

# BEHAVIOUR AND DESIGN OF COLD-FORMED HIGH STRENGTH STEEL RHS T-JOINTS UNDERGOING COMPRESSION LOADS AT ELEVATED TEMPERATURES

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## Abstract

This study presents a comprehensive numerical program aiming to investigate the static resistances of cold-formed high strength steel (CFHSS) T-joints with square and rectangular hollow section (SHS and RHS) braces and chords at elevated temperatures. The included angle between brace and chord members was 90°. The static behaviour of simply supported SHS and RHS T-joints undergoing compression loads through brace members was investigated at four elevated temperatures, including 400°C, 500°C, 600°C and 1000°C. The mechanical properties at elevated temperatures given in the literature for cold-formed S900 steel grade tubular members were used in this study. The numerical investigation was performed using the finite element (FE) models developed and validated by Pandey et al. [1] and Pandey and Young [2] for cold-formed S960 steel grade T-joints at ambient temperature and post-fire conditions. In total, 756 FE T-joint specimens were analysed in this numerical study, including 189 FE T-joint specimens for each elevated temperature. The tubular T-joint specimens were failed by chord face failure, chord side wall failure and a combination of these two failure modes. The resistances of investigated T-joints at elevated temperatures were compared with the nominal resistances predicted from design rules given in European code and CIDECT using the mechanical properties at elevated temperatures. Overall, it is shown that the current design rules given in European code and CIDECT are uneconomical and unreliable. As a result, economical and reliable design rules are proposed in this study through two design approaches for predicting the resistances of cold-formed steel SHS and RHS 90° T-joints of S900 grade at elevated temperatures.

*Keywords: Cold-formed steel; Design equations; Elevated temperature; FE analysis; Tubular members; Welded joints.*

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## 30 1. Introduction

31 Tubular steel structures are subjected to different types of loading and also susceptible to  
32 extreme natural events, including fire. Adequate performance of joints under different adverse  
33 conditions is a prerequisite to ensure the integrity of the overall structure. Welded joints of a tubular  
34 steel structure need careful design considerations due to the presence of geometric discontinuity,  
35 stress concentration, complex failures, residual stresses and fabrication defects. It is an acknowledged  
36 fact that steel materials are quite sensitive to fire. The strength and stiffness of steel materials sharply  
37 deteriorate at high elevated temperatures. Consequently, the failure load of a tubular joint at high  
38 elevated temperature could be significantly smaller than its joint resistance at ambient temperature,  
39 which could cause progressive or sudden collapse of the entire structure. Recent years have seen a  
40 significant increase in the structural applications of high strength steel (HSS) due to their superior  
41 strength-to-weight ratio. The recent growths in manufacturing and metallurgical sectors facilitated  
42 the production of HSS with reduced carbon content and improved toughness. HSS of S960 and S1100  
43 steel grades are used in the Fast Bridge 48 designed for the Swedish army. The bridge has a span of  
44 46 m and is designed for a 65 ton tank for more than 1000 crossings [3]. The structural applications  
45 of HSS are comprehensively detailed in Pandey and Young [4]. The high strengths combined with  
46 natural stiff form of hollow section members enable the construction of stronger and lighter structures.  
47 However, the lack of adequate research work and design recommendations are the primary reasons  
48 hampering the widespread use of high strength structural steels. In addition, some challenges also  
49 need to be addressed in order to implement large scale structural applications of HSS, including  
50 welding of HSS, high notch sensitivity of HSS, softening in the heat affected region of HSS,  
51 preheating of thin HSS material for welding, use of current ultimate deformation limit ( $0.03b_0$ ), high  
52 cost-to-material ratio, fatigue of HSS and so on.

53 It should be noted that a series of experimental investigations [4-9] on cold-formed S900 and  
54 S960 steel grades T- and X-joints were conducted by the authors. In addition, Pandey et al. [1,10]  
55 proposed design rules for predicting the static strengths of cold-formed S900 and S960 steel grades  
56 T- and TF-joints. Moreover, experimental and numerical investigations on box-section T- and X-  
57 joints with steel grades ranging from S460 to S960 were conducted by Lan et al. [11,12]. It is worth

58 noting that these studies [1,4-12] were performed at ambient temperature, and no investigation is  
59 currently available on the static performance of HSS tubular joints at elevated temperatures ( $T$ ). So  
60 far, all investigations on the static behaviour of hollow section joints at elevated temperatures were  
61 conducted on normal strength steel (i.e. steel grade less than and equal to S460) joints with main  
62 focus on CHS joints.

63 In this study, elevated temperature joint resistances ( $N_{f,T}$ ) of cold-formed high strength steel  
64 square and rectangular hollow section (SHS and RHS) 90° T-joints were numerically investigated.  
65 The  $N_{f,T}$  of cold-formed high strength steel (CFHSS) SHS and RHS (henceforth, RHS include SHS)  
66 T-joints undergoing compression loads were numerically studied at four elevated temperatures,  
67 including 400°C, 500°C, 600°C and 1000°C. It should be stressed that design rules for predicting the  
68 resistances of tubular joints at elevated temperatures are not given in international codes and guides.  
69 As a result, in this study, economical and reliable design rules are proposed by modifying the design  
70 equations proposed by Pandey et al. [1] for CFHSS RHS 90° T-joints at ambient temperature.  
71 Moreover, the applicability of current design rules given in EC3 [13] and CIDECT [14] using  
72 mechanical properties at elevated temperatures was also examined. Overall, it is shown that, on using  
73 the mechanical properties at elevated temperatures, the current design rules given in EC3 [13] and  
74 CIDECT [14] are uneconomical and unreliable. In addition, the predictions from design rules given  
75 in EC3 [13] and CIDECT [14] are quite dispersed.

## 76 **2. Review of investigations conducted on tubular joints at elevated temperatures**

77 Chen et al. [15] studied the static performance of CHS T-joints with ring stiffeners at elevated  
78 temperatures and finally proposed design equations for predicting the residual resistances of the  
79 investigated joints. Using transient state analysis, Gao et al. [16] studied the structural behaviour of  
80 CHS T-joints with collar plates. The residual resistances of concrete-filled CHS T-joints after fire  
81 exposures were studied by Gao et al. [17]. The influence of critical geometric parameters on the  
82 residual resistances of CHS T-joints at elevated temperatures was studied by Cheng et al. [18]. Lan  
83 and Huang [19] numerically investigated the joint resistances of duplex, austenitic and AISI 304  
84 stainless steel RHS T- and X-joints at elevated temperatures and proposed design equations for their

85 ultimate resistances. Feng and Young [20] carried out a numerical investigation on duplex and AISI  
86 304 stainless steel RHS T- and X-joints using mechanical properties proposed by Chen and Young  
87 [21] at elevated temperatures. Subsequently, design rules were proposed by applying temperature  
88 correction factors on design equations given in CIDECT [14]. Nassiraei et al. [22] proposed design  
89 equations for CHS X-joints at elevated temperatures, where specimens were reinforced with collar  
90 plates. Two methods for predicting the ultimate capacities of CHS T-joints at elevated temperatures  
91 were proposed by Shao et al. [23] by duly investigating the effects of critical geometric parameters.  
92 Using non-linear regression analysis, Dodaran et al. [24] proposed a design formula to predict the  
93 resistances of KT-joints at elevated temperatures. Lan et al. [25] numerically studied the static  
94 performance of duplex, austenitic and AISI 304 stainless steel RHS K- and N-joints at elevated  
95 temperatures. In addition, design rules were also proposed by Lan et al. [25] using residual yield  
96 strengths.

97         The residual joint resistances of CHS T-joints subjected to brace in-plane bending load were  
98 investigated by Fung et al. [26] at elevated temperatures. Static performance of CHS T-joint without  
99 internal stiffeners was studied by Tan et al. [27] using experimental and numerical methods. It was  
100 reported that the joint resistance sharply reduced at high temperatures. The critical temperature of  
101 CHS K-joints was determined using the deformation rate based criterion in He et al. [28].  
102 Compression loaded full-scale CHS T-joints were experimentally and numerically studied at elevated  
103 temperatures by Nguyen et al. [29,30]. The residual resistances of impacted CHS T-joints at elevated  
104 temperatures were investigated by Yu et al. [31]. The post-fire residual capacities of CHS T-joints  
105 were experimentally studied by Jin et al. [32]. Liu et al. [33] performed a numerical parametric study  
106 to investigate the static behaviour of CHS T-joints at elevated temperatures. The structural  
107 performance of CHS T-joints subjected to blast and fire was experimentally studied by Yu et al. [34].  
108 The technique of artificial neural network was used by Xu et al. [35] to estimate the resistances of  
109 CHS T-joints at elevated temperatures. Ozyurt et al. [36] numerically investigated the joint  
110 resistances of CHS and SHS T-, Y-, X-, K- and N-joints at elevated temperatures. Based on numerical  
111 results, reduction factors were proposed to estimate the residual resistances of the investigated joints.  
112 Ozyurt et al. [37] numerically investigated the joint resistances of elliptical hollow section (EHS) T-

113 and X-joints at elevated temperatures.

### 114 **3. Approach used in this investigation**

115 The numerical investigation was conducted using ABAQUS [38]. In the absence of any  
116 experimental investigation on CFHSS RHS T-joints at elevated temperatures, the numerical  
117 investigation in this study was performed using the finite element (FE) models developed and  
118 validated by Pandey et al. [1] for cold-formed S900 and S960 steel grades RHS 90° T-joints at  
119 ambient temperature. It is important to note that similar FE models were successfully used by Pandey  
120 and Young [2] to validate the test results of fire exposed (i.e. post-fire) cold-formed S900 and S960  
121 steel grades RHS 90° T-joints using post-fire mechanical properties. As natural fires have different  
122 temperature vs time curves and also due to substantial cost involved in a fire test, numerical studies  
123 are popularly used for such investigations. It is due to these reasons, the FE models of tubular joints  
124 validated against ambient temperature test results were used in many numerical studies  
125 [19,20,25,36,37,39-51] for their corresponding elevated temperatures investigations.

126 The numerical investigation in this study was performed using the constitutive stress-strain  
127 model proposed by Li and Young [52] for S900 steel grade tubular members at elevated temperatures.  
128 The tubular members used in Pandey et al. [1], Pandey and Young [2] and Li and Young [52,53] were  
129 produced by the identical manufacturer and had similar chemical compositions, therefore, the  
130 constitutive stress-strain model proposed by Li and Young [52] at elevated temperatures can safely  
131 be used in this study. The numerical investigation was then performed using the mechanical  
132 properties predicted from stress-strain model [52] at 400°C, 500°C, 600°C and 1000°C. It should be  
133 noted that coupon specimens were extracted from the flat regions of tubular members. The stress-  
134 strain curves of cold-formed S900 steel grade tubular member obtained using steady state tests for  
135 temperatures ranging from 100°C to 1000°C are reported in Li and Young [53]. It should be noted  
136 that for temperatures less than 400°C, the deterioration of mechanical properties of cold-formed S900  
137 steel grade tubular member was insignificant. As reported in Li and Young [53], the residual values  
138 of ultimate strength of cold-formed S900 steel grade tubular member at 400°C, 500°C, 600°C and  
139 1000°C were 83%, 60%, 35% and 2% of the corresponding ultimate strength at ambient temperature.

140 Therefore, in order to investigate a wide range of strength reductions at elevated temperatures, the  
141 numerical investigation in this study was performed at 400°C, 500°C, 600°C and 1000°C.

