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Sliding-Mode Current Control with Exponential Reaching Law for a Three-Phase Induction Machine Fed by a Direct Matrix Converter

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Abstract: The direct matrix converter (DMC) is considered to be an exciting power converter topology option for electric motor drives in industrial applications (elevators, hoists and cranes) and applications where size and weight are critical (e.g., the aerospace industry). Several control techniques have been developed to exploit the DMC's benefits and achieve the desired performance with classic control techniques, such as field-oriented control and direct torque control, and more sophisticated ones, such as model predictive control and sliding mode control (SMC). SMC is attractive due to its robustness and fast response. However, this control strategy suffers from a phenomenon called chattering. Thus, a solution based on the exponential reaching law (ERL) is implemented to resolve this issue. The proposed method was validated using simulation and experimental results from tests on a three-phase induction machine.

Keywords: current control; direct matrix converter; exponential reaching law; induction machine; sliding mode control



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1. Introduction

Power electronic converters are a fundamental part of applications related to using renewable energies (wind, solar) and propulsion of electric or hybrid vehicles [1,2]. The evolution in the development of power electronic semiconductors has led to the implementation of more efficient, more undersized and more lightweight power converters. These before-mentioned aspects are of outstanding significance in the race for power efficiency, electric-based transportation and the integration of renewables. Consequently, a power electronic converter that has become relevant recently is the direct matrix converter (DMC). The DMC is a direct AC–AC electronic power converter, which transforms AC power directly through an array of bidirectional switches, replacing the traditional AC–AC conversion method with rectification stage, intermediate filters and inversion [3,4]. The following advantages of the DMC have been observed compared to the commonly used back-to-back type power converters:

- Reduced volume as a consequence of the lack of large energy-storage capacitors,
- Decreased conduction losses and
- The option of regeneration of energy from the load to supply because of circuits' natural bi-directionality [5–8].

Furthermore, the DMC can adjust the output voltages, frequencies and amplitudes according to the requirement of the grid or load. However, these advantages do come at the cost of slightly more semiconductor devices and greater complexity in the development of modulation strategies; and at the time of experimental implementation, it requires

considerable computational time, depending on the control strategy to be implemented, so it is crucial to analyse the appropriate digital devices in terms of working bandwidth.

The DMC topology was first proposed in the mid-1970s [9]. At that moment, controllable semiconductor-based power devices were not available. However, in recent decades, industrial and investigation applications of DMCs have risen primarily because of the reduction in the cost of insulated gate bipolar transistor (IGBT) semiconductors, and more recently, silicon carbide-metal-oxide-semiconductor field-effect transistors (SiC-MOSFETs) [10–12].

The three-phase induction machine (IM) has been widely used in industry in low- and medium-power applications. Among the advantages that justify its use are its low cost, simple construction, high robustness and ease of maintenance [13]. High-power applications commonly employ multilevel converters, such as neutral point clamping (NPC) [14,15]. For low- and medium-power ones, the topologies named back-to-back (BTB) and voltage source inverter (VSI) are the most popular choices [16,17]. BTB consists of a two-stage AC-DC-AC conversion that employs huge capacitors for the DC link. This also implies a higher volume and higher weight of the power converter. Note that the DC-bus capacitor is an indispensable component of the VSI and accounts for up to two thirds of the volume of the inverter [18]. As an exciting alternative, the DMC can be considered for electric motor drives in industrial applications (elevators, hoists and cranes) and applications where size and weight are critical (e.g., the aerospace industry) [19].

To apply advanced control techniques to IMs, it is necessary to use a power electronic converter, which allows for regulating the frequency and amplitude of the currents or voltages delivered to the machine [20]. The most widely used three-phase IM control techniques in high-performance applications are field-oriented control (FOC) and direct torque control (DTC) [21,22].

Although there is vast experience in using three-phase IMs, the development of precise and robust control strategies continues to be a significant challenge due to their construction characteristics and nature. They are represented by multivariable mathematical models, in which not all variables are measurable and are also related to each other in a nonlinear way. This produces inaccuracies in controlling and estimating variables when using simplified or linearised systems [23]. With the development of higher-power digital signal processors, cutting-edge control approaches have been presented; some instances include finite-control-set model predictive control (FCS-MPC) and the sliding mode control (SMC) [24]. FCS-MPC is one of the IM's most popular control techniques [25]. FCS-MPC is typically implemented as predictive current control (PCC) or predictive torque control (PTC) in the inner control loop of field-oriented control [26]. Its quick dynamic response and straightforward inclusion of constraints are the main benefits of FCS-MPC [27]. Yet, it suffers from an elevated computational load and highly depends on the system's accurate model. Recently, SMC has appeared as a promising option due to its robustness, easy tuning of controller parameters, fast dynamic response and lack of a need for high computational power [28]. The following are a few recent works on SMC and its applications [29–31]. However, in practice, SMC presents an unwanted phenomenon called chattering, which can be reduced using the exponential reaching law (ERL).

