected optimal ceiling is the same as the one in the lemma as $E(\hat{p}(\eta)) = \hat{p}$. This is because the objective function only depends on the expectation of η , $E(\eta) = 0$. This simple reasoning is correct so long as $\hat{p} < p^*(n_{\min})$, which is the case if there is only relatively little uncertainty. Therefore, our result from the no-uncertainty case carries over to a model with relatively little uncertainty, and the price ceiling that maximizes expected consumer surplus binds regardless of the realization of demand.²¹ In contrast, if $\hat{p} > p^*(n_{\min})$, the analysis will be different: such a ceiling can bind for some realizations

²¹This analysis relates to the case in which the regulator faces a small amount of uncertainty over the demand intercept, though the slope is known. If, instead, the regulator knows the intercept or the market equilibrium point, for instance, but faces a small amount of uncertainty over the slope, the price ceiling that maximizes expected consumer surplus is below the equilibrium price, as in our framework.

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of demand but not for others. That is, ex post, the market clearing price can be above or below the price ceiling.

IV. Perfect Competition

In this section, we fully investigate the impact of arbitrary levels of demand uncertainty, focusing on price regulation where the ceiling satisfies $\bar{p} > C$, so that supply is positive.

For a given price ceiling \bar{p} , we define $n^*(\bar{p})$, the specific value of η for which the market clears, that is, $\bar{p} = p^*(\eta)$. Using equation (2), we obtain

$$n^{*}(\bar{p}) = \frac{(b+c)(\bar{p} - p_{e}^{*})}{c},$$
(7)

where p_e^* , the expectation of $p^*(\eta)$, is defined in equation (3). Using equation (7), we identify three price regions where the intervention has different implications. We then examine each of these regions as a potential location for the optimal value of \bar{p} .

- (a) The price ceiling always binds: $\bar{p} < p^*(n_{\min})$ (i.e., \bar{p} is such that $n^*(\bar{p}) < n_{\min}$) so a price ceiling binds regardless of η , and this results in excess demand.
- (b) The price ceiling never binds: $\bar{p} > p^*(n_{\max})$ (i.e., \bar{p} is such that $n^*(\bar{p}) > n_{\max}$) so a price ceiling does not bind regardless of η , and the free-market outcome prevails.
- (c) The price ceiling might or might not bind: p̄ ∈ [p*(n_{min}), p*(n_{max})] (i.e., p̄ is such that n*(p̄) ∈ [n_{min}, n_{max}]), so the effect of a price ceiling depends on the value of η. In particular, for low demand (when η ∈ [n_{min}, n*(p̄))) the price ceiling does not bind, whereas for high demand (when η ∈ [n*(p̄), n_{max}]) it results in excess demand.

Region (a). In the first case, as supply is a binding constraint regardless of η , output is $\min[q^d(\bar{p}), q^s(\bar{p})] = q^s(\bar{p}) = (\bar{p} - C)/c$. Consumer surplus is $CS(q^s(\bar{p}), \eta) = (\bar{p} - C)[2c(B + \eta - \bar{p}) - b(\bar{p} - C)]/2c^2$, and expected consumer surplus is $E(CS(q^s(\bar{p}), \eta)) = CS_d^L$, as given in equation (4). The price ceiling that solves the first-order condition of the optimization problem in this region is \hat{p} in equation (5).

Note that \hat{p} is also the optimal ceiling with little or no demand uncertainty, as we have shown in Section III. The limit on uncertainty for which this result holds can be specified in terms of n_{\min} (< 0). If n_{\min} is close enough to zero (i.e., uncertainty is small), then the price ceiling \hat{p} will bind for all realizations of η , but for n_{\min} further from zero it might

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or might not bind, depending on η . Using equations (2) and (5), let n_0 be the value of η at which \hat{p} is equal to the market-clearing price.

Definition 1. Let $n_0 = -[c(B - C)/(b + 2c)]$.

If there is little uncertainty (i.e., if $n_{\min} > n_0$), as $d^2 C S_d^L / d\bar{p}^2 < 0$, then equation (5) is a well-defined local maximum within the region $[C, p^*(n_{\min})]$. However, with greater uncertainty (i.e., if $n_{\min} \le n_0$), $C S_d^L$ is increasing for all $\bar{p} < p^*(n_{\min})$ and the critical value \hat{p} is weakly larger than $p^*(n_{\min})$, which is inconsistent with the region $[C, p^*(n_{\min})]$. This proves the following result.

Lemma 2. With small enough demand uncertainty (i.e., $n_{\min} > n_0$), in the region where $\bar{p} < p^*(n_{\min})$, the price ceiling that maximizes expected consumer surplus under perfect competition is given by equation (5). However, if $n_{\min} \le n_0$, then an optimal price ceiling cannot be strictly lower than $p^*(n_{\min})$.

After analyzing the other possible regions for the price ceiling, we explore under what conditions the price ceiling in equation (5) is globally optimal.

Region (b). For the second case (i.e., the price ceiling never binds), with a price ceiling in the region $\bar{p} > p^*(n_{\text{max}})$, regardless of the realization of η , the outcome is the same as with no intervention. For a given η , consumer surplus is $b(B + \eta - C)^2/2(b + c)^2$. So, expected consumer surplus becomes

$$\frac{b[(B-C)^2 + E(\eta^2)]}{2(b+c)^2} \equiv CS_d^H,$$
(8)

and it is the same as in the free-market equilibrium.

Region (c). For the third case (i.e., the price ceiling might or might not bind), $\bar{p} \in [p^*(n_{\min}), p^*(n_{\max})]$, so $n^*(\bar{p}) \in [n_{\min}, n_{\max}]$. In the following, we summarize the main steps of the analysis, but we relegate the derivation of the expected consumer surplus to the Appendix.

For any price ceiling $\bar{p} \ge p^*(\eta)$ (or, equivalently, $\eta \le n^*(\bar{p})$), the intervention does not bind, and so the market-clearing price $p^*(\eta)$ prevails and the quantity traded is $q^d(p^*, \eta) = q^s(p^*)$. Because $q^d(p^*, \eta) = (B + \eta - p^*)/b = (B + \eta - C)/(b + c) \equiv q_d^*$, consumer surplus in this case is given by $CS(q_d^*) = b(B + \eta - C)^2/2(b + c)^2$. We use $CS(q_d^*)$ to derive the expected consumer surplus conditional on $\bar{p} \ge p^*(\eta)$. For $\bar{p} \le p^*(\eta)$ (or, equivalently, $\eta \ge n^*(\bar{p})$), the intervention leads to excess demand. The realized consumer surplus from the $q^s(\bar{p}) = (\bar{p} - C)/c$ units produced is the same as in the first case, where the price ceiling always binds.