#### 142 **4. Outline of test programs carried out on cold-formed high strength steel RHS T-joints at** 143 **ambient temperature and post-fire conditions**

144 At ambient temperature, the static performance of cold-formed S900 and S960 steel grades  
145 RHS 90° T-joints was experimentally investigated by Pandey and Young [54]. The braces and chords  
146 were welded using robotic metal active gas welding. In total, twenty-four 90° T-joint tests were  
147 conducted, where simply supported test specimens were axially compressed via braces. The nominal  
148 0.2% proof stresses of tubular members were 900 and 960 MPa. The symbols  $b$ ,  $h$ ,  $t$  and  $R$  stand for  
149 cross-section width, depth, thickness and external corner radius of RHS member, respectively. The  
150 subscripts of symbols 0 and 1 denote chord and brace, respectively. Fig. 1 presents various notations  
151 for RHS T-joints. The failure modes identified in the tests [54] were chord face failure (F), chord side  
152 wall failure (S) and a combination of these two failure modes, named combined failure (F+S). The  
153 lengths of braces ( $L_1$ ) were equal to two times the maximum of brace cross-section width ( $b_1$ ) and  
154 depth ( $h_1$ ). On the other hand, the lengths of chords ( $L_0$ ) were equal to  $h_1 + 3h_0 + 180$  mm. The test  
155 results were obtained in the form of  $N$  vs  $u$  and  $N$  vs  $v$  curves, where  $N$ ,  $u$  and  $v$  stand for static brace  
156 axial compression load, chord face indentation and chord side wall deformation, respectively.

157 The static behaviour of cold-formed steel fire exposed RHS 90° T-joints of S900 and S960  
158 grades was investigated by Pandey and Young [55]. Before conducting the static joint tests, the test  
159 specimens were subjected to a total of three fire exposures with preselected post-fire peak  
160 temperatures ( $\psi$ ) equal to 300°C, 550°C and 750°C, respectively. In total, sixteen 90° T-joints were  
161 tested under compression loads with simply supported chords. The nominal 0.2% proof stresses of  
162 without fire exposed tubular members were 900 and 960 MPa. The braces and chords were welded  
163 using robotic metal active gas welding. The test specimens were exposed to fire inside a gas furnace,  
164 where the furnace temperature was increased in accordance with the ISO-834 [56]. After attaining  
165 the preselected post-fire peak temperatures ( $\psi$ ), the test specimens were allowed to naturally cool  
166 inside the furnace. Subsequently, at ambient temperature, RHS 90° T-joint test specimens were

167 axially compressed through brace members.

## 168 **5. Numerical programs on cold-formed high strength steel RHS T-joints at ambient** 169 **temperature and post-fire conditions**

### 170 5.1. General

171 The numerical investigations on cold-formed steel RHS 90° T-joints of S900 and S960 grades  
172 at ambient temperature and post-fire conditions were conducted by Pandey et al. [1] and Pandey and  
173 Young [2], respectively. The static (general) analysis procedure given in ABAQUS [38] was used as  
174 the solver. The isotropic strain hardening law was selected for the analysis, while the yielding onsets  
175 of FE models were based on the von-Mises yield theory. In the FE analyses, the growth of the time  
176 step was kept non-linear in order to reduce the overall computation time. Furthermore, the default  
177 Newton-Raphson method was used to find the roots of non-linear equilibrium equations. The material  
178 non-linearities were considered in the FE models developed for ambient temperature and post-fire  
179 conditions by assigning the measured values of ambient temperature and post-fire static stress-strain  
180 values of flat and corner portions of RHS members. However, experimentally obtained constitutive  
181 material curves both at ambient temperature and post-fire conditions were transformed into true  
182 stress-strain curves prior to their inclusion into the FE models. The true stress ( $\sigma_{true}$ ) and true plastic  
183 strain ( $\epsilon_{true,pl}$ ) were determined in accordance with ABAQUS [38], where  $\sigma_{true} = \sigma (1+\epsilon)$  and  $\epsilon_{true,pl} =$   
184  $\ln(1+\epsilon) - \sigma_{true} / E_o$ . The terms  $\sigma$  and  $\epsilon$  are the measured stress and strain obtained from tensile coupon  
185 tests, respectively. It is important to input the engineering stress-strain data as true stress and true  
186 plastic strain so that numerical analysis can correlate the current deformed state of the material with  
187 the history of previously deformed states and not with the initial undeformed state. In other words,  
188 true stress ( $\sigma_{true}$ ) and true plastic strain ( $\epsilon_{true,pl}$ ) are used for the accurate definition of plastic behaviour  
189 of ductile materials. On the other hand, the geometric non-linearities in both ambient temperature  
190 and post-fire FE models were considered by enabling the non-linear geometry parameter  
191 (\*NLGEOM) in ABAQUS [38]. The labelling of both ambient temperature and post-fire FE  
192 specimens was kept identical to the label system used in their corresponding test programs [54,55].  
193 Fig. 2 presents typical FE RHS T-joints modelled for ambient temperature investigation [1], which

194 also remain valid for corresponding post-fire numerical investigation [2].

## 195 5.2. Mesh spacing, element type and mechanical properties

196 Excluding welds, all other parts of both ambient temperature and post-fire FE models [1,2]  
197 were developed using the C3D20 elements. On the other hand, the C3D10 elements were used to  
198 model the weld parts due to their complicated shapes. The weld parts were freely meshed using the  
199 free-mesh algorithm, however, brace and chord parts were meshed using the structure-mesh  
200 algorithm. The use of solid elements helped in making realistic fusions between tubular and weld  
201 parts of FE models. Convergence studies were conducted using different mesh sizes, and finally,  
202 chord and brace members were seeded at spacing of 4 mm and 7 mm, respectively. Moreover, the  
203 seeding spacings of weld parts reciprocated the seeding spacings of their respective brace parts. In  
204 order to ensure the smooth transfer of stresses from flange to web regions, the corner portions of RHS  
205 were split into ten elements. FE analyses were also conducted to examine the influence of divisions  
206 along the wall thickness ( $t$ ) of RHS members. The results of these FE analyses demonstrated the  
207 trivial influence of wall thickness divisions on the load vs deformation curves of the investigated  
208 RHS T-joints. The use of the C3D20 element as well as the small thickness of test specimens [54,55]  
209 led to such observations. It is worth noting that similar findings were also obtained in other studies  
210 [1,10,57]. Thus, for the validations of both ambient temperature and post-fire FE models, the wall  
211 thickness of tubular members was not divided. The measured values of ambient temperature and  
212 post-fire static stress-strain curves of flat and corner portions of RHS members [54,58] were used in  
213 the corresponding FE models. In addition, the influence of cold-working was included in the FE  
214 models by assigning wider corner regions. Various distances for corner extension were considered in  
215 the sensitivity analyses, and finally, the corner portions were extended by  $2t$  into the neighbouring  
216 flat portions, which was in agreement with other studies conducted on CFHSS tubular members and  
217 joints [1,2,10,59-61].

## 218 5.3. Contact interactions and weld modelling

219 The RHS T-joint test specimens in the ambient and post-fire investigation [54,55] were welded



220 using automatic gas metal arc welding process. An FD-B4L series of robot from OTC Daihen was  
221 employed for the welding process. The brace and chord members of RHS T-joints were tack-welded  
222 initially after being carefully aligned using the measured dimensions of the tubular members. The  
223 tubular joints were then mounted on the automatic rotating chuck whose rotation was synchronized  
224 with the movements of the robotic arm. The entire welding operation was controlled by an  
225 experienced and certified welder. An active gas mixture comprising 80% Ar and 20% CO<sub>2</sub> at 15 to  
226 20 litres per minute was used for the shielding of fresh weld deposits during the course of the welding  
227 operation. Also, during the welding operation, the T-joint junction to welding nozzle distance varied  
228 between 10 to 15 mm. The welds were designed in accordance with the prequalified tubular joint  
229 details given in AWS D1.1M [62]. A low alloy solid carbon steel wire of diameter 1.2 mm,  
230 conforming to ER120S-G class of AWS A5.28M [63], was used as the filler material. The tensile  
231 material properties of the filler material used during the course of welding operation were also  
232 determined by fabricating and testing filler material coupons [64]. The measured average static 0.2%  
233 proof stress, tensile strength and elongation at the fracture of the filler material was 965.2 MPa,  
234 1023.4 MPa and 17.2%, respectively. For more detailed information, regarding the fabrication and  
235 test results of filler material coupons, reference can be made to Pandey and Young [64].

236 In order to avoid excessive heat input, and thus, any further damage to tubular members near  
237 the brace-chord junction region, the weld leg size and numbers of weld passes were kept minimum  
238 to satisfy their respective design criteria. During the welding process, adopted values of the arc  
239 voltage, current and weld deposition speed were 16 V, 150 A and 300 mm/min, respectively. These  
240 inputs for welding operation were carefully selected after several trials of welding in order to achieve  
241 the desired weld leg sizes, weld shapes and to control the heat input during welding process. Using  
242 these weld inputs, the calculated value of the heat input was 0.384 kJ/mm. The welds were modelled  
243 in both ambient temperature and post-fire FE models using the average values of measured weld  
244 sizes reported in test programs [54,55]. The fillet weld was modelled for FE specimens when  $\beta \leq$   
245 0.80, where  $\beta$  is equal to  $b_1/b_0$ . However, when  $\beta > 0.80$ , fillet and groove welds (FW and GW) were  
246 modelled along the chord face and chord side directions, respectively. The inclusions of weld  
247 geometries appreciably improved the overall accuracies of FE models. In addition, modelling of weld

248 parts helped attain realistic load transfer between brace and chord members.

249 A total of two types of contact interactions was defined in the FE models. First, contact  
250 interaction between brace and chord members of the FE models. Second, contact interaction between  
251 chord members and bearing blocks. In addition, a tie constraint was also established between weld  
252 and tubular members of the FE models. Both contact interactions were established using the built-in  
253 surface-to-surface contact definition. The contact interaction between brace and chord members of  
254 FE models was kept frictionless, while a frictional penalty equal to 0.3 was imposed on the contact  
255 interaction between chord member and bearing blocks. Along the normal direction of these two  
256 contact interactions, a ‘hard’ contact pressure overclosure was used. In addition, finite sliding was  
257 permitted between the interaction surfaces. For contact interactions and tie constraint, the surfaces  
258 were connected to each other using the ‘master-slave’ algorithm technique. This technique permits  
259 the separation of fused surfaces under tension, however, it does not allow penetration of fused  
260 surfaces under compression.

#### 261 5.4. Boundary conditions and load application

262 In order to apply boundary conditions, three reference points were created in each T-joint FE  
263 model, including one top reference point (TRP) and two bottom reference points (BRP-1 and BRP-  
264 2), as shown in Fig. 2. The TRP replicated the fixed boundary condition of the top brace end, while  
265 BRP-1 and BRP-2 replicated the boundary conditions of the roller positioned at each chord end. The  
266 TRP was created at the cross-section centre of the top brace end, while BRP-1 and BRP-2 were  
267 created at 20 mm below the centre of the bottom surfaces of bearing blocks, which was in accordance  
268 with the test setup [54,55]. The TRP, BRP-1 and BRP-2 were then coupled to their corresponding  
269 surfaces using the built-in kinematic coupling type. In order to exactly replicate the boundary  
270 conditions of the T-joint test setup, all degrees of freedom (DOF) of TRP were restrained. On the  
271 other hand, for BRP-1 and BRP-2, except for the translations along the vertical and longitudinal  
272 directions of the T-joint FE specimen as well as the rotation about the transverse direction of the  
273 chord member, all other DOF of BRP-1 and BRP-2 were also restrained. In addition, all DOF of other  
274 nodes of T-joint FE specimen were kept unrestrained for both rotation and translation. Using the

275 displacement control method, equal compression loads were then applied at the BRP-1 and -2 of FE  
276 models.

#### 277 5.5. Geometric imperfection in chord webs

278 Garifullin et al. [65] studied the influence of geometric imperfections on the static behaviour  
279 of cold-formed steel hollow section T-joints. The imperfection profiles of RHS T-joints were obtained  
280 by performing elastic buckling analyses in ABAQUS [38]. It was concluded by Garifullin et al. [65]  
281 that geometric imperfections had a trivial influence on the static behaviour of hollow section T-joints.  
282 However, Pandey et al. [1] reported that the maximum measured values of cross-section width and  
283 depth of RHS members were on an average 2.9% more than their respective nominal dimensions.  
284 Therefore, it was necessary to model this geometric imperfection as an outward bulging 3-point  
285 convex arc, as shown in Fig. 3. Also, as all failure modes in tests [54,55] and numerical investigations  
286 [1,2] were only governed by the deformation of chord members, therefore, Pandey et al. [1]  
287 numerically examined the influence of outward bulging of chord cross-section on the static behaviour  
288 of RHS T-joints. Finally, it was concluded that the effect of convex bulging of chord cross-section  
289 was only significant for equal-width (i.e.  $\beta=1.0$ ) RHS T-joints [1]. As a result, in both ambient  
290 temperature and post-fire FE models [1,2], geometric imperfections were introduced as a 3-point  
291 convex arc in the chord webs of equal-width RHS T-joints.

