Surrogate Thermal Model for Power Electronic Modules using Artificial Neural Network

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Abstract-Virtual prototyping of power electronic modules aims to allow rapid evaluation of potential designs without building and testing physical prototypes. Among the interests in thermal models of the virtual modules, process of compact thermal models needs effective methodology to fast generate small models describing the thermal performance of a potential design. This study chooses the Generalized Minimized Residual (GMRES) Algorithm to process thermal models due to its efficiency. Based on that, a machine learning aided surrogate model is proposed for the prediction of thermal performance since existing approaches take much time to determine the thermal response to a particular input power. This surrogate model is created by training a dedicated artificial neural network (ANN) on simulation data, after that this model can quickly map the module temperature and the power input in time domain. In the training process, crossvalidation method is introduced to determine which neuron structure should be selected for the practical data generated by thermal equations. The test group is noted in cross-validation to give the prediction performance of structure candidates. To verify the proposed method, the resulting data of trained surrogate models are compared with the accurate simulation data after the ANN based cross-validation.

Keywords— Artificial Neural Network (ANN), cross-validation, power electronic device (PED), thermal model, Generalized Minimized Residual (GMRES)

I. INTRODUCTION

Power electronic device (PED) is the core component of electrical power system (EPS) and it is now widely applied in not only electrical power transmission but electrical transportation [1]. However, it is usually operated under a high input/output power and produces considerable amount of heat, especially for that in rapid switching circuits. Therefore, PED is easy to be damaged for long-time usage and overheating owing to the limitation of their junction temperature [2]. Chen et al. [3] pointed out that repetitive thermal cycling leads to problems of PED like cracks, voids and delamination due to different CTEs (coefficients of thermal expansions). On the other hand, the trend of PED design and manufacture is to make it smaller with higher efficiency and longer lifetime which highlights the importance of effective thermal management [4]. Namely, it is crucial to analyze, design and optimize the thermal models of PED for the best balance between the reliability, performance and other metrics. Fig. 1 shows a typical application of power electronic device. Most of power loss in PED is transferred to thermal energy heating it, referred as P_{loss} in this figure.



Fig.1. A typical application of PED

To address the thermal problems, virtual prototyping technique has been developed for predicting electrical and thermal effects of a power electronic module before constructing an actual prototype of PED [5]. This technique can help designers modify and re-simulate their thermal modules in a loop to finally get the best design. The design process mainly involves model generation, simulation and performance evaluation. Due to the high-frequency switching of PED and its application in the complex EPS, one of the challenges for this virtual technique is the ability to generate signals in a short time using limited computational resource. Compact thermal model is therefore utilized to build system simulation model from geometry data since it has high computational efficiency. Large system thermal equations can be modeled by finite-difference discretization and then reduced to smaller ones in order to get efficient computation [6].

Many researchers focus in the Design for Reliability (DfR) area have mostly been on investigating the thermal loading of power devices [7, 8]. Nevertheless, these investigations in the existing literature are made on PEDs whose design parameters are initially fixed. This means that every time a designer would

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like to check how different design parameters affect the temperature distribution, he would need to exercise the timeconsuming simulations or experiments all over again. The aim of this paper is to bridge this research gap by building a dedicated surrogate thermal model based on the training of artificial neural network (ANN), a well-known method in artificial intelligence (AI). We take advantage of this surrogate model to estimate the temperature variation of any device with regards to input power and time. The estimation would be several orders of magnitude faster compared to running the detailed simulation model.

The rest of the paper is organized as follows: Section II describes the background and fundamentals of thermal model with applied simulation method. In Section III, basic ANN theory is briefly discussed and two different ANN designs are given for comparative studies. In addition, the cross-validation method of ANN model is introduced in Section IV, aimed at choosing the best structure according to the mean error of prediction. Lastly, the case study in Section V shows that the applied surrogate model can predict the temperature variation of a new input power with the error less than 0.1 °C after training the simulation data.

II. THERMAL SIMULATION BASED ON COMPACT THERMAL MODEL

The studied thermal compact model for PED is based on heat equations. The relation among inner heat generation, material and thermal conduction is a conservation of energy problem which is presented in (1). This equation states that any internal heat generation of an object must keep balance with the sum of heat flux that responsible for object temperature changing and flowing through the object.

$$c\rho \frac{\partial T}{\partial t} + \nabla \cdot \vec{q} = q_{int} \tag{1}$$

where c is the object's material specific heat capacity, J/(kg×K); ρ is mass density, kg/m³; T is temperature, K; t is time, second; \vec{q} is heat flux vector, W/m²; q_{int} is object internal heat generation, W/m³.