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In the Appendix, we derive the expressions for expected consumer surplus in these two cases. Then, we obtain the total expected consumer surplus in region (c), which we denote by CS_d . An interior optimum solves $dCS_d/d\bar{p} = 0$, where

$$\frac{dCS_d}{d\bar{p}} = -[1 - \mathcal{F}(n^*(\bar{p}))] \frac{(b+2c)(\bar{p}-C) - c(B-C)}{c^2} - \mathcal{F}(n^*(\bar{p})) \frac{1}{c} \frac{\epsilon_d^L(n^*(\bar{p}))}{\mathcal{F}(n^*(\bar{p}))},$$
(9)

with $\epsilon_d^L(n^*(\bar{p})) = \int_{n_{\min}}^{n^*(\bar{p})} \eta d\mathcal{F}(\eta)$. The two terms in equation (9) are related to the fact that a price ceiling \bar{p} might or might not bind, and they are weighted by their respective probabilities. The fraction $-[(b+2c)(\bar{p}-C)-c(B-C)]/c^2$ is the value of $dCS_d/d\bar{p}$ when there is no uncertainty and supply is the binding constraint, as in our preliminary analysis. The second term in equation (9) shows the impact of demand uncertainty. Note that $\epsilon_d^L(n^*(\bar{p}))/\tilde{\mathcal{F}}(n^*(\bar{p}))$ (< 0) is the expected value of η , conditional on the ceiling not binding, and a more negative value represents greater demand uncertainty.

The next result combines the analyses of the three regions, and uses equations (4), (8), and (A4).

Lemma 3. With demand uncertainty, expected consumer surplus under perfect competition is (a) continuous and differentiable for all values of $\bar{p} > C$, and (b) independent of \bar{p} at any price ceiling $\bar{p} \geq p^*(n_{\max})$ because the intervention is not binding in this range.

In the Appendix, using Lemma 3, and as the hazard rate of η is strictly increasing, we show that the objective function is single-peaked over the three regions and the location of the optimal ceiling depends on the degree of uncertainty. This leads to the following result.

Proposition 1. Under perfect competition, if demand uncertainty is small (i.e., $n_{\min} > n_0$), then the unique price ceiling that globally maximizes expected consumer surplus always binds and is given by equation (5). However, if demand uncertainty is large (i.e., if $n_{\min} \leq n_0$), then it lies in the interval $[p^*(n_{\min}), p^*(n_{\max}))$ and might or might not bind, ex post.

This proposition highlights the effects of the degree of uncertainty on optimal pro-consumer regulation. The solution for $n_{\min} > n_0$ is related to the effects discussed in Section III. It generalizes the result that, under no uncertainty, a price ceiling $\bar{p} = \hat{p}$ below the market equilibrium maximizes consumer surplus. When demand is stochastic, it is not known ex ante whether supply will be a binding constraint on consumption. However,

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with small uncertainty, CS_d is maximized with the same price ceiling, $\bar{p} = \hat{p}$. Moreover, the analysis preceding Proposition 1 shows that an optimal ceiling cannot lie in $[p^*(n_{\min}), p^*(n_{\max})]$. Instead, it is strictly lower than $p^*(n_{\min})$ and, implicitly, lower than the expected market-clearing price p_e^* . Nevertheless, if the regulator faces enough uncertainty $(n_{\min} \le n_0)$, this favors setting a price ceiling that is relatively high and, therefore, less likely to bind.

Intuitively, taking the no-uncertainty case, at the optimal ceiling \hat{p} , supply is a binding constraint and so $q = q^{s}(\hat{p})$. If we allow for small uncertainty (i.e., $n_{\min} > n_0$), then at price ceiling \hat{p} , supply remains a binding constraint, $q = q^s(\hat{p})$ for any η , and \hat{p} remains the optimal ceiling. If, instead, uncertainty is large (i.e., $n_{\min} \leq n_0$) and the regulator still sets $\bar{p} = \hat{p}$, this ceiling would not bind for very low demand realizations (as the equilibrium price is below \hat{p}), but it would still bind for high demand realizations. Suppose the regulator marginally increases the ceiling to $\bar{p} = \hat{p} + \varepsilon$ for small $\varepsilon > 0$. For very low demand realizations, $\bar{p} = \hat{p} + \varepsilon$ would still not bind and ex post output (and consumer surplus) would be the same as at $\bar{p} = \hat{p}$. For high demand realizations, both $\bar{p} = \hat{p}$ and $\bar{p} = \hat{p} + \varepsilon$ would bind. However, $\bar{p} = \hat{p} + \varepsilon$ would result in higher consumer surplus because $\bar{p} = \hat{p}$ is the optimal ceiling when $\eta = 0$, and it is lower than the optimal ceiling that would apply for any high demand realization (where $\eta > 0$). Hence, with great enough uncertainty, expected consumer surplus is larger at $\bar{p} = \hat{p} + \varepsilon$ than at $\bar{p} = \hat{p}$, and so the optimal price ceiling is higher than when there is no or little uncertainty.²²

We now compare the optimal ceiling first to the expected marketclearing price and then to the optimal ceiling under no uncertainty.

Corollary 1. With demand uncertainty and perfect competition, if $n_{\min} > n_0$, the optimal ceiling lies below the expected market-clearing price p_e^* . However, if $n_{\min} \le n_0$, the optimal ceiling might be greater or smaller than p_e^* , as CS_d is maximized at $\bar{p} \ge p_e^*$ when $-[1 - F(0)]c(B - C) - (b + c)\epsilon_d^L(0) \ge 0$.

Thus, with large enough uncertainty the optimal pro-consumer price ceiling can exceed p_e^* . The following example illustrates this.

