

COLD-FORMED HIGH STRENGTH STEEL CHS-to-RHS T- AND X-JOINTS: PERFORMANCE AND DESIGN AFTER FIRE EXPOSURES

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Abstract

The post-fire structural performance of cold-formed high strength steel (CFHSS) T- and X-joints with circular hollow section (CHS) braces and square and rectangular hollow section (SHS and RHS) chords is numerically investigated in this study. The tubular members had the nominal 0.2% proof stress of 900 MPa. The CHS-to-RHS T- and X-joints were subjected to compression loads through brace members. The nominal values of peak fire temperatures (ψ) were 300°C, 550°C, 750°C and 900°C. Tests carried out by the authors investigating the post-fire static response of cold-formed S900 steel grade CHS-to-RHS T- and X-joints were formed the basis of the numerical investigation carried out in this study. The test results reported by the authors were used to develop accurate finite element (FE) models. The validated FE models were used to perform extensive numerical parametric studies comprising 768 FE specimens. The validity ranges of critical geometric parameters were extended beyond current limits mentioned in international codes and guides. The residual strengths of test and FE specimens were compared with the nominal resistances predicted from design equations given in Eurocode 3 and *Comité International pour le Développement et l'Etude de la Construction Tubulaire* (CIDECT) Design Guide 3 using the measured post-fire residual material properties. Generally, design rules given in Eurocode 3 and CIDECT are shown to be quite conservative with very dispersed unreliable predictions. As a result, accurate and reliable design rules are proposed in this study.

Keywords: *Cold-formed Steel; Fire; High Strength Steel; Hollow Section Joint; Post-fire; Tubular Members.*

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30

31 **1. Introduction**

32 Owing to rapid increase in fire incidents of structures in recent years, the post-fire assessments
33 of fire exposed structures are important. Without scientific assessments, structures exposed to high
34 temperatures cannot be allowed for their direct reuse. During the cooling phase, the temperature of
35 steel drops down, and eventually, the steel material would shrink. Consequently, the thermal-induced
36 shrinkage deformations would lock inside the fire exposed structural steel members, and the situation
37 could be dangerous. Thus, a reliable evaluation method is required to confirm whether a fire exposed
38 structure should be allowed for its direct reuse, repair or just demolish, thereby highlighting the
39 strategic importance of the post-fire assessment [1]. The outcomes of the post-fire investigation
40 facilitate various stakeholders of the property to opt for best reuse strategies for fire exposed
41 structures. Generally, steel structures are more vulnerable to fires compared to concrete structures,
42 which in turn highlight the critical importance of post-fire investigation of fire exposed steel
43 structures. In addition to various structural applications, it is worth noting that CHS-to-RHS joints
44 have also been used in the manufacture of equipment and structural systems in the road transport and
45 agricultural industries [2]. Moreover, Fig. 1 presents a pedestrian truss bridge with CHS brace and
46 RHS chord at Westminster Millennium Pier in London, United Kingdom [3].

47 Tubular members are frequently used in both onshore and offshore structures subjected to
48 different types of loading because of high torsional strength, ability to confine in-filled material,
49 superior aesthetic appearance and so on. Tubular member made of high strength steel (HSS) (in this
50 paper, HSS refers to steels with steel grades higher than S460) provides additional merits, including
51 superior strength per unit weight, reduced handling costs and time. Primarily, the focus of
52 investigations on tubular joints in the last six decades was on their structural performance at room
53 temperature, while investigations of tubular joints at peak fire temperatures (ψ) largely remain
54 exiguous. The post-fire behaviour of circular hollow section (CHS) T-joints made of Q345B steel
55 grade was investigated by Jin et al. [4]. It was concluded that the effect of preload on the residual
56 capacities of fire exposed CHS T-joints was negligible. Experimental and numerical studies were
57 carried out by Gao et al. [5] to investigate the cyclic performance of fire exposed CHS T-joints made

58 of normal strength steel (in this study, refer to steels with steel grades less than or equal to S460).
59 The CHS T-joints were reinforced with doubler plates. It was noticed that the energy dissipation
60 capacities of CHS T-joints were significantly reduced after fire exposures. The post-fire behaviour of
61 concrete in-filled CHS T-joints was experimentally and numerically investigated by Gao et al. [6]. It
62 was found that the residual capacities of fire exposed concrete in-filled CHS T-joints were less than
63 the corresponding fire exposed hollow CHS T-joints. Pandey and Young [7] carried out tests to
64 investigate the residual strengths ($N_{f,\psi}$) of ISO-834 [8] fire exposed cold-formed S900 steel grade T-
65 and X-joints with CHS braces and square and rectangular hollow section (SHS and RHS) chords.
66 The literature review confirmed that except above mentioned studies, no other investigation is
67 available on the post-fire behaviour of normal and high strength steel tubular joints. It should be
68 noted that, henceforth, RHS also includes SHS in this paper.

69 A detailed numerical investigation was performed in this study to gain an in-depth
70 understanding of various critical parameters that affected the static behaviour of CHS-to-RHS T- and
71 X-joints. Accurate finite element (FE) models were developed for CHS-to-RHS T- and X-joints using
72 the test results reported in Pandey and Young [7]. The validated FE models were used to perform
73 extensive numerical parametric studies that comprised 768 FE specimens, including 384 T-joints and
74 384 X-joints made of CHS braces and RHS chords. The residual strengths ($N_{f,\psi}$) of test [7] and FE
75 specimens were compared with the nominal resistances predicted from design equations given in
76 EC3 [9] and CIDECT [10] using the measured post-fire residual material properties investigated by
77 Pandey and Young [1]. Generally, it has been demonstrated that the predictions from design rules
78 given in EC3 [9] and CIDECT [10] are quite conservative but largely dispersed and unreliable for
79 the range of fire exposed CHS-to-RHS T- and X-joints investigated in this study. Therefore, using
80 two design approaches, accurate and reliable design equations are proposed in this study to predict
81 the residual strengths ($N_{f,\psi}$) of cold-formed S900 steel grade CHS-to-RHS T- and X-joints subjected
82 to post-fire temperatures ranging from 300°C to 900°C.

83

84 2. Outline of test programs on CHS-to-RHS T- and X-joints under post-fire conditions

85 The static residual strengths of cold-formed high strength steel (CFHSS) fire exposed CHS-to-
86 RHS T- and X-joints subjected to compression loads were investigated by Pandey and Young [7].
87 Before conducting the static joint tests, the test specimens were subjected to a total of three fire
88 exposures. The preselected peak temperatures (ψ) of three fire exposures were 300°C, 550°C and
89 750°C, respectively. In total, 7 T-joints and 7 X-joints made of CHS braces and RHS chords were
90 fabricated. The nominal 0.2% proof stress of hollow section members was 900 MPa. The braces and
91 chords were welded using robotic metal active gas welding. The test specimens were grouped in 3
92 series for the 3 fire exposures (i.e. $\psi_1=300^\circ\text{C}$, $\psi_2=550^\circ\text{C}$ and $\psi_3=750^\circ\text{C}$). All 3 series of CHS-to-RHS
93 T- and X-joints test specimens were exposed to fire inside a gas furnace, where the furnace
94 temperature was increased in accordance with ISO-834 [8]. After attaining the preselected peak
95 temperatures (ψ), the test specimens were allowed to naturally cool inside the furnace. Subsequently,
96 CHS-to-RHS T- and X-joints test specimens were tested at room temperature by applying
97 compression loads through brace members. Fig. 2 presents the definitions of various notations for
98 CHS-to-RHS X-joints, which remain valid for CHS-to-RHS T-joints. The static behaviour of CHS-
99 to-RHS T- and X-joints primarily depends on geometric ratios, namely β (d_1/b_0), τ (t_1/t_0) and 2γ (b_0/t_0).
100 The symbols b , h , t and R stand for cross-section width, depth, thickness and external corner radius
101 of tubular member, respectively. The symbol d denotes the diameter of CHS member. The subscripts
102 0 and 1 represent chord and brace, respectively. In the experimental investigation, β varied from 0.74
103 to 0.89, τ varied from 0.76 to 1.02 and 2γ varied from 25.1 to 30.6.

104 The lengths of braces (L_1) were equal to two times the brace diameter (d_1). On the other hand,
105 the lengths of chords (L_0) were equal to $h_1 + 3h_0 + 180$ and $h_1 + 3h_0$ for T- and X-joints, respectively.
106 The test results were obtained in the form of $N_{f,\psi}$ vs u and $N_{f,\psi}$ vs v curves, where $N_{f,\psi}$, u and v
107 respectively stand for residual load, chord face indentation and chord side wall deformation. It should
108 be noted that $N_{f,\psi}$ vs u curves were used to determine the $N_{f,\psi}$ of fire exposed CHS-to-RHS T- and X-
109 joints. The material properties of ISO-834 [8] fire exposed cold-formed S900 steel grade CHS and

110 RHS members were investigated by Pandey and Young [1] for post-fire temperatures ranging from
111 300°C to 900°C. The test specimens in the experimental program [7] were fabricated from tubular
112 members that belonged to the identical batch of tubes used in Pandey and Young [1]. Thus, the
113 material properties of fire exposed CHS and RHS members can be referred to Pandey and Young [1].
114 It should be noted that the cold-formed S900 steel grade CHS-to-RHS T- and X-joints [7] and tubular
115 members [1] were simultaneously exposed to fire inside the gas furnace. The measured values of
116 static yield strength of fire exposed tubular members ranged from 1033 to 1087 MPa for $\psi_1=300^\circ\text{C}$,
117 889 to 991 MPa for $\psi_2=550^\circ\text{C}$, 269 to 371 MPa for $\psi_3=750^\circ\text{C}$ and 233 to 390 MPa for $\psi_4=900^\circ\text{C}$.

118

119 **3. Numerical program**

120 3.1. Finite element (FE) models of CHS-to-RHS T- and X-joints

121 3.1.1. General

122 ABAQUS [11] was used to perform comprehensive FE analyses in this study. As the induced
123 strains in the FE models during the applied load were unidirectional, the isotropic strain hardening
124 law was selected for the analysis. The yielding onsets of FE models in this study were based on the
125 von-Mises yield theory. The default Newton-Raphson method was used to find the roots of non-linear
126 equilibrium equations. The material non-linearities were considered in the FE models by assigning
127 the measured values of post-fire residual static stress-strain curves of flat, corner and curved portions
128 of RHS and CHS members in the plastic material definition part of the FE models. However,
129 experimentally obtained constitutive material curves were transformed into true stress-strain curves
130 prior to their inclusion in the FE models. On the other hand, the geometric non-linearities in FE
131 models were considered by enabling the non-linear geometry parameter (*NLGEOM) in ABAQUS
132 [11], which allowed the FE models to undergo large displacement during the analyses. Furthermore,
133 various parameters, including through-thickness division, contact interactions, mesh seed spacing,
134 corner region extension and element types, were also studied and reported in the following sections
135 of this paper. The labelling of parametric FE specimens was kept identical to the label system used

136 in the test program [7]. Figs. 3 and 4 present typical CHS-to-RHS T- and X-joints FE specimens
137 modelled in this study, respectively.

138 3.1.2. Element type, material properties and mesh spacing

139 Except for the welds, all other parts of the FE models were developed using second-order
140 hexahedral elements, particularly using the C3D20 elements. On the other hand, the second-order
141 tetrahedral element, C3D10, was used to model the weld parts owing to their complicated shapes.
142 The use of solid elements helped in making realistic fusions between tubular and weld parts of the
143 FE models. Convergence studies were conducted using different mesh sizes, and finally, chord and
144 brace members were seeded at 4 mm and 7 mm intervals, respectively, along their corresponding
145 longitudinal and transverse directions. Moreover, the seeding spacings of weld parts reciprocated the
146 seeding spacings of their respective brace parts. In order to ensure the smooth transfer of stresses
147 from flange to web regions, the corner portions of RHS were split into ten elements. FE analyses
148 were also conducted to examine the influence of divisions along the wall thickness (t) of tubular
149 members. The results of these FE analyses demonstrated the trivial influence of wall thickness
150 divisions on the load vs deformation curves of the investigated CHS-to-RHS T- and X-joints. The
151 use of the C3D20 element as well as the small thickness of test specimens [7] led to such observations.
152 It is worth noting that similar findings were also noticed by Pandey et al. [12,13] and Pandey and
153 Young [14,15]. Thus, for the validations of FE models, the wall thicknesses of tubular members were
154 not divided.