According to Fourier's Law, heat flux can be expressed as (2), where k represents for the thermal conductivity of this object, unit $W/(m \times K)$, which can be assumed as a constant or piecewise constant in compact thermal model.

$$\vec{q} = -k\nabla T \tag{2}$$

Therefore,

$$c\rho \frac{\partial T}{\partial t} - k\nabla^2 T = q_{int} \tag{3}$$

For a 3-dementional Cartesian system, this formula is:

$$c\rho \frac{\partial T}{\partial t} - k \cdot \left(\frac{\partial^2 T}{\partial x^2} + \frac{\partial^2 T}{\partial y^2} + \frac{\partial^2 T}{\partial z^2} \right) = q_{int}$$
(4)

This formula discretizes thermal conduction problem spatially by separating it into smaller region and using the approximately adjacent regions substituting the spatial partial derivatives to simplify calculation. Finite difference method (FDM) solves infinite continuous problem by converting it to finite point parameters. In this method, temperature distribution is divided into lots of discrete points and the central difference approximations are used to substitute the second order spatial derivatives. Assuming the distance between two adjacent discrete point (node) are δx , δy and δz (for x, y, z direction respectively). Fig. 2 sketches the 2-dimensional structure of mesh near node i, j, k in Y-Z plane, this node can be expressed by (5).

$$T(i, j, k) = (i\delta x, j\delta y, k\delta z)$$
(5)



Fig.2. 2-dimensional node finite-difference mesh in Y-Z Plane

For node i,j,k, the approximately first order temperature partial for z-derivatives are expressed by:

$$\partial \frac{T(i,j,k-1)}{\sigma} \approx \frac{T_{i,j,k} - T_{i,j,k-1}}{\sigma}$$
(6)

$$\partial \frac{T(i,j,k+1)}{\partial z} \approx \frac{T_{i,j,k+1} - T_{i,j,k}}{\delta z}$$
(7)

Then, second order z-derivative of central difference approximation can be given by:

$$= \frac{\partial^2 \frac{T(i,j,k)}{\partial z^2}}{\frac{T_{i,j,k+1}}{\partial z} - \frac{\partial \frac{T_{i,j,k+1}}{\partial z}}{\frac{\delta z}{\delta z}}}{\frac{\delta z}{(\delta z)^2}}$$
(8)

Similar equation can be found for x-derivative and yderivative. Then (4) can be expressed as:

$$\delta v c \rho \frac{\partial T_{i,j,k}}{\partial t} - k \cdot \left(\frac{\delta y \delta z}{\delta x} (T_{i+1,j,k} + T_{i-1,j,k} - 2T_{i,j,k}) + \frac{\delta x \delta z}{\delta y} (T_{i,j+1,k} + T_{i,j-1,k} - 2T_{i,j,k}) \right)$$

$$+ \frac{\delta x \delta z}{\delta y} (T_{i,j,k+1} + T_{i,j,k-1} - 2T_{i,j,k})$$

$$- 2T_{i,j,k}) = \delta v q_{i,j,k}$$
(9)

In this equation δv represents for a small volume ($\delta v = \delta x \delta y \delta z$). In a 3-d equivalent mesh, there is an electrical equivalent circuit existing in every node of the finite difference mesh, this equivalent circuit is the basic unit of the mesh. Meshing details can be found in Section 3.2.3 of [9]. For each

node there is a set of thermal resistances only depends of the material property.

Ultimately, the nodal temperatures can be described by a matrix equation, (10), in which M, A and B are matrices representing for nodal thermal capacities, internode thermal conductivities and heat source respectively. \vec{U} is a vector which involves two elements, ambient temperature T_a and input power P_{in} . T is the instantaneous temperature which can be solved by utilising time-stepping integration algorithm in time-domain.

$$[M]\frac{d\vec{T}}{dt} - [A]\vec{T} = [B]\vec{U}$$
 (10)

For steady state, dT/dt=0, thus the initial temperature T_0 can be obtained. In time dependent situation, $dT=T_n-T_{n-1}$, (10) can be rewritten as (11), in which *h* is the time step between two frames, T_n is instantaneous temperature, T_{n-1} is the previous temperature.

$$([M] - h[A])T_n = h[A]T_{n-1} + h[B]\vec{U}$$
(11)

The time dependent temperature distribution of PED model can be found by solving (11). Since the matrices are very large, this process can be time-consuming. The matrices A and M in (11) are very sparse because there are only several elements per row are nonzero elements in [A], while for [M], only those elements on diagonal are non-zero. Therefore, Compressed Sparse Row (CSR) format is applied to reduce most of computational time and resources spent on zero multiplying other values. After using CSR, Generalized Minimal Residual Method (GMRES) is utilised to solve the matrix equation and generate instantaneous temperature distribution of this model. This method does not solve the equation directly but guessing the temperature T_n and multiplying the estimate value and matrix until the results meet the accuracy requirements. In summary, time consumption of GMRES depends on the sparse of matrices, the initial value of input vector and the tolerance requirement, thus it is a fast solution. More details can be found in [6].