#### 292 5.6. Validations of RHS T-joint FE models at ambient temperature and post-fire conditions

293 Both ambient temperature and post-fire FE models of cold-formed steel RHS 90° T-joints of  
294 S960 grade [1,2] were developed using the modelling techniques described in the preceding sub-  
295 sections of this paper. The validations of FE models were confirmed by duly comparing the joint  
296 resistances, load vs deformation curves and failure modes between tests [54,55] and corresponding  
297 FE [1,2] specimens. The measured dimensions of tubular members and welds were used to develop  
298 all FE models. In addition, measured ambient temperature and post-fire static mechanical properties  
299 of flat and corner portions of cold-formed S960 steel grade tubular members were used in the  
300 validations of corresponding ambient temperature and post-fire FE models. It is worth mentioning

301 that for both ambient temperature and post-fire investigations, the peak load or 3% deformation limit  
302 load, whichever occurred earlier in the  $N$  vs  $u$  curve, was taken as the joint resistance [14]. For the  
303 ambient temperature investigation of cold-formed S960 steel grade RHS T-joints, the overall values  
304 of the mean ( $P_m$ ) and coefficients of variation (COV) ( $V_p$ ) of the comparisons between test and FE  
305 resistances were 1.00 and 0.014, respectively [1]. Besides, on using the similar FE models with post-  
306 fire static mechanical properties, the overall values of  $P_m$  and  $V_p$  of comparisons between post-fire  
307 test and FE resistances were 1.00 and 0.012, respectively [2]. In addition, the comparisons of load vs  
308 deformation curves between test and FE RHS T-joint specimens for ambient temperature and post-  
309 fire investigations are shown in Figs. 4 and 5, respectively. Furthermore, Figs. 6 and 7 present  
310 comparisons of distinct failure modes between typical test and FE RHS T-joint specimens for ambient  
311 temperature and post-fire investigations, respectively. Hence, it can be concluded that the verified FE  
312 models precisely replicated the overall static behaviour of cold-formed steel RHS 90° T-joints of  
313 S960 grade for both ambient temperature and post-fire investigations [1,2].

## 314 **6. Numerical program of cold-formed high strength steel RHS T-joints at elevated** 315 **temperatures**

### 316 6.1. Parametric study

317 In the parametric study, the static behaviour of RHS 90° T-joints was investigated at 400°C,  
318 500°C, 600°C and 1000°C. The FE analyses of parametric specimens were performed using  
319 mechanical properties at elevated temperatures predicted from the constitutive material model  
320 proposed by Li and Young [52] for cold-formed S900 steel grade tubular members. Fig. 8 presents  
321 the stress-strain curves at 400°C, 500°C, 600°C and 1000°C. Table 1 presents the mechanical  
322 properties at 400°C, 500°C, 600°C and 1000°C, which include Young's modulus ( $E_0$ ), 0.2% proof  
323 stress ( $\sigma_{0.2}$ ), ultimate strength ( $\sigma_u$ ) and ultimate strain ( $\epsilon_u$ ). With the exception of mechanical properties  
324 at elevated temperatures, all FE modelling techniques described in Section 5 of this paper were used  
325 to perform the numerical parametric study on cold-formed S900 steel grade RHS T-joints at elevated  
326 temperatures. In total, 756 RHS 90° T-joint FE specimens were analysed in the parametric study,  
327 including 189 FE specimens corresponding to each elevated temperature. The validity ranges of

328 governing geometric parameters were purposefully widened beyond the present limitations set by  
329 EC3 [13] and CIDECT [14]. Table 2 presents the overall ranges of various critical parameters  
330 considered in this investigation. In the parametric study, the values of cross-section width and depth  
331 of braces and chords of FE specimens varied from 30 mm to 600 mm, while the wall thickness of  
332 braces and chords varied from 2.25 mm to 12.5 mm. The external corner radii of braces and chords  
333 ( $R_l$  and  $R_o$ ) conformed to commercially produced HSS members [66]. In this study,  $R_l$  and  $R_o$  were  
334 kept as  $2t$  for  $t \leq 6$  mm,  $2.5t$  for  $6 < t \leq 10$  mm and  $3t$  for  $t > 10$  mm, which in turn also met the limits  
335 detailed in EN [67]. The lengths of braces ( $L_l$ ) and chords ( $L_o$ ) of RHS T-joint FE specimens were  
336 determined using the identical formulae used for the test specimens [54,55].

337 For meshing along the longitudinal and transverse directions of RHS members, seedings were  
338 approximately spaced at the minimum of  $b/30$  and  $h/30$ . Overall, the adopted mesh sizes of  
339 parametric FE specimens varied from 3 to 12 mm. On the other hand, the seeding interval of weld  
340 parts of parametric FE specimens reciprocated the seeding interval of their corresponding brace parts.  
341 For precise replication of RHS curvatures, the corner portions of RHS members were split into ten  
342 parts. For RHS members with  $t \leq 6$  mm, no divisions were made along the wall thickness of the  
343 parametric FE specimens. However, for RHS members with  $t > 6$  mm, the wall thickness of  
344 parametric FE specimens was divided into two layers. With regard to the weld modelling, FW was  
345 modelled for FE specimens with  $\beta \leq 0.80$ . However, for FE specimens with  $\beta > 0.80$ , GW and FW  
346 were respectively modelled along the chord side and chord face directions. Following the prequalified  
347 tubular joint details given in AWS D1.1M [62], the leg size of FW was designed as 1.5 times the  
348 minimum of  $t_l$  and  $t_o$ . In addition, referring to the prequalified tubular joint details given in AWS  
349 D1.1M [62], the weld reinforcement of GW was taken as half of the minimum wall thickness of brace  
350 and chord member. The designs of both FW and GW were consistent with the numerical  
351 investigations performed at ambient temperature and post-fire conditions [1,2]. The weld parts were  
352 also assigned the mechanical properties determined from the constitutive material model proposed  
353 by Li and Young [52]. In addition, as shown in Fig. 3, the flat part of each chord web (i.e.  $h_o - 2R_o$ ) of  
354 equal-width RHS T-joint was outward bulged at its centre by  $0.015b_o$ . Fig. 9 presents the stress  
355 nephograms of typical RHS T-joints failed by F, F+S and S modes.

## 356 6.2. Failure modes identified at elevated temperatures

357 Overall, three types of failure modes were identified in this numerical investigation. First,  
358 failure of RHS T-joints by chord flange yielding, which was termed as chord face failure and denoted  
359 by the letter 'F' in this study. Second, failure of RHS T-joints due to buckling of chord webs, which  
360 was termed as chord side wall failure and denoted by the letter 'S' in this study. Third, failure of RHS  
361 T-joints due to the combination of chord face and chord side wall failures, which was named as  
362 combined failure and denoted by 'F+S' in this study. The RHS T-joints were failed by the F mode,  
363 when the  $N_{f,T}$  was determined using the  $0.03b_0$  limit criterion. The applied load of RHS T-joint failed  
364 by the F mode was monotonically increasing. In this investigation, RHS T-joints were failed by the  
365 F mode when  $0.30 \leq \beta \leq 0.75$ . On the other hand, RHS T-joints were failed by the S mode when  
366  $\beta=1.0$ . For RHS T-joints that failed by the F+S mode, the  $N_{f,T}$  vs  $u$  curve exhibited a clear ultimate  
367 load. Additionally, evident deformations of chord flange, chord webs and chord corner regions were  
368 noticed in the specimens that failed by the F+S mode. The specimens were failed by the F+S mode  
369 in this investigation when  $0.80 \leq \beta \leq 0.90$ . Figs. 10 to 12 respectively present the variations of  $N_{f,T}$  vs  
370  $u$  curves for typical RHS T-joints that failed by the F, F+S and S failure modes.

## 371 7. Design rules

372 Currently, design rules for predicting the residual strengths of tubular joints at elevated  
373 temperatures are not given in international codes and guides. In order to examine the suitability of  
374 EC3 [13] and CIDECT [14] design provisions for cold-formed S900 steel grade RHS T-joints at  
375 elevated temperatures, in this study, the nominal resistances from design equations given in EC3 [13]  
376 and CIDECT [14] ( $N_{E,T}$  and  $N_{C,T}$ ) were determined using the mechanical properties shown in Table  
377 1. The design rules given in EC3 [13] and CIDECT [14] are shown below:

378 Chord face failure ( $\beta \leq 0.85$ )

379 EC3 [13]:

$$N_{E,T} = C_f \left[ k_n \frac{f_{y0,T} t_0^2}{(1-\beta) \sin \theta_1} \left( \frac{2\eta}{\sin \theta_1} + 4\sqrt{1-\beta} \right) / \gamma_{M5} \right] \quad (1)$$

380 CIDECT [14]:

$$N_{C,T} = C_f \left[ Q_f \frac{f_{y0,T} t_0^2}{\sin \theta_1} \left( \frac{2\eta}{(1-\beta) \sin \theta_1} + \frac{4}{\sqrt{1-\beta}} \right) \right] \quad (2)$$

381 Chord side wall failure ( $\beta = 1.0$ )

382 EC3 [13]:

$$N_{E,T} = C_f \left[ k_n \frac{f_{b,T} t_0}{\sin \theta_1} \left( \frac{2h_1}{\sin \theta_1} + 10t_0 \right) / \gamma_{M5} \right] \quad (3)$$

383 CIDECT [14]:

$$N_{C,T} = C_f \left[ Q_f \frac{f_{k,T} t_0}{\sin \theta_1} \left( \frac{2h_1}{\sin \theta_1} + 10t_0 \right) \right] \quad (4)$$

384 The nominal resistances from EC3 [13] were determined using the 0.2% proof stress at elevated  
 385 temperatures and partial safety factor ( $\gamma_{M5}$ ) equal to 1.0. In addition, a material factor ( $C_f$ ) equal to  
 386 0.80 was adopted as per EC3 [68]. On the other hand, CIDECT [14] uses the minimum of 0.2% proof  
 387 stress and 0.80 times the corresponding ultimate strength for joint resistance calculation. Moreover,  
 388 design provisions given in CIDECT [14] recommend the use of  $C_f$  equal to 0.90 for tubular joints  
 389 with steel grade exceeding S355 and up to S460. Unlike EC3 [13], CIDECT [14] uses different values  
 390 of partial safety factors ( $\gamma_M$ ) for different tubular joints and their corresponding failure modes, which  
 391 are given in IIW [69]. However, their effects have already been implicitly included inside the  
 392 CIDECT [14] design provisions. Referring to IIW [69], the value of partial safety factor ( $\gamma_M$ ) for RHS  
 393 T-joints failed by both chord face failure and chord side wall failure modes is equal to 1.0. Thus,  
 394 nominal resistances from CIDECT [14] were calculated using  $\gamma_M$  equal to 1.0 for both chord face  
 395 failure and chord side wall failure modes. In Eqs. (1) to (4), chord stress functions are denoted by  $k_n$   
 396 and  $Q_f$ , yield stress of chord member at elevated temperatures is denoted by  $f_{y0,T}$ , the parameter  $\eta$  is  
 397 equal to  $h_1/b_0$ , chord side wall buckling stresses at elevated temperatures are denoted by  $f_{b,T}$  and  $f_{k,T}$ ,  
 398 and the angle between brace and chord is denoted by  $\theta_1$  (in degrees).

399 In addition, a reliability analysis was performed as per AISI S100 [70]. In this study, the design  
 400 equation was treated as reliable when the value of the reliability index ( $\beta_0$ ) was greater than or equal  
 401 to 2.50. The values of various statistical parameters and load combinations used in the reliability  
 402 index calculation are identical to those values adopted in Pandey et al. [1].