155 The measured post-fire static stress-strain curves of flat and corner portions of RHS members
156 and curved portion of CHS members were used in the FE models. In this study, the influence of cold-
157 working in RHS members was included by assigning wider corner portions in the FE models. Various
158 distances for corner extension were considered in the sensitivity analyses, and finally, the corner
159 portions of RHS members were extended by $2t$ into the neighbouring flat portions, which agreed with
160 other studies [12-21] conducted on CFHSS tubular members and joints.

161 3.1.3. Weld modelling and contact interactions

162 The fillet welds were modelled in all FE specimens using the average values of measured weld
163 sizes reported in Pandey and Young [7]. The inclusions of weld geometries improved the overall
164 accuracies of FE models. In addition, modelling of weld parts helped in attaining realistic load
165 transfer between brace and chord members. The selection of the C3D10 element maintained optimum
166 stiffness around the joint perimeter due to its ability to take complicated shapes. In total, two types
167 of contact interactions were defined in CHS-to-RHS T- and X-joints FE models. First, contact
168 interaction between brace and chord members of CHS-to-RHS T- and X-joints FE models. Second,
169 contact interaction between chord members and chord end bearing blocks of CHS-to-RHS T-joint FE
170 models. Both contact interactions were established using the built-in surface-to-surface contact
171 definition. In addition, a tie constraint was also established between weld and tubular members of
172 CHS-to-RHS T- and X-joints FE models. The contact interactions between brace and chord members
173 of CHS-to-RHS T- and X-joints FE models was kept frictionless, while a frictional penalty equal to
174 0.3 was imposed on the contact interaction between chord member and chord end bearing blocks of
175 CHS-to-RHS T-joint FE models. Along the normal direction of these two contact interactions, a ‘hard’
176 contact pressure overclosure was used. In addition, finite sliding was permitted between the
177 interaction surfaces. For contact interactions and tie constraint, the surfaces were connected to each
178 other using the ‘master-slave’ algorithm technique.

179 3.1.4. Boundary conditions

180 The boundary conditions in CHS-to-RHS T- and X-joints FE models were assigned by creating
181 reference points. Three reference points were created for the CHS-to-RHS T-joint FE model,
182 including one top reference point (TRP) and two bottom reference points (BRP-1 and BRP-2), as
183 shown in Fig. 3. The TRP replicated the fixed boundary condition of the top brace end, while BRP-
184 1 and BRP-2 replicated the boundary conditions of roller positioned at each chord end. The TRP was
185 created at the cross-section centre of the top brace end, while BRP-1 and BRP-2 were created at 20
186 mm below the centre of the bottom surfaces of chord end bearing blocks. The TRP, BRP-1 and BRP-
187 2 were then coupled to their corresponding surfaces using the built-in kinematic coupling type. In
188 order to exactly replicate the boundary conditions of the CHS-to-RHS T-joint test setup, all degrees

189 of freedom (DOF) of TRP were restrained. On the other hand, for BRP-1 and BRP-2, except for the
190 translations along the vertical and longitudinal directions of the CHS-to-RHS T-joint FE specimen as
191 well as the rotation about the transverse direction of the chord member, all other DOF of BRP-1 and
192 BRP-2 were also restrained. In addition, all DOF of other nodes of CHS-to-RHS T-joint FE specimen
193 were kept unrestrained for both rotation and translation.

194 With regard to the CHS-to-RHS X-joint FE model, the top and bottom reference points (TRP
195 and BRP) were created at the cross-section centres of the top and bottom brace members, as shown
196 in Fig. 4. Subsequently, TRP and BRP were coupled to their respective brace end cross-section
197 surfaces using the kinematic coupling type. In order to exactly replicate the boundary conditions of
198 the CHS-to-RHS X-joint test setup, all DOF of TRP were restrained. However, except for the vertical
199 translation, all other DOF of BRP were also restrained. Moreover, all DOF of other nodes of the
200 CHS-to-RHS X-joint FE specimen were kept unrestrained for both rotation and translation. Using
201 the displacement control method, compression load was then applied at the bottom reference points
202 of the CHS-to-RHS T- and X-joints FE models. In addition, the size of the step increment was kept
203 small in order to obtain smooth load vs deformation curves. Following this approach, the boundary
204 conditions and load applications in FE models were identical to the test program [7].

205 3.2. Validations of CHS-to-RHS T- and X-joints FE models

206 The numerical modelling techniques described in the preceding section of this paper were used
207 to develop CHS-to-RHS T- and X-joints FE models. The validations were performed by comparing
208 the residual strengths ($N_{f,\psi}$), load vs deformation histories and failure modes of test and FE specimens.
209 The measured dimensions of tubular members and welds were used to develop all FE models. In
210 addition, measured post-fire residual static material properties of tubular members were used in the
211 validation process. It is worth mentioning that both ultimate load and 3% deformation limit (i.e.
212 $0.03b_0$) load were used to determine the $N_{f,\psi}$ of test and FE specimens, whichever occurred earlier in
213 the $N_{f,\psi}$ vs u curves. The residual strengths ($N_{f,\psi}$) of CHS-to-RHS T- and X-joints test specimens were
214 compared with those predicted from their corresponding FE models (N_{FE}), as shown in Tables 1 and
215 2, respectively. Referring to Table 1, the mean (P_m) and coefficients of variation (COV) (V_p) of the

216 comparisons for CHS-to-RHS T-joints are 1.02 and 0.009, respectively. On the other hand, as shown
217 in Table 2, the P_m and V_p of the comparisons for CHS-to-RHS X-joints are 0.99 and 0.007,
218 respectively. In addition, the comparisons of load vs deformation curves between CHS-to-RHS T-
219 and X-joints test and FE specimens are shown in Figs. 5 and 6, respectively. Moreover, Figs. 7 and 8
220 present the comparisons of failure modes between typical CHS-to-RHS T- and X-joints test and FE
221 specimens, respectively. From Tables 1-2 and Figs. 5-8, it can therefore be concluded that the
222 validated FE models precisely replicated the overall static behaviour of CFHSS fire exposed CHS-
223 to-RHS T- and X-joints.

224 3.3. Parametric study of CHS-to-RHS T- and X-joints

225 3.3.1. General

226 In the parametric study, 4 fire exposures with peak temperatures (ψ) equal to 300°C, 550°C,
227 750°C and 900°C were investigated, which were consistent with the test programs [1,7]. In total, 768
228 FE analyses were performed in the parametric study, including 384 CHS-to-RHS T-joints and 384
229 CHS-to-RHS X-joints. The validity ranges of important geometric ratios were purposefully widened
230 beyond the present limitations set by EC3 [9] and CIDECT [10]. Table 3 presents the overall ranges
231 of various critical parameters considered in the numerical investigation. In the parametric study, all
232 FE modelling techniques described earlier in this paper were used.

233 3.3.2. Details of finite element models

234 The values of brace diameter of parametric FE specimens varied from 15 mm to 450 mm, while
235 the values of cross-section width and depth of RHS chords of parametric FE specimens varied from
236 50 mm to 500 mm. However, the values of wall thickness of braces and chords varied from 2 mm to
237 10 mm. The external corner radius of RHS member (R_0) conformed to commercially produced HSS
238 members [22]. In this study, R_0 was kept as $2t$ for $t \leq 6$ mm, $2.5t$ for $6 < t \leq 10$ mm and $3t$ for $t > 10$
239 mm, which in turn also meet the limits detailed in EN 10219-2 [23]. The formulae used to determine
240 the lengths of braces and chords of CHS-to-RHS T- and X-joints FE specimens were identical to
241 those used in the test program [7]. For meshing along the longitudinal and transverse directions of

242 RHS members, seedings were approximately spaced at the minimum of $b/30$ and $h/30$. On the other
243 hand, CHS brace members were meshed approximately at an interval of $d/30$. Overall, the adopted
244 mesh sizes of parametric FE specimens varied from 3 mm to 12 mm. On the other hand, the seeding
245 interval of weld parts of parametric FE specimens reciprocated the seeding interval of their
246 corresponding brace parts.

247 For precise replication of RHS curvatures, the corner portions of RHS members were split into
248 ten parts. Likewise, in the validation process, the corner portions of RHS members were extended by
249 $2t$ into their neighbouring flat portions. For tubular members with $t \leq 6$ mm, no divisions were made
250 along the wall thickness of the parametric FE specimens. However, when $t > 6$ mm, the wall thickness
251 of parametric FE specimens was divided into two layers. Following the prequalified tubular joint
252 details given in AWS D1.1M [24], the leg size (w) of the fillet weld of CHS-to-RHS T- and X-joints
253 FE specimens was designed as 1.5 times the minimum of t_1 and t_0 , which was consistent with the test
254 program [7]. For different fire exposure series (i.e. $\psi_1=300^\circ\text{C}$, $\psi_2=550^\circ\text{C}$, $\psi_3=750^\circ\text{C}$ and $\psi_4=900^\circ\text{C}$)
255 of the FE parametric study, the corresponding measured post-fire residual static material properties
256 of CHS 88.9 \times 4 and RHS 120 \times 60 \times 4 [1] were respectfully assigned to the CHS and RHS members of
257 the FE specimens. Figs. 9 and 10 present the measured post-fire residual static stress-strain curves of
258 CHS 88.9 \times 4 and RHS 120 \times 60 \times 4 for different fire exposure series, respectively. Besides, the
259 measured static weld material properties at room temperature [25] were retained as 100%, 85%, 57%
260 and 48% for 300 $^\circ\text{C}$, 550 $^\circ\text{C}$, 750 $^\circ\text{C}$ and 900 $^\circ\text{C}$ post-fire temperatures, respectively. These retention
261 percentages correspond to the average retention values of the ultimate stress of tubular members of
262 different fire exposure series. Table 4 presents the measured post-fire residual static material
263 properties of CHS 88.9 \times 4 and RHS 120 \times 60 \times 4 adopted in the parametric study, which include
264 Young's modulus (E), 0.2% proof stress and strain ($\sigma_{0.2}$ and $\varepsilon_{0.2}$), ultimate stress and strain (σ_u and ε_u)
265 and fracture strain (ε_f).

266 3.3.3. Failure modes of CHS-to-RHS T- and X-joints under post-fire conditions

267 Overall, two types of failure modes were identified for both CHS-to-RHS T- and X-joints. First,
268 the failure of CHS-to-RHS T- and X-joints by the yielding of chord flange, which was named as

269 chord face failure and denoted by the letter ‘F’ in this study. Second, the failure of CHS-to-RHS T-
270 and X-joints due to the combination of chord face and chord side wall failure modes, which was
271 named as the combined failure mode and denoted by ‘F+S’ in this study. It is important to note that
272 these failure modes were defined corresponding to the $N_{f,\psi}$, which in turn was computed by
273 combinedly considering the ultimate and $0.03b_0$ limit loads, whichever occurred earlier in the $N_{f,\psi}$ vs
274 u curve. The test and parametric FE specimens were failed by the F mode, when the $N_{f,\psi}$ was
275 determined using the $0.03b_0$ limit. The applied loads of fire exposed CHS-to-RHS T- and X-joints
276 failed by the F mode were monotonically increasing. The CHS-to-RHS T- and X-joints were failed
277 by the F mode in this investigation, when $0.30 \leq \beta < 0.75$. For test and parametric FE specimens that
278 failed by the F+S mode, the load vs deformation curves exhibited clear ultimate load. Additionally,
279 evident deformations of chord flange, chord webs and chord corner regions were noticed in the test
280 and parametric FE specimens that failed by the F+S mode. The CHS-to-RHS T- and X-joints were
281 failed by the F+S mode in this investigation, when $0.75 \leq \beta \leq 0.90$. Moreover, none of the test and
282 FE specimens were failed by the global buckling of braces. Figs. 11 and 12 present the variations of
283 $N_{f,\psi}$ vs u curves of typical CHS-to-RHS T- and X-joints FE specimens that failed by the F and F+S
284 modes for different post-fire temperatures investigated in this study, respectively.