In time domain, the temperature effect of PED will increase gradually from an initial temperature to the steady state temperature with regards to a certain input power. In this procedure, the average temperature of nodes in the studied module is used to plot the temperature variation under each power condition. Even applying GMRES in compact thermal model, time cost of simulation will probably be a little bit long because for every input power tens of thousand times of matrix operation need to be finished before the temperature reaching to the steady state, especially for the module which is divided into large number of small cubes.

III. ANN BASED MODELING

As explained above, it is essential to establish a simple thermal model of power electronic module that would be able to translate the power and time data into temperature variation. The state of art approaches deal with this task by simulating the detailed model of electronic modules. However, the detailed model is very complex thus the simulation usually suffers from the inefficient use of memory space. In order to come around this difficulty, this paper proposes the usage of a forward artificial neural network (ANN) to serve as a fast, dedicated and flexible surrogate model of electronic module.

ANN is based on a nonparametric regression model which is a technique for supervised learning. User does not need to specify the relationship between the predictors (input) and responses (output) with a predetermined regression function since ANN will learn them automatically by using only several training parameters (i.e. weights and bias).

A. ANN fundamentals

This study selects forward ANN as the surrogate thermal model. Although feedforward ANN is the simplest type of ANN devised, it has been applied already to various electrical engineering problems, from predicting the voltage distortion in electrical distribution networks [10], to reliability study of power electronic systems [11].

A basic forward ANN comprises an input layer, one or more hidden layers, and an output layer. To calculate the output of a certain neuron n_i^l in layer l (l > 1), the outputs of all the neurons p_j^{l-1} ($j = [1..N_{l-1}]$, N_{l-1} is the neuron number of Layer l - 1) are multiplied with given weights ω_{ij}^l and then the bias b_i^l is added. The result is processed through an activation function f_{σ} that usually takes the form of a sigmoid function, i.e. $f_{\sigma}(z) = 1/(1 + e^{-z})$, to generate the output p_i^l . This output then becomes one of the inputs for the next layer, l + 1, and the same procedure is repeated to calculate the output of other neurons in layer l.

In Layer 1 (input layer), p_i^1 takes the form of inputs through the neuron n_i^1 , no bias in this layer. On the other hand, Layer L (output layer) typically uses the linear activation function to integrate signal(s) of Layer L - 1 for the desired output data p_i^L . In summary, the complete signal flow of ANN can be described as follows:

• Layer 1:

$$p_i^1 = x_i, i = 1, \dots, N_1$$
(12)
where x_i are the inputs.

• Layers $l = 2, \dots L - 1$ (hidden):

$$p_{i}^{l} = f_{\sigma} \Big(\sum_{j=1}^{N_{l-1}} \omega_{ij}^{l} p_{j}^{l-1} + b_{i}^{l} \Big), i = 1, \dots, N_{l}$$
(13)
Layer *L* (output):

$$y_i = \omega_i^L p_i^L, i = 1, ..., N_L$$
 (14)
where y_i are the outputs.

B. Deployment of ANN for the thermal model

This section elaborates the deployment of two dedicated ANNs, both of them serve as a surrogate model of the studied electronic module and aim to predict the accurate temperature variation with regard to input power and time data; however, in order to obtain a better prediction performance, this study proposes ANN_2 by using temperature gradient value as another output based on ANN_1 whose output layer has only one neuron. It should be noted that the step of input time data is small and stays unchanged for all power inputs thus the difference between the temperatures of current and next sampling time can be directly regarded as the gradient at each moment.

1) ANN_1 :

The first neural network (labeled as ANN₁) follows the basic thinking of power electronic module regarding inputoutput data. The purpose of this network is to map the operating condition (input power, P_{in}) and time variable (t_{sim}) into the junction temperature (T_0). The data of three variables required to train this network is collected by running a detailed simulation model of the PED module for many times to cover some specific range of input parameter variations.

Concerning the structure of ANN₁, it comprises an input layer, two hidden layers, and an output layer, as shown in Fig. 3(a). The numbers of neurons in the input layer and output layer are 2 and 1 ($N_1=2$, $N_4=1$); however, the neuron numbers of the hidden layers are not given at the beginning since they should be decided by training the specific practical data via crossvalidation. This will be discussed in the Section IV.