## 403 8. Comparisons of joint resistances at elevated temperatures with nominal resistances

404 For different observed failure modes, the overall summary of comparisons between  $N_{f,T}$  and  
405 nominal resistances predicted from design rules given in EC3 [13] and CIDECT [14] using  
406 mechanical properties at elevated temperatures are shown in Tables 3 to 5. The comparisons are also  
407 graphically shown in Figs. 13 to 15 for different failure modes. Table 3 and Fig. 13 present  
408 comparisons for RHS T-joint specimens that failed by the F mode. The comparison results proved  
409 that using the mechanical properties at elevated temperatures, the design rules given in EC3 [13] and  
410 CIDECT [14] are very conservative but scattered and unreliable for the design of cold-formed S900  
411 steel grade RHS T-joints at elevated temperatures. In Fig. 13, generally, RHS T-joint specimens with  
412 small values of  $\beta$  and  $\eta$  ratios and large values of  $2\gamma$  ratio ( $b_0/t_0$ ) lie below the unit slope line (i.e.  $y=x$ ).  
413 For such specimens, the joint resistance corresponding to the  $0.03b_0$  limit was not sufficient to cause  
414 the yielding of chord flanges. On the contrary, the yield line theory has been used to derive the  
415 existing design equation for RHS T-joint specimens that failed by the F mode [13,14]. Consequently,  
416  $N_{f,T}$  of RHS T-joint specimens became smaller than the corresponding nominal resistances predicted  
417 from design rules given in EC3 [13] and CIDECT [14] using mechanical properties at elevated  
418 temperatures. As a result, such cases fall below the line of unit slope. The data above the line of unit  
419 slope, on the other hand, indicate RHS T-joint specimens with medium to large values of  $\beta$  and  $\eta$   
420 ratios and small values of  $2\gamma$  ratio.

421 The comparison results of RHS T-joint specimens that failed by the F+S mode at elevated  
422 temperatures are shown in Table 4 and Fig. 14. It can be noticed that using mechanical properties at  
423 elevated temperatures, the current design provisions given in EC3 [13] and CIDECT [14] are found  
424 to be largely conservative but quite dispersed and unreliable. The data above the unit slope line in  
425 Fig. 14 typically represent RHS T-joints with large values of  $\beta$  ratio and small values of  $2\gamma$  and  $h_0/t_0$   
426 ratios. As the  $\beta$  ratio of RHS T-joint failed by the F+S mode increased, the brace member gradually  
427 approached the chord corner regions. Consequently, the  $N_{f,T}$  of such joints increased due to enhanced  
428 rigidity of the chord corner regions. On the other hand, the corresponding increase in nominal  
429 resistances predicted from design rules given in EC3 [13] and CIDECT [14] was lower than the  $N_{f,T}$   
430 of RHS T-joints. Subsequently, such data fall above the line of unit slope in Fig. 14. Table 5 and Fig.



431 15 present the comparison results of RHS T-joint specimens that failed by the S mode. The existing  
 432 design rules, using mechanical properties at elevated temperatures, apparently provided very  
 433 conservative predictions and were accompanied by significantly large values of COV. The EC3 [13]  
 434 and CIDECT [14] design provisions for the S failure mode considered chord webs as pin-ended  
 435 columns, which resulted in very conservative predictions as  $h_0/t_0$  ratio increased.

## 436 9. Proposed design rules

437 Using two design approaches, named as proposal-1 and -2, design rules are proposed in this  
 438 study for different failure modes of the investigated cold-formed steel RHS 90° T-joints of S900  
 439 grade at elevated temperatures ( $T$ ). The design rules proposed in both the approaches (i.e. proposal-  
 440 1 and -2) were based on the design equations proposed by Pandey et al. [1] for CFHSS RHS T-joints  
 441 at ambient temperature. In the first design approach (i.e. proposal-1), mechanical properties at  
 442 ambient temperature used in the design equations proposed by Pandey et al. [1] are replaced with the  
 443 mechanical properties at elevated temperatures. In addition, a correction factor ( $\Omega$ ) based on the  
 444 elevated temperature is also applied on the proposed design rules. On the other hand, in the second  
 445 design approach (i.e. proposal-2), only a correction factor based on the elevated temperature is  
 446 applied on the design rules proposed by Pandey et al. [1] at ambient temperature. It should be noted  
 447 that the design rules proposed in this study are valid for  $400^\circ\text{C} \leq T \leq 1000^\circ\text{C}$  and included angle ( $\theta_l$ )  
 448 equal to  $90^\circ$ . In order to obtain design resistances ( $N_d$ ), the proposed nominal resistances ( $N_{pn1}$  and  
 449  $N_{pn2}$ ) in the following sub-sections of this paper shall be multiplied by their correspondingly  
 450 recommended resistance factors ( $\phi$ ), i.e.  $N_d = \phi (N_{pn1} \text{ or } N_{pn2})$ .

### 451 9.1. RHS T-joints failed by F mode at elevated temperatures ( $0.30 \leq \beta \leq 0.75$ )

#### 452 Proposal-1:

453 Using mechanical properties at elevated temperatures ( $T$ ):

$$454 N_{pn1} = \left(0.67e^{0.0009T}\right) \left[ f_{y0,T} t_0^2 \left( \frac{30\beta + 4.5\eta - 6.6}{0.5 + 0.03(2\gamma)} \right) \right] \quad (5)$$

#### 454 Proposal-2:

455 Using mechanical properties at ambient temperature and elevated temperature correction factor ( $\Omega$ ):

$$N_{pn2} = \Omega \left[ f_{y0} t_0^2 \left( \frac{30\beta + 4.5\eta - 6.6}{0.5 + 0.03(2\gamma)} \right) \right] \quad (6)$$

456 where

$$\Omega = \begin{cases} 1.58 - 2 \times 10^{-3} T & \text{for } 400^\circ\text{C} \leq T \leq 600^\circ\text{C} \\ 0.9 - 8.67 \times 10^{-4} T & \text{for } 600^\circ\text{C} < T \leq 1000^\circ\text{C} \end{cases} \quad (7)$$

457 The Eqs. (5) and (6) are valid for  $0.30 \leq \beta \leq 0.75$ ,  $16.6 \leq 2\gamma \leq 50$ ,  $16.6 \leq h_0/t_0 \leq 50$ ,  $0.3 \leq \eta \leq$   
 458  $1.2$  and  $0.75 \leq \tau \leq 1.0$ . As shown in Table 3, the  $P_m$  and  $V_p$  of proposal-1 (i.e. Eq. (5)) are 1.01 and  
 459 0.201, respectively, while the  $P_m$  and  $V_p$  of proposal-2 (i.e. Eq. (6)) are 1.02 and 0.199, respectively.  
 460 For Eqs. (5) and (6),  $\phi$  equal to 0.75 is recommended, resulting in  $\beta_0$  equal to 2.51 and 2.54,  
 461 respectively. Thus, Eqs. (5) and (6) must be multiplied by  $\phi$  equal to 0.75 to obtain their  
 462 corresponding design resistances ( $N_d$ ), respectively. The comparisons of  $N_{fT}$  of RHS T-joint  
 463 specimens with nominal resistances predicted from design equations given in EC3 [13], CIDECT  
 464 [14] as well as predictions from proposal-1 and -2 are graphically presented in Fig. 13.

465 9.2. RHS T-joints failed by F+S mode at elevated temperatures ( $0.80 \leq \beta \leq 0.90$ )

466 Proposal-1:

467 Using mechanical properties at elevated temperatures ( $T$ ):

$$N_{pn1} = \left( 0.6e^{0.0009T} \right) \left[ f_{y0,T} t_0^2 \left( \frac{55\beta + 4.5\eta - 33}{0.75 + 0.0075(2\gamma)} \right) \right] \quad (8)$$

468 Proposal-2:

469 Using mechanical properties at ambient temperature and elevated temperature correction factor ( $\Omega$ ):

$$N_{pn2} = \Omega \left[ f_{y0} t_0^2 \left( \frac{55\beta + 4.5\eta - 33}{0.75 + 0.0075(2\gamma)} \right) \right] \quad (9)$$

470 where

$$\Omega = \begin{cases} 1.55 - 2 \times 10^{-3} T & \text{for } 400^\circ\text{C} \leq T \leq 600^\circ\text{C} \\ 0.83 - 8 \times 10^{-4} T & \text{for } 600^\circ\text{C} < T \leq 1000^\circ\text{C} \end{cases} \quad (10)$$

471 The Eqs. (8) and (9) are valid for  $0.80 \leq \beta \leq 0.90$ ,  $16.6 \leq 2\gamma \leq 50$ ,  $16.6 \leq h_0/t_0 \leq 50$ ,  $0.6 \leq \eta \leq$   
 472  $1.2$  and  $0.75 \leq \tau \leq 1.0$ . As shown in Table 4, the  $P_m$  and  $V_p$  of proposal-1 (i.e. Eq. (8)) are 1.00 and  
 473 0.150, respectively, while the  $P_m$  and  $V_p$  of proposal-2 (i.e. Eq. (9)) are 0.97 and 0.144, respectively.  
 474 For Eqs. (8) and (9),  $\phi$  equal to 0.80 and 0.75 are recommended, resulting in  $\beta_0$  equal to 2.51 and  
 475 2.63, respectively. Thus, Eqs. (8) and (9) must be multiplied by  $\phi$  equal to 0.80 and 0.75 to obtain

476 their corresponding design resistances ( $N_d$ ), respectively. The comparisons of  $N_{f,T}$  of RHS T-joint  
 477 specimens with nominal resistances predicted from design equations given in EC3 [13], CIDECT  
 478 [14] as well as predictions from proposal-1 and -2 are graphically presented in Fig. 14.

479 9.3. RHS T-joints failed by S mode at elevated temperatures ( $\beta = 1.0$ )

480 Proposal-1:

481 Using mechanical properties at elevated temperatures ( $T$ ):

$$N_{pn1} = \begin{cases} N_1 = (1.29 - 0.0008T) \left[ \frac{f_{k,T}(2b_w t_0)}{(1.5\eta + 1)} \left( \frac{1.83 - 0.05(2\gamma) + 1.2\tau}{588 \left( \frac{h_0}{t_0} \right)^{-2.17}} \right) \right] & \text{for } 400^\circ\text{C} \leq T \leq 600^\circ\text{C} \\ N_2 = 12.74 \left( \frac{h_0}{t_0} \right)^{-0.95} \left[ \frac{f_{k,T}(2b_w t_0)}{(1.5\eta + 1)} \left( \frac{1.83 - 0.05(2\gamma) + 1.2\tau}{588 \left( \frac{h_0}{t_0} \right)^{-2.17}} \right) \right] & \text{for } T = 1000^\circ\text{C} \\ \text{Linear interpolation between } N_1 \text{ and } N_2 & \text{for } 600^\circ\text{C} < T < 1000^\circ\text{C} \end{cases} \quad (11)$$

482 Proposal-2:

483 Using mechanical properties at ambient temperature and elevated temperature correction factor ( $\Omega$ ):

$$N_{pn2} = \Omega \left[ \frac{f_k(2b_w t_0)}{(1.5\eta + 1)} \left( \frac{1.83 - 0.05(2\gamma) + 1.2\tau}{588 \left( \frac{h_0}{t_0} \right)^{-2.17}} \right) \right] \quad (12)$$

484 where

$$\Omega = \begin{cases} 1.77 - 2.3 \times 10^{-3} T & \text{for } 400^\circ\text{C} \leq T \leq 600^\circ\text{C} \\ 0.945 - 9.2 \times 10^{-4} T & \text{for } 600^\circ\text{C} < T \leq 1000^\circ\text{C} \end{cases} \quad (13)$$

485 The Eqs. (11) and (12) are valid for  $\beta = 1.0$ ,  $16.6 \leq 2\gamma \leq 50$ ,  $10 \leq h_0/t_0 \leq 60$ ,  $0.6 \leq \eta \leq 1.2$  and  
 486  $0.75 \leq \tau \leq 1.25$ . As shown in Table 5, the  $P_m$  and  $V_p$  of proposal-1 (i.e. Eq. (11)) are 1.01 and 0.200,  
 487 respectively, while the  $P_m$  and  $V_p$  of proposal-2 (i.e. Eq. (12)) are 1.03 and 0.200, respectively. For  
 488 Eqs. (11) and (12),  $\phi$  equal to 0.75 is recommended, resulting in  $\beta_0$  equal to 2.52 and 2.57,  
 489 respectively. Thus, Eqs. (11) and (12) must be multiplied by  $\phi$  equal to 0.75 to obtain their

490 corresponding design resistances ( $N_d$ ), respectively. The comparisons of  $N_{f,T}$  of RHS T-joint  
491 specimens with nominal resistances predicted from design equations given in EC3 [13], CIDECT  
492 [14] as well as predictions from proposal-1 and -2 are graphically presented in Fig. 15. The buckling  
493 curve 'a' of EC3 [71] was used to determine the  $f_{k,T}$  and  $f_k$  in Eqs. (11) and (12). Moreover, the flat  
494 portions of chord side walls were equal to  $h_0-2R_0$ . Additionally, instead of assuming pin-ended  
495 boundary conditions for the flat portions of chord side walls, the effective length of the chord side  
496 wall column was determined using a factor equal to 0.85. Therefore, in this study, the effective lengths  
497 of the flat portions of chord side walls were equal to  $0.85 \times (h_0-2R_0)$ . The definition of the width of  
498 the chord web column ( $b_w$ ) was identical to that given in EC3 [13] and CIDECT [14].

