

1 **Steel-Reinforced Grout (SRG) Strengthening of Shear-Critical RC Beams**

2

3 **Highlights:**

- 4 • Nine shear critical RC beams were strengthened using SRG jacketing.
- 5 • The effectiveness of U- and fully-wrapped SRG jackets was investigated.
- 6 • Strength and deformation capacity increased up to 160% and 450%, respectively.
- 7 • Digital Image Correlation confirmed the effectiveness of SRG jacketing.
- 8 • Expressions are proposed for estimating the effective strain of the SRG jacket.

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24 **Steel-Reinforced Grout (SRG) Strengthening of Shear-Critical RC Beams**

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27 **Abstract:** This paper investigates the effectiveness of Steel-Reinforced Grout (SRG) jackets to  
28 strengthen shear critical reinforced concrete (RC) beams. Eleven RC beams were tested in  
29 three-point bending. Key parameters of investigation were the strengthening configuration (U-  
30 and fully-wrapped jackets), the density of the fabric (1.57 and 4.72 cords/cm) and the number  
31 of the strengthening layers (one and two). The test results demonstrated the efficiency of SRG  
32 jacketing in increasing both strength (up to 160%) and deformation capacity (up to 450%) of  
33 the shear critical beams. Expressions are proposed for estimating the effective strain of the SRG  
34 jacket.

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36 **Keywords:** SRG; FRCM; Jackets; Steel fabric; Mortar; RC Beams; Shear; Strengthening

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## 1. Introduction

44 The vast majority of reinforced concrete (RC) structures was built at times when general  
45 understanding about the importance of reinforcement detailing in seismic response was still at  
46 a premature stage. Poor material and construction quality as well as aging of materials (e.g.  
47 steel corrosion) are other key factors that increase the vulnerability of substandard structures to  
48 future earthquake events. In the pre-1970s construction practice, shear reinforcement generally  
49 comprised of smooth rectangular stirrups anchored with 90° hooks in the ends, made of StI  
50 (yield strength 220 MPa) 6–8 mm diameter bars spaced at 250–300 mm on centres along the  
51 lengths of beams and columns [1]. Strength hierarchy checks performed on structural members  
52 with the aforementioned detailing, revealed that in most cases, and especially for beams, shear  
53 failure was the dominant mode of failure [1-3]. Such brittle failures can spread out across  
54 different locations of the building and jeopardize the overall structural integrity and ultimately  
55 lead to collapses.

56 In general, using externally bonded composites provides an effective way to alleviate  
57 deficiencies at local (member) level associated with shear critical members. Fibre Reinforced  
58 Polymer (FRP) jacketing is a popular and effective intervention method that has been used  
59 extensively for strengthening of substandard RC structures worldwide [e.g. 4-7]. However, FRP  
60 jacketing systems have several drawbacks, mainly related to the use of epoxy, such as poor  
61 behaviour to fire conditions, relatively high cost of epoxy resins and lack of vapour permeability  
62 with adverse effects on RC structures. In the last few years a new generation of mortar-based  
63 systems has been introduced, which retains the advantages of FRP applications but eliminates  
64 the previous shortcomings by using mortar instead of resin. Depending on the type of the textile,  
65 the following Fibre-Reinforced Cementitious Mortar (FRCM) systems have been developed:  
66 (i) TRM (Textile-Reinforced Mortar) where bidirectional textiles made of continuous carbon

67 or glass fibres are applied using mortars [e.g. 8-10]; (ii) PBO-FRCM (poliparafenilen  
68 benzobisoxazole fibre-reinforced cementitious matrix) where PBO nets are embedded in a  
69 cement based matrix [e.g. 11-12]; and (iii) SRG (steel-reinforced grout) system where Ultra  
70 High Tensile Strength Steel (UHTSS) textiles are combined with inorganic binders [e.g. 13-23].

71 Several experimental studies have demonstrated the efficiency of TRM and PBO-FRCM  
72 jacketing at improving the response of shear critical beams (TRM [24-32], PBO-FRCM [33-  
73 37]. Regardless of the adopted textile architecture, the number of layers and the jacket  
74 configuration, FRCM jackets have been proved quite efficient in increasing the shear capacity  
75 of deficient beams and in some cases activating flexural yielding. In case of SRG jacketing, the  
76 research conducted on shear strengthening of deficient RC beams is rather limited. In a recent  
77 study, Gonzalez-Libreros et al. [38] tested four beams retrofitted by adding U-shaped SRG  
78 jackets made of galvanized unidirectional sheets of an equivalent thickness of 0.27 mm.  
79 Parameters of investigation were the shear reinforcement of the beams (2 beams with  $\varnothing 6/200$   
80 and 2 beams with  $\varnothing 6/300$ ) and the textile installation (with and without anchors). The SRG  
81 jacketed beams failed in shear and similar cracking patterns were observed between the beams  
82 with and without anchors. In general, the addition of SRG jackets increased the shear strength  
83 of the beams. The presence of the anchors prevented detachment of the composite, but it did  
84 not increase the shear strength any further.

85 The main objective of this paper is to further investigate the role of key design parameters  
86 on the response of shear critical beams retrofitted with SRG jackets. An experimental study is  
87 carried out where one- or two-layered U-wrapped, U-wrapped with mechanical anchorage and  
88 fully-wrapped SRG jackets are applied to nine two-span beams (two additional beams are used  
89 as control specimens). The efficiency of two densities of Ultra-High Tensile Strength Steel  
90 (UHTSS) textiles is also examined (1.57 and 4.72 cords/cm). The test results demonstrate the  
91 effectiveness of SRG jacketing in increasing both strength and deformation capacity of the

92 shear critical beams. It is shown that the fully-wrapped SRG jackets can substantially modify  
93 the response of the original member by allowing it to fail in flexure. The experimental values  
94 of the shear strength of the SRG strengthened beams are then compared to the predicted values  
95 using existing design guidelines. Based on the experimental data, new expressions are derived  
96 which relate the effective strain of the SRG jacket to its axial rigidity.

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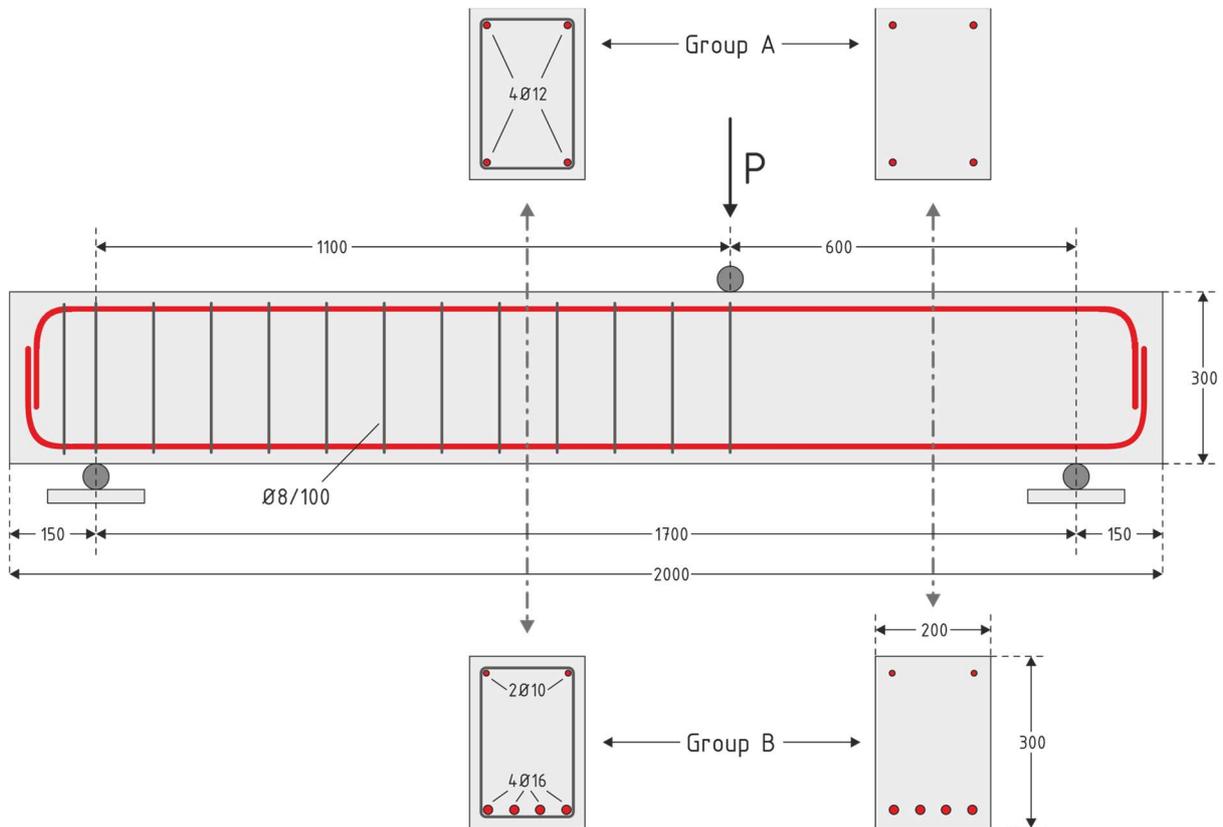
## 2. Experimental program

### 2.1 Specimen Details

98 Eleven RC beams were tested in three-point bending with a clear span to depth ratio of  $a/d =$   
99 2.2. The beams are characterized as short and it is expected that a major portion of the load  
100 capacity after the inclined cracking will be due to load transfer by the compression strut. All  
101 beams had a rectangular cross section 200 mm in width and 300 mm in height and were 2000  
102 mm long. The beams were divided into two groups (A and B) according to the arrangement of  
103 the longitudinal steel reinforcement. Group A comprised one control and four SRG  
104 strengthened beams, whereas Group B consisted of one control and five SRG strengthened  
105 beams.

106 The longitudinal tensile and compressive reinforcement in Group A beams comprised two  
107 bottom and two top 12-mm diameter bars ( $\rho_l = 0.75\%$ ), respectively (see Fig. 1). In case of  
108 Group B, the reinforcement of the beams consisted of longitudinal deformed steel bars with  
109 2 $\varnothing$ 10 bars at the top and 4 $\varnothing$ 16 bars at the bottom of the cross-section of the beam ( $\rho_l = 1.60\%$ ).  
110 Deformed steel 8 mm diameter closed stirrups were distributed at a uniform spacing of 100 mm  
111 in the longer span 1100 mm in length. All the beams were designed to be deficient in shear in  
112 the shorter shear span (600 mm in length, Fig. 1). Although, the presence of transversal internal  
113 steel (i.e. stirrups) would influence the response of the SRG jacketed beams, it was decided not  
114 to be considered as an additional parameter of study, since the objective was to directly assess

115 the efficiency of SRG jacketed on the retrofitted beams. Hence, no transverse reinforcement  
 116 was provided in the critical shorter shear span of 600 mm (Fig. 1), and the SRG jacketing was  
 117 only applied in the critical shear span. The anchorage zones for the longitudinal reinforcement  
 118 were 150-mm in length and two stirrups of 8-mm diameter were provided (Fig. 1).



119  
 120 Figure 1: Geometry and reinforcement details of Group A and Group B beam specimens.