285

286 4. EC3 (2005) and CIDECT (2009) design provisions

287 Currently, design rules to predict the post-fire residual strengths of tubular joints are not given
288 in any code and guideline. Therefore, in order to examine the suitability of EC3 [9] and CIDECT [10]
289 design provisions for CFHSS fire exposed CHS-to-RHS T- and X-joints, in this study, the nominal
290 resistances from design equations given in EC3 [9] and CIDECT [10] ($N_{E,\psi}$ and $N_{C,\psi}$) were
291 determined using the measured post-fire residual static material properties shown in Table 4. The
292 design rules given in EC3 [9] and CIDECT [10] are shown below:

293 Chord face failure ($\beta \leq 0.85$)

294 EC3 [9]:

$$N_{E,\psi} = C_f \left[\frac{\pi}{4} k_n \frac{f_{y0,\psi} t_0^2}{(1-\beta) \sin \theta_1} \left(\frac{2\eta}{\sin \theta_1} + 4\sqrt{1-\beta} \right) / \gamma_{M5} \right] \quad (1)$$

295 CIDECT [10]:

$$N_{C,\psi} = C_f \left[\frac{\pi}{4} Q_f \frac{f_{y0,\psi} t_0^2}{\sin \theta_1} \left(\frac{2\eta}{(1-\beta)\sin \theta_1} + \frac{4}{\sqrt{1-\beta}} \right) \right] \quad (2)$$

296 Chord side wall failure ($\beta = 1.0$)

297 EC3 [9]:

$$N_{E,\psi} = C_f \left[\frac{\pi}{4} k_n \frac{f_{b,\psi} t_0}{\sin \theta_1} \left(\frac{2d_1}{\sin \theta_1} + 10t_0 \right) / \gamma_{M5} \right] \quad (3)$$

298 CIDECT [10]:

$$N_{C,\psi} = C_f \left[\frac{\pi}{4} Q_f \frac{f_{k,\psi} t_0}{\sin \theta_1} \left(\frac{2d_1}{\sin \theta_1} + 10t_0 \right) \right] \quad (4)$$

299 The nominal resistances of CHS-to-RHS T- and X-joints from design equations given in EC3
300 [9] were determined using 0.2% proof stress and partial safety factor (γ_{M5}) equal to 1.0. In addition,
301 a material factor (C_f) equal to 0.80 was adopted as per EC3 [26]. On the other hand, CIDECT [10]
302 uses the minimum of 0.2% proof stress and 0.80 times the corresponding ultimate stress for joint
303 resistance calculation. Moreover, design provisions given in CIDECT [10] recommend the use of C_f
304 equal to 0.90 for tubular joints with steel grade exceeding S355. Unlike EC3 [9], CIDECT [10] uses
305 different values of partial safety factors (γ_M) for different types of tubular joints and their
306 corresponding failure modes, which are given in IIW [27]. However, their effects are implicitly
307 included inside the CIDECT [10] design provisions. In this study, nominal resistances of CHS-to-
308 RHS X-joints from design equations given in CIDECT [10] were calculated using γ_M equal to 1.0
309 and 1.25 for chord face failure and chord side wall failure modes, respectively. On the other hand,
310 nominal resistances of CHS-to-RHS T-joints from design equations given in CIDECT [10] were
311 calculated using γ_M equal to 1.0 for both chord face failure and chord side wall failure modes. In Eqs.
312 (1) to (4), chord stress functions are denoted by k_n and Q_f , post-fire yield stress of chord member is
313 denoted by $f_{y0,\psi}$, the parameter η is equal to d_1/b_0 , post-fire chord side wall buckling stresses are
314 denoted by $f_{b,\psi}$ and $f_{k,\psi}$, and the angle between brace and chord is denoted by θ_1 (in degrees). For
315 CHS-to-RHS T-joints, the effect of chord-in-plane bending was considered through k_n and Q_f
316 functions. However, for CHS-to-RHS X-joints, the values of k_n and Q_f were adopted as 1.0.

317 In addition, a reliability analysis was performed as per AISI S100 [28]. In this study, design

318 equation was treated as reliable when the value of reliability index (β_0) was greater than or equal to
319 2.50. The values of various statistical parameters and load combinations used in the reliability index
320 calculation are identical to those values adopted in Pandey et al. [12,13] and Pandey and Young
321 [14,15,19-21].

322

323 **5. Comparisons between residual strengths and nominal resistances**

324 Tables 5 and 6 present the overall summary of comparisons between $N_{f,\psi}$ and nominal
325 resistances predicted from design equations given in EC3 [9] and CIDECT [10] for CHS-to-RHS T-
326 joints failed by the F and F+S failure modes, respectively. On the other hand, Tables 7 and 8 present
327 the overall summary of comparisons between $N_{f,\psi}$ and nominal resistances predicted from design
328 equations given in EC3 [9] and CIDECT [10] for CHS-to-RHS X-joints failed by the F and F+S
329 failure modes, respectively. In total, 782 data are presented in Tables 5 to 8, including 14 test data [7]
330 and 768 parametric FE data generated in this study. The comparisons are also graphically shown in
331 Figs. 13 and 14 for CHS-to-RHS T-joints, and in Figs. 15 and 16 for CHS-to-RHS X-joints.

332 Table 5 presents the overall summary of comparisons for CHS-to-RHS T-joint test and FE
333 specimens that failed by the F mode. It can be noticed that the design rules given in EC3 [9] are found
334 to be slightly unconservative and unreliable when nominal resistances are predicted using the post-
335 fire material properties. In addition, predictions are largely dispersed. On the contrary, the design
336 rules in CIDECT [10] are found to be slightly conservative but unreliable when the post-fire material
337 properties are used to predict the nominal resistances. Moreover, predictions are also largely
338 dispersed. For CHS-to-RHS T-joint test and FE specimens that failed by the F+S mode, the design
339 rules given in EC3 [9] and CIDECT [10] are found to be quite conservative but unreliable, as shown
340 in Table 6. Furthermore, when using the post-fire material properties, the predictions from design
341 equations given in EC3 [9] and CIDECT [10] are quite dispersed.

342 With regard to CHS-to-RHS X-joint test and FE specimens that failed by the F mode, the
343 overall summary of comparisons is shown in Table 7. It is evident that, when using post-fire material
344 properties, the design rules given in EC3 [9] and CIDECT [10] are found to be slightly conservative

345 but unreliable. In addition, predictions are largely dispersed. On the other hand, Table 8 presents the
346 overall summary of comparisons for CHS-to-RHS X-joint test and FE specimens that failed by the
347 F+S mode. The design rules given in EC3 [9] and CIDECT [10] are found to be quite conservative
348 but unreliable. Moreover, predictions calculated using post-fire material properties are quite
349 dispersed.

350 In Figs. 13 and 15, generally, test and parametric FE specimens with small values of β and η
351 ratios and large values of 2γ ratio lie below the unit slope line (i.e. $y=x$). For such specimens, the joint
352 resistance corresponding to the $0.03b_0$ limit was not sufficient to cause the yielding of chord flanges.
353 On the contrary, the yield line theory was used to derive the existing design equation for RHS T- and
354 X-joints that failed by the F mode. Consequently, the $N_{f,\psi}$ of CHS-to-RHS T- and X-joints specimens
355 became smaller than the corresponding nominal resistances predicted from design equations given in
356 EC3 [9] and CIDECT [10]. As a result, the data of such specimens fall below the line of unit slope.
357 The data above the line of unit slope, on the other hand, indicate CHS-to-RHS T- and X-joints
358 specimens with medium to large values of β and η ratios and small values of 2γ ratio. The stress-
359 strain behaviour of HSS material is quite different to that of mild steel [29-34], which could change
360 the deformation extent of chord connecting face(s). For CHS-to-RHS T- and X-joints that failed by
361 the F+S mode, the data above the unit slope line in Figs. 14 and 16 typically represent specimens
362 with large values of β ratio and small values of 2γ and h_0/t_0 ratios. As the β ratio of CHS-to-RHS T-
363 and X-joints failed by the F+S mode increased, the brace member gradually approached the chord
364 corner regions. Consequently, the $N_{f,\psi}$ of such T- and X-joints increased due to the enhanced rigidity
365 of chord corner regions. On the other hand, the corresponding increase in nominal resistances
366 predicted from design equations given in EC3 [9] and CIDECT [10] was lower than the $N_{f,\psi}$ of CHS-
367 to-RHS T- and X-joints. Subsequently, the data of such specimens fall above the line of unit slope in
368 Figs. 14 and 16.

369

370 6. Proposed design rules

371 Using two design approaches, named as proposal-1 and -2, design rules are proposed in this

372 study for CFHSS fire exposed CHS-to-RHS T- and X-joints failed by F and F+S failure modes. For
373 CFHSS fire exposed CHS-to-RHS T-joints, the design rules proposed in both the approaches (i.e.
374 proposal-1 and -2) are based on the design equations proposed by Pandey et al. [12] for without fire
375 exposed S900 steel grade CHS-to-RHS T-joints. On the other hand, for CFHSS fire exposed CHS-
376 to-RHS X-joints, the proposed design rules under proposal-1 and -2 are based on the design equations
377 proposed by Pandey and Young [15] for S900 steel grade CHS-to-RHS X-joints without fire exposure.
378 In the first design approach (i.e. proposal-1), the room temperature material properties used in the
379 design equations proposed by Pandey et al. [12] and Pandey and Young [15] are replaced with the
380 corresponding post-fire residual material properties. In addition, a correction factor (ζ) based on post-
381 fire peak temperature (ψ) is also applied on the proposed design rules. On the other hand, in the
382 second design approach (i.e. proposal-2), only a correction factor based on the post-fire peak
383 temperature (ψ) is applied on the design rules proposed by Pandey et al. [12] and Pandey and Young
384 [15] using the room temperature material properties. Therefore, design equations under proposal-1
385 can predict the $N_{f,\psi}$ of fire exposed CHS-to-RHS T- and X-joints when post-fire residual material
386 properties are available. However, design equations under proposal-2 can predict the $N_{f,\psi}$ only using
387 the post-fire peak temperature (ψ).

388 It should be noted that the design rules proposed in this study are valid for $300^{\circ}\text{C} \leq \psi \leq 900^{\circ}\text{C}$.
389 In this investigation, the validity ranges of important factors influencing the static behaviour of CHS-
390 to-RHS T- and X-joints were extended beyond their existing limits given in EC3 [9] and CIDECT
391 [10]. Furthermore, as welds were modelled in all parametric FE specimens, the influence of weld
392 was implicitly included in the proposed design rules. In order to obtain design resistances (N_d), the
393 proposed nominal resistances (N_{pn1} and N_{pn2}) shall be multiplied by their correspondingly
394 recommended resistance factors (ϕ), i.e. $N_d = \phi (N_{pn1} \text{ or } N_{pn2})$.