499 It is important to note that for RHS T-joint specimens with  $0.75 < \beta < 0.80$  and  $0.90 < \beta < 1.0$ ,  
500 the nominal resistances under proposal-1 can be obtained by performing a linear interpolation  
501 between Eqs. (5) & (8) and Eqs. (8) & (11), respectively. Similarly, for proposal-2, the nominal  
502 resistances of RHS T-joint specimens with  $0.75 < \beta < 0.80$  and  $0.90 < \beta < 1.0$  can be obtained by  
503 performing a linear interpolation between Eqs. (6) & (9) and Eqs. (9) & (12), respectively.

## 504 10. Conclusions

505 A numerical program has been conducted in this study with an aim to investigate the static  
506 performance of cold-formed steel 90° T-joints of S900 grade with square and rectangular hollow  
507 section (SHS and RHS) braces and chords at elevated temperatures ( $T$ ). The resistances of simply  
508 supported RHS 90° T-joints undergoing brace axial compression loads were determined at 400°C,  
509 500°C, 600°C and 1000°C. The numerical investigation was performed through the finite element  
510 (FE) method using the constitutive stress-strain model proposed by Li and Young [52] for cold-  
511 formed S900 steel grade tubular members at elevated temperatures. A total of 756 FE 90° RHS T-  
512 joint specimens were analysed in the parametric study, where the validity ranges of important  
513 geometric parameters exceeded the limits prescribed in EC3 [13] and CIDECT [14]. The welds were  
514 modelled in all RHS T-joint specimens. Overall, RHS T-joints were failed by three failure modes,  
515 including chord face failure (F), chord side wall failure (S), and a combination of these two failure  
516 modes, i.e. combined failure (F+S) mode. The nominal resistances predicted from design rules given

517 in EC3 [13] and CIDECT [14], using mechanical properties at elevated temperatures, were compared  
518 with the resistances of RHS T-joints investigated in this study. Generally, it has been shown that the  
519 current design rules given in EC3 [13] and CIDECT [14] are uneconomical and unreliable for the  
520 investigated T-joints. Moreover, the predictions from design rules given in EC3 [13] and CIDECT  
521 [14] are quite dispersed. Consequently, for the design of cold-formed steel RHS 90° T-joints of S900  
522 grade at elevated temperatures ranging from 400°C to 1000°C, economical and reliable design rules  
523 are proposed in this study using the two design approaches.

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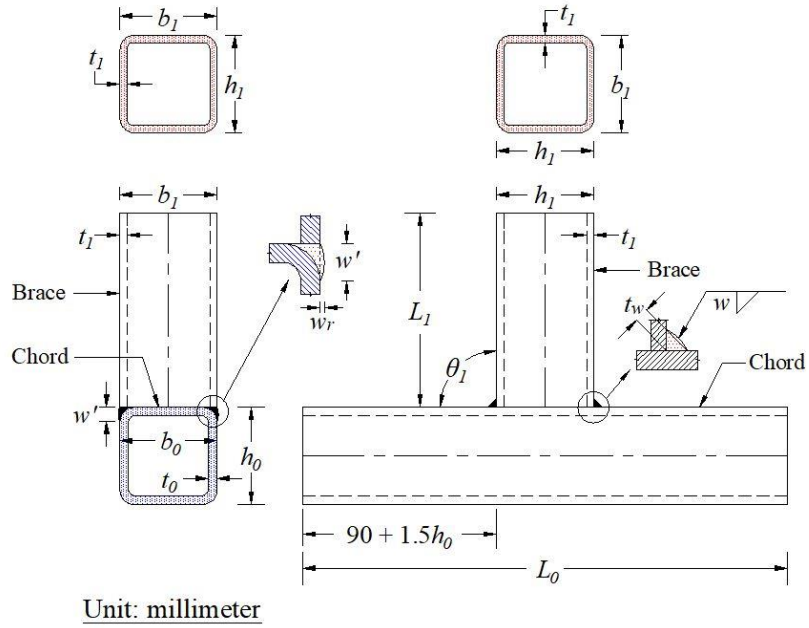
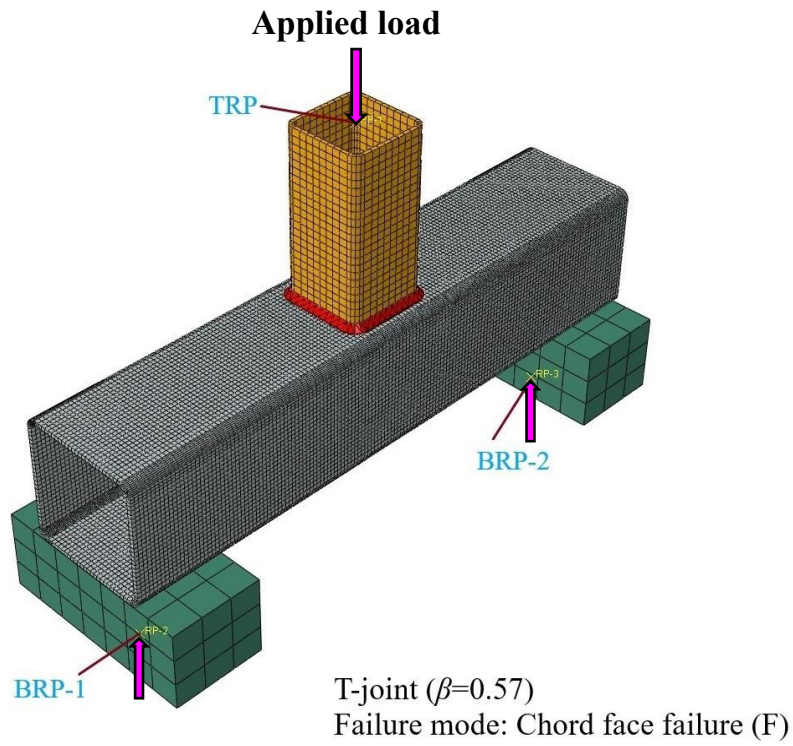
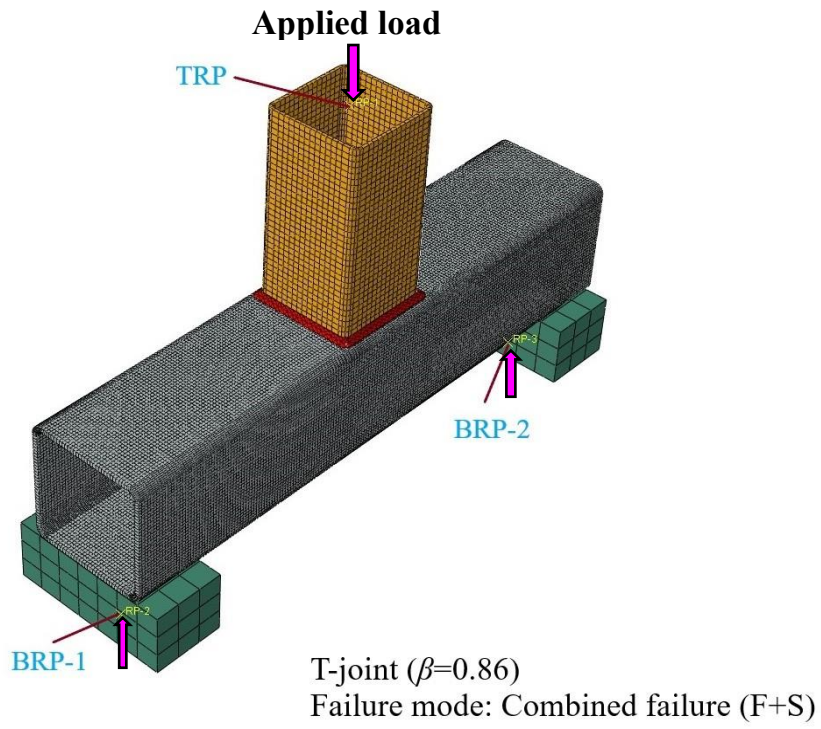


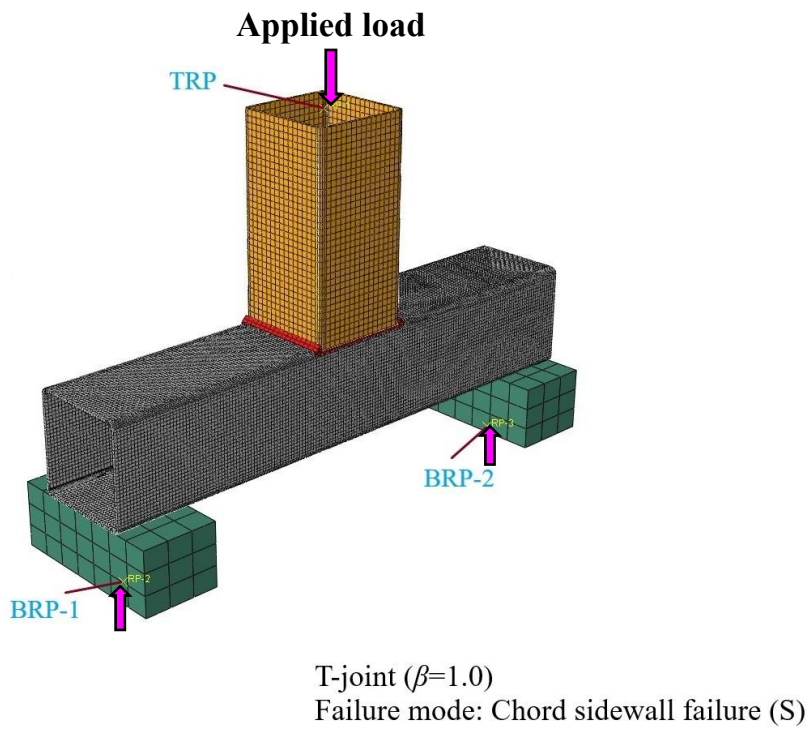
Fig. 1. Representation of geometric notations for RHS T-joint.



(a) 3D geometrical view of typical FE model of RHS T-joint with  $\beta=0.57$ .



(b) 3D geometrical view of typical FE model of RHS T-joint with  $\beta=0.86$ .



(c) 3D geometrical view of typical FE model of RHS T-joint with  $\beta=1.0$ .

Fig. 2. 3D geometrical views of typical FE models of RHS T-joints.