121  
 122 The key parameters of investigation were: (i) the density of the Ultra-High Tensile Strength  
 123 Steel (UHTSS) textile which was 1.57 and 4.72 cords/cm, (ii) the number of applied SRG layers  
 124 (one and two) and (iii) the strengthening configuration which consisted of U-wrapped, U-  
 125 wrapped with mechanical anchorage and fully-wrapped SRG jackets. The beams were given  
 126 the notation XYZW, where X stands for the group of the beams (A or B in Table 1), Y  
 127 corresponds to the type of the jacketing system with 0 for the control specimen, U for the U-  
 128 wrapped jacket, UM for the U-wrapped jackets with mechanical anchorage and F for the fully-

129 wrapped jackets, Z indicates the density of the fabric with L and H for the 1.57 and 4.72  
 130 cords/cm fabrics, respectively, and finally W refers to the number of layers with 1 and 2 for  
 131 single- and double-layered SRG jackets. The details of all test specimens are given in Table 1.  
 Table 1: Details of the specimens

Group	Name	$f_c$ (MPa)	Type of jacket	Density (cords/cm)	Layers
Group A	A0	28.0	control	-	-
	AUH1		U-wrapped	4.72	1
	AUML1		U-wrapped mechanical anchorage	1.57	1
	AFL1		Fully-wrapped	1.57	1
	AFH1		Fully-wrapped	4.72	1
Group B	B0	23.3	control	-	-
	BUL1		U-wrapped	1.57	1
	BUL2		U-wrapped	1.57	2
	BUML1		U-wrapped mechanical anchorage	1.57	1
	BFL1		Fully-wrapped	1.57	1
	BFL2		Fully-wrapped	1.57	2

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## 2.2 Material Properties

134 The RC beams of Group A were casted in one batch having an average compressive strength  
 135 of  $f_c = 28$  MPa (standard deviation, SD = 2.47 MPa) at the day of the test obtained from six  
 136 standard cylinders (150×300mm). The beam specimens of Group B were casted in two batches  
 137 of three using the same mix. The average compressive strength at the day of the tests was  $f_c =$   
 138 23.3 MPa (standard deviation, SD = 1.36 MPa), which was determined from the average of six  
 139 standard cylinders (150 ×300mm). The steel grade used for internal longitudinal (i.e. Ø10, Ø12,  
 140 Ø16) and transverse reinforcement (i.e. Ø8) was B500C.

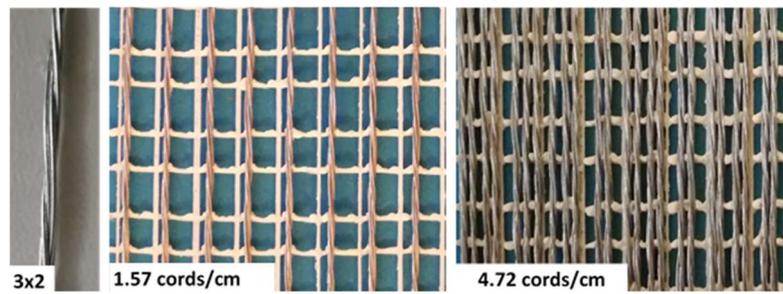
141 In this study, nine beams (four from Group A and five from Group B, see Table 1) were  
 142 retrofitted by using the SRG jacketing, in which externally bonded Ultra High Tensile Strength  
 143 Steel (UHTSS) textiles were embedded in an inorganic mortar matrix [13-14]. The textiles were  
 144 made of galvanized unidirectional high strength steel 3X2 cords fixed to a fiberglass micromesh

145 to facilitate installation (see Fig. 2). The fiberglass micromesh keeps the cords in place without  
 146 contributing to strength of the composite system [39, 40]. Each cord was made by twisting five  
 147 individual wires; three straight filaments wrapped by two filaments at a high twist angle as  
 148 shown in Fig. 2. The geometrical and mechanical properties of the single cords are given in  
 149 Table 2 as provided by the manufacturers. More details regarding the stress-strain curve of the  
 150 cords can be found in Napoli et al. [39] and Santis et al. [40].

151 Table 2: Geometrical and mechanical properties of single cords as provided by the  
 152 manufacturer

Cord type	Cord diameter (mm)	Cord area (mm <sup>2</sup> )	Break load (N)	Tensile strength $f_{fu}$ (MPa)	Strain to failure $\epsilon_{fu}$ (mm/mm)	Elastic modulus $E_f$ (MPa)
3X2	0.827	0.538	1506	2800	0.015	190000

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154

155 Figure 2: Steel cords and densities of the UHTSS textiles used

156 One of the critical design parameters of the SRG jacketing technique is the density of the  
 157 textiles (i.e. the spacing between successive cords) since it should be designed to provide  
 158 uninhibited flow of the cementitious grout through the steel fabric and develop adequate bond  
 159 between the textile and the matrix [13]. Two different densities 1.57 and 4.72 cords/cm were  
 160 examined in this experimental study with an equivalent thickness per unit width for a single  
 161 layer of steel fabric,  $t_f$ , equal to 0.084 and 0.254 mm, respectively (Table 1, Fig. 2). The axial  
 162 stiffness of the textile,  $K_f (= A_f \cdot E_f)$ , which is directly related to the density of the textile, was  
 163 calculated equal to 15960 and 48260 N/mm for the 1.57 and the 4.72 cords/cm textiles,  
 164 respectively (these figures should be doubled for the two-layered jackets).

165 A commercial geo-mortar with a crystalline reaction geobinder base and a very low  
 166 petrochemical polymer content and free from organic fibres was used in this study. The  
 167 component mortar was utilised as the substrate material applied to the concrete surface of the  
 168 specimens, the bonding material between the applied layers of the steel fabric and as a final  
 169 cover. The mechanical properties of the mortar appear in Table 3.

170 Table 3: Mechanical properties of the mortar at 28 days as provided by the manufacturer

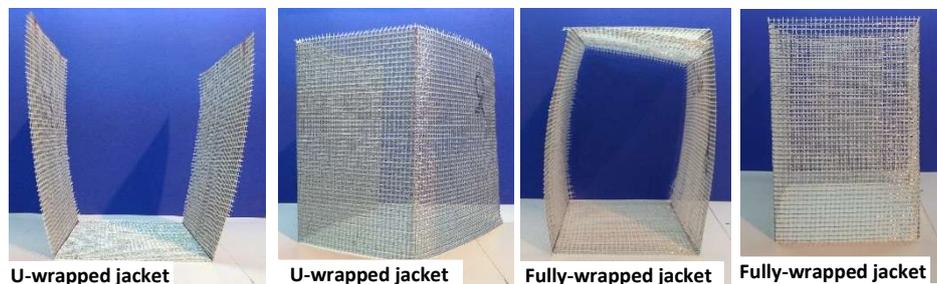
Mortar	Modulus of elasticity $E_m$ (MPa)	Flexural strength $f_{mf}$ (MPa)	Compressive strength $f_{mc}$ (MPa)	Adhesive bond $f_{mb}$ (MPa)
	25000	10.0	55.0	2.0

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### 2.3 SRG Strengthening

172 As mentioned above, nine RC beams (four from Group A and five from Group B) were  
 173 strengthened in the 600 mm shear critical span by applying the following three strengthening  
 174 configurations: U-wrapped, U-wrapped with mechanical anchorage and fully-wrapped SRG  
 175 jackets (see Table 1). The textiles originally were in roles of 300 mm width, thus 2 and 4 pieces  
 176 of fabric were utilized for the single- and double-layered SRG jackets, respectively. Before  
 177 starting the strengthening procedure, the fabrics were cut and pre-bent in order to follow the  
 178 shape of the jacket (Fig. 3). The edges of the beam cross section were not rounded, hence at  
 179 these areas the fabrics were pre-bent at right angle. The sides of the beams were roughened  
 180 using mechanical grinding to expose the aggregates and then were cleaned and saturated with  
 181 water before proceeding to the application of the mortar (Fig. 4a). Subsequently, the mortar was  
 182 applied in approximately 3 mm-thick layers manually with the help of a trowel directly onto  
 183 the lateral surface of the specimens (Fig. 4b). The textile was placed immediately after the  
 184 application of the cementitious mortar (Fig. 4c) and the mortar was squeezed out between the  
 185 steel fibres by applying pressure manually. In case of the fully-wrapped one- and two-layered  
 186 SRG jackets, after the application of the fabric to one and two full-cycles, respectively, the  
 187 remaining length, which was equal to the width of the beam (200 mm), was lapped over the top

188 surface of the beam. It should be noted that in the case of two-layered fully-wrapped jackets the  
189 fabric was continuous, while in the case of two-layered U-wrapped jacket each layer was  
190 independent. Straight after the application of the first layer of the textile, the next layer of the  
191 mortar covered it completely and the second layer of the fabric was applied by following the  
192 procedure described above. A final coat of the cementitious mortar was applied to the exposed  
193 surface. The effect of SRG jacketing on the geometric dimensions of the specimens was small.  
194 Each layer of the mortar including the textile was 7 and 10 mm thick for the one- and two-  
195 layered SRG jackets, respectively.

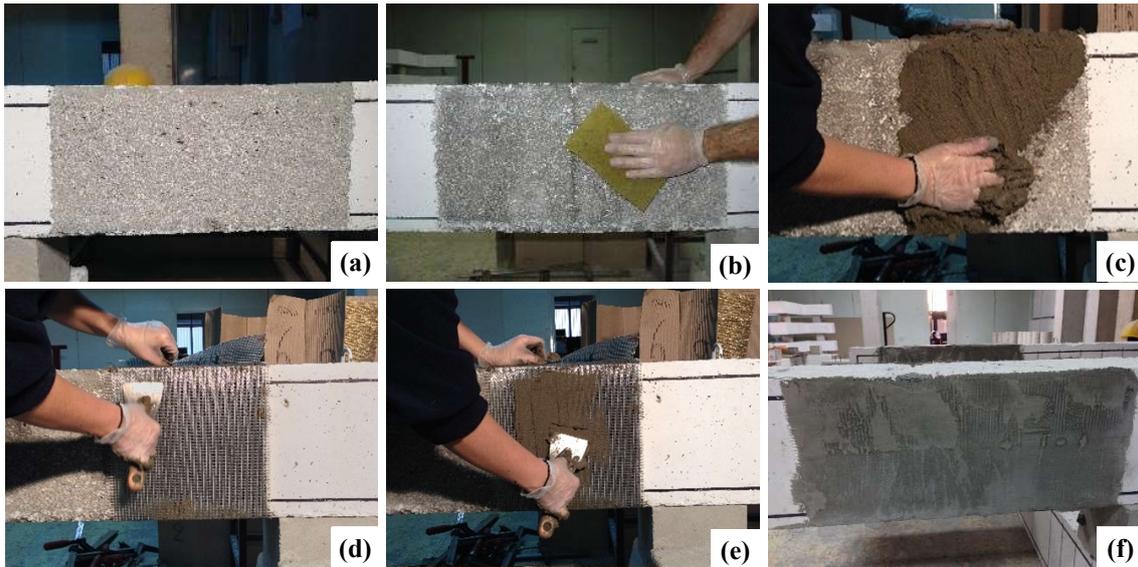


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Figure 3: Preparation of the UHTSS textiles