2) ANN_2 :

Inspired by ANN₁ and temperature variation, another network (labeled as ANN₂) is proposed to pursue better performance of network prediction. As shown in Fig. 3(b), the difference between these two networks locates in the output layer (N_4) where there are two neurons in this layer of ANN₂ because it is of interest to find out two variables that characterize the junction temperature: real-time temperature value (T_0) and the variation gradient (ΔT). After simulation, the original data should be processed for giving the gradient with regards to the time variable. Based on that, the structure of hidden layers in ANN₂ can be determined by training the processed data via cross-validation.



Fig. 3. Structures of two studied ANNs. Layer 1 is the input layer, Layer 2 and Layer 3 are hidden layers (neuron numbers to be determined by cross-validation), Layer 4 is the output layer. For simplicity, weights and bias terms are omitted from the figure.

IV. PROPOSED SURROGATE MODLE BASED ON CROSS-VALIDATION

Regarding the structure of the network, if too few neurons are used, the strong nonlinear relationships may not be captured. On the other hand, overfitting may occur in ANNs with too many neurons. ANN structures in many studies are selected using trial-and-error method [11]. However, crossvalidation can give a relatively objective criterion for the structure selection. That will be discussed as follows:

A. Cross-validation

Cross-validation based ANN training is the way to find that using which structure the prediction performance is the best, namely the structure is most suitable for the given inputoutput data. The applied procedure of cross-validation is shown in Fig. 4. The overall procedure comprises 4 steps:

a). The first step is to process simulation results for ANN training following the structure design. This step can be divided into two aspects: input data and output data. Regarding the former, both ANN₁ and ANN₂ have two variables, P_{in} and t_{sim} ; however, there are two variables (T_0 , ΔT) for the output layer of ANN₂ while only T_0 for ANN₁. Therefore, original simulation data should be collected and processed properly for these two networks.



Fig. 4. Cross-validation procedure for choosing the best ANN structure

b). Normalization and division of input-output data are located in the second step. Firstly, the data of each variable should be normalized separately for the following cross-validation work. Furthermore, in order to better evaluate the prediction performance of the ANN candidates, the input-output data should be divided into two original groups: training group (S_{Tr_o}) and test group (S_{Te_o}) , in which the test group will not be used for training during the whole process.

c). Concerning the cross-validation, further grouping of original training data needs to be done by dividing the training data S_{Tr_o} into 2 different subgroups for m times. Assume that there are N_s samples in above two original groups $(S_{Tr_o}$ and $S_{Te_o})$, divide S_{Tr_o} into m sub groups followed by setting each sub group as the sub test data $(S_{Te_s}^i, 1 \le i \le m)$ one by one. After each $S_{Te_s}^i$ has been confirmed, the remaining data in S_{Tr_o} constitute the related sub training data $(S_{Tr_s}^i, 1 \le i \le m)$ with $N_s(1 - 1/m)$ samples. Therefore, the grouping work in

this step is only for S_{Tr_o} because the other group (S_{Te_o}) is only responsible for performance test.

d). This step is to train the sub training data from $S_{Tr_s}^1$ to $S_{Tr_s}^m$. ANNs are trained using the train command, which is a part of Matlab's Deeping Learning Toolbox. It is noted that $S_{Tr_s}^i$ is randomly divided into three data sets (training set, validation set and testing set) by train command in Matlab for confirming the termination condition. After the training stops, the trained ANNs will be tested using the corresponding $S_{Te_s}^i$ and the original test data S_{Te_o} . The used index for the evaluation of prediction performance is Root Mean Square Error (RMSE) which is a popular formula to measure the error rate of a regression model.

B. ANN selection for surrogate model



As discussed in Section III.B, both ANN_1 and ANN_2 need to select proper numbers of neuron for Layer 2 and Layer 3 via the cross-validation. For the selection pool, we can just try different structures evenly within a certain range and record the related prediction performance (RMSE). The best structure can finally be chosen according to the minimum principle. The basic process of ANN structure selection is shown in Fig. 5.

Firstly, give ranges $[N_{L2}^{min}, N_{L2}^{max}]$ and $[N_{L3}^{min}, N_{L3}^{max}]$ to N_2 and N_3 separately. Then, try all pairs (structure candidates) within these two ranges one by one; for every candidate, set corresponding number values to ANN training model. After that, train and test ANN using the proposed cross-validation which results in the RMSE value for each network candidate. Lastly, choose the best structure whose RMSE is the minimum among the selection pool.