395 6.1. For CHS-to-RHS T-joints

396 6.1.1. Chord face failure (F) mode ($0.30 \leq \beta < 0.75$)

397 Proposal-1:

398 Using post-fire material properties and post-fire peak temperature (ψ) correction factor:

$$N_{pm1} = \xi \left[f_{y0,\psi} t_0^2 \left(\frac{1.2e^{3.1\beta}}{0.6 + 0.025(2\gamma)} \right) \right] \quad (5)$$

399 where

$$\xi = \begin{cases} 0.965 & \text{for } 300^\circ\text{C} \leq \psi \leq 550^\circ\text{C} \\ 0.0023\psi - 0.3 & \text{for } 550^\circ\text{C} < \psi \leq 900^\circ\text{C} \end{cases} \quad (6)$$

400 Proposal-2:

401 Using room temperature material properties and post-fire peak temperature (ψ) correction factor:

$$N_{pm2} = (1.3 - 0.001\psi) \left[f_{y0} t_0^2 \left(\frac{1.2e^{3.1\beta}}{0.6 + 0.025(2\gamma)} \right) \right] \quad (7)$$

402 The Eqs. (5) and (7) are valid for $0.30 \leq \beta < 0.75$, $16.6 \leq 2\gamma \leq 50$, $15 \leq h_0/t_0 \leq 50$ and $0.50 \leq \tau$
 403 ≤ 0.90 . As shown in Table 5, the P_m and V_p of proposal-1 (i.e. Eq. (5)) are 1.00 and 0.119, respectively,
 404 while the P_m and V_p of proposal-2 (i.e. Eq. (7)) are 1.01 and 0.138, respectively. For both Eqs. (5)
 405 and (7), ϕ equal to 0.80 is recommended, resulting in β_0 equal to 2.63 and 2.59, respectively. The
 406 comparisons of $N_{f,\psi}$ of CHS-to-RHS T-joint specimens with nominal resistances predicted from
 407 design equations given in EC3 [9] and CIDECT [10] as well as predictions from proposal-1 and -2
 408 are graphically presented in Fig. 13. In addition, the distributions of the ratios of $N_{f,\psi}$ of CHS-to-RHS
 409 T-joint specimens-to-nominal resistances predicted from Eqs. (1), (2), (5) and (7) are shown in Fig.
 410 17.

411 6.1.2. Combined failure (F+S) mode ($0.75 \leq \beta \leq 0.90$)

412 Proposal-1:

413 Using post-fire material properties and post-fire peak temperature (ψ) correction factor:

$$N_{pm1} = \xi \left[f_{y0,\psi} t_0^2 \left(\frac{57\beta - 30}{0.8 + 0.013(2\gamma)} \right) \right] \quad (8)$$

414 where

$$\xi = \begin{cases} 0.85 & \text{for } 300^\circ\text{C} \leq \psi \leq 550^\circ\text{C} \\ 0.001\psi + 0.3 & \text{for } 550^\circ\text{C} < \psi \leq 900^\circ\text{C} \end{cases} \quad (9)$$

415 Proposal-2:

416 Using room temperature material properties and post-fire peak temperature (ψ) correction factor:

$$N_{pm2} = (1.17 - 0.001\psi) \left[f_{y0} t_0^2 \left(\frac{57\beta - 30}{0.8 + 0.013(2\gamma)} \right) \right] \quad (10)$$

417 The Eqs. (8) and (10) are valid for $0.75 \leq \beta \leq 0.90$, $16.6 \leq 2\gamma \leq 50$, $15 \leq h_0/t_0 \leq 50$ and $0.75 \leq \tau$

418 ≤ 1.0 . As shown in Table 6, the P_m and V_p of proposal-1 (i.e. Eq. (8)) are 1.03 and 0.124, respectively,
 419 while the P_m and V_p of proposal-2 (i.e. Eq. (10)) are 1.05 and 0.145, respectively. For Eqs. (8) and
 420 (10), ϕ equal to 0.85 and 0.80 are recommended which resulted in β_0 equal to 2.50 and 2.69,
 421 respectively. The comparisons of $N_{f,\psi}$ of CHS-to-RHS T-joint specimens with nominal resistances
 422 predicted from design equations given in EC3 [9] and CIDECT [10] as well as predictions from
 423 proposal-1 and -2 are graphically presented in Fig. 14. In addition, the distributions of the ratios of
 424 $N_{f,\psi}$ of CHS-to-RHS T-joint specimens-to-nominal resistances predicted from Eqs. (1) to (4), (8) and
 425 (10) are shown in Fig. 18.

426 6.2. For CHS-to-RHS X-joints

427 6.2.1. Chord face failure (F) mode ($0.30 \leq \beta < 0.75$)

428 Proposal-1:

429 Using post-fire material properties and post-fire peak temperature (ψ) correction factor:

$$N_{pm1} = \xi \left[f_{y0,\psi} t_0^2 \left(\frac{1.5e^{3\beta}}{0.65 + 0.025(2\gamma)} \right) \right] \quad (11)$$

430 where

$$\xi = \begin{cases} 0.915 & \text{for } 300^\circ\text{C} \leq \psi \leq 550^\circ\text{C} \\ 0.0023\psi - 0.35 & \text{for } 550^\circ\text{C} < \psi \leq 900^\circ\text{C} \end{cases} \quad (12)$$

431 Proposal-2:

432 Using room temperature material properties and post-fire peak temperature (ψ) correction factor:

$$N_{pm2} = (1.28 - 0.001\psi) \left[f_{y0} t_0^2 \left(\frac{1.5e^{3\beta}}{0.65 + 0.025(2\gamma)} \right) \right] \quad (13)$$

433 The Eqs. (11) and (13) are valid for $0.30 \leq \beta < 0.75$, $16.6 \leq 2\gamma \leq 50$, $15 \leq h_0/t_0 \leq 50$ and $0.50 \leq$
 434 $\tau \leq 0.90$. As shown in Table 7, the P_m and V_p of proposal-1 (i.e. Eq. (11)) are 1.01 and 0.139,
 435 respectively, while the P_m and V_p of proposal-2 (i.e. Eq. (13)) are 1.01 and 0.148, respectively. For
 436 both Eqs. (11) and (13), ϕ equal to 0.80 is recommended, resulting in β_0 equal to 2.58 and 2.55,
 437 respectively. The comparisons of $N_{f,\psi}$ of CHS-to-RHS X-joint specimens with nominal resistances
 438 predicted from design equations given in EC3 [9] and CIDECT [10] as well as predictions from
 439 proposal-1 and -2 are graphically presented in Fig. 15. In addition, the distributions of the ratios of
 440 $N_{f,\psi}$ of CHS-to-RHS X-joint specimens-to-nominal resistances predicted from Eqs. (1), (2), (11) and

441 (13) are shown in Fig. 19.

442 6.2.2. Combined failure (F+S) mode ($0.75 \leq \beta \leq 0.90$)

443 Proposal-1:

444 Using post-fire material properties and post-fire peak temperature (ψ) correction factor:

$$N_{pm1} = \xi \left[f_{y0,\psi} t_0^2 \left(\frac{65\beta - 35}{0.75 + 0.015(2\gamma)} \right) \right] \quad (14)$$

445 where

$$\xi = \begin{cases} 0.9 & \text{for } 300^\circ\text{C} \leq \psi \leq 550^\circ\text{C} \\ 0.001\psi + 0.35 & \text{for } 550^\circ\text{C} < \psi \leq 900^\circ\text{C} \end{cases} \quad (15)$$

446 Proposal-2:

447 Using room temperature material properties and post-fire peak temperature (ψ) correction factor:

$$N_{pm2} = (1.17 - 0.001\psi) \left[f_{y0} t_0^2 \left(\frac{65\beta - 35}{0.75 + 0.015(2\gamma)} \right) \right] \quad (16)$$

448 The Eqs. (14) and (16) are valid for $0.75 \leq \beta \leq 0.90$, $16.6 \leq 2\gamma \leq 50$, $15 \leq h_0/t_0 \leq 50$ and $0.75 \leq$
449 $\tau \leq 1.0$. As shown in Table 8, the P_m and V_p of proposal-1 (i.e. Eq. (14)) are 1.00 and 0.107,
450 respectively, while the P_m and V_p of proposal-2 (i.e. Eq. (16)) are 1.08 and 0.131, respectively. For
451 Eqs. (14) and (16), ϕ equal to 0.80 and 0.85 are recommended which resulted in β_0 equal to 2.68
452 and 2.63, respectively. The comparisons of $N_{f,\psi}$ of CHS-to-RHS X-joint specimens with nominal
453 resistances predicted from design equations given in EC3 [9] and CIDECT [10] as well as predictions
454 from proposal-1 and -2 are graphically presented in Fig. 16. In addition, the distributions of the ratios
455 of $N_{f,\psi}$ of CHS-to-RHS X-joint specimens-to-nominal resistances predicted from Eqs. (1) to (4), (14)
456 and (16) are shown in Fig. 20.

457

458 7. Conclusions

459 This paper presents post-fire static behaviour and design of cold-formed S900 steel grade T-
460 and X-joints made of circular hollow section (CHS) braces and square and rectangular hollow section
461 (SHS and RHS) chords. In this study, CHS-to-RHS T- and X-joints specimens were numerically
462 investigated under compression loads. Test results of cold-formed S900 steel grade CHS-to-RHS T-

463 and X-joints reported in Pandey and Young [7] were used to develop accurate finite element (FE)
464 models in this study. The numerical investigation corresponding to 300°C, 550°C, 750°C and 900°C
465 post-fire temperatures was performed using the measured post-fire residual static material properties
466 of S900 steel grade CHS and RHS members investigated by Pandey and Young [1]. A comprehensive
467 numerical parametric study comprising of 768 CHS-to-RHS T- and X-joints specimens was
468 performed using the validated FE models. The inclusion of welds in all FE models appreciably
469 improved the accuracies of the numerical results.

470 Overall, CHS-to-RHS T- and X-joints specimens were failed by chord face failure (F) mode
471 and a combination of chord face failure and chord side wall failure modes, i.e. combined failure (F+S)
472 mode. The residual static strengths of CHS-to-RHS T- and X-joints specimens corresponding to
473 300°C, 550°C, 750°C and 900°C post-fire temperatures were compared with the nominal resistances
474 predicted from design equations given in EC3 [9] and CIDECT [10] using the post-fire residual
475 material properties. Generally, it is shown that the design rules in EC3 [9] and CIDECT [10] are
476 unsuitable and unreliable for the range of fire exposed CHS-to-RHS T- and X-joints investigated in
477 this study with extended validity limits of critical geometric parameters. Therefore, using the two
478 design approaches, accurate, less dispersed and reliable design rules are proposed in this study for
479 the design of S900 steel grade CHS-to-RHS T- and X-joints subjected to post-fire temperatures
480 ranging from 300°C to 900°C.

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Fig. 1. Pedestrian truss bridge with CHS brace and RHS chord at Westminster Millennium Pier in London [3].