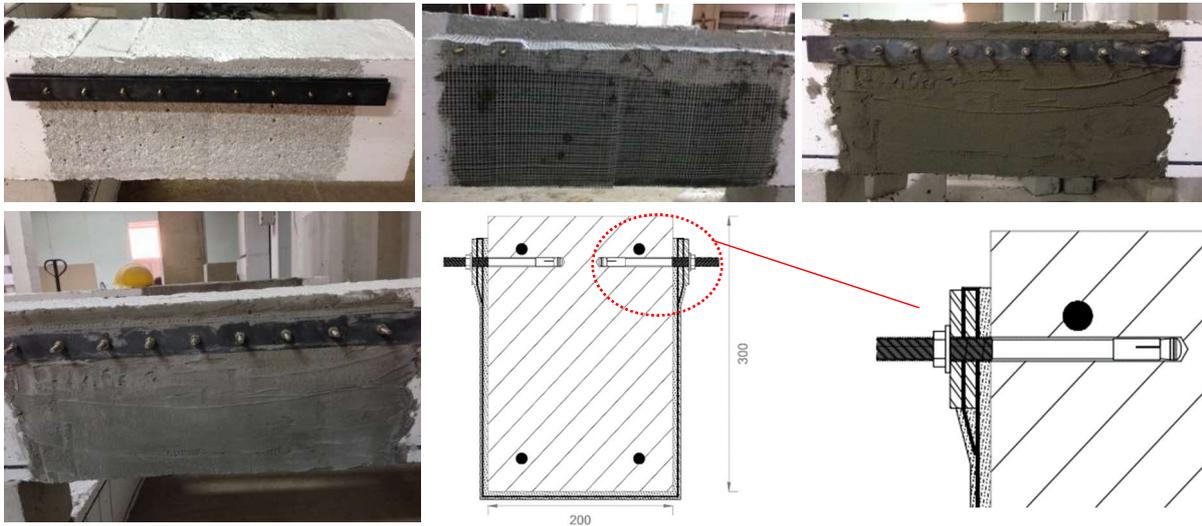
198 In two of the beams (AUML1 and BUML1, see Table 1) a custom-made mechanical  
199 anchorage system was applied to enhance the anchorage of the U-wrapped SRG jackets to the  
200 concrete substrate. The system comprised four 700×50×5 mm metal plates (2 placed on each  
201 side of the beam), which covered the full-length of the strengthened area. The metal plates were  
202 drilled at their mid-height so that in total 9 holes were opened with 70 mm spacing (Fig. 5). The  
203 beams were drilled following the same pattern and the metal plates attached 50 mm above the  
204 upper fibre. Subsequently, the stud anchors were installed and properly wedged in the beam  
205 holes. A thin layer of mortar was applied onto the roughened concrete substrate and the fabric  
206 was then passed through the anchors and well stretched before the first metal plate was put in  
207 place. The free end-zone of the fabric, which was pre-bent, was wrapped over the first metal  
208 plate and then the second metal plate was put in place. The last stage involved screwing in the  
209 metal plates on each side of the beam to ensure that any sliding of the fabric would be avoided.



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Figure 4: SRG jacketing application steps



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Figure 5: Preparation of the mechanical anchorage of the SRG U-wrapped beams

#### 2.4 Test setup and experimental methodology

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The employed three-point bending setup is depicted in Fig. 6. The RC beam was simply supported on a pair of steel pedestals seated on the strong floor and anchored together with a pair of threaded rods in order to prevent transverse sliding (span elongation) due to the second order horizontal reactions at the beam supports. Loading was vertically applied by a 1000 kN capacity single-ended actuator (MTS 243.60) using a displacement control system externally measured by a draw-wire sensor placed underneath the beam along the vertical loading axis.

219 The external load was monotonically increased up to beam failure, which was triggered upon a  
220 40 % drop of the maximum measured reaction of the actuator load cell. The load was applied  
221 at displacement rate 0.05mm/sec. Moreover, a Digital Image Correlation (DIC) configuration  
222 was utilised for capturing the strain contours of the tested beams [41]. The shear critical region  
223 of each beam (the area of interest (AOI)) was painted with a speckle pattern using a special  
224 brush and black ink. A DSLR camera was placed on a tripod at a distance, focusing on the  
225 beam's AOI, remotely and automatically shuttered from the main acquisition controller at given  
226 displacement intervals (4 photos per mm). Finally, the captured high-resolution speckle images  
227 for each specimen were post-processed using a DIC software to produce strain contours at  
228 characteristic points on the resulting load-displacement response curve.



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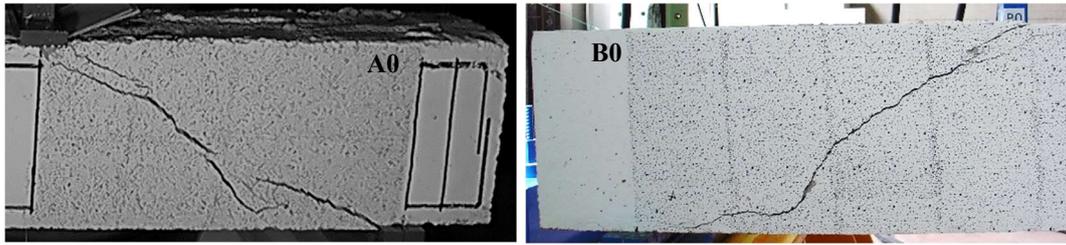
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Figure 6: Test setup and details of instrumentation

### 3. Test results and discussion

#### 3.1 Failure modes

231 The control beams of both Groups A and B (i.e. A0 and B0) exhibited a diagonal tension failure  
232 mode as observed in Fig. 7. A single inclined crack along the loading and the support points  
233 appeared in the shear span at the early stages of loading, which progressed further as the loading  
234 increased leading to a brittle shear failure.



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Figure 7: Failure mode of the control specimens

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The different SRG jacketing schemes applied to the shear-critical beams of Group A led to flexural failure of the strengthened beams (Fig. 8). The internal bottom steel reinforcement reached yielding (i.e.  $\epsilon_{sy}=f_{sy}/E_s=500/200000=0.0025$  for steel grade B500C. Strain measurements were taken from the Digital Image Correlation (DIC) technique) and the beams failed in a ductile manner, while flexural cracks formed on both sides of the applied point load (Fig. 8). Apart from the cracks developed along the beam transverse direction that coincided with the gap between successive cords, the textile did not show any further damage.



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Figure 8: Failure modes of the SRG-strengthened specimens of Group A

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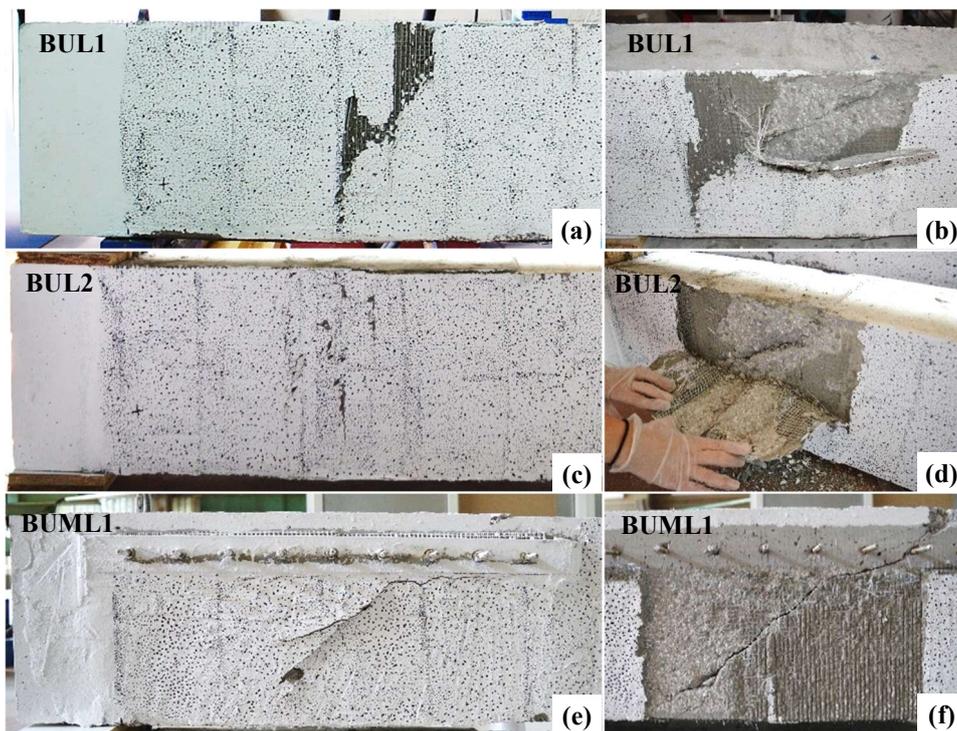
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The U-wrapped SRG strengthened beams of Group B (BUL1 and BLU2, Table 1) both failed in shear (Fig. 9). The general mode of failure observed was the detachment of the composite system at the interface between the UHTSS textile and the mortar and/or at the interface between the mortar and the concrete substrate, with damage of the external face of the concrete cover.

251 The beam with the single-layered U-wrapped SRG jacket (BUL1, Table 1) failed suddenly  
 252 when the textile between the mid-point of the shear-critical region and the loading point was  
 253 detached. The state of the critical region of the beam at the end of the test and after exposing  
 254 the substrate, is shown in Figs. 9a and 9b, respectively. It is observed that only a single shear  
 255 crack formed, having the same inclination as that in the original beam B0 (see Fig. 7). In case  
 256 of the two-layered U-wrapped SRG jacketed beam (BUL2, Table 1), the detachment of the  
 257 composite system occurred at two stages. First, part of the textile placed between the support  
 258 and the mid-point of the critical region was detached. The beam continued to carry load and, at  
 259 a later stage, the textile between the mid-point of the critical span and the loading point was  
 260 detached. Fig. 9c shows the BUL2 beam at the end of the test. Again, as shown in Fig. 9d, one  
 261 single crack formed with the same inclination as the crack in the original beam B0 (see Fig. 7).

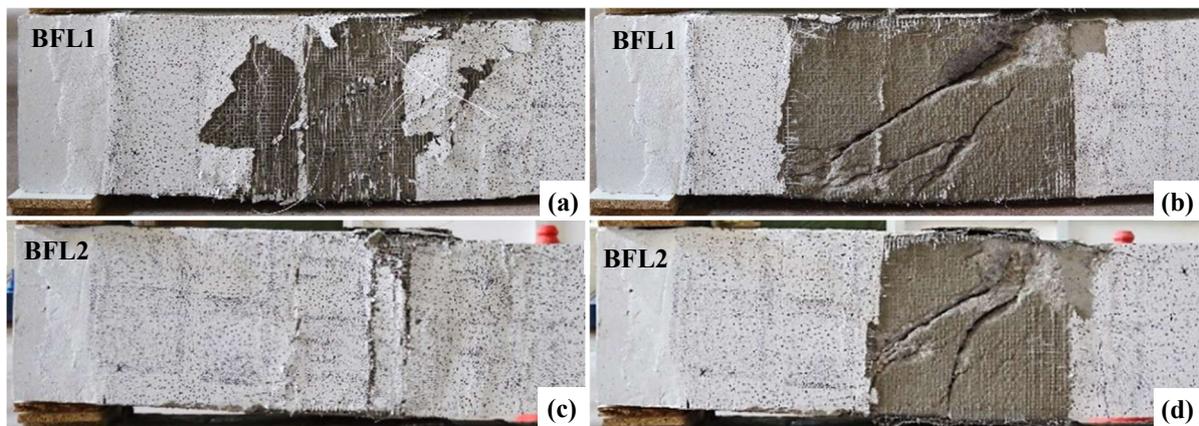


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263 Figure 9: Failure modes of the U-wrapped SRG beams of Group B in the shear-critical  
 264 span.  
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266 After the first stages of loading of the U-wrapped beam with the mechanical anchorage  
 267 (BUML1, Table 1), an inclined crack formed on the jacket surface below the metal plate, as

268 shown in Fig. 9e. The existing crack became wider as the load increased. Soon enough the  
269 textile detached by forming a new horizontal crack along the bottom side of the metal plate and  
270 headed towards the loading point (Fig. 9e). The test was terminated when the inclined crack  
271 propagated towards the loading point passed through one of the stud anchors (Fig. 9f). The  
272 removal of the jacket and the metal plates revealed that the dominant mode of failure was  
273 diagonal tension failure (Fig. 9f) as also observed in the other U-wrapped beams. The SRG  
274 jacket remained intact and no damage was visible in the mechanical anchorage system.