Example 1. Let $\eta \sim U[-n, n]$. Then, $\epsilon_d^L(0) = -n/4$, $\mathcal{F}(0) = 1/2$, and $n_{\min} \leq n_0 \Leftrightarrow n \geq c(B-C)/(b+2c)$. Here, CS_d is maximized at $\bar{p} \geq p_e^*$ as $n \geq 2c(B-C)/(b+c)$. So, for $n \in [c(B-C)/(b+2c), 2c(B-C)/(b+c)]$ (for n > 2c(B-C)/(b+c)), the optimal ceiling is lower (higher) than p_e^* .

Although this section focuses on the role of regulatory uncertainty, the setting with no uncertainty in Section III is a special case where η has a

²²This intuition also applies when the regulator knows the demand intercept but faces uncertainty over the slope, which suggests that our results carry over unchanged to such an environment.

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degenerate distribution so that $n_{\min} = n_{\max} = 0$. With greater uncertainty (for $n_{\min} \le n_0$), a price ceiling in the middle region, $\bar{p} \in [p^*(n_{\min}), p^*(n_{\max})]$, is optimal. In this case, the no-uncertainty optimal ceiling \hat{p} also belongs to the middle region. Evaluating equation (9) at \hat{p} , we obtain

$$\frac{dCS_d(\bar{p})}{d\bar{p}}\Big|_{\bar{p}=\hat{p}} = -\frac{1}{c}\epsilon_d^L(n^*(\hat{p})) \ge 0,$$

where the weak inequality follows from $\epsilon_d^L(n^*(\hat{p})) \leq 0$, and holds with equality only for $n_{\min} = n_0$ (or, $p^*(n_{\min}) = \hat{p}$).

Corollary 2. With large enough uncertainty $(n_{\min} \le n_0)$, the optimal price ceiling is strictly higher than \hat{p} , the optimal ceiling with smaller or no uncertainty.

Thus, larger regulatory uncertainty calls for softer intervention, with the price ceiling set at a relatively high level compared to a case where there is no uncertainty.

V. Imperfect Competition

We now analyze the price ceiling that maximizes expected consumer surplus in the imperfectly competitive model presented in Section II. This framework, where suppliers have (some) market power, allows us to study the impact of the degree of competition on the optimal pro-consumer ceiling, and it can be interpreted as the reduced form of a model where firms compete in supply functions. However, we show that our analysis is also applicable in the limiting case of a monopoly market. Here, $\delta < 1$ measures competitive pressure, and a larger value corresponds to more intense competition.

With no uncertainty, the optimal pro-consumer price ceiling from Section III is still obtained with imperfect competition as consumer surplus is maximized at the same price level. Recall that aggregate marginal cost is the same under perfect and imperfect competition (see the discussion in Section II and footnote 14). A binding price ceiling becomes marginal revenue for all firms, and the total quantity is given by equating this ceiling with aggregate marginal cost, as in the perfectly competitive case. However, as we show below, this is no longer true with large enough uncertainty.

Consider a realization of demand η . Then, the equilibrium price in the imperfectly competitive market is given by

$$p^{\delta}(\eta, \delta) = \frac{c(B+\eta) + \delta bC}{\delta b + c} > p^*(\eta),$$

where $p^*(\eta)$ is the perfectly competitive price (see Figure 2).

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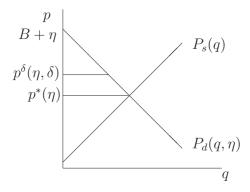


Fig. 2. Imperfectly competitive price

A price ceiling \bar{p} binds or not depending on its position relative to $p^{\delta}(\eta, \delta)$. If $\bar{p} \geq p^{\delta}(\eta, \delta)$, then the intervention does not bind and the imperfectly competitive market outcome prevails. If $\bar{p} < p^{\delta}(\eta, \delta)$, then the intervention binds and either demand or supply can be a constraint depending on the position of \bar{p} relative to the perfectly competitive price $p^*(\eta)$. More specifically, if $\bar{p} < p^*(\eta)$, the quantity traded will be $q^s(\bar{p})$ and there is excess demand. If $p^*(\eta) < \bar{p} < p^{\delta}(\eta)$, then the quantity traded will be $q^d(\bar{p})$ and there is excess supply.

Consider our supply function competition interpretation. If the market is unregulated, the firms compete by choosing price-quantity schedules. However, in the presence of a binding price ceiling, the firms can no longer adjust the price, so they can only choose optimally the output levels.²³ When the intervention binds, \bar{p} becomes the (constant) marginal revenue. Therefore, the firms will supply the quantity at which \bar{p} equals marginal cost $P^s(q)$ unless demand is a binding constraint, in which case they supply the quantity demanded at \bar{p} . So, the quantity traded in the market at the regulated price is min{ $q^d(\bar{p}), q^s(\bar{p})$ }, where $q^s(\bar{p})$ is the quantity at which marginal cost equals \bar{p} .²⁴ This is different from the perfectly competitive model where a binding ceiling could only result in excess demand.

As before, we examine different price regions as potential locations for the optimal price ceiling. The same three regions from Section IV apply,

²³In this sense, in a market where, without intervention, firms compete in supply functions, the introduction of a binding price ceiling leads to a change in competition as the firms become price-takers.

 $^{^{24}}q^s(p)$ is the same as the perfectly competitive supply. In contrast, $q^s(p, \delta)$ is the aggregate supply in the unregulated market where the firms compete in supply functions and $q^s(p, \delta) = \delta q^s(p)$.