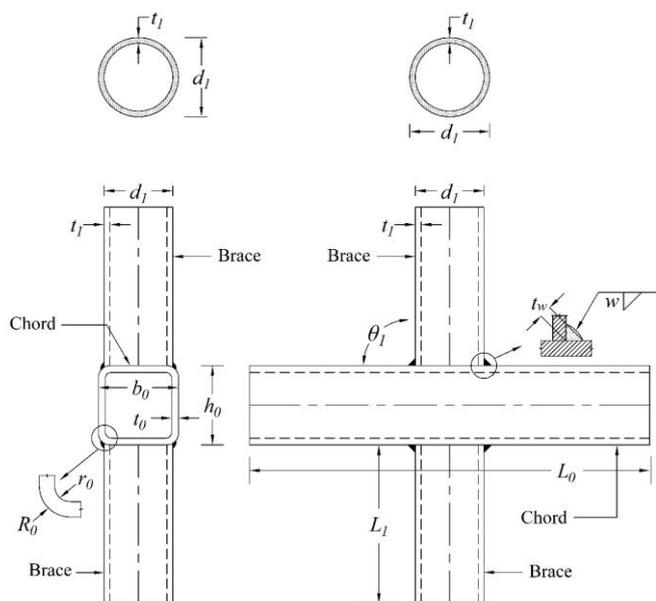
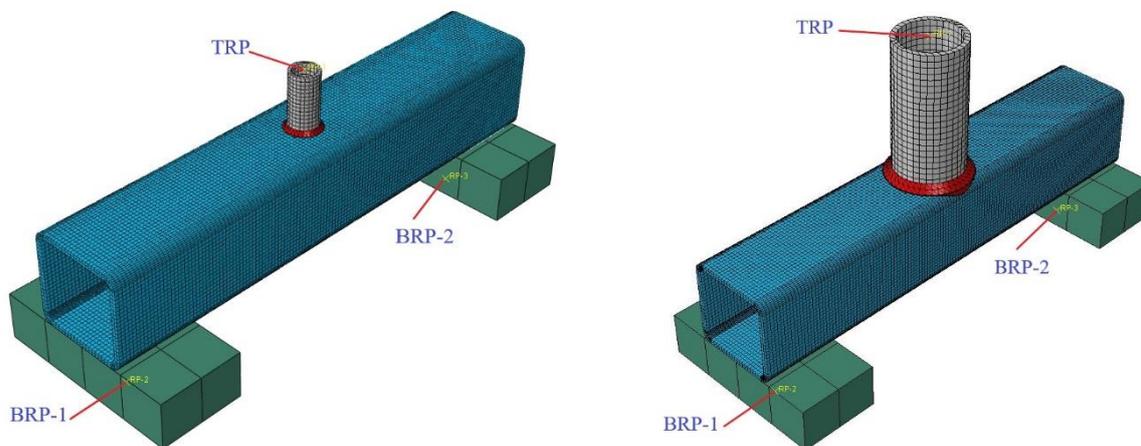


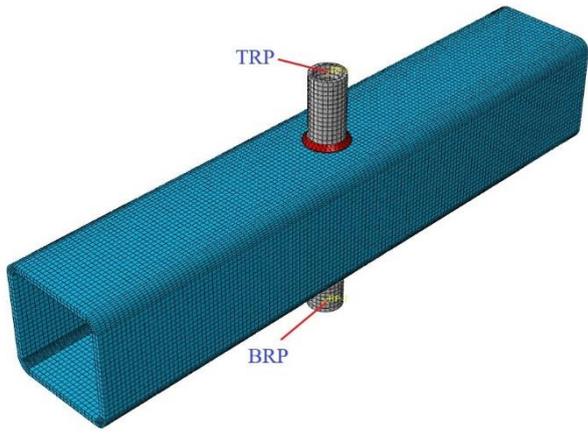
Fig. 2. Definitions of notations for CHS-to-RHS X-joint (also valid for CHS-to-RHS T-joint).



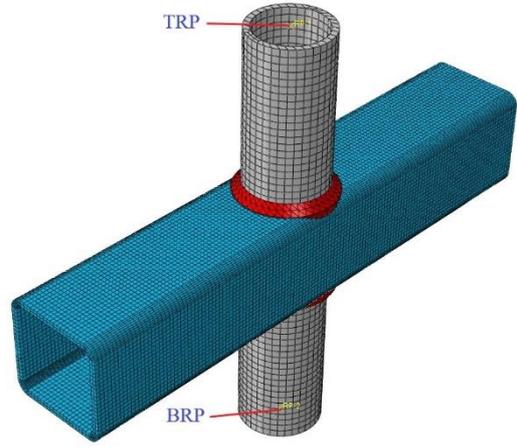
(a) CHS-to-RHS T-joint with $\beta=0.30$.

(b) CHS-to-RHS T-joint with $\beta=0.80$.

Fig. 3. Typical CHS-to-RHS T-joint FE models.

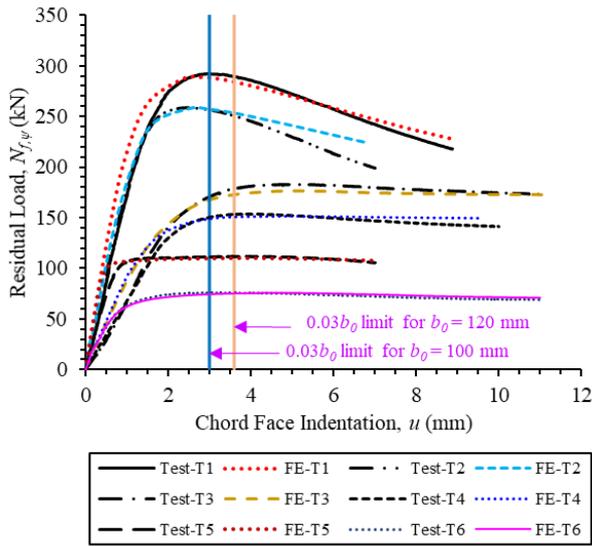


(a) CHS-to-RHS X-joint with $\beta=0.30$.

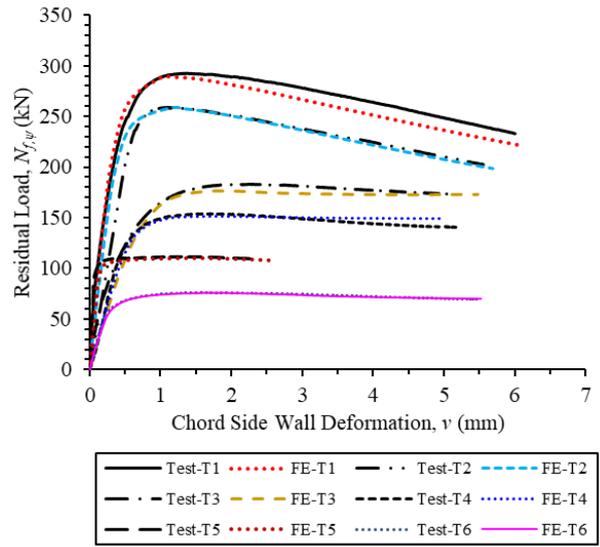


(b) CHS-to-RHS X-joint with $\beta=0.80$.

Fig. 4. Typical CHS-to-RHS X-joint FE models.

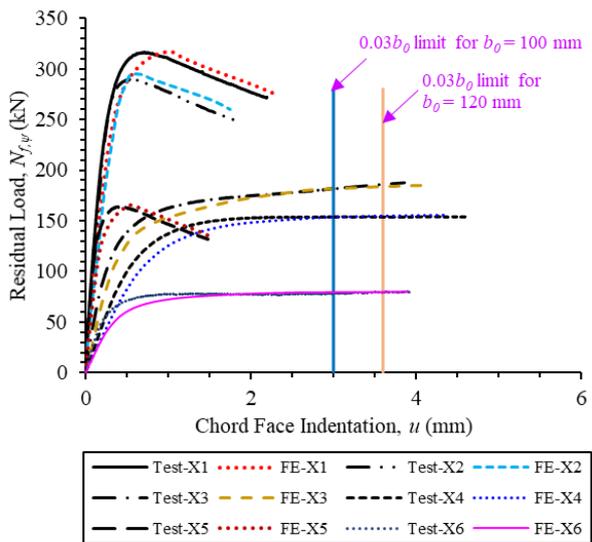


(a) Residual Load vs chord face indentation curves.

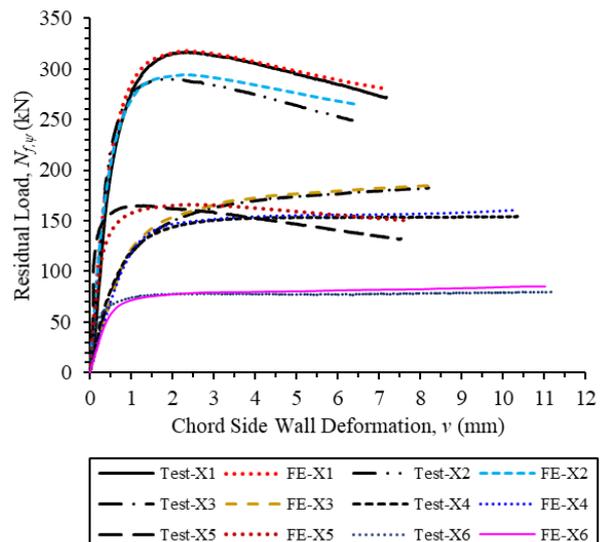


(b) Residual Load vs chord side wall deformation curves.

Fig. 5. Test vs FE load-deformation curves for CHS-to-RHS T-joints.

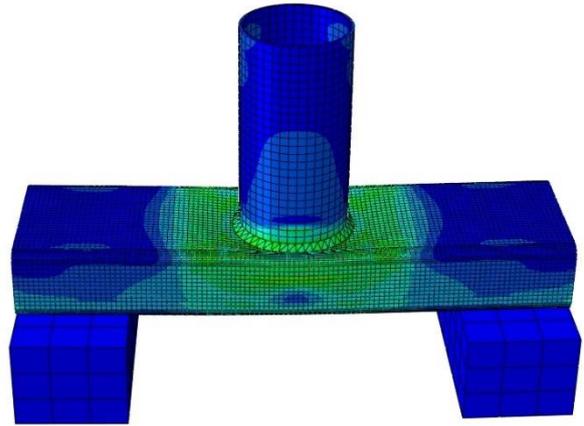


(a) Residual Load vs chord face indentation curves.

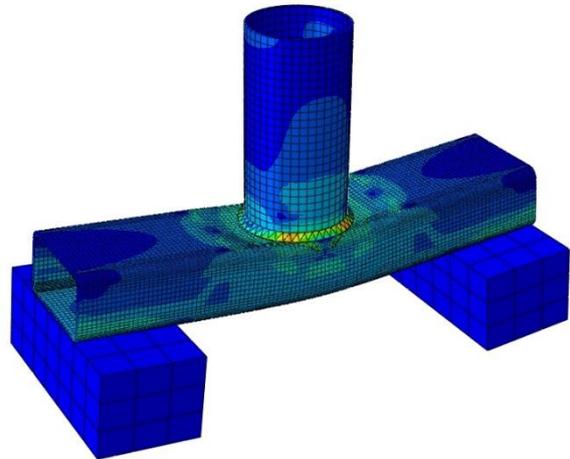


(b) Residual Load vs chord side wall deformation curves.

Fig. 6. Test vs FE load-deformation curves for CHS-to-RHS X-joints.

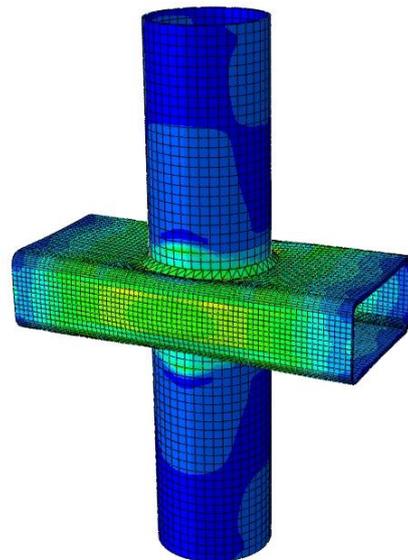


(a) Comparison of test and FE CHS-to-RHS T-joint failed by F mode.