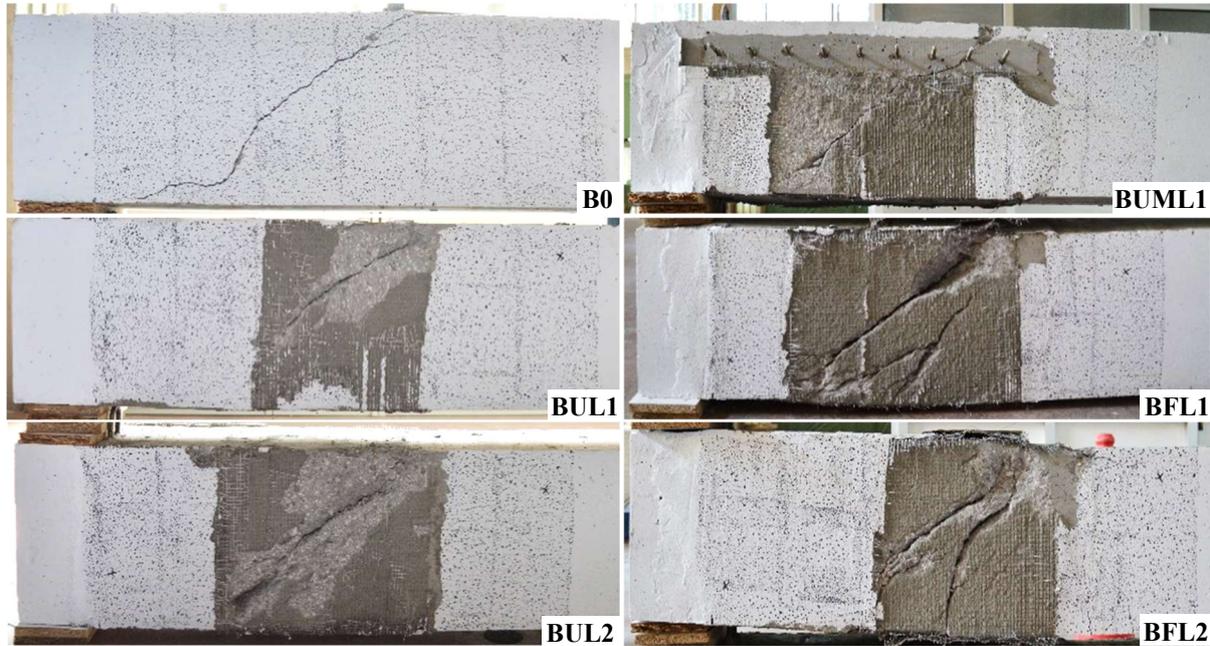


275  
276 Figure 10: Failure modes of the fully-wrapped SRG beams of Group B in the shear-critical  
277 span.  
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279 The fully-wrapped SRG beams (BFL1 and BFL2, Table 1) behaved in a more ductile manner  
280 compared to the U-wrapped and the original beams. In case of BFL1 beam, a shear-flexure  
281 crack formed on the jacket surface within the critical region at the initial stage of loading. As  
282 the load increased, damage localized within the inclined area bounded between the loading  
283 point and a 150 mm distance from the support, until the external surface of the SRG jacket was  
284 heavily cracked (Fig. 10a). At this stage, the beam could not sustain any additional load, but it  
285 continued to deform due to passive confinement provided by the SRG jacket. The beam  
286 exhibited a ductile behaviour up to the point where gradual rupture of the cords initiated at the  
287 upper and bottom sharp edges on both beam faces. The beam failed due to debonding of the  
288 textile in the anchorage region (i.e. the region where the end of the fabric overlapped with the

289 beginning of the textile) next to the applied point load. The cracking pattern of beam BFL1 was  
290 different from that of the U-wrapped beams and more flexure-shear cracks were observed as  
291 shown in Fig. 10b. Similar to the previous case, beam BFL2 failed in a ductile manner with the  
292 internal tensile steel reinforcement reaching yielding. At the initial stage of loading, the first  
293 flexural crack appeared in the middle of the SRG jacketed shear span. Subsequently, two more  
294 flexural cracks appeared in the opposite side of the critical shear span (i.e. the un-strengthened  
295 side of the beam) next to the applied point load. As the load increased, no additional flexural  
296 cracks were developed, whereas the existing ones became wider. The confinement provided by  
297 two-layered SRG jackets could significantly increase the deflection capacity of the beam, and  
298 therefore, the beam managed to sustain the load applied after yielding. The rupture of the cords  
299 occurred gradually, and it was mainly concentrated between the mid-point of the shear span  
300 and the point at which the load applied. The beam finally failed when the free end-zone of the  
301 textile was detached from the anchorage region next to the applied point load. The flexural  
302 cracks developed in the critical shear span are shown in Fig. 10d.

303 The evolution of damage in the SRG jacketed beams of Group B was influenced by the SRG  
304 jacket configuration applied, as shown in Fig. 11. Although the U-wrapped SRG jackets could  
305 not prevent shear failure, this was delayed until higher levels of loading. It is observed that  
306 similar to the control beam (B0), a single inclined crack was appeared in the U-wrapped beams  
307 (BUL1, BUL2, BUML1). The response of the SRG jacketed beams was improved substantially  
308 when SRG closed-type jackets (i.e. fully-wrapped) were applied. The confinement provided by  
309 the one-layered fully-wrapped jacket (BFL1) led to a ductile behaviour upon shear failure with  
310 the presence of a multiple shear–flexure cracking pattern (Fig. 11). The two-layered fully-  
311 wrapped SRG jacket (BFL2) improved substantially the response of the original beam by  
312 alleviating the deficiencies related to old type detailing. The SRG jacketed beam failed in  
313 flexure with flexural cracks formed near the applied point load.



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Figure 11: Crack patterns at failure in Group B beams

### 3.2 Load deflection curves

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The load deflection response curves of Group A and B specimens are presented in Fig. 12. A

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summary of the test results is also provided in Table 4. The key performance parameters include

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the peak load ( $P_{max}$ ) and the corresponding deflection ( $\delta_{max}$ ), the ultimate load at a 20 % drop

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of the peak load ( $P_u$ ) and the corresponding deflection ( $\delta_u$ ), and finally the displacement

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ductility ( $\mu_\delta$ ). In case that no descending branch appears in the load–deflection curve, the last

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point of the curve is considered as the ultimate deflection ( $\delta_u$ ). The displacement ductility was

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defined after idealizing the experimental load–deflection curve by a bilinear curve according to

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the recommendations of ASCE/SEI Standard 41-06 recommendations [42].

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In general, the results indicate that the SRG shear strengthening intervention could

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considerably improve the strength and deformation capacity of the control beams. The different

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jacket configurations applied in Group A beams showed the same level of efficiency in

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modifying the structural response from brittle to ductile (Fig. 12a). The strength increase at

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peak load varied between 27.6 to 38.1 %, whereas the displacement ductility ranged between

329

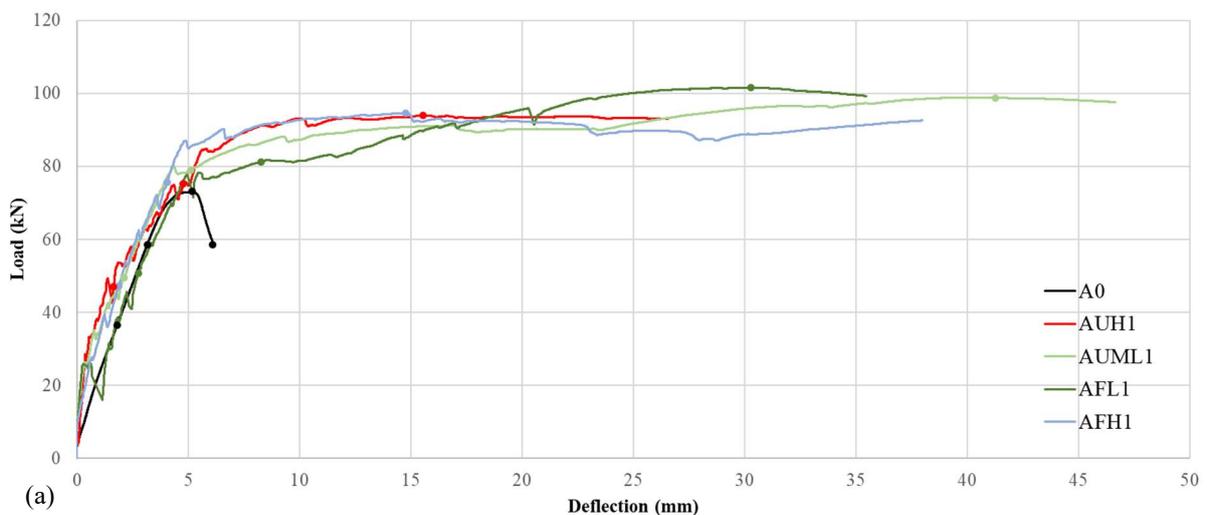
9.1 to 12.3 (Table 4). The lowest increase in the strength and displacement ductility levels was

330 observed for the high density U- and fully-wrapped SRG jackets (AUH1 and AFH1). This is  
331 because when dense textiles are used in SRG applications, as for example the 4.72 cords/cm  
332 density textile, the small gaps between the cords impose difficulties in the penetration of the  
333 mortar. Hence, the fact that the cords are not well embedded in the mortar renders the SRG  
334 system less efficient. A similar observation was reported by Thermou et al. [19] for retrofitting  
335 of RC columns using SRG jacketing. The main conclusion drawn from Group A beams is that  
336 in case of lightly reinforced RC beams ( $\rho_1 = 0.75\%$ ), which are representative of the old  
337 construction practice in southern Europe, the lower density (1.57 cords/cm) U-wrapped jackets  
338 can be very effective in preventing shear failure and modifying the response from brittle to  
339 ductile.