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depending on the realization of η . For clarity, in this section, we will refer to these regions as (a'), (b'), and (c'). With imperfect competition, the potential outcomes for region (c') are more complicated than for region (c) in Section IV, because either demand or supply can bind. We outline the analysis for each region here but leave the details to the Appendix. There is a minor difference in the argument depending on whether $p^{\delta}(n_{\min}, \delta)$ (i.e., the ex post equilibrium price under imperfect competition for the lowest demand realization) is greater or smaller than $p^*(n_{\max})$ (i.e., the ex post equilibrium price under perfect competition for the highest demand realization).²⁵ We proceed on the assumption that $p^{\delta}(n_{\min}, \delta) < p^*(n_{\max})$ and cover the reverse case in footnote 27.²⁶

- (a') The price ceiling always binds ($\bar{p} < p^*(n_{\min})$). The corresponding analysis in Section IV carries over unchanged. So, if $p^{\delta}(n_{\min}, \delta) < p^*(n_{\max})$ and $n_{\min} > n_0$, the optimal pro-consumer price ceiling in this region is given by equation (5). However, if $n_{\min} \le n_0$, an optimal ceiling cannot be strictly lower than $p^*(n_{\min})$ as expected consumer surplus is increasing in \bar{p} .
- (b') The price ceiling never binds $(\bar{p} > p^*(n_{\max}))$. For values of η at which the ceiling binds, demand is a constraint, that is $\min\{q^d(\bar{p}), q^s(\bar{p})\} = q^d(\bar{p})$. Hence, a small decrease in \bar{p} leads to an increase in consumer surplus. At values of η where the ceiling does not bind, a decrease in the ceiling either has no effect on consumer surplus or, if it has, it boosts consumer surplus as the unregulated market price is above the competitive level for $\delta < 1$. In effect, an optimal price ceiling cannot belong to this region.
- (c') The price ceiling might or might not bind $(\bar{p} \in [p^*(n_{\min}), p^*(n_{\max})])$. We identify two subregions as potential locations for the optimal price ceiling, $[p^*(n_{\min}), p^{\delta}(n_{\min}, \delta)]$ and $(p^{\delta}(n_{\min}, \delta), p^*(n_{\max})]$. We sketch the arguments below and relegate the details to the Appendix.
 - (c'1) Consider, first, $\bar{p} \in [p^*(n_{\min}), p^{\delta}(n_{\min}, \delta)]$. As the upper bound $p^{\delta}(n_{\min}, \delta)$ is the lowest possible unregulated market price, the ceiling binds regardless of η . However, depending on η , the

²⁵The sign of $p^{\delta}(n_{\min}, \delta) - p^*(n_{\max})$ depends on all the parameters in the model. However, at least for a symmetric distribution where $\eta \in [-n, n]$, there is a cut-off level of uncertainty at $n = b(1-\delta)(B-C)/b(1+\delta) + 2c \equiv \hat{n}$. For $n > (<)\hat{n}, p^{\delta}(n_{\min}, \delta) - p^*(n_{\max}) < (>)0$.

²⁶Even if, for some values of δ , $p^{\delta}(n_{\min}, \delta) \geq p^*(n_{\max})$, there exists a cut-off value δ_0 , so that for $\delta \in [\delta_0, 1)$, $p^{\delta}(n_{\min}, \delta) < p^*(n_{\max})$. This is because $\lim_{\delta \to 1} p^{\delta}(n_{\min}, \delta) = p^*(n_{\min}) < p^*(n_{\max})$. When $\delta \to 1$, the market becomes almost perfectly competitive. The cut-off value δ_0 is implicitly defined by $p^*(n_{\max}) = p^{\delta}(n_{\min}, \delta_0)$.

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intervention can lead to excess demand or excess supply. The derivation is the same as in the perfectly competitive case (with the critical value $\eta = n^*(\bar{p})$), except that the upper bound to the region is at a higher price ceiling.

(c'2) For $\bar{p} \in (p^{\delta}(n_{\min}, \delta), p^*(n_{\max})]$, the price ceiling might or might not bind depending on the value of η . The critical value $\eta = n^*(\bar{p})$ again applies, and for high enough demand realizations $(\eta > n^*(\bar{p}))$ there is excess demand, so that $q = q^s(\bar{p})$. However, for lower demand realizations $(\eta \le n^*(\bar{p}))$ there is only excess supply if demand is not too low. If, for example, $\eta = n_{\min}$, the equilibrium unregulated price is $p^{\delta}(n_{\min}, \delta)$, which is below this subregion, and so the price ceiling does not bind. More generally, for values of η below a cut-off value $n^{**}(\bar{p}, \delta)$, the price ceiling does not bind and the quantity traded is $q^d(p^{\delta}(\eta, \delta))$.²⁷

In the Online Appendix, we show that for $n_{\min} > n_0$, the globally optimal price ceiling is strictly lower than $p^*(n_{\min})$ and given by equation (5), whereas for $n_{\min} \le n_0$ it lies in the interval $[p^*(n_{\min}), p^*(n_{\max})]$.²⁸ We are now ready to state the following result.

Proposition 2. For sufficiently large demand uncertainty $(n_{\min} \le n_0)$, the optimal pro-consumer price ceiling with imperfect competition is increasing with the degree of competition. For smaller uncertainty $(n_{\min} > n_0)$, it is independent of the degree of competition.

With no uncertainty, the optimal ceiling is independent of δ . However, with sufficient uncertainty, it is increasing with the degree of competition and, therefore, it is lower than the optimal ceiling in the perfectly competitive market. A decrease in the optimal ceiling generates significant gains in consumer surplus under high demand realizations. If the optimal ceiling is lower than $p^{\delta}(n_{\min}, \delta)$, so that it binds regardless of the realized demand, then it is independent of the degree of competition and is weakly lower than in the competitive case. If the optimal ceiling is higher than $p^{\delta}(n_{\min}, \delta)$, it might or might not bind depending on the realization of demand, and it is smoothly increasing with the degree of competition.

With great enough uncertainty, the optimal ceiling is lower if the market is less competitive. We use \bar{p}_c to denote the price ceiling that is optimal under perfect competition and we suppose it is set in an imperfectly

²⁸We show in the Appendix that expected consumer surplus is single peaked.

²⁷If $p^{\delta}(n_{\min}, \delta) \ge p^*(n_{\max})$, the analysis is qualitatively the same as we have outlined in the text, except in one respect. By definition, subregion (c'2) does not exist. Intuitively, the analysis in (c'1) applies now to the entire range.