This article presents the DMC as an alternative to feed the three-phase IM and proposes a robust current regulator based on the SMC approach. This innovative system inherits the advantages of both IM machines and the DMC mentioned above. According to the best of the authors knowledge, most of the proposed current control techniques applied to this system fall into deviations of FOC or FCS-MPC. Therefore, the principal contribution of this article focuses on implementing a robust SMC equipped with the ERL. In this context, experimental analyses are presented to validate the proposal and thus contribute to the state-of-the-art of controlling the system mentioned above. The experimental results were obtained by analyzing different conditions, considering stationary and transient operating regimes under different gains of the proposed controller and varying the electrical parameters.

The remainder of the article is organized as follows. Section 2 provides the three-phase IM mathematical model employed for the SMC. Section 3 presents the classical SMC, the sliding surface design and the enhanced SMC, namely, SMC-ERL. The results obtained are given in Sections 4 and 5—simulation and experimental, respectively. Ultimately, the findings future research works are included in Section 6.

2. System Conversion Description

The DMC is connected to an AC voltage source via an input filter, which is intended to prevent over-voltages and reduce high-frequency elements in the input currents. A single-stage converter with $m \times n$ bidirectional power switches connecting an m phase voltage source to an n phase load constitutes the schematic circuit of the DMC, as shown in Figure 1. Each bidirectional switch is identified with a variable S_{ij} , also named the switching function, $i \in \{u, v, w\}$ being the input and $j \in \{a, b, c\}$ the output. Note that S_{ij} can take the following values: $S_{ij} = 1$ (when the switch ij is conducting, on or closed) or $S_{ij} = 0$ (when the switch ij is blocked, off or open). It is important to mention that, in each column, only one switch can be flipped. This is because of the existence of capacitors at the DMC input.

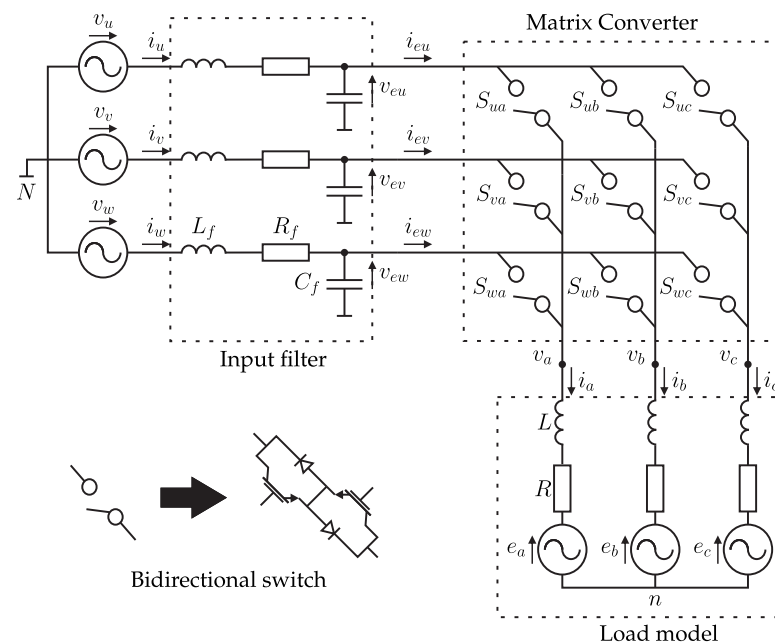


Figure 1. Direct matrix converter schematic circuit.

In addition, due to the load’s inductive nature, it is unthinkable to interrupt the current flowing through it suddenly. Consequently, in each column, at least one switch must be activated. The above constraints can be represented mathematically using the following equation: $S_{uj} + S_{vj} + S_{wj} = 1, \forall j \in \{a, b, c\}$. Under these constraints, the DMC gives 27 possible switching combinations allowed among the $2^9 = 512$ total combinations.