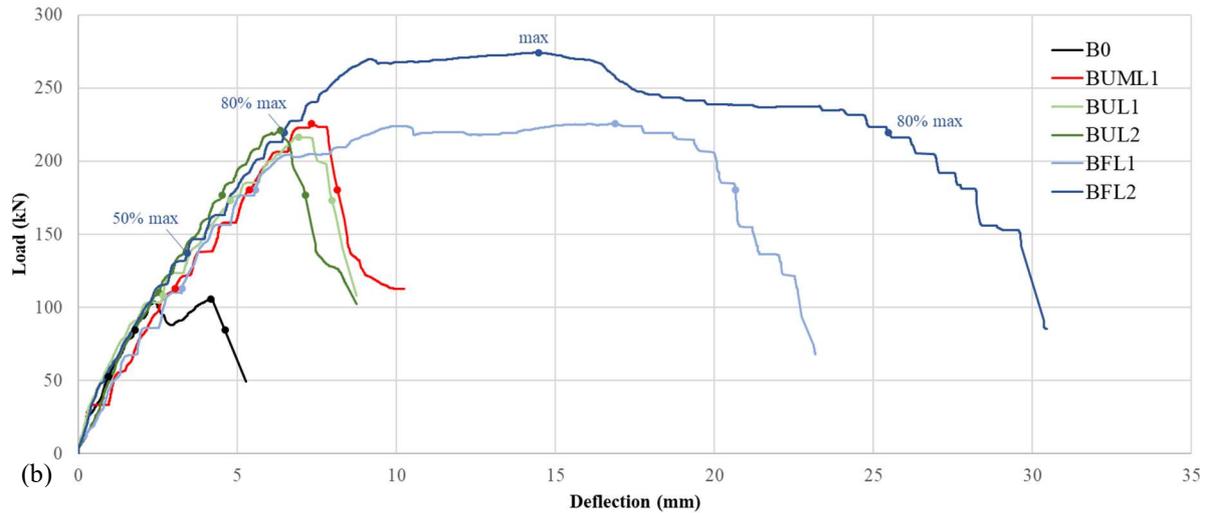
340 The effect of the type of the SRG jacket on the load–deflection response of Group B beams  
341 is shown in Fig. 12b. The control beam (B0) failed by diagonal tension failure at a peak load of  
342 105.6 kN (Table 4). The single- and doubled-layered U-wrapped beams (BUL1, BUL2) as well  
343 as the single-layered U-wrapped beam with the mechanical anchorage (BUML1) failed in shear  
344 at peak loads of 216.7, 221.1 and 225.7 kN, respectively (Table 4). The increase in the strength  
345 of BUL1, BUL2 and BUML1 beams compared to the control beam (B0) at peak load was 105,  
346 110 and 114 %, respectively. The deflection increase at ultimate load was 73, 55 and 77 % for  
347 BUL1, BUL2 and BUML1 beams, respectively. As observed, the U-wrapped SRG jacket with  
348 the mechanical anchorage (BUML1) exhibited the highest load and deflection increase amongst  
349 the U-wrapped jackets. This is mainly attributed to the presence of the mechanical anchorage  
350 which kept the jacket in place for a higher sustained load compared to the other two U-wrapped  
351 SRG jackets (i.e. BUL1, BUL2) and thus contributed further to the resistance of the beam. It  
352 can be noted that the single-layered fully-wrapped SRG jacket (BFL1) reached the same peak  
353 load as the single-layered U-wrapped SRG jacket with the mechanical anchorage (BUML1) but  
354 presented a more ductile post-peak load–deflection response. The fully-wrapped jacketed beam

355 deformed up to 20.7 mm deflection at ultimate load, which implies that 349 % increase in the  
 356 deflection capacity (or deformability) was achieved compared to the control beam before failing  
 357 due to debonding of the textile in the anchorage region. The displacement ductility for BFL1  
 358 beam was estimated equal to 3.4. Using two-layered fully-wrapped SRG jackets in BFL2 beam  
 359 could substantially increase the shear strength allowing flexural failure to occur. The peak load  
 360 in this case was 274.2 kN, which corresponds to almost 160 % increase when compared to the  
 361 control beam (B0). The second layer of full jacket increased the deflection at ultimate to 25.5  
 362 mm. The displacement ductility was estimated equal to 3.8, which is rather satisfying  
 363 considering the inherent deficiency of the beam.

364 Comparison between the results for BLF1 and BLF2 beams shows that increasing the  
 365 number of SRG layers had a limited effect (around 10%) on the ductility of the specimens,  
 366 while it could considerably increase the maximum strength and deflection capacity of the  
 367 specimens (up to 23%). The results in Table 4 also indicate that SRG jacketing was more  
 368 efficient in increasing the deformation capacity and ductility of the beams with lower  
 369 longitudinal reinforcement ratio (i.e. Group A). However, the effect of SRG jacketing on  
 370 improving the maximum strength was more pronounced for the beam elements with higher  
 371 longitudinal reinforcement ratio (i.e. Group B).



372



373

374

Figure 12: Load-deflection curves for (a) Group A; (b) Group B beams.

375

Table 4: Summary of test results

Group	Name	$P_{max}$ (kN)	$P_u$ (kN)	$\delta_{max}$ (mm)	$\delta_u$ (mm)	Strength increase at peak (%)	Deflection increase at ultimate (%)	Ductility $\mu_\delta$	Failure mode
Group A	A0	73.6	58.9	5.3	6.2	-	-	-	Shear
	AUH1	93.9	93.0	15.5	26.5	27.6	326.0	9.1	Flexural
	AUML1	98.8	97.6	41.3	46.7	34.3	649.3	12.3	Flexural
	AFL1	101.6	99.4	29.2	34.4	38.1	452.5	12.1	Flexural
	AFH1	94.6	92.6	14.8	38.0	28.5	510.0	10.7	Flexural
Group B	B0	105.6	84.5	4.2	4.6	-	-	-	Shear
	BUL1	216.7	173.3	6.9	8.0	105.2	73.3	-	Shear
	BUL2	221.1	176.9	6.4	7.1	109.5	55.0	-	Shear
	BUML1	225.7	180.5	7.3	8.1	113.8	77.0	-	Shear
	BFL1	225.4	180.4	16.9	20.7	113.5	349.1	3.4	Shear/Flexural
BFL2	274.2	219.3	14.5	25.5	159.7	453.5	3.8	Flexural	

376

### 3.3 Evolution of damage based on Digital Image Correlation

377

As described previously, the additional measurement technique of Digital Image Correlation

378

(DIC) was applied on all specimens by painting a speckle pattern on the shear critical region

379

(area of interest – AOI) of each beam. During testing, a DSLR camera captured high-resolution

380

images of the AOI at given displacement intervals and these images were postprocessed for

381

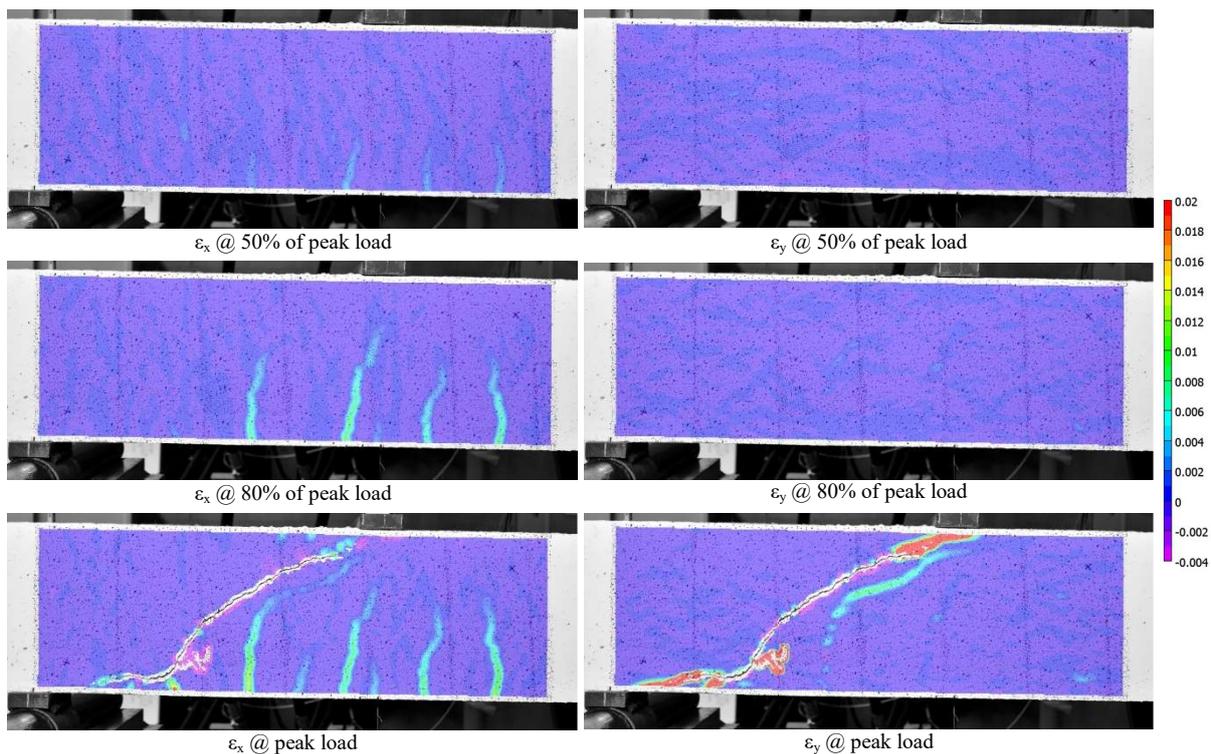
producing strain contours at preselected characteristic points on the load-displacement response

382

curve. The characteristic points were selected to represent 50%, 80% and 100% of the peak

383 load (ascending branch) as well as 20% drop of peak load in the descending branch (see Fig.  
384 12). The results were used to demonstrate the evolution of damage on the AOI surface in terms  
385 of horizontal ( $\epsilon_x$ ) and vertical ( $\epsilon_y$ ) strain distribution.

386 Figure 13 shows the strain evolution of the control specimen B0. It is observed that minor  
387 flexural cracks started to develop on the bottom edge of the beam up to the attainment of the  
388 peak load when the localized diagonal shear crack was formed. At that point, the longitudinal  
389 strain ( $\epsilon_x$ ) reached about 1‰, substantially lower than the reinforcement yielding point (about  
390 2.5‰). It is notable that a second shear crack also started to develop parallel to the major one;  
391 however, it could not fully form due to the brittle shear failure (no descending branch was  
392 captured in this case). It was confirmed that the behaviour of the control beam B0 fully  
393 corresponds to the typical textbook shear failure type.



394 Figure 13: Strain evolution for beam B0 using DIC

395 The strain evolution of the U-wrapped specimen with single layer (BUL1) is depicted in Fig.  
396 14. In this case, the flexural cracks sustained larger longitudinal strains (well over 2‰) at the  
397

398 peak load, where also an inclined yet diffused cracking pattern appeared due to the presence of  
 399 the SRG U-wrap. This justifies the increased shear strength already recorded during testing for  
 400 this type of SRG jacketing. For the mechanical anchorage (BUML1) and double-layer U-  
 401 wrapped (BUL2) specimens, this diffusion was wider, with less inclined straining (i.e.  
 402 longitudinal strains only) observed, especially for the latter case.