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competitive market. For those high-demand realizations for which \bar{p}_c binds under perfect competition, it will also bind under imperfect competition, and so the same outcome obtains regardless of the degree of competition. In contrast, for those demand realizations for which \bar{p}_c does not bind under perfect competition, the price obtained under imperfect competition (either $p^{\delta}(\eta)$ or \bar{p}_c , depending on the value of η) is higher than the perfectly competitive price (i.e., the market-clearing price $p^*(\eta)$). However, for any given demand realization η , consumer surplus is maximized at a price $\hat{p}(\eta) < p^*(\eta)$. Thus, for each possible lower demand realization, price under perfect competition exceeds the corresponding optimal price ceiling, and under imperfect competition is greater still. To limit such effects, the optimal ceiling under imperfect competition is lower than that under perfect competition, and it decreases with the degree of market power. In this sense, our analysis shows that, with sufficient regulatory uncertainty, competitive pressure weakens the scope for pro-consumer regulatory intervention.²⁹

In our imperfect competition model, aggregate output is a fraction δ of the competitive supply. This result builds on the supply function competition microfoundation and, in the Online Appendix, we show that $\delta \geq 2c/(c + \sqrt{c(2b + c)})$ for $N \geq 2$. However, the reduced-form model with an output restriction can also capture a monopoly market when $\delta = c/(b + c)$. Therefore, the analysis in this section directly applies to a market with a monopoly supplier.

VI. Inefficient Rationing

We now focus on the impact of rationing inefficiency on the optimal proconsumer price ceiling under perfect competition. We show that, if rationing efficiency α is great enough, the qualitative results from Section IV still hold, although the level of the optimal ceiling might depend on the value of α . We identify a cut-off rationing efficiency below which a price ceiling should not be set.

We use the three regions for the optimal ceiling specified in Section IV. In region (b), as a price ceiling never binds ($\bar{p} > p^*(n_{\text{max}})$), expected consumer surplus is unaffected by rationing inefficiency and so is given by equation (8). However, in region (c), supply might be a binding constraint and, in region (a), it surely is. So, for these regions, inefficiency of rationing plays an important role. For regions (a) and (c), we write the regulator's

 $^{^{29}}$ We focus here on the optimal ceiling that maximizes expected consumer surplus in the presence of regulatory uncertainty under imperfect competition. Our intuition is that, in this setting, the expected welfare maximizing ceiling would be at or above the expected market-clearing price and – as the optimal pro-consumer ceiling – is increasing with the degree of competition.

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objective function as the weighted sum of expected surplus under fully efficient rationing (with weight $\alpha \in [0, 1]$) and under extremely inefficient rationing (with weight $1 - \alpha$). Below, we outline the basic reasoning underlying the analysis of inefficient rationing, but the full derivation is relegated to the Online Appendix.

When supply binds for a given price ceiling \bar{p} , output $q^s(\bar{p}) = (\bar{p} - C)/c$ is bought by the consumers with the lowest valuations amongst those willing to pay at least \bar{p} . Then, the $q^s(\bar{p}) = (\bar{p} - C)/c$ units available are purchased by consumers along the lowest part of the demand curve at and above \bar{p} (i.e., from $q^d(\bar{p}) - q^s(\bar{p})$ to $q^d(\bar{p})$). For a given realization of demand η , at $q^d(\bar{p}) - q^s(\bar{p})$ consumer surplus per unit is $B + \eta - b(q^d(\bar{p}) - q^s(\bar{p})) - \bar{p}$, while at $q^d(\bar{p})$ it is zero. So, using equation (1), total consumer surplus is then $b(\bar{p} - C)^2/2c^2 \equiv CS^L_{d0}$ (and independent of η). We use CS^L_{d0} to calculate expected consumer surplus under extremely inefficient rationing, taking into account that in region (a) supply always binds, whereas in region (c) it binds only for $\eta \ge n^*(\bar{p})$.

Below, we extend Proposition 1 for arbitrary values of α . To do so, we define a critical level of the price ceiling and a threshold degree of uncertainty, which generalize the value in equation (5) and Definition 1, respectively, for arbitrary rationing efficiency α :

$$\hat{p}(\alpha) = \frac{\alpha c(B+C) - (1-2\alpha)bC}{2\alpha(b+c) - b}$$
(10)

$$n_0(\alpha) = -\frac{[\alpha(b+c)-b](B-C)}{2\alpha(b+c)-b}.$$
 (11)

Both $\hat{p}(\alpha)$ and $n_0(\alpha)$ are well defined for $\alpha \neq b/2(b+c)$. For $\alpha = 1$, $\hat{p}(\alpha)$ reduces to the value specified in equation (5) and $n_0(\alpha) = n_0$.

Proposition 3. Assume perfect competition. For rationing efficiency $\alpha > b/(b + c)$, there is a unique price ceiling that globally maximizes expected consumer surplus: if $n_{\min} > n_0(\alpha)$, this optimal ceiling is given by equation (11) and always binds; while if $n_{\min} \le n_0(\alpha)$, it lies in the interval $[p^*(n_{\min}), p^*(n_{\max}))$. For rationing efficiency $\alpha \le b/(b + c)$, any price ceiling decreases expected consumer surplus.

This proposition highlights the combined effects of rationing efficiency and the degree of uncertainty on the optimal ceiling. Provided that $\alpha > b/(b+c)$, the qualitative conclusions in Section IV carry over. If uncertainty is relatively small $(n_{\min} > n_0(\alpha))$ a price ceiling in the low region (a), which is sure to bind, is optimal. This situation is illustrated in the right panel of Figure 1. If uncertainty is greater $(n_{\min} \le n_0(\alpha))$, the optimal ceiling is in region (c) and might or might not bind. The critical uncertainty level, as represented by $n_0(\alpha)$, is decreasing with α . Thus, the greater the rationing

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efficiency, the greater the maximum amount of uncertainty for which the optimal ceiling lies in the low region, and this binds for sure. The condition $\alpha > b/(b + c)$ is consistent with a wide range of inefficiency; for example, if demand is less steep than supply (b < c), it is consistent with random rationing $(\alpha = 1/2)$.

For large uncertainty $(n_{\min} \le n_0(\alpha))$ and sufficiently efficient rationing $(\alpha > b/(b + c))$, the optimal ceiling can lie above or below the expected market-clearing price. In the Online Appendix, we present a condition that generalizes Corollary 1, and also shows that, when rationing efficiency α is smaller (but $\alpha > b/(b + c)$), the level of demand uncertainty required for \bar{p} to exceed p_e^* is greater.

When instead $\alpha \leq b/(b+c)$, a price ceiling should not be set, regardless of the amount of demand uncertainty. If rationing efficiency is this low, price regulation has a large allocative cost that eliminates the scope for pro-consumer intervention. If b > c, this non-intervention result holds even for random rationing; but, if b < c, intervention can increase expected consumer surplus even with worse than random rationing.