2.1. IM Mathematical Model

The following equations represent the mathematical model of the IM in the state-space representation [32]:

$$\begin{aligned} \dot{\mathbf{x}}(t) &= \mathbf{f}(\mathbf{x}, t) + \mathbf{g} \mathbf{u}(t), \\ \mathbf{y}(t) &= \mathbf{C} \mathbf{x}(t), \end{aligned} \tag{1}$$

being the state vector composed of the stator and rotor currents in (α, β) subspace and the rotor speed as follows: $\mathbf{x}(t) = [i_{s\alpha}, i_{s\beta}, i_{r\alpha}, i_{r\beta}, \omega_r]^T$. In addition, $\mathbf{f}(\mathbf{x}, t)$, \mathbf{g} and \mathbf{C} are given by:

$$f(\mathbf{x}, t) = \mathcal{L} \begin{bmatrix} L_r R_s i_{s\alpha} - L_m^2 \omega_r i_{s\beta} - L_m R_r i_{r\alpha} - L_m L_r \omega_r i_{r\beta} \\ L_m^2 \omega_r i_{s\alpha} + L_r R_s i_{s\beta} + L_m L_r \omega_r i_{r\alpha} - L_m R_r i_{r\beta} \\ -L_m R_s i_{s\alpha} + \omega_r L_m L_s i_{s\beta} + R_r L_s i_{r\alpha} + \omega_r L_r L_s i_{r\beta} \\ -\omega_r L_m L_s i_{s\alpha} - L_m R_s i_{s\beta} - \omega_r L_r L_s i_{r\alpha} + R_r L_s i_{r\beta} \\ \left(-\frac{B}{J} \omega_r + P^2 \frac{L_m}{J} (i_{r\alpha} i_{s\beta} - i_{r\beta} i_{s\alpha}) - \frac{P}{J} T_L\right) \frac{1}{\mathcal{L}} \end{bmatrix}, \quad (2)$$

$$g = \mathcal{L} \begin{bmatrix} -L_r & 0 \\ 0 & -L_r \\ L_m & 0 \\ 0 & L_m \\ 0 & 0 \end{bmatrix}, \quad (3)$$

$$\mathcal{L} = (L_m^2 - L_s L_r)^{-1}, \quad (4)$$

$$\mathbf{C} = \begin{bmatrix} 1 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 \end{bmatrix}. \quad (5)$$

The input vector consists of the stator voltage and is written as follows: $\mathbf{u} = [u_{s\alpha}, u_{s\beta}]^T$. On the other hand, the output vector is composed of the stator current and is given by: $\mathbf{y} = [i_{s\alpha}, i_{s\beta}]^T$. Rotor currents are estimated, since they cannot be measured [33–35].

2.2. Classic SMC

The SMC is a nonlinear control technique that has been verified to be an efficacious, robust control strategy for nonlinear systems or systems whose modelling is incomplete. The SMC is a discontinuous control action that switches between two system structures. Then, a system movement named a sliding mode exists on a sliding surface that produces desensitisation to the variation of parameters and total immunity to external disturbances. This mentioned attribute can be considered the most remarkable one of the SMC.

In general, the SMC has an unwanted phenomenon called chattering, which is generally perceived as oscillating around the sliding surface. This phenomenon causes inaccuracies in control, losses due to the Joule effect in the electrical circuits and high wear of the moving mechanical parts [36,37], which is why it must be minimised.

2.3. SMC Design

Several SMC design methods can be found in the literature, mainly consisting of two phases. The foremost concerns the design of a sliding surface $S(\mathbf{x}, t)$ that fulfills the expected performance during the sliding phase. Then, the second phase focuses on designing a control effort $\mathbf{u}(t)$. The aim is that the expected performance is achieved and maintained. Therefore, $\mathbf{u}(t)$ guides the system to reach the sliding surface in a finite time. Figure 2b illustrates the state trajectory's evolution composed of both mentioned phases.

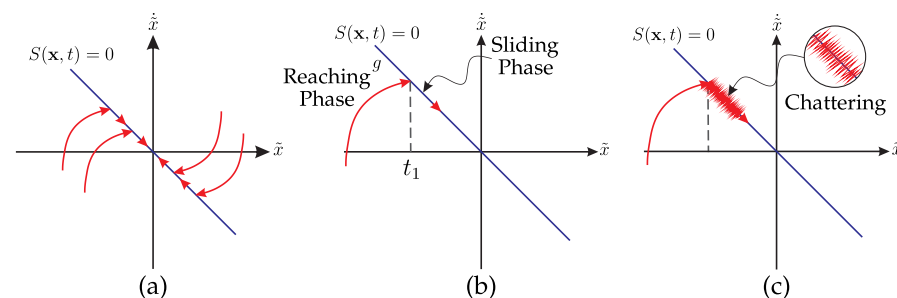


Figure 2. Graphic interpretation of the SMC. (a) State trajectories. (b) Evolution of the state trajectory. (c) Chattering.