It should be noted that this selection process needs to be exercised twice as there are two ANNs in this study and their output data have difference architectures (see Fig. 3). The final ANN_1 and ANN_2 selected by training the simulation data can both serve as the overall representation of the thermal model for the targeted PED module.

V. CASE STUDY

The PED studied here is a power diode whose model was divided into 724 meshes in simulation. The input power is from

1 *W* to 7 *W*, and the ambient temperature is 0° C. The time consumption for a PC equipped with a i5-6200U CPU at dual core 2.3Ghz is about 22 minutes for each power input.

The original data were given by simulating the detailed model of the PED module with associated thermal network for several selected P_{in} and extracting the corresponding T_0 with regards to time variable (t_{sim}) . Concerning the cross-validation work, the data used for ANN training (S_{Tr_0}) is shown in Fig. 6 and the data of 3 W is chosen as S_{Te_0} , which means it was not involved in ANN training but only for testing the trained ANN. S_{Tr_0} was then divided into 10 (value of m) sub testing groups. Setting each of them as $S_{Te_0}^i$ ($1 \le i \le 10$) one by one while the remaining data in S_{Tr_0} must be $S_{Tr_0}^i$. After the grouping work, for each ANN structure design, $S_{Tr_0}^i$ is utilized for training ANN while $S_{Te_0}^1$ and data of 3 W (S_{Te_0}) are for testing. Lastly, RMSE was recorded for each corresponding ANN structure.

For every input power, time variable was swept from 0.8 to 80000 s with a step of 0.8 s. As there are 7 different power conditions, the total number of sample points in this case is 100000*7.



TABLE I. NO. OF STRUCTURE CANDIDATES FOR ANN₁AND ANN₂

Table Head	Serial number of ANN structure candidates with regards to neuron number								
No.	1	2	3	4	5	6	7	8	9
N ₂	2	2	2	2	2	3	3	3	3
N ₃	2	3	4	5	6	2	3	4	5
No.	10	11	12	13	14	15	16	17	18
N ₂	3	4	4	4	4	4	5	5	5
N ₃	6	2	3	4	5	6	2	3	4
No.	19	20	21	22	23	24	25		
N ₂	5	5	6	6	6	6	6		
N ₃	5	6	2	3	4	5	6		

Regarding the best structure selection for ANN₁ and ANN₂, the rang [2, 6] were given to both networks. The reason of not setting N_{L2}^{min} and N_{L3}^{min} as 1 is that there are two neurons in the input layer which determines that the nonlinear relationships between input and output should not be captured by that

structure. Therefore, there are 25 structure candidates in the selection pool, as shown in Table 1.

The next step is to explore all pairs of N_2 , N_3 and calculate RMSE for each structure following the process discussed in Section IV.B. As mentioned above, the structure selection should be exercised for ANN₁ and ANN₂ separately as they have different network architectures. The RMSE results of all structure candidates for ANN₁ and ANN₂ are shown in Fig. 7. In this figure, if the value of ANN RMSE is larger than 6 °C, the structure was distributed to an Up Group; if not, distributed to the Down Group. Therefore, the blue points of Fig. 7 are in the Up Group while the red points are in the Down Group.



Fig. 7. RMSE results of 25 structure candidates for ANN₁ and ANN₂



Fig. 8. Prediction result of 3 W data using the best structure. There are two neurons in the output layer, $N_2 = 6$, $N_3 = 5$.

The best structure for ANN₁ is No. 22 ($N_2 = 6, N_3 = 3$) whose RMSE value is 0.1273; Regarding 25 structure candidates for ANN₂, the best structure is No. 24 ($N_2 = 6, N_3 =$ 5). The RMSE value is 0.06689 °C and it is the only candidate whose RMSE is smaller than 0.1. On the other hand, average RMSE of ANN₂ structures is 1.5836 °C while average RMSE of ANN₁ is 2.4070 °C. Therefore, the RMSE results demonstrate that the overall prediction performance of ANN₂ is better than ANN₁, and the final surrogate thermal model selected for the studied diode model is the No. 24 structure of ANN_2 . Fig. 8 shows the predicted temperature variation of 3 *W* input power using the best structure. Compared with the original data, the prediction performance is excellent.

VI. CONCLUSIONS AND FURTURE WORK

This paper proposes a method of ANN aided thermal prediction for power electronic devices and gives a case study on a power diode. In addition, two different architectures of ANN are designed for the surrogate thermal model and crossvalidation is noted to choose the best ANN structure for the thermal data given by the simulation system.

The future study will focus on the data processing for ANN training and the application of other methods in AI, e.g. support vector machine (SVM). Moreover, sensitivity analysis of training parameters in ANN for better prediction performance is also worth of studying.

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