403

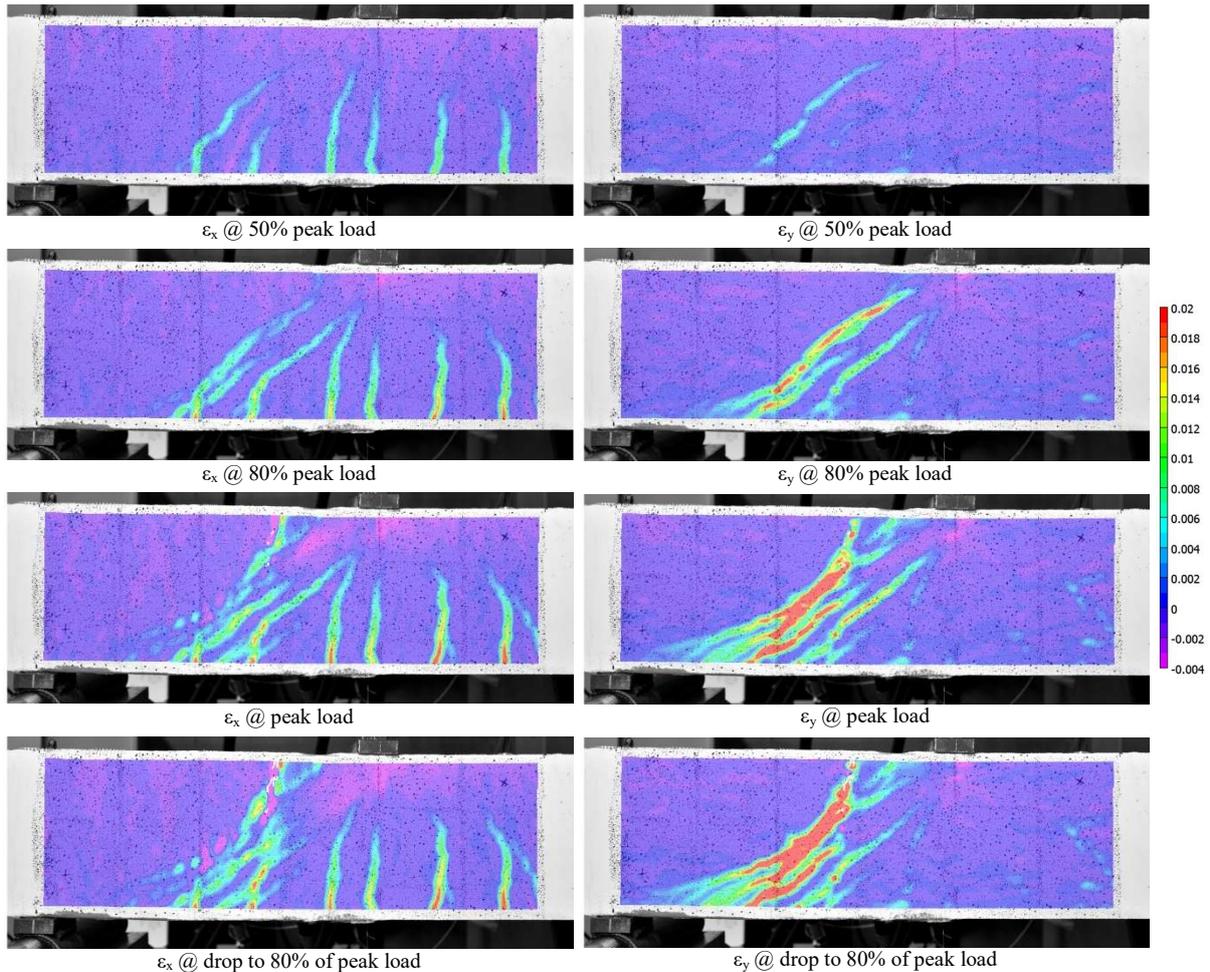


Figure 14: Strain evolution for beam BUL1 using DIC

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Finally, for the fully-wrapped cases (BFL1 and BFL2), the strain evolution on the AOI surface shows that the SRG layer(s) completely prevented the development of diagonal straining of the steel material (see Fig 15). It is observed that strains were strongly diffused only in the longitudinal direction and the failure pattern clearly corresponded to the rupture of the steel cords.

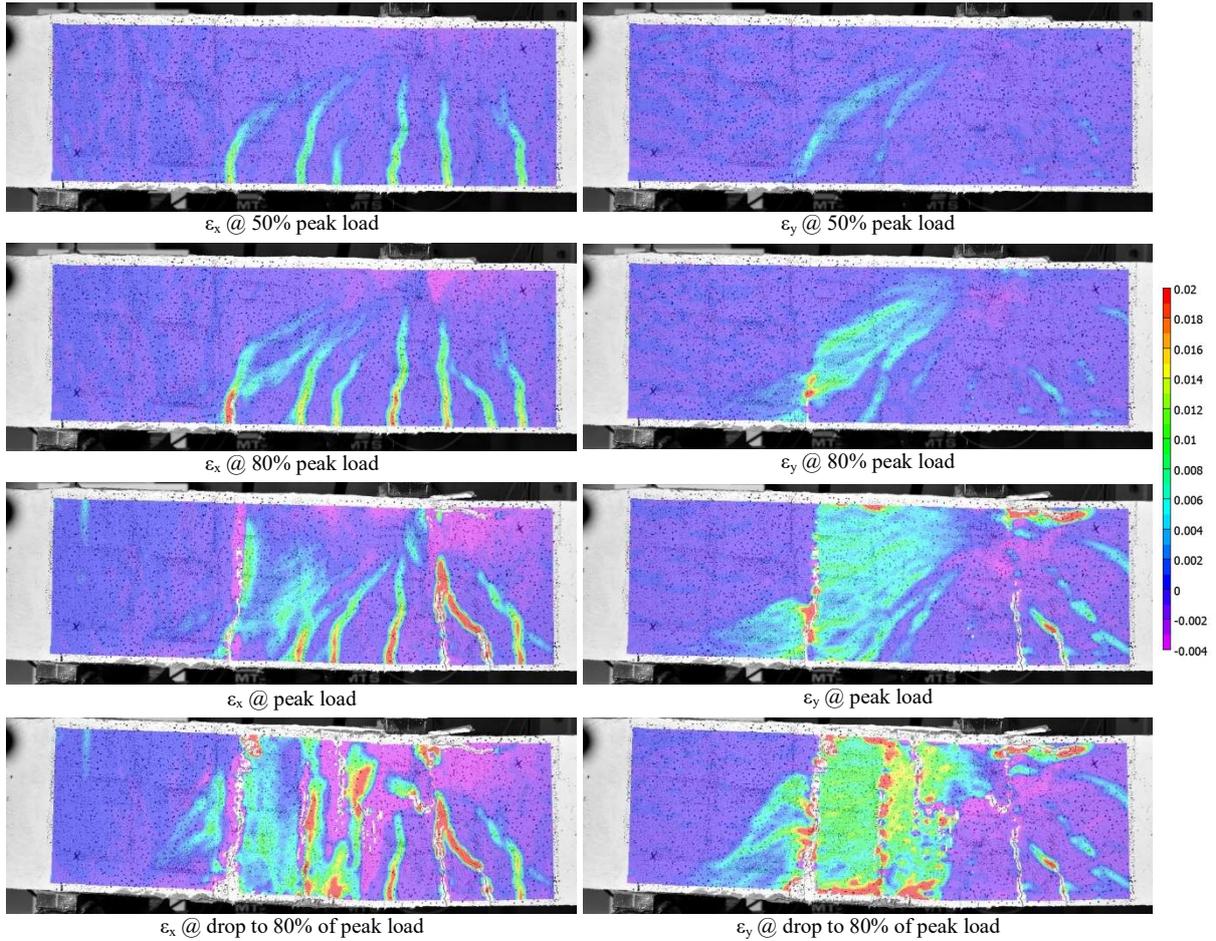


Figure 15: Strain evolution for beam BFL2 using DIC

412

413

#### 4. Comparison of experimental results to analytical predictions

414

##### 4.1 Shear resistance of the SRG jacketed beams

416 The total shear strength of SRG jacketed RC beams,  $V_{shear}$ , comprises shear strength  
 417 contributions from concrete, ( $V_c$ ), steel stirrups, ( $V_s$ ), and SRG jacket, ( $V_{SRG}$ ):

$$418 \quad V_{shear} = V_c + V_s + V_{SRG} \leq V_{Rd,max} \quad (1)$$

419  $V_{shear}$  estimated according to Eq. (1) shall not exceed the limit value for shear,  $V_{Rd,max}$ , which  
 420 corresponds to crushing of the diagonal compression struts in the web of the member [43].

421 Since the studied beams did not contain any stirrups in the critical shear span, the term  $V_s$  can  
 422 be neglected from Eq. (1). The shear strength contribution from concrete,  $V_c$ , is calculated  
 423 herein by using the EC2 [43] and ACI 318 [44] design guidelines:

424 
$$V_c^{EC2} = 0.12 \cdot k \cdot (100 \cdot \rho_l \cdot f_c)^{1/3} \cdot b_w \cdot d \geq 0.035 \cdot k^{3/2} \cdot f_c^{1/2} \cdot b_w \cdot d \quad (2)$$

425 
$$V_c^{ACI} = 0.167 \sqrt{f_c} \cdot b_w \cdot d \quad (3)$$

426 where  $f_c$  is the concrete compressive strength,  $b_w$  is the width of the cross section,  $d$  is the depth  
 427 of the cross section,  $k (= 1 + \sqrt{(200/d)} \leq 2$  with  $d$  in mm) is a factor that considers the size effect  
 428 and  $\rho_l$  is the area ratio of the tensile reinforcement.

429 Similar to the approach adopted for other externally bonded composite materials (e.g. FRP,  
 430 FRCM), the shear strength contribution of the SRG jackets is determined following the truss  
 431 analogy model [e.g. 45-49]. The steel fabric is considered to have an equivalent thickness per  
 432 unit width and an effective strain,  $\varepsilon_{f,eff}$  [14]. By considering the effects of fibre orientation and  
 433 assuming a crack pattern, the shear force sustained by the SRG can be calculated as:

434 
$$V_{SRG} = n \cdot \rho_f \cdot b_w \cdot h_f \cdot \varepsilon_{f,eff} \cdot E_f \cdot (\cot \theta + \cot \alpha) \cdot \sin \alpha \quad (4)$$

435 where  $n$  is the number of textile layers applied;  $\rho_f (= 2 \cdot t_f / b_w)$  is the SRG web reinforcement ratio  
 436 for a single layer;  $b_w$  is the width of the cross section;  $h_f$  is the effective depth of the jacket taken  
 437 as  $(h - 0.1d) \approx 0.9d$  ( $h$  and  $d$  are the height and the effective depth of the cross section,  
 438 respectively) for full-depth SRG jackets;  $\varepsilon_{f,eff}$  is the effective strain in the cords;  $E_f$  is the elastic  
 439 modulus of the SRG fabric;  $\alpha$  is the angle between the fibres and the beam axis perpendicular  
 440 to the shear force; and  $\theta$  is the angle between the concrete compression strut and the beam axis  
 441 perpendicular to the shear force.