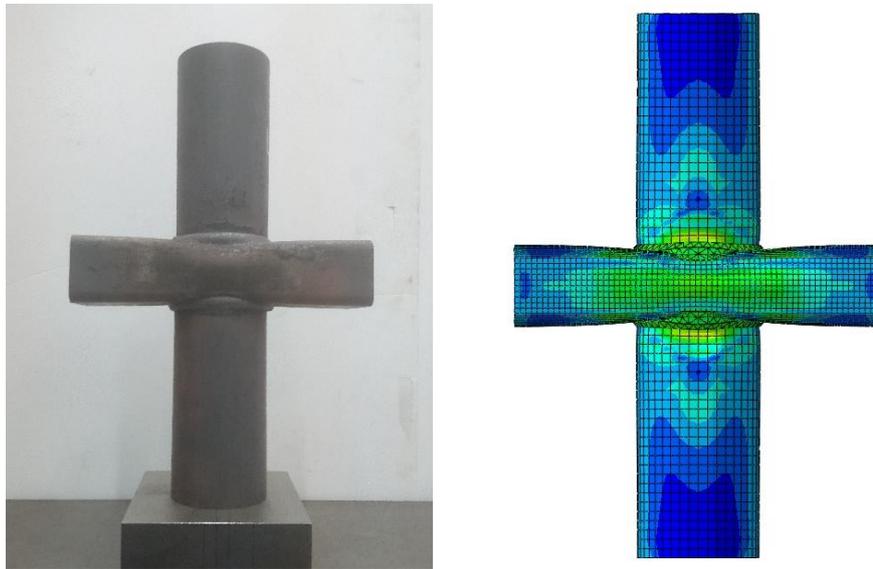


(b) Comparison of test and FE CHS-to-RHS T-joint failed by F+S mode.

Fig. 7. Failure modes comparisons between typical test and FE CHS-to-RHS T-joints.



(a) Comparison of test and FE CHS-to-RHS X-joint failed by F mode.



(b) Comparison of test and FE CHS-to-RHS X-joint failed by F+S mode.

Fig. 8. Failure modes comparisons between typical test and FE CHS-to-RHS X-joints.

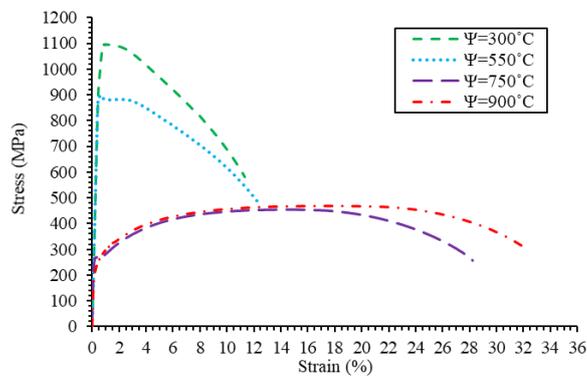
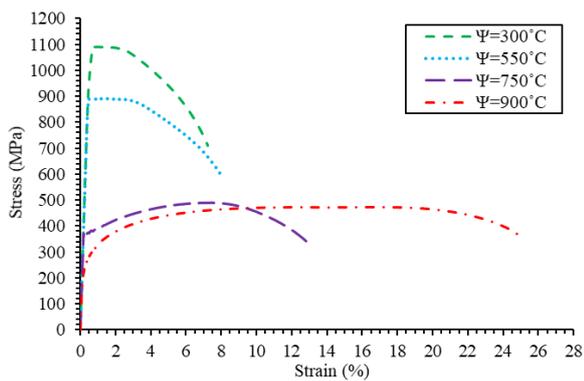
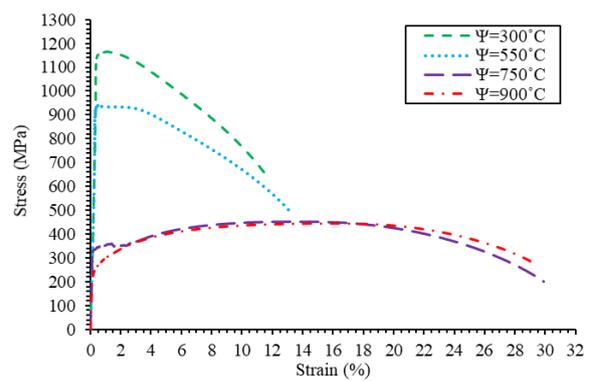


Fig. 9. Measured static post-fire stress-strain curves of CHS 88.9×4 [1].

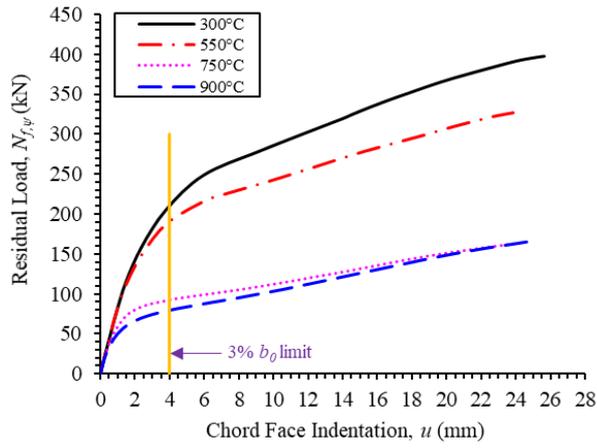


(a) Measured static post-fire stress-strain curves for flat portions of RHS 120×60×4.

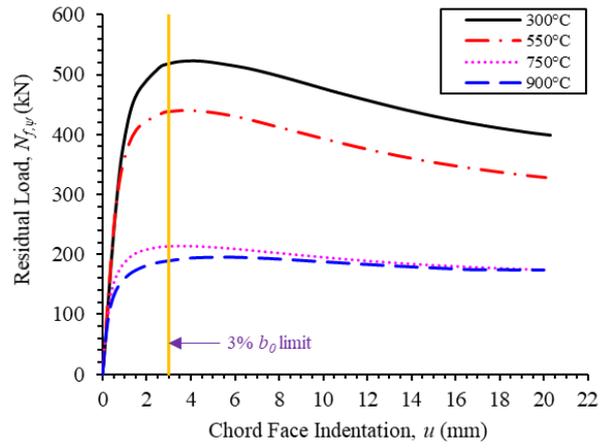


(b) Measured static post-fire stress-strain curves for corner portions of RHS 120×60×4.

Fig. 10. Measured static post-fire stress-strain curves of RHS 120×60×4 [1].

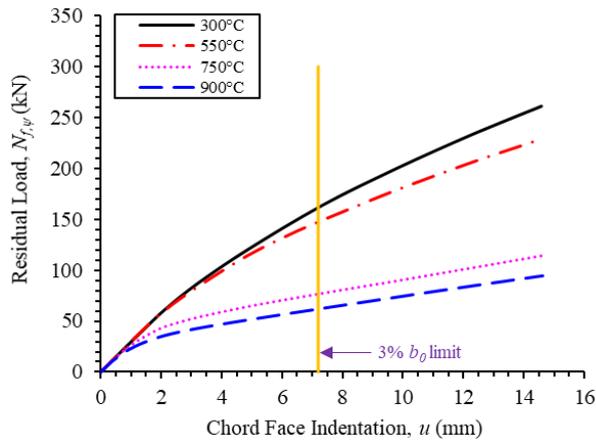


(a) For T-40×4-133×240×8 ($\beta=0.30$).

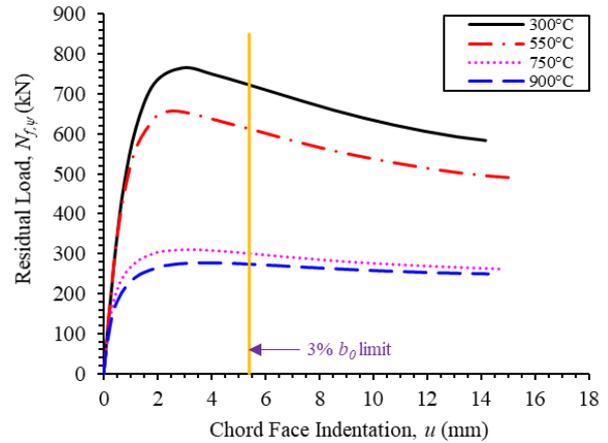


(b) For T-80×6-100×100×6 ($\beta=0.80$).

Fig. 11. Variations of load-deformation curves for typical CHS-to-RHS T-joints failed by F and F+S modes for different fire exposures.

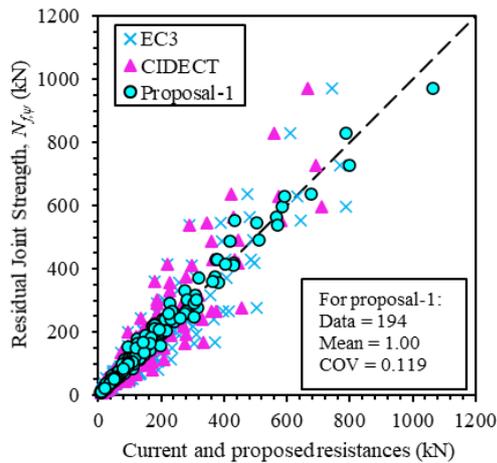


(a) For X-120×4.2-240×100×6 ($\beta=0.50$).

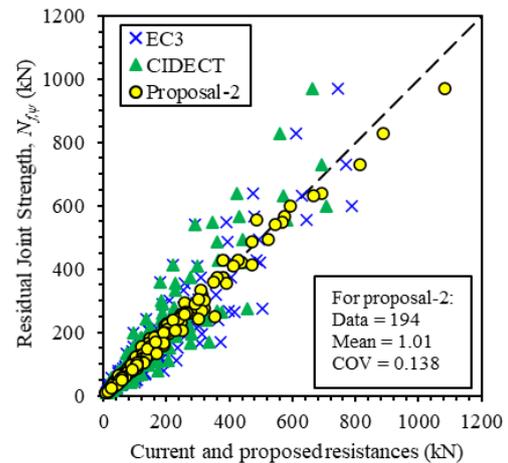


(b) For X-162×6-180×100×6 ($\beta=0.90$).

Fig. 12. Variations of load-deformation curves for typical CHS-to-RHS X-joints failed by F and F+S modes for different fire exposures.

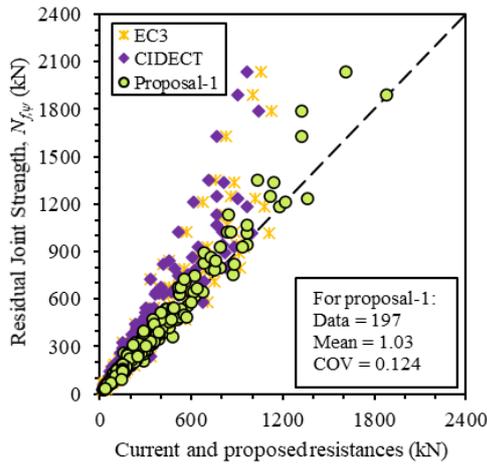


(a) For Proposal-1.

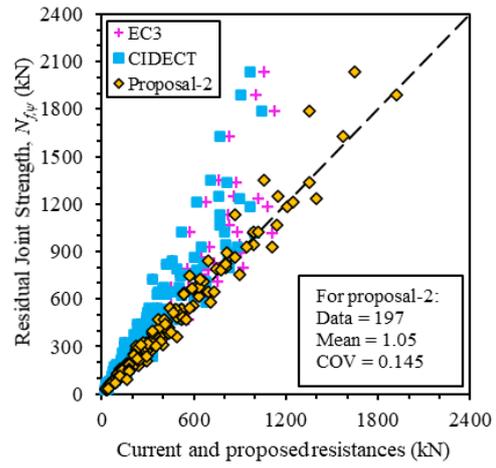


(b) For Proposal-2.

Fig. 13. Comparisons of residual joint strengths with current and proposed nominal resistances for CHS-to-RHS T-joints failed by F mode.