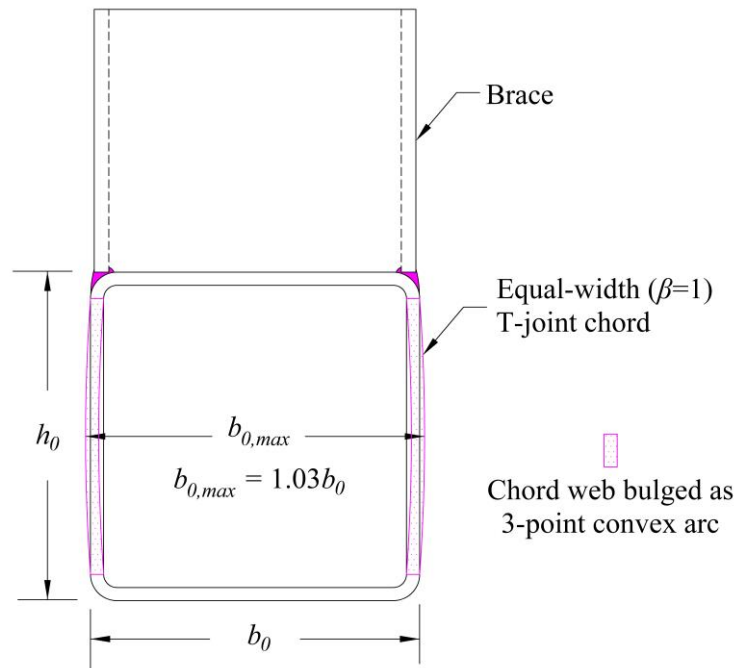
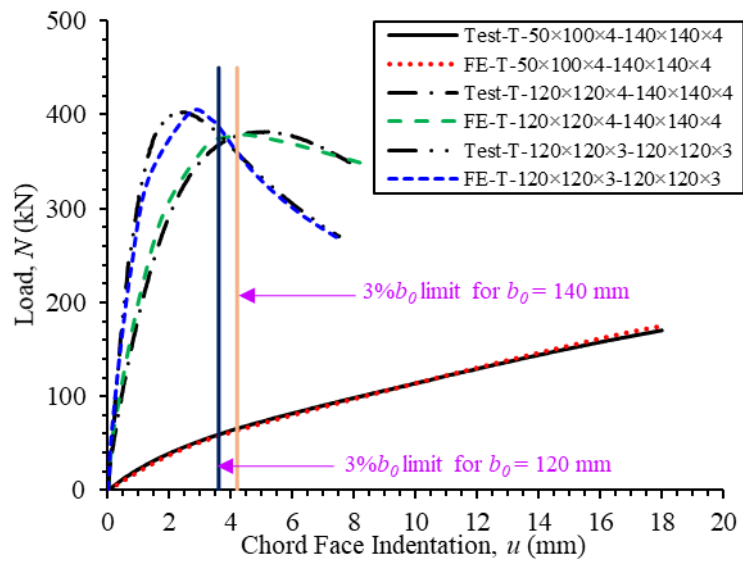
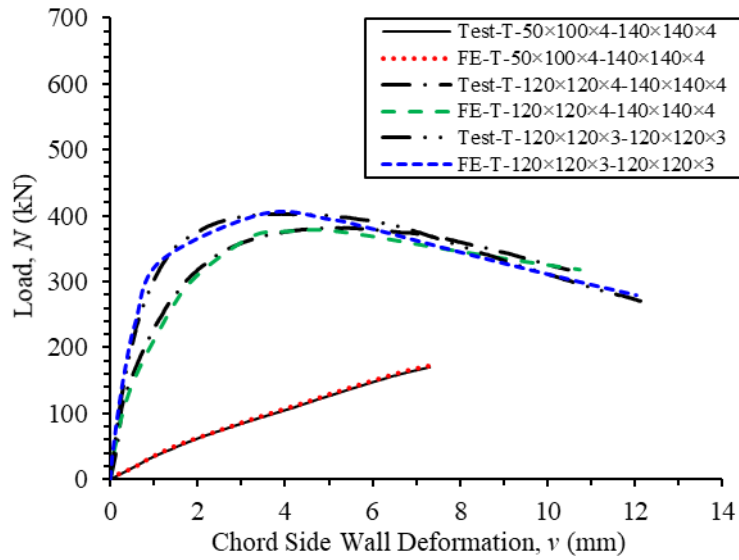


Fig. 3. Initial geometric imperfection modelled in chord webs of equal-width RHS T-joint.

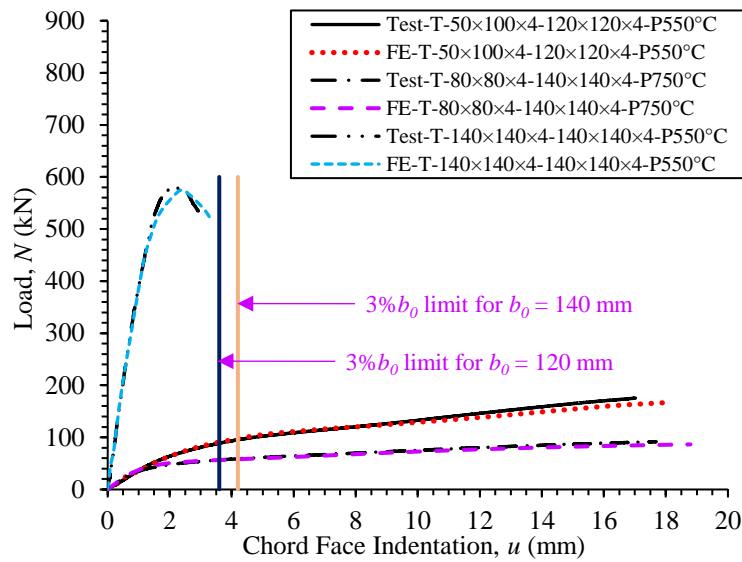


(a) Load vs chord face indentation curves.

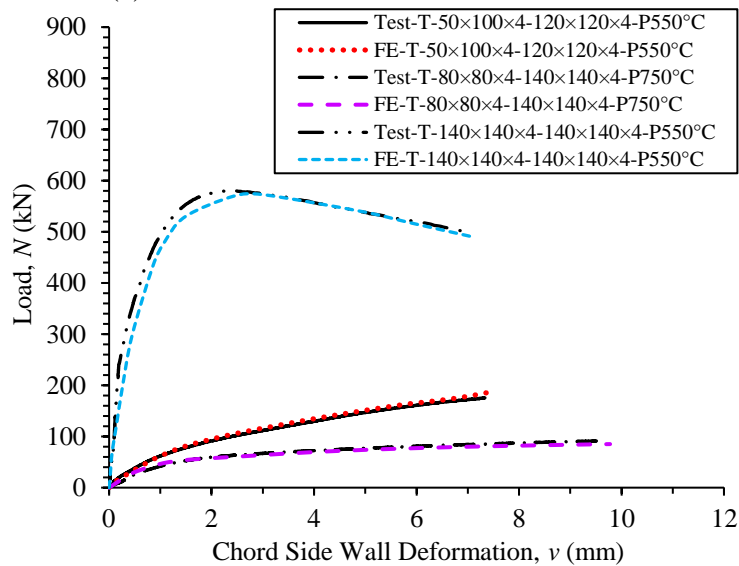


(b) Load vs chord side wall deformation curves.

Fig. 4. Test vs FE load-deformation curves for RHS T-joints at ambient temperature.

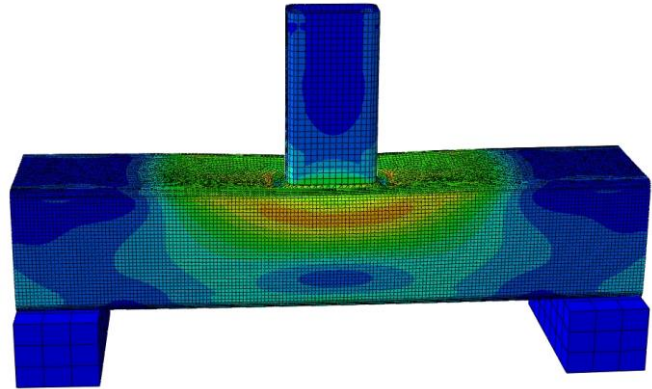
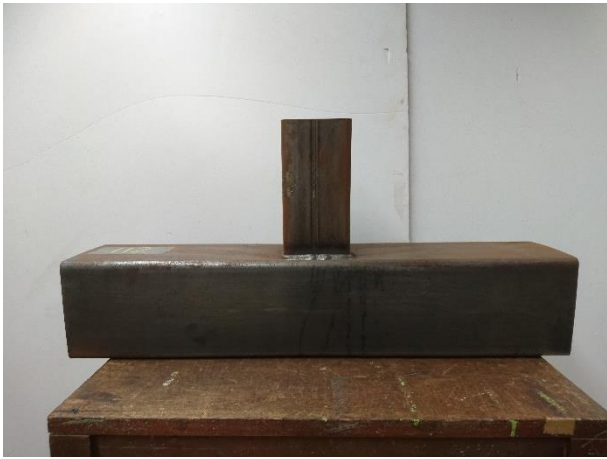


(a) Load vs chord face indentation curves.

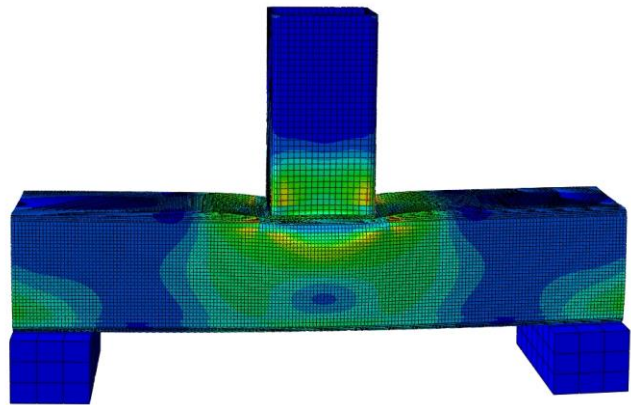


(b) Load vs chord side wall deformation curves.

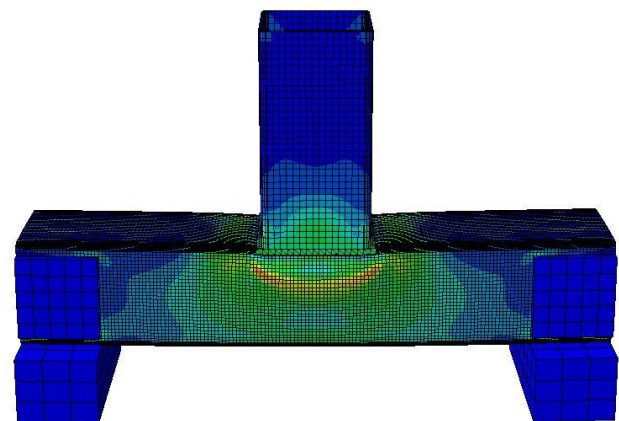
Fig. 5. Test vs FE load-deformation curves for RHS T-joints for post-fire conditions.



(a) Test vs FE comparison for RHS T-joint failed by F mode at ambient temperature.

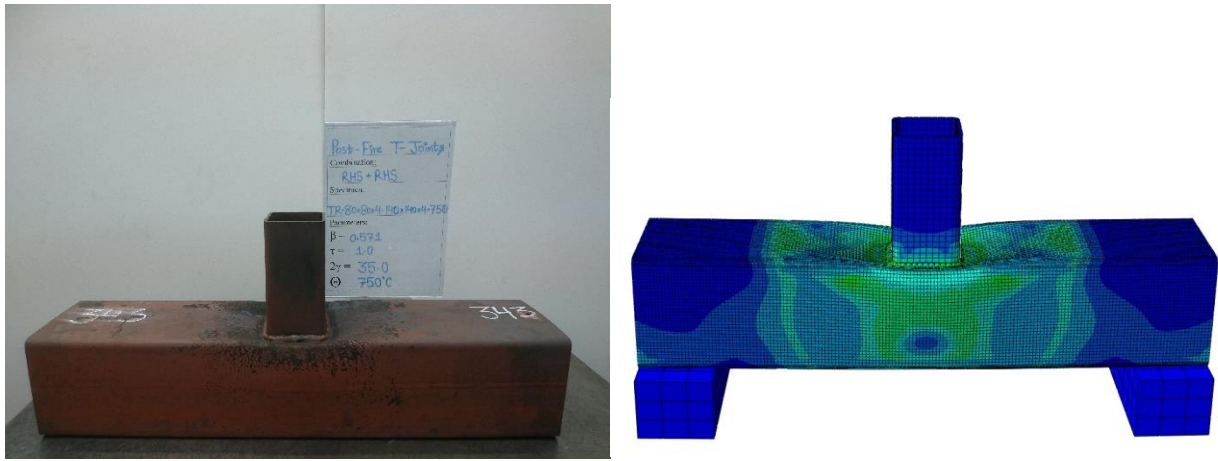


(b) Test vs FE comparison for RHS T-joint failed by F+S mode at ambient temperature.