442 Depending on whether the textile will be applied in strips of width  $b_f$  at a longitudinal  
 443 distance  $s_f$  or as a continuous fabric with an equivalent thickness,  $t_f$ , and by considering  $\alpha=90^\circ$   
 444 (i.e. fibres aligned perpendicular to the horizontal axis) and  $\theta=45^\circ$  (i.e. the angle between the  
 445 concrete compression strut and the beam axis perpendicular to the shear force), Eq. (4) is  
 446 simplified to:

447 
$$V_{SRG} = 2 \cdot n \cdot t_f \cdot h_f \cdot \varepsilon_{f,eff} \cdot E_f \quad \text{for continuous fabric} \quad (5a)$$

448 
$$V_{SRG} = 2 \cdot n \cdot t_f \cdot h_f \cdot \frac{b_f}{s_f} \cdot \varepsilon_{f,eff} \cdot E_f \quad \text{for strips} \quad (5b)$$

449 In Eqs. (4, 5), the effective strain,  $\varepsilon_{f,eff}$ , corresponds to a fraction of the rupture strain for the  
 450 cords,  $\varepsilon_{fu}$ , and is used to account for the non-uniform distribution of stress in the textile  
 451 intersecting the shear crack and for the reduction of SRG strength due to bending of the fibres  
 452 at the corners of the cross section. The strain efficiency factor  $k_\varepsilon (= \varepsilon_{f,eff} / \varepsilon_{fu} < 1)$  is implemented  
 453 for estimating the effective strain,  $\varepsilon_{f,eff}$ .

454 Different values for  $k_\varepsilon$  have been suggested by various researchers and code provisions.  
 455 Based on an experimental study on carbon TRM jackets, Triantafillou and Papanikolaou [24]  
 456 concluded that  $\varepsilon_{f,eff}$  corresponds to approximately 50% of the ultimate strain,  $\varepsilon_{fu}$ , of the cords.  
 457 In a different study, by investigating experimentally the performance of RC beams shear  
 458 strengthened with various TRM jacketing systems, Escrig et al. [34] proposed a methodology  
 459 for estimating TRM contribution to the shear capacity based on the following expressions for  
 460 the effective strain,  $\varepsilon_{f,eff}$ :

461 
$$\varepsilon_{f,eff} = 0.035 \cdot \left( \frac{f_c^{2/3}}{n \cdot E_f \cdot \rho_f} \right)^{0.65} \cdot \varepsilon_{fu} \quad \text{fully wrapped} \quad (6a)$$

462 
$$\varepsilon_{f,eff} = 0.020 \cdot \left( \frac{f_c^{2/3}}{n \cdot E_f \cdot \rho_f} \right)^{0.55} \cdot \varepsilon_{fu} \quad \text{side bonded or U-wrapped} \quad (6b)$$

463 where  $f_c$  (in MPa) is the concrete compressive strength,  $\varepsilon_{fu}$  is the strain at failure,  $E_f$  (in GPa)  
 464 is the elastic modulus of the textile, and  $\rho_f$  is the web reinforcement ratio for a single SRG layer.

465 The definition of the modulus of elasticity and the effective strain adopted by the ACI 549-  
 466 9R-13 [46] for the design of externally bonded FRCM systems are based on the behaviour of  
 467 the cracked composite material. For the case of effective strain of the SRG composite,  $\varepsilon_{f,eff}^*$ , an  
 468 upper limit of 0.004 is used in this study [46]. The modulus of elasticity of the SRG composite,

469  $E_f^*$ , is taken equal to 168000 MPa which corresponds to the average modulus of elasticity  
 470 defined by tensile tests of the SRG composite [51].

471 In the following section, the adequacy of the above effective strain definitions (suggested by  
 472 [24, 34, 46]) to predict the shear capacity of RC beams strengthen by SRG jackets is  
 473 investigated compared to the experimental results.

474

#### 475 **4.2 Experimental results versus analytical predictions**

476 The experimental shear strength values corresponding to the shear critical region,  $V_{shear}^{exp}$  (=  $P_{max} \cdot L_2/L$ ); where  $L_2(=1.1$  m) is the longer span and  $L(=1.8$  m) is the distance between the  
 477 supports, are presented in Table 5 for all tested specimens (column (3)). The shear strength  
 478 contributions from concrete,  $V_c$  (Eqs. (2) and (3)), and SRG jacket,  $V_{SRG}$  (Eq. 5a), are also given  
 479 in Table 5 (Columns (7)-(11)).  $V_{SRG}$  and consequently  $V_{shear}$  are calculated by adopting the  
 480 three alternative definitions for effective strain,  $\varepsilon_{f,eff}$ , as discussed in the previous section. The  
 481 experimental values of the shear strength of the SRG jackets,  $V_{SRG}^{exp}$ , are provided by subtracting  
 482 the shear strength of the control specimen,  $V_c^{exp}$ , from the shear strength of the SRG jacketed  
 483 beams,  $V_{shear}^{exp}$  (see column (4) in Table 5). The experimental values of the effective strain,  $\varepsilon_{f,eff}^{exp}$ ,  
 484 are calculated according to column (6) in Table 5:

$$486 \quad \varepsilon_{f,eff}^{exp} = \frac{V_{shear}^{exp} - V_c^{exp}}{2 \cdot n \cdot t_f \cdot h_f \cdot \varepsilon_{f,eff} \cdot E_f} \quad (7)$$

487 where  $n$  is the number of textile layers applied;  $t_f$  is the equivalent thickness of the textile;  $h_f$  is  
 488 the effective depth of the jacket;  $\varepsilon_{f,eff}$  is the effective strain;  $E_f$  is the elastic modulus of the  
 489 textile; and  $V_{SRG}^{exp}$  and  $V_c^{exp}$  correspond to the experimental values of the shear strength of the  
 490 SRG jackets and the control specimen, respectively. The same expression can be used for

491 calculating the effective strain of the SRG composite,  $\varepsilon_{f,eff}^*$ , if the modulus of elasticity of the  
492 SRG composite,  $E_f^*$ , is used ( column (5) in Table 5).

493 The experimental and the predicted normalized shear stress provided by the SRG system are  
494 calculated from:

$$495 \quad v_{SRG}^{exp} = \frac{V_{SRG}^{exp}}{b_w \cdot d \cdot f_c} \quad (8a)$$

$$496 \quad v_{SRG} = \frac{V_{SRG}}{b_w \cdot d \cdot f_c} \quad (8b)$$

497 where  $b_w$  is the width of the cross section,  $d$  is the depth of the cross section,  $f_c$  is the concrete  
498 compressive strength,  $V_{SRG}^{exp}$  and  $V_{SRG}$  correspond to the experimental and analytical values of  
499 the shear strength of the SRG jackets, respectively.  
500

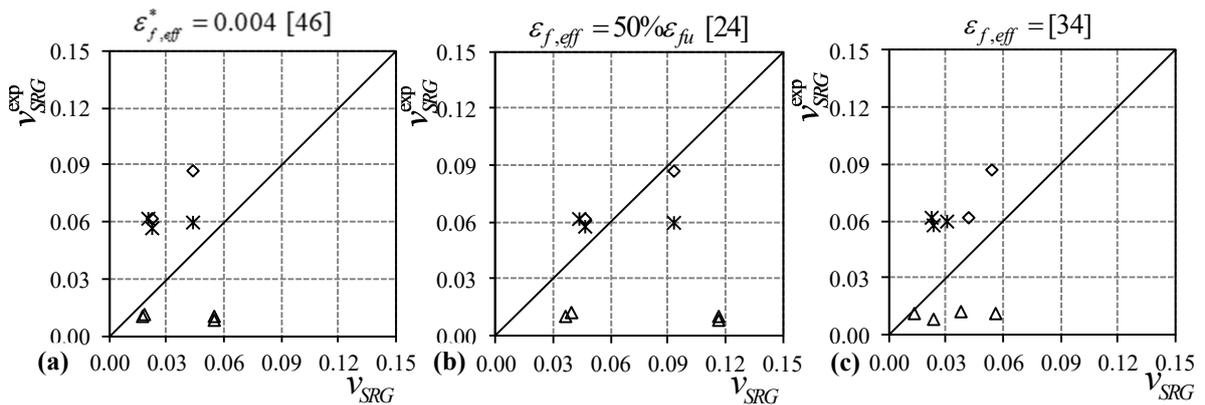
501 Fig. 16 compares the experimental values of the normalized shear stress,  $v_{SRG}^{exp}$ , with the  
502 predicted ones,  $v_{SRG}$ , for the three different definitions of the effective strain,  $\varepsilon_{f,eff}$ , adopted  
503 herein. Based on the observed mode of failure, the beam test data are divided into three  
504 categories; no damage to the textile for beams in Group A, debonding of the textile for the U-  
505 wrapped Group B beams, and rupture of the textile for the fully-wrapped beams of Group B.  
506 The 45° linear lines in Fig. 13 can provide direct insight on whether the adopted model  
507 underestimates or overestimates the predicted values for the shear stress,  $v_{SRG}$ ; and therefore,  
508 determine how safe is to use these particular models. In case of Group A beams, where no  
509 damage was observed in the textile,  $v_{SRG}$  is overestimated for all the three definitions of the  
510 effective strain adopted in this study (see Fig. 13a-c). The ACI 549-9R-13 [46] and Escrig et al.  
511 [34] models generally provided safe results, since the predicted values were lower than the  
512 experimental ones for the beams that failed due to debonding and rupture of the textile (see the

513 points plotted above the linear line in Figs. 13a and 13c). For the same modes of failure, the  
 514 Triantafillou and Papanikolaou [24] model provided both safe and unsafe predictions as  
 515 illustrated in Fig. 13(b).

516 The accuracy of the adopted models is further investigated by employing statistical indices  
 517 such as the mean value (AVR), the standard deviation (STD), the coefficient of variation  
 518 (COV=STD/AVR) and also the average absolute error (AAE) defined as follows:

$$519 \quad AAE = \frac{\sum_{i=1}^N \left| \frac{(v_{SRG})_i - (v_{SRG}^{exp})_i}{(v_{SRG}^{exp})_i} \right|}{N} \quad (9)$$

520 where  $(v_{SRG})_i$  and  $(v_{SRG}^{exp})_i$  represent the predicted and experimental values of the shear strength  
 521 and N corresponds to the total number of beams. Table 6 presents the calculated statistical  
 522 indices for each model based on the mode of failure observed. The minimum AAE value is  
 523 observed for the Triantafillou and Papanikolaou [24] model when rupture and debonding are  
 524 the anticipated modes of failure. For the same modes of failure, the minimum COV corresponds  
 525 to the Escrig et al. [34] model.