If uncertainty is great enough $(n_{\min} \le n_0)$, then, generalizing our result for efficient rationing, the optimal price ceiling lies in region (c) and is strictly higher than $\hat{p}(\alpha)$, the optimal ceiling with smaller or no uncertainty. Moreover, Proposition 3 allows us to characterize fully the relationship between the efficiency of rationing α and the optimal price ceiling.

Corollary 3. With perfect competition, for $\alpha \ge b/(b + c)$, the optimal proconsumer price ceiling is strictly decreasing with the rationing efficiency α .

Thus, whenever it is optimal to set a price ceiling that can bind, there is a negative relationship between the optimal level and the efficiency of rationing.

VII. Conclusions

We explore the impact of market conditions on optimal price ceiling regulation in a setting where the regulator maximizes expected consumer surplus and is imperfectly informed about demand. Under perfect competition, regulatory uncertainty does not eliminate the rationale for price ceiling intervention, but sufficient uncertainty calls for softer intervention, with the ceiling set at a relatively high level. Under imperfect competition, if there is sufficient uncertainty, the optimal ceiling increases with the degree of competition, and so competitive pressure justifies less restrictive regulatory intervention. This result is broadly consistent, for example, with Oftel's decision in 2002 to increase the price ceiling imposed on British Telecom once new suppliers entered the telecommunications market. We extend the perfect competition model to allow for rationing inefficiency and we identify a cut-off level of rationing inefficiency above which a ceiling should not be used. Above this level, our qualitative results from the model with efficient rationing carry over unchanged.

We focus on demand uncertainty, but our results are qualitatively robust in settings with supply uncertainty only, or where the regulator faces both demand and supply uncertainty, as we formally show in the Online Appendix. For tractability, we focus on linear demand and supply, but the intuition suggests that our results are qualitatively robust to more general assumptions.³⁰ Likewise, the main insights would be relevant in settings where the regulatory standard is a weighted sum of consumer surplus and profit.

Appendix

Preliminary Analysis

Proof of Lemma 1: (a) At $\bar{p} \ge p^*$, $dCS(q^d(p^*))/d\bar{p} = 0$. (b) When $\bar{p} < p^*$, the first-order condition $\partial CS_d^L/\partial \bar{p} = 0$ gives equation (5). The second-order condition is always satisfied. The optimal ceiling lies in (C, p^*) , so is well defined.

Perfect Competition

(c) The price ceiling might or might not bind

Remark 1. Equation (7) implies that $prob(p^* \leq \bar{p}) = prob(\eta \leq n^*(\bar{p})) = \mathcal{F}(n^*(\bar{p})).$

Using Remark 1, expected consumer surplus conditional on $\bar{p} \geq p^*(\eta)$ is given by

$$E[CS(q_d^*) \mid \eta \le n^*(\bar{p})] = \frac{\int_{n_{\min}}^{n^*(p)} CS(q_d^*) d\mathcal{F}(\eta)}{\mathcal{F}(n^*(\bar{p}))} \equiv CS_d^*.$$
(A1)

Substituting for $CS(q_d^*) = b(B + \eta - C)^2/2(b + c)^2$ in equation (A1), and using $\epsilon_d^L(n^*(\bar{p})) = \int_{n_{\min}}^{n^*(\bar{p})} \eta d\mathcal{F}(\eta)$ and $\Upsilon_d^L(n^*(\bar{p})) = \int_{n_{\min}}^{n^*(\bar{p})} \eta^2 d\mathcal{F}(\eta)$, we have $CS^*_{*} = \frac{b[(B - C)^2 \mathcal{F}(n^*(\bar{p})) + 2(B - C)\epsilon_d^L(n^*(\bar{p})) + \Upsilon_d^L(n^*(\bar{p}))]}{2}$.

$$CS_d^* = \frac{b[(B-C)^{-}\mathcal{F}(n(p)) + 2(B-C)\epsilon_d^{-}(n(p)) + 1_d^{-}(n(p))]}{2(b+c)^2\mathcal{F}(n^*(\bar{p}))}$$

³⁰More precisely, as long as demand and supply (marginal cost) are well behaved, demand is finite for all positive prices, and there is scope for trade ex post, then the intuitive arguments carry over.

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The expected consumer surplus conditional on $\bar{p} \leq p^*(\eta)$ is

$$E[CS(q^s(\bar{p}),\eta) \mid \eta \ge n^*(\bar{p})] = \frac{\int_{n^*(\bar{p})}^{n_{\max}} CS(q^s(\bar{p}),\eta) d\mathcal{F}(\eta)}{1 - \mathcal{F}(n^*(\bar{p}))} \equiv CS_d^S.$$
(A2)

Substituting for $CS(q^s(\bar{p}) \text{ in equation (A2), and letting } \epsilon_d^H(n^*(\bar{p})) = \int_{n^*(\bar{p})}^{n_{\max}} \eta d\mathcal{F}(\eta)$, we obtain

$$\frac{(\bar{p}-C)[2c(B-\bar{p})-b(\bar{p}-C)]}{2c^2} + \frac{(\bar{p}-C)\epsilon_d^H(n^*(\bar{p}))}{c(1-\mathcal{F}(n^*(\bar{p})))} \equiv CS_d^S.$$
 (A3)

Total expected consumer surplus for any given price ceiling $\bar{p} \in [p^*(n_{\min}), p^*(n_{\max})]$ is

$$E[CS(\bar{p})] = \mathcal{F}(n^*(\bar{p}))CS_d^* + (1 - \mathcal{F}(n^*(\bar{p})))CS_d^S \equiv CS_d.$$
(A4)

Proof of Lemma 3: It is easy to see from equations (4), (8), and (A4) that expected consumer surplus is piecewise continuous and differentiable. So we focus on the continuity and differentiability of the expected consumer surplus at $p^*(n_{\min})$ and $p^*(n_{\max})$.