2.3.1. Sliding Surface Design

Consider the nonlinear system described by (1), with $\mathbf{x}(t)$ being the state variables and $\mathbf{u}(t)$ the control input. The following are continuous functions in \mathbf{x} : $f(\mathbf{x}, t)$ and g [37,38]. The control slogan is to keep track of the status of the $\mathbf{x}(t)$ to track a variant state in the desired time frame $\mathbf{x}_d(t)$ in the presence of inaccuracies in the model of the $f(\mathbf{x}, t)$ y g . In order that tracking is possible using a finite control input $\mathbf{u}(t)$, the initial value of the desired state $\mathbf{x}_d(0)$ should be such that $\mathbf{x}_d(0) = \mathbf{x}(0)$. Otherwise, follow-up is achieved after a transient [39].

Let $\epsilon(t)$ be the tracking error vector in \mathbf{x} . Then, the following equation defines the time-invariant surface $S(\mathbf{x}, t)$, in the state-space \mathbb{R}^n :

$$S(\mathbf{x}, t) = \left(\frac{d}{dt} + \Lambda \right)^{(n-1)} \epsilon(t), \quad (6)$$

Λ being a positive definite diagonal matrix. Thus, the $\mathbf{x}(t)$ tracking problem is equivalent to the problem of staying on the surface $S(\mathbf{x}, t)$ for all $t > 0$. Indeed, $\epsilon(t) \equiv 0$ is the only solution of the linear differential equation represented by $S(\mathbf{x}, t) \equiv 0$ [39].

An analogous result is acquired using integral control, i.e., by establishing $\int_0^t \epsilon(t) dt$ as the variable of interest. In this case, the sliding surface is represented as:

$$S(\mathbf{x}, t) = \left(\frac{d}{dt} + \Lambda \right)^{(n-1)} \int_0^t \epsilon(t) dt. \quad (7)$$

The effective reduction of chattering is achieved using the integral sliding surface to design the switching function, and the accuracy of the SMC is improved [40].

2.3.2. Control Effort Design

The control input in SMC is designed to reach the sliding surface $S(\mathbf{x}, t) = 0$, and then moves on it indefinitely [37]. It is composed of a sliding phase and a reaching phase. The former spans from the initial state to the intersection with the sliding surface, and the latter spans from the intersection with the sliding surface to the origin [38]. Figure 2a shows the state trajectories reaching the sliding surface. In Figure 2c, the phenomenon called chattering is observed, and in Figure 2b, the evolution of one of the state trajectories can be observed in more detail.

This gives rise to the so-called “range condition”, which must be satisfied by manipulating the control input $\mathbf{u}(t)$. It can be written as $S^T(\mathbf{x}, t) \dot{S}(\mathbf{x}, t) < 0$ and ensures that the trajectory of the system states always points to the sliding surface.

2.3.3. SMC-ERL Design

The range law specifies the dynamics of the switching function. The constant ratio scope law is given by $\dot{S} = -Y \text{sign}(S)$, where Y represents the constant ratio. Under this law, the switching variable is constrained to reach the sliding surface at a constant velocity. This law is notable for its simplicity. However, the choice of a minimal value for Y causes a very high reach time, and a huge value can cause severe chattering.

The ERL is represented by $\dot{S} = -Y \text{sign}(S) - K S$. Note that including the proportional term improves the convergence ratio when the value of the sliding variable is relatively large. Consequently, smaller values in the Y constant can be used without renouncing propitious effects in the range phase. However, the proportional term decreases in the vicinity of the switching surface, which allows chattering to decrease [41].

3. Design of Current Controllers Based on SMC Technique

The schematic of the system to implement the current control based on the sliding mode technique is shown in Figure 3. Two stages can be distinguished: the power stage and the control stage. The power stage comprises the DMC, an input filter, the clamp

protection circuit and a three-phase IM. The control stage includes the control block and the other blocks necessary for its implementation.