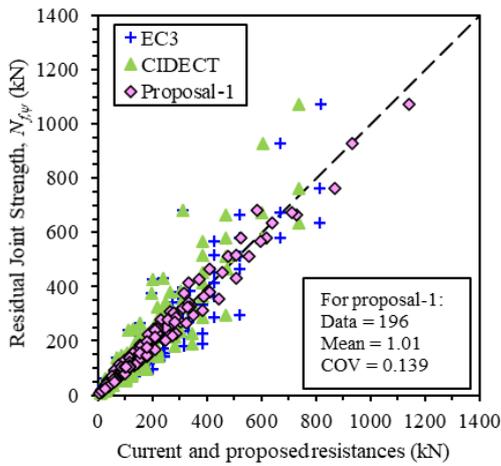


(a) For Proposal-1.

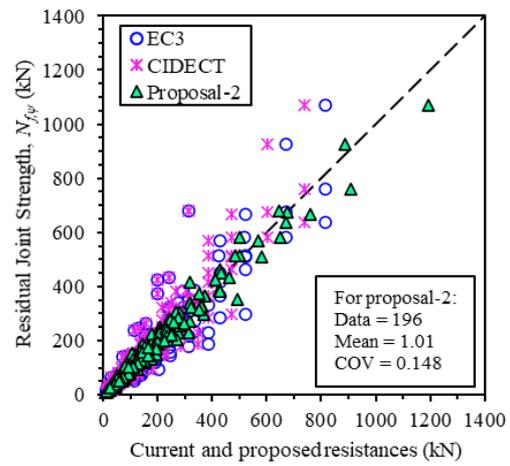


(b) For Proposal-2.

Fig. 14. Comparisons of residual joint strengths with current and proposed nominal resistances for CHS-to-RHS T-joints failed by F+S mode.

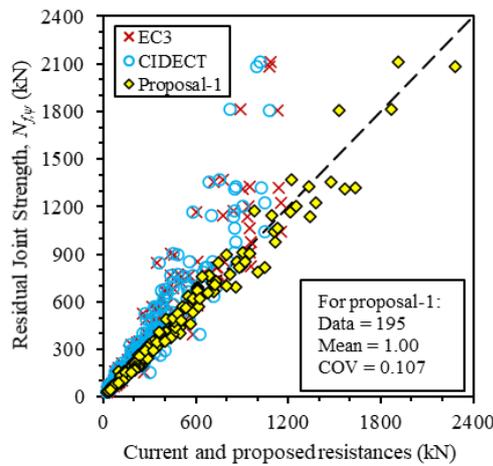


(a) For Proposal-1.

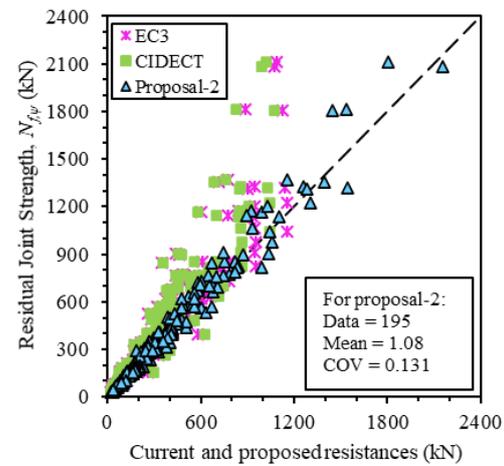


(b) For Proposal-2.

Fig. 15. Comparisons of residual joint strengths with current and proposed nominal resistances for CHS-to-RHS X-joints failed by F mode.

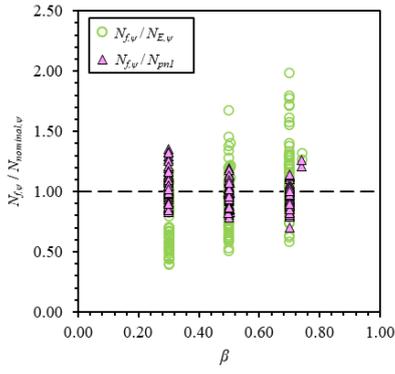


(a) For Proposal-1.

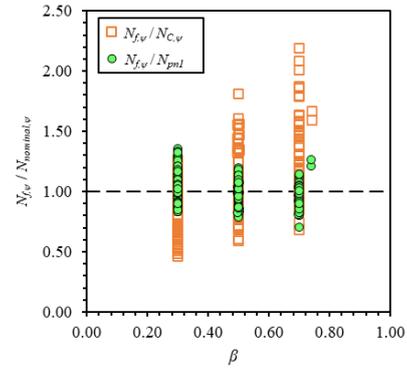


(b) For Proposal-2.

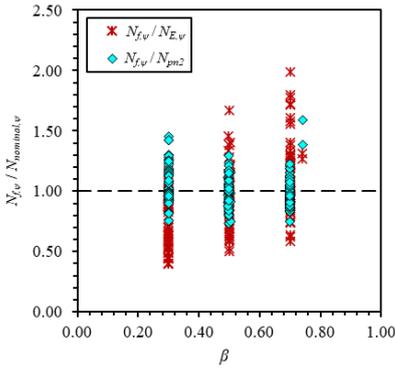
Fig. 16. Comparisons of residual joint strengths with current and proposed nominal resistances for CHS-to-RHS X-joints failed by F+S mode.



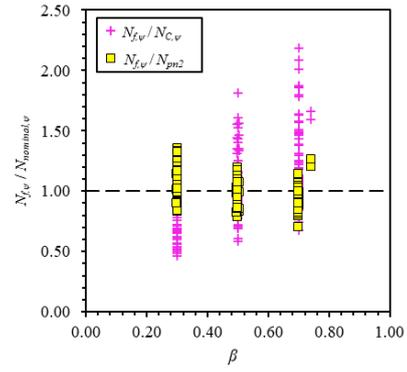
(a) EC3 [9] vs Proposal-1.



(b) CIDECT [10] vs Proposal-1.

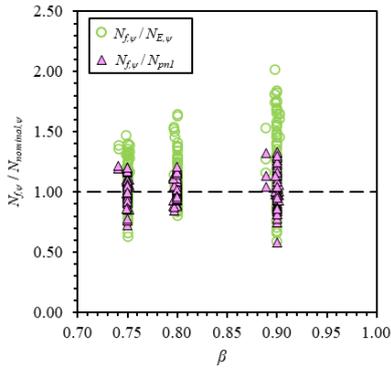


(c) EC3 [9] vs Proposal-2.

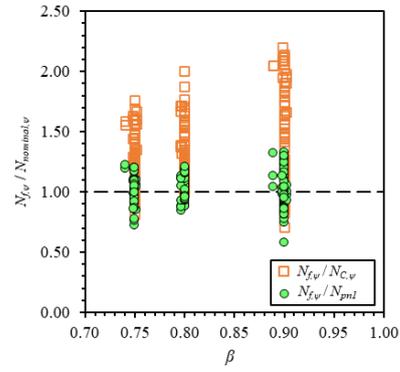


(d) CIDECT [10] vs Proposal-2.

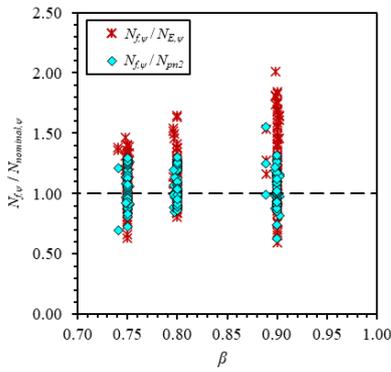
Fig. 17. Distributions of residual joint strength-to-current and proposed nominal resistance comparison ratios for CHS-to-RHS T-joints failed by F mode.



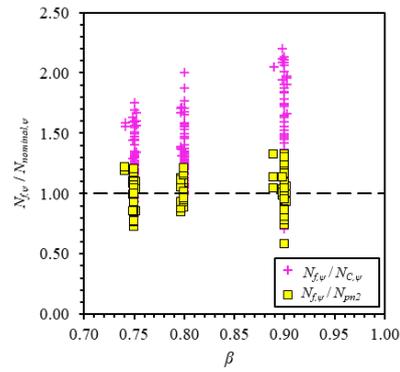
(a) EC3 [9] vs Proposal-1.



(b) CIDECT [10] vs Proposal-1.

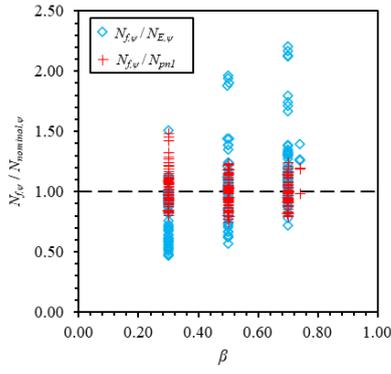


(c) EC3 [9] vs Proposal-2.

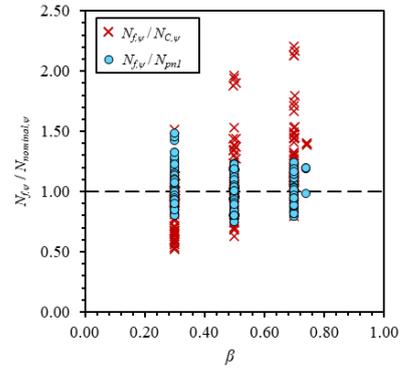


(d) CIDECT [10] vs Proposal-2.

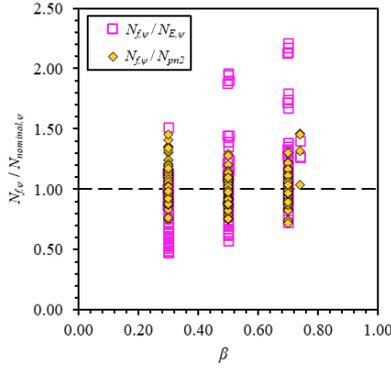
Fig. 18. Distributions of residual joint strength-to-current and proposed nominal resistance comparison ratios for CHS-to-RHS T-joints failed by F+S mode.



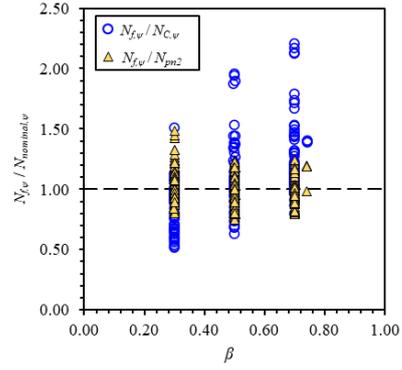
(a) EC3 [9] vs Proposal-1.



(b) CIDECT [10] vs Proposal-1.

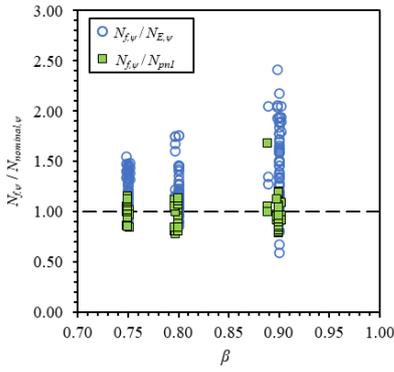


(c) EC3 [9] vs Proposal-2.

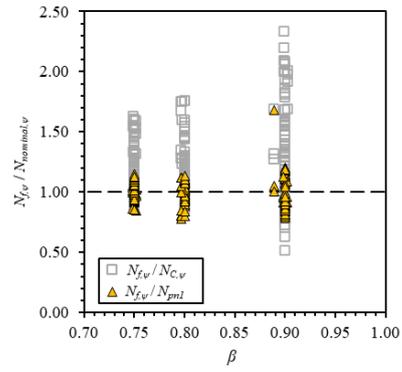


(d) CIDECT [10] vs Proposal-2.