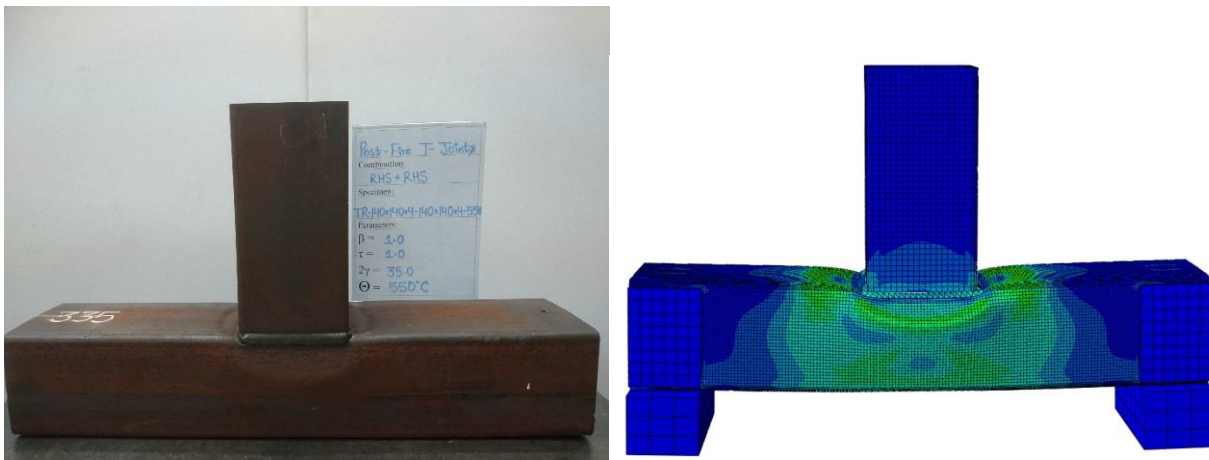


(c) Test vs FE comparison for RHS T-joint failed by S mode at ambient temperature.

Fig. 6. Test vs FE comparisons of failure modes for RHS T-joints at ambient temperature.



(a) Test vs FE comparison for RHS T-joint failed by F mode for post-fire condition.



(b) Test vs FE comparison for RHS T-joint failed by S mode for post-fire condition.

Fig. 7. Test vs FE comparisons of failure modes for RHS T-joints for post-fire conditions.

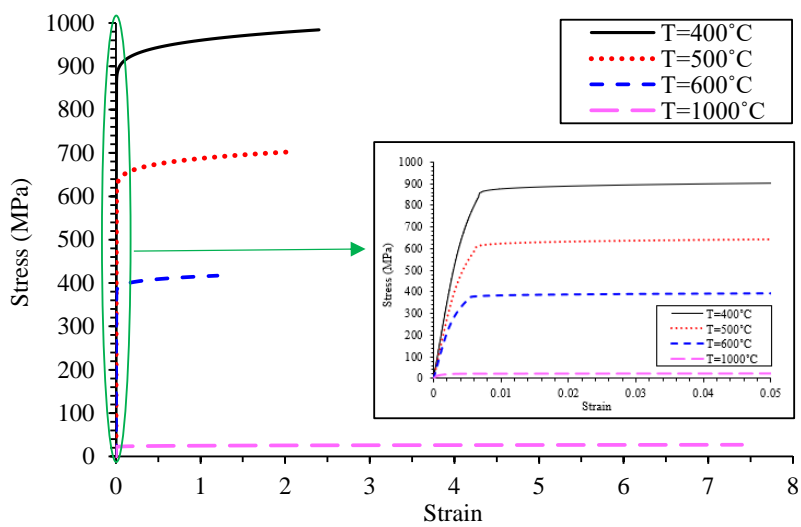
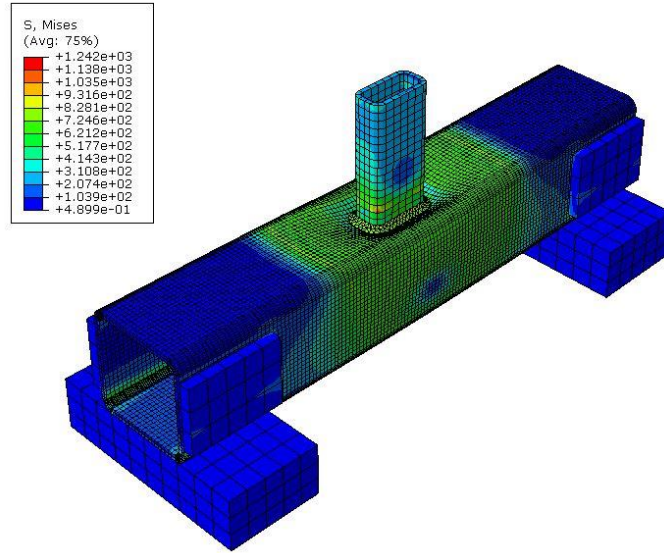
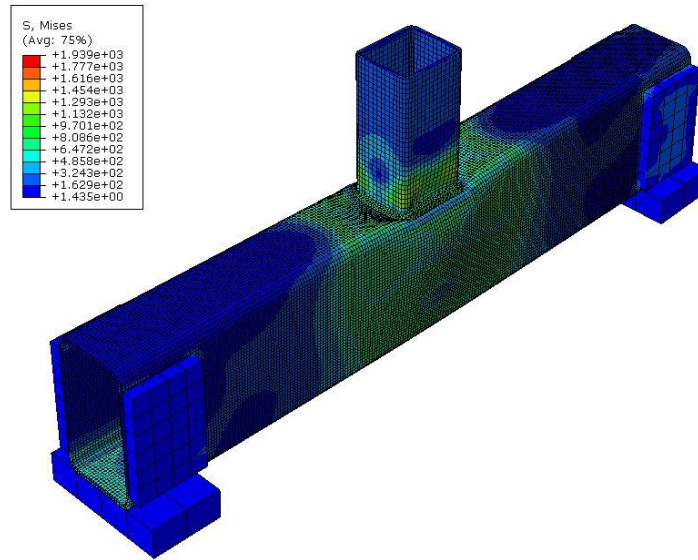


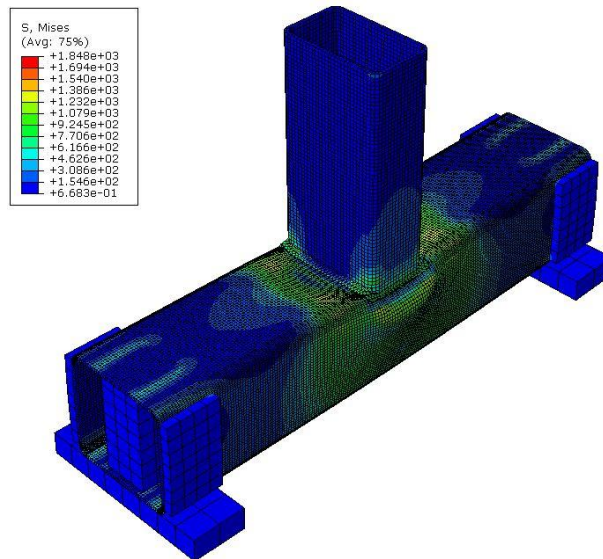
Fig. 8. Stress-strain curves used in parametric study at elevated temperatures [52].



(a) Stress nephogram of RHS T-joint FE model failed by F mode.



(b) Stress nephogram of RHS T-joint FE model failed by F+S mode.



(c) Stress nephogram of RHS T-joint FE model failed by S mode.

Fig. 9 Stress nephograms of typical RHS T-joints at elevated temperatures.



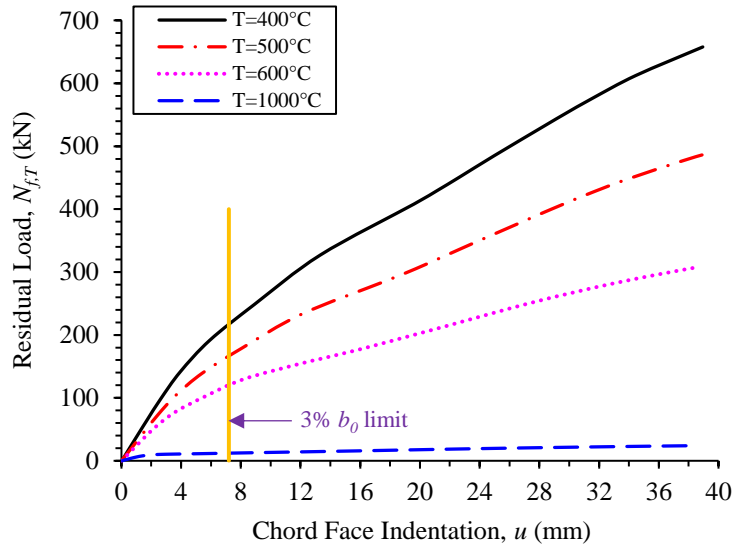


Fig. 10. Variations of load vs deformation curves for typical RHS T-joint (T-72×216×6-240×240×8;  $\beta=0.30$ ) failed by F mode at elevated temperatures.

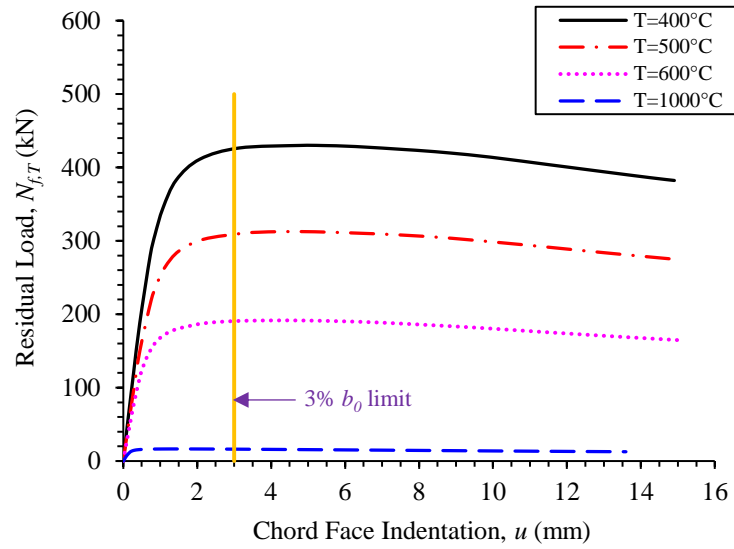


Fig. 11. Variations of load vs deformation curves for typical RHS T-joint (T-80×60×4.5-100×100×6;  $\beta=0.80$ ) failed by F+S mode at elevated temperatures.