Continuity at $p^*(n_{\min}) = [c(B + n_{\min}) + bC]/(b + c) : \lim_{\bar{p} \nearrow p^*(n_{\min})} CS_d^L(\bar{p}) = CS_d^S(p^*(n_{\min}))$, where CS_d^S is given in equation (A3). The equality follows as $\mathcal{F}(n_{\min}) = \epsilon_d^H(n_{\min}) = 0$. Because $\Upsilon_d^L(n_{\min}) = \epsilon_d^L(n_{\min}) = 0$, then $\lim_{\bar{p} \nearrow p^*(n_{\min})} CS_d^L(\bar{p}) = CS_d(n_{\min})$ so the result follows.

Continuity at $p^*(n_{\max})$: as $\mathcal{F}(n_{\max}) = 1$, $\epsilon_d^L(n_{\max}) = 0$ and $\Upsilon_d^L(n_{\max}) = E(\eta^2)$, then $CS_d(n_{\max}) = CS_d^*(n_{\max}) = \lim_{\bar{p} \searrow p^*(n_{\max})} CS_d^H(\bar{p}) = CS_d^H$ and the result follows.

Differentiability at $p^*(n_{\min})$: in region (a), $\lim_{\bar{p} \nearrow p^*(n_{\min})} \partial CS_d^L / \partial \bar{p} = [c(B-C) - (p^*(n_{\min}) - C)(b+2c)]/c^2$. In region (c), as $\epsilon_d^L(n_{\min}) = \mathcal{F}(n_{\min}) = 0$, $\partial CS_d(p^*(n_{\min})) / \partial \bar{p} = \lim_{\bar{p} \nearrow p^*(n_{\min})} \partial CS_d^L / \partial \bar{p}$. The result follows.

Differentiability at $p^*(n_{\max})$: in region (c), using $\partial CS_d/\partial \bar{p}$ given in equation (9), along with $\epsilon_d^L(n_{\max}) = 0$ and $\mathcal{F}(n_{\max}) = 1$, it follows that $\partial CS_d(p^*(n_{\max}))/\partial \bar{p} = 0$. As equation (8) is independent of \bar{p} , $\lim_{\bar{p} \to p^*(n_{\max})} \partial CS_d^H/\partial \bar{p} = 0$. The result follows.

The second part of the lemma follows, as expected consumer surplus is continuous at $p^*(n_{\text{max}})$ and equation (8) is independent of \bar{p} .

Proof of Proposition 1: Suppose that $n_{\min} \leq n_0$. From equation (9),

$$\frac{d^2 C S_d}{d\bar{p}^2} = \frac{-(b+2c)[1-\mathcal{F}(n^*(\bar{p}))] + (b+c)(\bar{p}-C)\mathcal{F}'(n^*(\bar{p}))}{c^2}$$

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As $\epsilon_d^L(n_{\max}) = E(\eta) = 0$ and $\mathcal{F}(n_{\max}) = 1$, $p^*(n_{\max})$ satisfies the firstorder condition in region (c). CS_d is convex at this point, and so $p^*(n_{\max})$ is a local minimum. Hence, CS_d is decreasing with \bar{p} as it approaches $p^*(n_{\max})$ from below. Also, by Lemma 3, all $\bar{p} > p^*(n_{\max})$ give the same level of expected consumer surplus as $\bar{p} = p^*(n_{\max})$. Using equations (7) and (9), CS_d is increasing at $p^*(n_{\min})$ iff $n_{\min} \leq n_0$. Moreover, by Lemma 2, if $n_{\min} \leq n_0$, there is no candidate optimal ceiling strictly below $p^*(n_{\min})$. Hence, if $n_{\min} \leq n_0$, the global optimal ceiling must belong to $[p^*(n_{\min}, p^*(n_{\max}))$ and is unique, and

$$sign\frac{d^2CS_d}{d\bar{p}^2} = sign\left\{\frac{\mathcal{F}'(n^*(\bar{p}))/[1 - \mathcal{F}(n^*(\bar{p}))] - (b + 2c)}{c^2(b + c)(\bar{p} - C)}\right\},\$$

where $\mathcal{F}'(n^*(\bar{p}))/[1 - \mathcal{F}(n^*(\bar{p}))]$ is, by assumption, strictly increasing on $[p^*(n_{\min}), p^*(n_{\max})]$. As $1/(\bar{p} - C)$ is strictly decreasing with \bar{p}, CS_d has a unique inflexion point, p_I^d . Because, at $p^*(n_{\max}), d^2CS_d/d\bar{p}^2 > 0$, so CS_d is convex for all $\bar{p} \in (p_I^d, p^*(n_{\max}))$. However, if $\bar{p} < p_I^d$, then $1/(\bar{p} - C)$ is greater and the hazard rate is smaller, so that $d^2CS_d/d\bar{p}^2 < 0$ for all $\bar{p} \in (p^*(n_{\min}), p_I^d)$. Thus, when $n_{\min} \le n_0$ there is a unique globally optimal price ceiling in $[p^*(n_{\min}), p^*(n_{\max}))$.

Now suppose $n_{\min} > n_0$. For $\bar{p} > p^*(n_{\max})$, the ceiling does not bind and CS_d is the same as for $\bar{p} = p^*(n_{\max})$. For $\bar{p} < p^*(n_{\min})$, by Lemma 2 CS_d is maximized at $\bar{p} = \hat{p}$. Lastly, consider the region $\bar{p} \in [p^*(n_{\min}), p^*(n_{\max})]$. From (7) and (9) $dCS_d/d\bar{p} < 0$ at $p^*(n_{\min})$ and so, from our argument above, $dCS_d/d\bar{p} < 0$ for the whole region. Hence, across the three regions CS_d is maximized at $\bar{p} = \hat{p}$.

Proof of Corollary 1: For $n_{\min} > n_0$, the result follows from equations (3) and (5). For $n_{\min} \le n_0$, we evaluate $dCS_d/d\bar{p}$ at $\bar{p} = p_e^*$ as given in equation (3), and we obtain

$$\frac{dCS_d(p_e^*)}{d\bar{p}} = -\frac{(1-\mathcal{F}(0))(B-C)}{b+c} - \frac{\epsilon_d^L(0)}{c}.$$

The second term is non-positive, while the first is non-negative as $\epsilon_d^L(0) < 0$. Depending on the sign of $dCS_d(p_e^*)/d\bar{p}$, CS_d is maximized at $\bar{p} \gtrless p_e^*$. \Box

Imperfect Competition

Analysis for region (c'). As $p^{\delta}(n_{\min}, \delta) \in [p^*(n_{\min}), p^*(n_{\max})]$, we explore two subregions $[p^*(n_{\min}), p^{\delta}(n_{\min}, \delta)]$ and $(p^{\delta}(n_{\min}, \delta), p^*(n_{\max})]$.