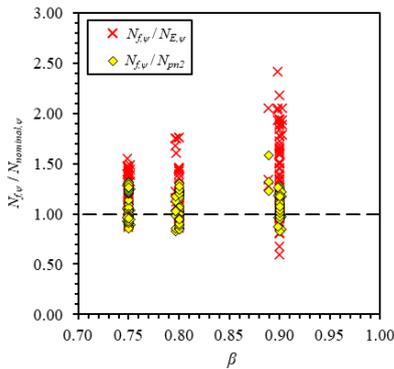
Fig. 19. Distributions of residual joint strength-to-current and proposed nominal resistance comparison ratios for CHS-to-RHS X-joints failed by F mode.



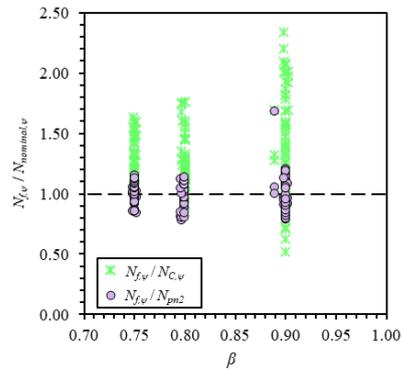
(a) EC3 [9] vs Proposal-1.



(b) CIDECT [10] vs Proposal-1.



(c) EC3 [9] vs Proposal-2.



(d) CIDECT [10] vs Proposal-2.

Fig. 20. Distributions of residual joint strength-to-current and proposed nominal resistance comparison ratios for CHS-to-RHS X-joints failed by F+S mode.

Table 1. Test vs FE residual strength comparisons for CHS-to-RHS T-joints.

Specimen Numbers	Specimens $T-d_1 \times t_1 - b_0 \times h_0 \times t_0 - \Psi$	β	Test Strengths [#] (kN)	FE Strengths (kN)	$\frac{N_{f,\psi}}{N_{FE}}$
			$N_{f,\psi}$	N_{FE}	
T1	T-88.9×4-100×60×4-P300°C	0.89	292.2	288.7	1.01
T2	T-88.9×4-100×60×4-P550°C	0.89	258.7	257.9	1.00
T3	T-88.9×3-120×60×4-P300°C	0.74	178.5	174.1	1.03
T4	T-88.9×3-120×60×4-P550°C	0.74	153.4	151.2	1.01
T5	T-88.9×4-100×60×4-P750°C	0.89	112.0	110.3	1.02
T6	T-88.9×3-120×60×4-P750°C	0.74	76.3	75.8	1.01
T7	T-88.9×3-120×60×4-P750°C-R	0.74	78.1	75.9	1.03
				Mean (P_m)	1.02
				COV (V_p)	0.009

Note: [#]Data obtained from Pandey and Young [7].

Table 2. Test vs FE residual strength comparisons for CHS-to-RHS X-joints.

Specimen Numbers	Specimens $X-d_1 \times t_1 - b_0 \times h_0 \times t_0 - \Psi$	β	Test Strengths [#] (kN)	FE Strengths (kN)	$\frac{N_{f,\psi}}{N_{FE}}$
			$N_{f,\psi}$	N_{FE}	
X1	X-88.9×4-100×60×4-P300°C	0.89	316.6	317.0	1.00
X2	X-88.9×4-100×60×4-P550°C	0.89	289.8	294.3	0.98
X3	X-88.9×3-120×60×4-P300°C	0.74	186.0	184.9	1.01
X4	X-88.9×3-120×60×4-P550°C	0.74	153.8	155.1	0.99
X5	X-88.9×4-100×60×4-P750°C	0.89	164.3	165.9	0.99
X6	X-88.9×3-120×60×4-P750°C	0.74	79.3	79.6	1.00
X7	X-88.9×3-120×60×4-P550°C-R	0.74	153.3	155.2	0.99
				Mean (P_m)	0.99
				COV (V_p)	0.007

Note: [#]Data obtained from Pandey and Young [7].

Table 3. Overall ranges of critical parameters used in parametric study.

Parameters	Validity Ranges
ψ	[300°C to 900°C]
$\beta (d_1/b_0)$	[0.30 to 0.90]
$2\gamma (b_0/t_0)$	[16.6 to 50]
h_0/t_0	[16.6 to 50]
$\tau (t_1/t_0)$	[0.50 to 1.0]

Table 4. Post-fire material properties of tubular members used in parametric study [1].

Post-fire			Measured Post-fire Material Properties						
Temperatures (ψ)	Materials	Regions	E (GPa)	$\sigma_{0.2}$ (MPa)	$\varepsilon_{0.2}$ (%)	σ_u (MPa)	$0.80\sigma_u$ (MPa)	ε_u (%)	ε_f (%)
300°C	RHS (120×60×4)	Flat	214	1084	0.71	1090	872	1.00	7.23 ^a
	RHS (120×60×4)	Corner	232	1161	0.70	1166	933	1.12	11.68 ^b
	CHS (88.9×4)	Curved	207	1062	0.71	1096	877	1.04	11.32 ^b
550°C	RHS (120×60×4)	Flat	219	889	0.61	891	713	1.37	8.10 ^a
	RHS (120×60×4)	Corner	231	937	0.61	933	746	2.19	13.06 ^b
	CHS (88.9×4)	Curved	214	893	0.62	882	706	2.17	12.45 ^b
750°C	RHS (120×60×4)	Flat	207	371	0.38	491	392	7.44	13.17 ^a
	RHS (120×60×4)	Corner	244	337	0.34	452	362	13.39	29.89 ^b
	CHS (88.9×4)	Curved	198	269	0.34	455	364	14.32	28.23 ^b
900°C	RHS (120×60×4)	Flat	200	257	0.33	473	378	16.56	25.01 ^a
	RHS (120×60×4)	Corner	227	251	0.31	445	356	16.44	29.03 ^b
	CHS (88.9×4)	Curved	202	233	0.32	469	375	17.30	32.39 ^b

Note: ^afracture strain based on 50 mm gauge length; ^bfracture strain based on 25 mm gauge length.

Table 5. Summary of comparisons between test and FE residual strengths with current and proposed nominal resistances for CHS-to-RHS T-joints failed by F mode.

Post-fire		Comparisons			
Temperatures (ψ)	Parameters	$\frac{N_{f,\psi}}{N_{E,\psi}}$	$\frac{N_{f,\psi}}{N_{C,\psi}}$	$\frac{N_{f,\psi}}{N_{pn1}}$	$\frac{N_{f,\psi}}{N_{pn2}}$
300°C	No. of data (n)	49	49	49	49
	Mean (P_m)	0.78	0.95	0.98	0.97
	COV (V_p)	0.294	0.315	0.081	0.096
550°C	No. of data (n)	49	49	49	49
	Mean (P_m)	0.81	0.98	1.02	1.10
	COV (V_p)	0.313	0.331	0.111	0.123
750°C	No. of data (n)	48	48	48	48
	Mean (P_m)	1.07	1.16	1.03	0.94
	COV (V_p)	0.290	0.308	0.114	0.114
900°C	No. of data (n)	48	48	48	48
	Mean (P_m)	1.10	1.20	0.97	1.04
	COV (V_p)	0.196	0.220	0.152	0.152
Overall	No. of data (n)	194	194	194	194
	Mean (P_m)	0.94	1.07	1.00	1.01
	COV (V_p)	0.309	0.307	0.119	0.138
	Resistance factor (ϕ)	1.00	1.00	0.80	0.80
	Reliability index (β_0)	1.03	1.46	2.63	2.59

Table 6. Summary of comparisons between test and FE residual strengths with current and proposed nominal resistances for CHS-to-RHS T-joints failed by F+S mode.

Post-fire		Comparisons			
Temperatures (ψ)	Parameters	$\frac{N_{f,\psi}}{N_{E,\psi}}$	$\frac{N_{f,\psi}}{N_{C,\psi}}$	$\frac{N_{f,\psi}}{N_{pn1}}$	$\frac{N_{f,\psi}}{N_{pn2}}$
300°C	No. of data (n)	49	49	49	49
	Mean (P_m)	1.13	1.41	1.02	1.02
	COV (V_p)	0.272	0.251	0.129	0.132
550°C	No. of data (n)	49	49	49	49
	Mean (P_m)	1.08	1.34	0.99	1.14
	COV (V_p)	0.226	0.238	0.092	0.105
750°C	No. of data (n)	51	50	51	51
	Mean (P_m)	1.25	1.39	1.09	0.94
	COV (V_p)	0.180	0.197	0.097	0.106
900°C	No. of data (n)	48	48	48	48
	Mean (P_m)	1.21	1.36	1.02	1.10
	COV (V_p)	0.233	0.243	0.154	0.154
Overall	No. of data (n)	197	197	197	197
	Mean (P_m)	1.17	1.37	1.03	1.05
	COV (V_p)	0.233	0.231	0.124	0.145
	Resistance factor (ϕ)	1.00	1.00	0.85	0.80
	Reliability index (β_o)	1.83	2.42	2.50	2.69

Table 7. Summary of comparisons between test and FE residual strengths with current and proposed nominal resistances for CHS-to-RHS X-joints failed by F mode.

Post-fire		Comparisons			
Temperatures (ψ)	Parameters	$\frac{N_{f,\psi}}{N_{E,\psi}}$	$\frac{N_{f,\psi}}{N_{C,\psi}}$	$\frac{N_{f,\psi}}{N_{pn1}}$	$\frac{N_{f,\psi}}{N_{pn2}}$
300°C	No. of data (n)	49	49	49	49
	Mean (P_m)	0.87	0.96	1.03	0.97
	COV (V_p)	0.279	0.279	0.117	0.126
550°C	No. of data (n)	50	50	50	50
	Mean (P_m)	0.91	1.01	1.07	1.12
	COV (V_p)	0.272	0.272	0.089	0.106
750°C	No. of data (n)	49	49	49	49
	Mean (P_m)	1.20	1.20	1.10	0.95
	COV (V_p)	0.332	0.332	0.163	0.163
900°C	No. of data (n)	48	48	48	48
	Mean (P_m)	1.16	1.16	0.99	1.01
	COV (V_p)	0.197	0.197	0.144	0.144

	No. of data (n)	196	196	196	196
	Mean (P_m)	1.03	1.08	1.01	1.01
Overall	COV (V_p)	0.310	0.289	0.139	0.148
	Resistance factor (ϕ)	1.00	1.00	0.80	0.80
	Reliability index (β_0)	1.27	1.54	2.58	2.55

Table 8. Summary of comparisons between test and FE residual strengths with current and proposed nominal resistances for CHS-to-RHS X-joints failed by F+S mode.

Post-fire		Comparisons			
Temperatures (ψ)	Parameters	$\frac{N_{f,\psi}}{N_{E,\psi}}$	$\frac{N_{f,\psi}}{N_{C,\psi}}$	$\frac{N_{f,\psi}}{N_{pn1}}$	$\frac{N_{f,\psi}}{N_{pn2}}$
			No. of data (n)	49	49
300°C	Mean (P_m)	1.26	1.35	0.99	1.05
	COV (V_p)	0.253	0.239	0.097	0.099
	No. of data (n)	49	49	49	49
550°C	Mean (P_m)	1.20	1.29	0.96	1.18
	COV (V_p)	0.224	0.227	0.085	0.098
	No. of data (n)	49	49	49	49
750°C	Mean (P_m)	1.34	1.30	1.04	0.94
	COV (V_p)	0.223	0.212	0.120	0.098
	No. of data (n)	48	48	48	48
900°C	Mean (P_m)	1.33	1.30	1.01	1.14
	COV (V_p)	0.259	0.265	0.110	0.110
	No. of data (n)	195	195	195	195
Overall	Mean (P_m)	1.28	1.31	1.00	1.08
	COV (V_p)	0.243	0.235	0.107	0.131
	Resistance factor (ϕ)	1.00	1.00	0.80	0.85
	Reliability index (β_0)	2.06	2.26	2.68	2.63