526  $\Delta$ No damage – Group A     $\times$ Debonding - U-wrapped Group B     $\diamond$  Rupture - Fully-wrapped Group B

527 Figure 16: Comparison between experimental,  $v_{SRG}^{exp}$ , and predicted,  $v_{SRG}$ , shear strength.

Table 5: Comparison between experimental and predicted values of shear strength

Group	Specimen	Experimental values					Analytical predictions								
		$V_c^{exp}$ (kN)	$V_{shear}^{exp}$ (kN)	$V_{SRG}^{exp}$ (kN)	$\varepsilon_{f,eff}^{*exp}$ $\times 10^3$	$\varepsilon_{f,eff}^{exp}$ $\times 10^3$	$V_c^{ACI}$ (kN)	$V_c^{EC2}$ (kN)	$\varepsilon_{f,eff}^*$ [46]	$\varepsilon_{f,eff}$ [24]	$\varepsilon_{f,eff}$ [34]	$\varepsilon_{f,eff}^*$ [46]	$\varepsilon_{f,eff}$ [24]	$\varepsilon_{f,eff}$ [34]	
									$V_{SRG}$ (kN)	$V_{SRG}$ (kN)	$V_{SRG}$ (kN)	$V_{shear}$ (kN)	$V_{shear}$ (kN)	$V_{shear}$ (kN)	
	(1)	(2)	(3)	(4)=(3)-(2)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)=(7)+(9)	(13)=(8)+(10)	(14)=(8)+(11)	
A	AUH1	47.6	60.8	13.1	0.63	0.56	47.9	27.4	83.3	176.7	35.8	131.2	204.1	63.2	
	AUML	47.6	63.9	16.3	2.55	2.25	47.9	27.4	25.6	54.3	20.1	73.5	81.8	47.6	
	AFL1	47.6	65.8	18.1	2.61	2.31	47.9	27.4	27.8	58.9	57.3	75.7	86.3	84.7	
	AFH1	47.6	63.9	16.3	0.78	0.69	47.9	27.4	83.3	176.7	84.1	131.2	204.1	111.6	
B	BUL1	68.3	146.0	71.9	10.43	9.22	43.4	39.3	27.6	58.5	30.0	70.9	97.7	69.3	
	BUL2	68.3	140.2	74.8	5.42	4.80	43.4	39.3	55.1	116.9	38.2	98.5	156.2	77.5	
	BUML	68.3	143.1	77.6	12.11	10.71	43.4	39.3	25.6	54.3	27.9	69.0	93.6	67.1	
	BFL1	68.3	145.9	77.6	11.25	9.95	43.4	39.3	27.6	58.5	52.5	70.9	97.7	91.8	
	BFL2	68.3	177.4	109.1	7.92	7.00	43.4	39.3	55.1	116.9	66.9	98.5	156.2	106.2	

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534

Table 6: Statistical indices for  $v_{SRG}^{exp}/v_{SRG}$

Statistical indices	No damage			Debonding			Rupture		
	$\epsilon_{f,eff}^*$	$\epsilon_{f,eff}$	$\epsilon_{f,eff}$	$\epsilon_{f,eff}^*$	$\epsilon_{f,eff}$	$\epsilon_{f,eff}$	$\epsilon_{f,eff}^*$	$\epsilon_{f,eff}$	$\epsilon_{f,eff}$
	[46]	[24]	[34]	[46]	[24]	[34]	[46]	[24]	[34]
AVR	3.64	7.72	3.07	0.48	1.03	0.43	0.43	0.91	0.64
STD	2.46	5.23	1.62	0.22	0.47	0.08	0.11	0.22	0.04
COV	67.7%	67.7%	52.7%	45.7%	45.7%	17.9%	24.6%	24.6%	7.0%
AAE	263.9%	671.7%	206.8%	51.6%	35.0%	57.1%	57.0%	15.9%	35.5%

For better comparison, the normalized experimental value of the effective strain,  $\epsilon_{f,eff}^{exp}/\epsilon_{fu}$ , is plotted against the quantity  $\rho_f \cdot E_f/f_c^{2/3}$  in Fig. 17. The term  $\rho_f \cdot E_f$  expresses the axial rigidity of the textile or the composite in case the modulus of elasticity is that of the composite,  $E_f^*$ . The term  $f_c^{2/3}$  is related to the tensile strength of the concrete, where  $f_c$  is the compressive strength of concrete. It is shown in Fig. 17 that, similar to observations made for FRP composites [52],  $\epsilon_{f,eff}^{exp}/\epsilon_{fu}$  decreases as  $\rho_f \cdot E_f/f_c^{2/3}$  increases. The horizontal line corresponds to  $\epsilon_{f,eff}^{exp}/\epsilon_{fu} = 50\%$  [24].

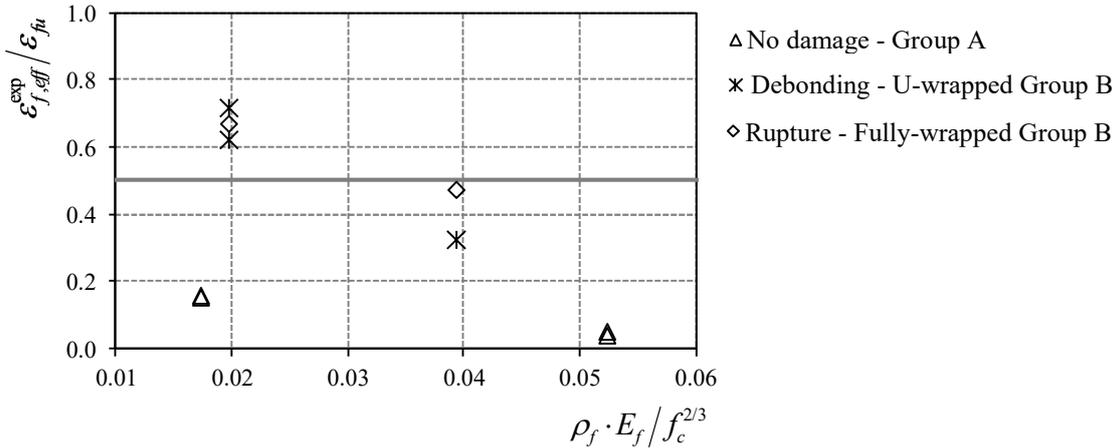


Figure 17: Normalized experimental effective strain,  $\epsilon_{f,eff}^{exp}/\epsilon_{fu}$ , versus  $\rho_f \cdot E_f/f_c^{2/3}$ .

The experimental data were used to derive best fit curves that relate  $\epsilon_{f,eff}^{exp}/\epsilon_{fu}$  to  $\rho_f \cdot E_f/f_c^{2/3}$  as presented in Fig. 18. It should be mentioned that the U-wrapped beams with the mechanical

anchorage (AUML1 and BUML1 in Table 1) were excluded from the utilized data since the objective was to include only specimens where no additional connection measures for the jackets were taken. The following expressions have been derived:

$$\varepsilon_{f,eff} = 0.010 \cdot \left( \frac{f_c^{2/3}}{n \cdot E_f \cdot \rho_f} \right)^{0.47} \cdot \varepsilon_{fu} \quad \text{no damage in the textile} \quad (10a)$$

$$\varepsilon_{f,eff} = 0.015 \cdot \left( \frac{f_c^{2/3}}{n \cdot E_f \cdot \rho_f} \right)^{0.94} \cdot \varepsilon_{fu} \quad \text{side bonded or U-wrapped} \quad (10b)$$

$$\varepsilon_{f,eff} = 0.066 \cdot \left( \frac{f_c^{2/3}}{n \cdot E_f \cdot \rho_f} \right)^{0.59} \cdot \varepsilon_{fu} \quad \text{fully wrapped} \quad (10c)$$

It should be noted that the above equations are based on limited experimental data and need to be verified by more data before used for practical design purposes. However, the results of this study should prove useful in understanding the influence of key design parameters on the effectiveness of shear strengthening of RC beams using SRG jackets.

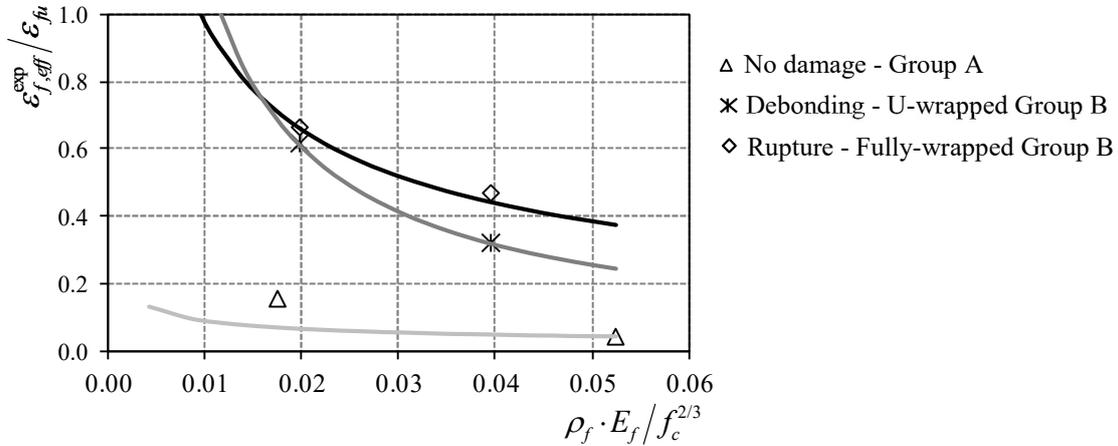


Figure 18: Best fit curves that relate  $\varepsilon_{f,eff}^{exp} / \varepsilon_{fu}$  to  $\rho_f \cdot E_f / f_c^{2/3}$ .

## 5. CONCLUSIONS

An experimental study was carried out to investigate the effectiveness of SRG jacketing as a relatively new composite system for strengthening shear-deficient RC beams. Eleven two-span RC beams were constructed and classified into two groups according to the arrangement of the internal reinforcement. Two of the beams served as control specimens whereas the rest were strengthened with one- or two-layered U-wrapped, U-wrapped with mechanical anchorage and fully-wrapped SRG jackets. Apart from the jacket configuration, parameters of study were the density of the fabric and the number of layers. Digital Image Correlation (DIC) was applied on all specimens to produce strain contours at several characteristic points on the load-displacement response curve. The strain evolution within the critical span and the crack patterns were analysed, while the rupture of the steel cords was verified by the strains diffusion observed in the longitudinal direction. The main conclusions drawn from this study are summarized as follows:

- The different types of SRG jackets applied to the lightly-reinforced Group A beams ( $\rho_l = 0.75\%$ ) could increase the peak load capacity and displacement ductility by up to 38% and 12%, respectively. In all cases the shear failure was prevented, and the response was modified from brittle to ductile.
- The U-wrapped SRG beams of Group B ( $\rho_l = 1.60\%$ ) failed in shear due to detachment of the composite system in the shear-critical region. The use of the suggested mechanical anchorage system could keep the SRG jacket in place for a higher sustained load compared to the U-wrapped SRG beams. The average strength and deflection capacity increase of the U-wrapped beams compared to the control beam was 110% and 70%, respectively.
- The single-layered fully-wrapped SRG jacket applied on Group B beams resulted in a ductile behaviour (displacement ductility  $\mu_s = 3.4$ ) upon failure with the presence of multiple shear-flexure cracks. The two-layered fully-wrapped SRG jacket modified substantially the

response of the original member by allowing it to fail in flexure (displacement ductility  $\mu_s = 3.8$ ). The maximum strength increased to 114 and 160% of that of the original shear deficient beam by using single-layered and two-layered fully-wrapped SRG jackets, respectively.

- The experimental values of the shear stress were compared to the predicted ones utilizing the effective strain as defined by Triantafillou and Papanicolaou [24], Escrig et al. [34] and ACI 549-9R-13 [44]. The minimum AAE value was observed for the Triantafillou and Papanicolaou [24] model when rupture and debonding are the anticipated modes of failure.
- Based on the experimental data of current study, new expressions were developed for estimating the effective strain of the SRG jacket using different jacketing systems as a function of the axial rigidity of the SRG textile. However, more experimental data are required to assess the validity of the proposed expressions before they can be widely adopted.

The results of this study in general indicate that the SRG jacketing can be considered as a promising strengthening technique for shear-deficient RC beams. Further investigation is deemed necessary on the interaction of internal and externally bonded SRG reinforcement.

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