(c'1) If $\bar{p} \in [p^*(n_{\min}), p^{\delta}(n_{\min}, \delta)]$, the ceiling binds regardless of η . For a given $\bar{p}, \exists \eta = n^*(\bar{p})$ s.t. $p^*(\eta) = \bar{p}$. This is the same as $n^*(\bar{p})$ in equation (7). If $\bar{p} \ge p^*(\eta)$ (i.e., if $\eta \le n^*(\bar{p})$), there is excess supply,

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so consumer surplus is determined by $q^d(\bar{p})$. If $\bar{p} < p^*(\eta)$ (i.e., if $\eta > n^*(\bar{p})$), then there is excess demand, so consumer surplus is determined by $q^s(\bar{p})$, the quantity at which marginal cost equals \bar{p} . Let CS^L_{δ} be the expected consumer surplus in this case. Then, using $\epsilon^L_d(n^*(\bar{p}))$ as defined in Section IV, $dCS^L_{\delta}/d\bar{p}$ is given by

$$-\frac{1}{b}(B-\bar{p}) - \frac{b+c}{bc}\epsilon_d^L(n^*(\bar{p})) + \frac{(b+c)[c(B-C) - (b+c)(\bar{p}-C)]}{bc^2} \times [1 - \mathcal{F}(n^*(\bar{p}))].$$
(A5)

(c'2) For $\bar{p} \in (p^{\delta}(n_{\min}, \delta), p^*(n_{\max})]$, the ceiling might or might not bind, depending on η . There is a cut-off η . Let this be $n^{**}(\bar{p}, \delta)$, implicitly defined by $p^{\delta}(n^{**}, \delta) = \bar{p}$, so that for $\eta < n^{**}(\bar{p}, \delta)$ the ceiling does not bind and the quantity traded is $q^d(p^{\delta}(\eta, \delta))$. For $\eta \ge n^{**}(\bar{p}, \delta)$, the ceiling can lead to excess demand or excess supply depending on the value of η . Specifically, $\exists \eta = n^*(\bar{p})$ for which $p^*(\eta) = \bar{p}$. This is the same as in equation (7), and $n^{**}(\bar{p}, \delta) < n^*(\bar{p})$. If $n^{**}(\bar{p}, \delta) \le \eta \le n^*(\bar{p})$, there is excess supply, so that consumer surplus is determined by $q^d(\bar{p})$. If $\eta > n^*(\bar{p})$, there is excess demand and consumer surplus is determined by $q^s(\bar{p})$, the quantity at which marginal cost equals \bar{p} . Let CS^H_{δ} be the expected consumer surplus in this case. Then, $dCS^H_{\delta}/d\bar{p}$ is given by

$$-\frac{1}{b} (B - \bar{p})[\mathcal{F}(n^{*}(\bar{p})) - \mathcal{F}(n^{**}(\bar{p}, \delta))] - \frac{b + c}{bc} \epsilon_{d}^{L}(n^{*}(\bar{p}))$$
(A6)
$$+\frac{1}{b} \epsilon_{d}^{L}(n^{**}(\bar{p}, \delta)) + \frac{c(B - \bar{p}) - (b + c)(\bar{p} - C)}{c^{2}} [1 - \mathcal{F}(n^{*}(\bar{p}))],$$

where $n^{**}(\bar{p}, \delta) = [(\delta b + c)p - cB - \delta bC]/c$ and $\epsilon_d^L(n^{**}(\bar{p})) = \int_{n_{\min}}^{n^{**}(\bar{p})} \eta d\mathcal{F}(\eta).$

Proof of Proposition 2: Suppose $n_{\min} > -c(B - C)/(b + 2c)$. Then, the globally optimal price ceiling is given by equation (5) and is independent of δ .

Suppose $n_{\min} < -c(B-C)/(b+2c)$. Let $p^{\delta}(n_{\min}, \delta) < p^*(n_{\max})$. If the globally optimal ceiling lies in $[p^*(n_{\min}), p^{\delta}(n_{\min}, \delta))$, it solves $dCS_{\delta}^L/d\bar{p} = 0$ (see equation (A5)). Evaluating equation (A5) at the ceiling that solves $dCS_d/d\bar{p} = 0$ (i.e., the optimal ceiling under perfect competition; see equation (9)), we obtain

$$-\frac{(B-\bar{p})\mathcal{F}(n^*(\bar{p}))+\epsilon_d^L(n^*(\bar{p}))}{h}<0.$$

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The inequality follows as

$$\frac{\epsilon_d^L(n^*(\bar{p}))}{\mathcal{F}(n^*(\bar{p}))} = E(\eta \mid \eta < n^*(\bar{p})) \in [n_{\min}, n_{\max}].$$

If the globally optimal ceiling lies in $[p^{\delta}(n_{\min}, \delta), p^*(n_{\max}))$, it solves $dCS^H_{\delta}/d\bar{p} = 0$ (see equation (A6)). Whenever CS^H_{δ} has an interior maximum in the interval $(p^{\delta}(n_{\min}, \delta), p^*(n_{\max})]$, the optimal ceiling is increasing with δ . This follows from the local concavity of CS^H_{δ} at the optimal ceiling and from

$$\frac{d(CS_H^o)^2}{d\bar{p}\,d\delta} = \frac{\delta b(\bar{p}-C)^2 \mathcal{F}'(n^{**}(\bar{p},\delta))}{c^2} > 0.$$

If the optimal price ceiling with imperfect competition lies in this subregion, it is strictly lower than the optimal ceiling with perfect competition. Let $p^{\delta}(n_{\min}, \delta) \ge p^*(n_{\max})$. Then, the globally optimal ceiling lies in $[p^*(n_{\min}), p^*(n_{\max}))$ and solves $dCS^L_{\delta}/d\bar{p} = 0$. The above comparison with the optimal ceiling under perfect competition applies, and the result follows.

Supporting Information

Additional supporting information may be found online in the Supporting Information section at the end of the article.

Online Appendix

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