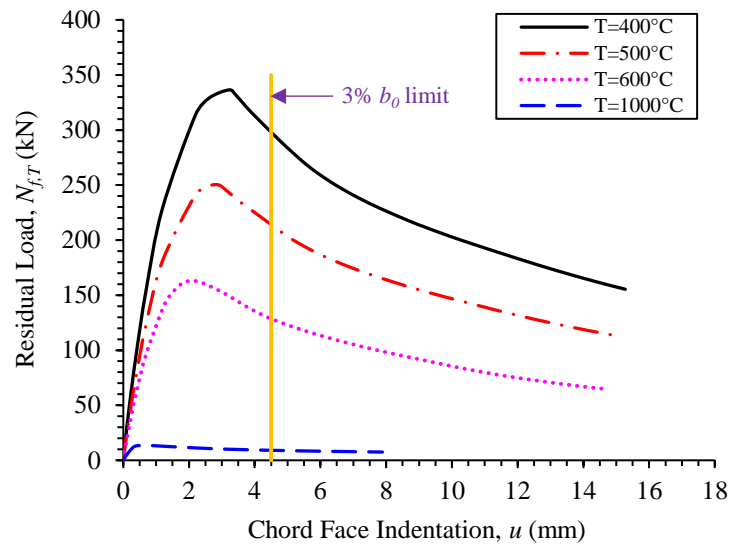
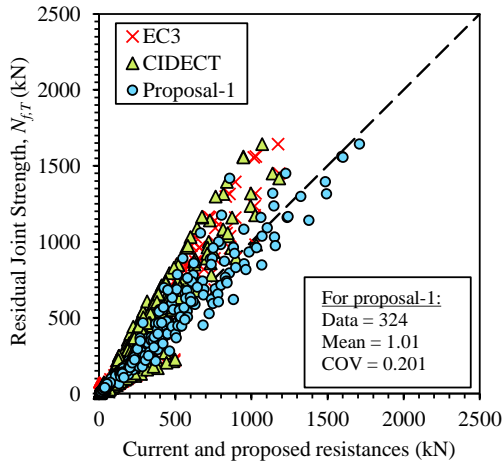
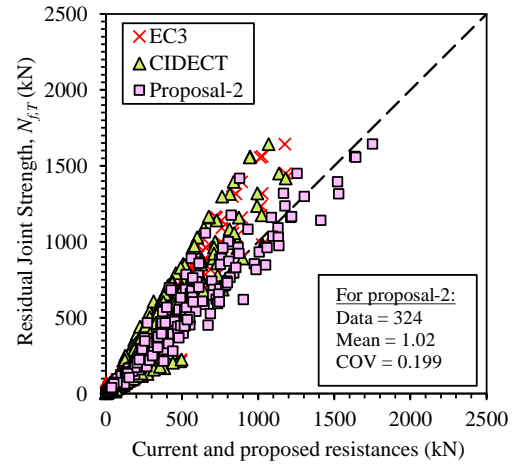


Fig. 12. Variations of load vs deformation curves for typical RHS T-joint (T-150×180×3.75-150×120×3;  $\beta=1.0$ ) failed by S mode at elevated temperatures.

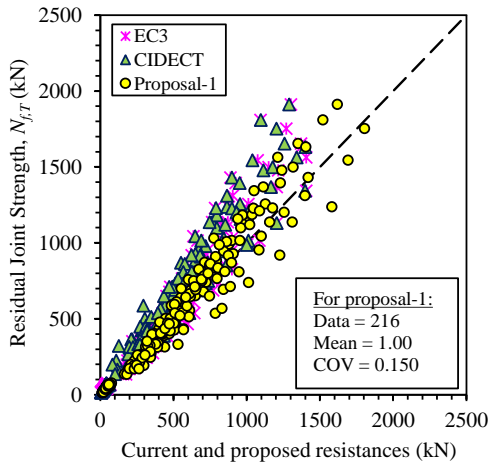


(a) For Proposal-1.

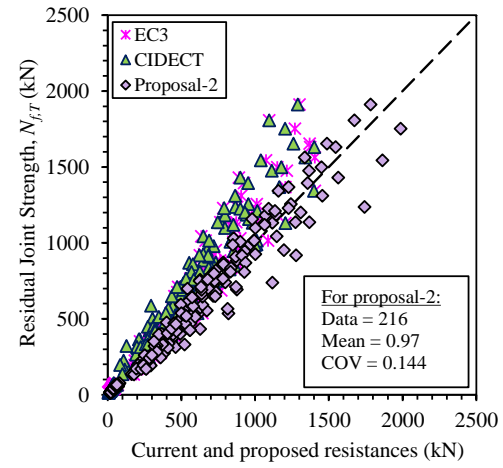


(b) For Proposal-2.

Fig. 13. Comparisons of joint resistances at elevated temperatures with current and proposed nominal resistances for RHS T-joints failed by F mode.

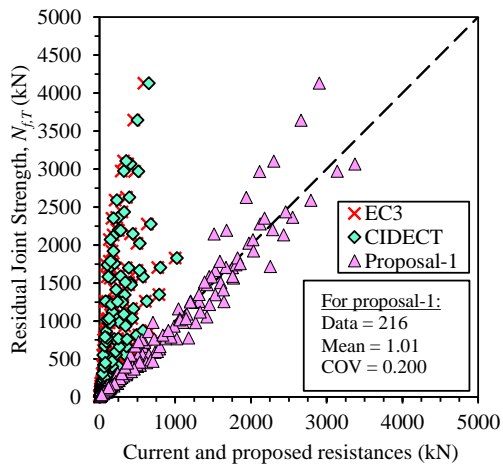


(a) For Proposal-1.

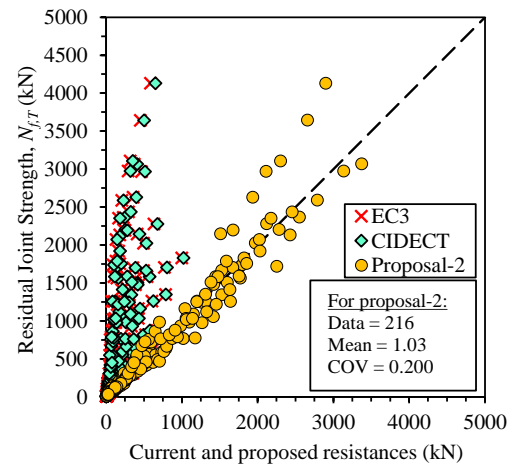


(b) For Proposal-2.

Fig. 14. Comparisons of joint resistances at elevated temperatures with current and proposed nominal resistances for RHS T-joints failed by F+S mode.



(a) For Proposal-1.



(b) For Proposal-2.

Fig. 15. Comparisons of joint resistances at elevated temperatures with current and proposed nominal resistances for RHS T-joints failed by S mode.

Table 1. Mechanical properties at elevated temperatures [52].

Temperatures (°C)	Nominal Yield Strengths (MPa)	Mechanical properties at elevated temperatures				
		$E_0$	$\sigma_{0.2}$	$\sigma_u$	$0.80\sigma_u$	$\epsilon_u$
		(GPa)	(MPa)	(MPa)	(MPa)	(%)
21	900	207	1024	1181	945	2.4
400	900	179	839	984	787	2.4
500	900	143	594	703	562	2.1
600	900	114	368	417	334	1.2
1000	900	30	21	27	22	7.4

Table 2. Overall ranges of critical parameters used in parametric study.

Parameters	Validity Ranges
$T$	[400°C to 1000°C]
$\beta (b_1/b_0)$	[0.30 to 1.0]
$2\gamma (b_0/t_0)$	[16.6 to 50]
$h_0/t_0$	[10 to 60]
$\eta (h_1/b_0)$	[0.3 to 1.2]
$\tau (t_1/t_0)$	[0.75 to 1.25]

Table 3. Summary of comparisons between joint resistances at elevated temperatures with existing and proposed nominal resistances for RHS T-joints failed by F mode.

Elevated Temperatures ( $T$ )	Parameters	Comparisons			
		$\frac{N_{f,T}}{N_{E,T}}$	$\frac{N_{f,T}}{N_{C,T}}$	$\frac{N_{f,T}}{N_{pn1}}$	$\frac{N_{f,T}}{N_{pn2}}$
400°C	No. of data ( $n$ )	81	81	81	81
	Mean ( $P_m$ )	1.08	1.18	1.04	1.02
	COV ( $V_p$ )	0.308	0.345	0.175	0.175
500°C	No. of data ( $n$ )	81	81	81	81
	Mean ( $P_m$ )	1.13	1.22	1.01	1.02
	COV ( $V_p$ )	0.310	0.338	0.187	0.187
600°C	No. of data ( $n$ )	81	81	81	81
	Mean ( $P_m$ )	1.05	1.22	0.96	1.01
	COV ( $V_p$ )	0.292	0.326	0.226	0.226
1000°C	No. of data ( $n$ )	81	81	81	81

	Mean ( $P_m$ )	1.48	1.70	1.03	1.02
	COV ( $V_p$ )	0.267	0.306	0.209	0.209
	No. of data ( $n$ )	324	324	324	324
Overall	Mean ( $P_m$ )	1.18	1.33	1.01	1.02
	Maximum	2.10	2.64	1.65	1.70
	Minimum	0.26	0.28	0.49	0.51
	COV ( $V_p$ )	0.327	0.364	0.201	0.199
	Resistance factor ( $\phi$ )	1.00	1.00	0.75	0.75
	Reliability index ( $\beta_0$ )	1.55	1.80	2.51	2.54

Table 4. Summary of comparisons between joint resistances at elevated temperatures with existing and proposed nominal resistances for RHS T-joints failed by F+S mode.

Elevated		Comparisons			
Temperatures ( $T$ )	Parameters	$\frac{N_{f,T}}{N_{E,T}}$	$\frac{N_{f,T}}{N_{C,T}}$	$\frac{N_{f,T}}{N_{pn1}}$	$\frac{N_{f,T}}{N_{pn2}}$
			No. of data ( $n$ )	54	54
400°C	Mean ( $P_m$ )	1.17	1.32	1.06	0.96
	COV ( $V_p$ )	0.165	0.172	0.134	0.134
	No. of data ( $n$ )	54	54	54	54
500°C	Mean ( $P_m$ )	1.18	1.35	0.99	0.95
	COV ( $V_p$ )	0.171	0.206	0.140	0.140
	No. of data ( $n$ )	54	54	54	54
600°C	Mean ( $P_m$ )	1.09	1.30	0.93	0.96
	COV ( $V_p$ )	0.161	0.211	0.159	0.159
	No. of data ( $n$ )	54	54	54	54
1000°C	Mean ( $P_m$ )	1.49	1.72	1.01	0.99
	COV ( $V_p$ )	0.248	0.228	0.142	0.142
	No. of data ( $n$ )	216	216	216	216
Overall	Mean ( $P_m$ )	1.23	1.41	1.00	0.97
	Maximum	3.50	3.13	1.33	1.29
	Minimum	0.74	0.87	0.62	0.64
	COV ( $V_p$ )	0.235	0.240	0.150	0.144
	Resistance factor ( $\phi$ )	1.00	1.00	0.80	0.75
	Reliability index ( $\beta_0$ )	1.97	2.46	2.51	2.63
	No. of data ( $n$ )	216	216	216	216

Table 5. Summary of comparisons between joint resistances at elevated temperatures with existing and proposed nominal resistances for RHS T-joints failed by S mode.

Elevated Temperatures ( $T$ )	Parameters	Comparisons			
		$\frac{N_{f,T}}{N_{E,T}}$	$\frac{N_{f,T}}{N_{C,T}}$	$\frac{N_{f,T}}{N_{pn1}}$	$\frac{N_{f,T}}{N_{pn2}}$
400°C	No. of data ( $n$ )	54	54	54	54
	Mean ( $P_m$ )	5.72	6.03	1.02	0.98
	COV ( $V_p$ )	0.774	0.644	0.202	0.200
500°C	No. of data ( $n$ )	54	54	54	54
	Mean ( $P_m$ )	5.39	5.73	1.06	0.99
	COV ( $V_p$ )	0.775	0.634	0.206	0.197
600°C	No. of data ( $n$ )	54	54	54	54
	Mean ( $P_m$ )	3.99	4.40	0.97	0.97
	COV ( $V_p$ )	0.712	0.565	0.236	0.250
1000°C	No. of data ( $n$ )	54	54	54	54
	Mean ( $P_m$ )	2.01	2.35	1.00	1.18
	COV ( $V_p$ )	0.603	0.296	0.144	0.151
Overall	No. of data ( $n$ )	216	216	216	216
	Mean ( $P_m$ )	4.36	4.89	1.01	1.03
	Maximum	18.69	16.77	1.72	1.58
	Minimum	0.88	1.37	0.65	0.67
	COV ( $V_p$ )	0.856	0.687	0.200	0.200
	Resistance factor ( $\phi$ )	1.00	1.00	0.75	0.75
	Reliability index ( $\beta_0$ )	2.17	2.84	2.52	2.57