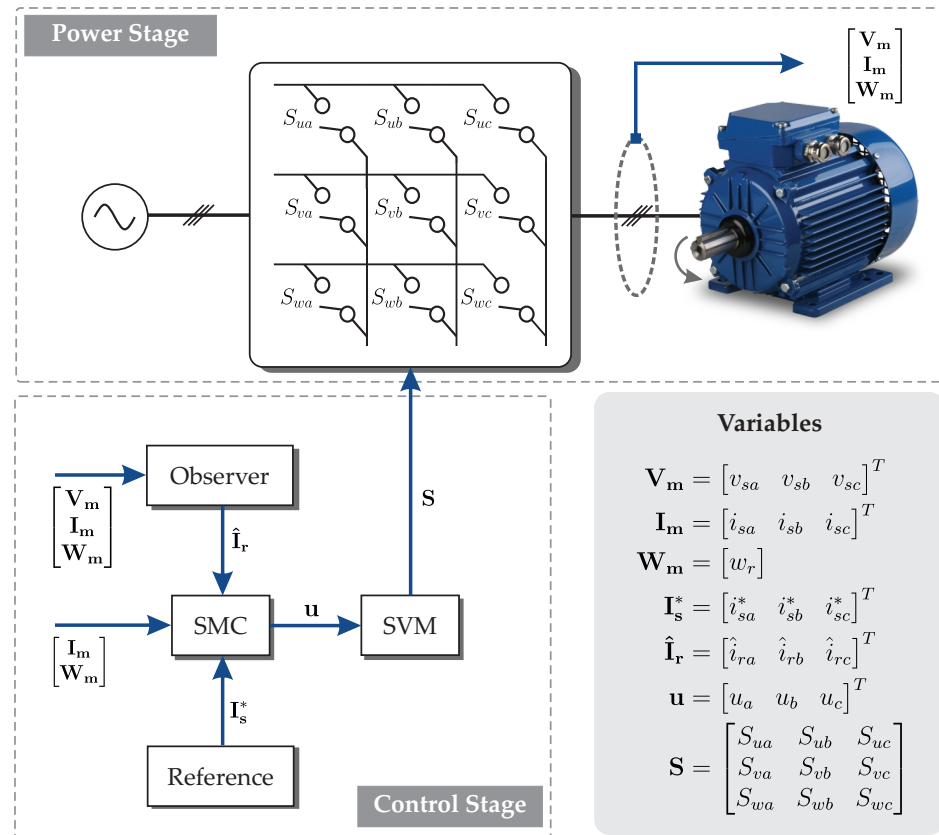


Figure 3. Proposed control method based on the SMC.

The output vector must be forced to follow the reference current so that $\mathbf{y}^*(t) = [i_{sa}^*, i_{sb}^*]^T$, since the stator currents are the variables to be controlled. Then, $\mathbf{e}(t) = \mathbf{y}(t) - \mathbf{y}^*(t) = \mathbf{C}\boldsymbol{\epsilon}(t)$ is the tracking error vector. Subsequently, the sliding surface is designed as follows, using integral control:

$$S(\mathbf{x}, t) = \mathbf{e}(t) + \Lambda \int_0^t \mathbf{e}(t) dt, \tag{8}$$

where Λ is:

$$\Lambda = \begin{bmatrix} \lambda_1 & 0 \\ 0 & \lambda_2 \end{bmatrix}.$$

The following equation is obtained by performing the first derivative of (8):

$$\begin{aligned} \dot{S}(\mathbf{x}, t) &= \dot{\mathbf{e}}(t) + \Lambda \mathbf{e}(t) \\ &= \dot{\mathbf{y}}(t) - \dot{\mathbf{y}}^*(t) + \Lambda \mathbf{e}(t) \\ &= \mathbf{C}\dot{\mathbf{x}}(t) - \dot{\mathbf{y}}^*(t) + \Lambda \mathbf{e}(t) \\ &= \mathbf{C}(f(\mathbf{x}, t) + \mathbf{g}\mathbf{u}(t)) - \dot{\mathbf{y}}^*(t) + \Lambda \mathbf{e}(t) \\ &= \mathbf{C}f(\mathbf{x}, t) + \mathbf{C}\mathbf{g}\mathbf{u}(t) - \dot{\mathbf{y}}^*(t) + \Lambda \mathbf{e}(t). \end{aligned} \tag{9}$$

Then, $\mathbf{u}(t)$ can be acquired from (9), and the following expression for the control input is obtained:

$$\mathbf{u}(t) = (\mathbf{C}\mathbf{g})^{-1} (\dot{S}(\mathbf{x}, t) - \mathbf{C}f(\mathbf{x}, t) + \dot{\mathbf{y}}^*(t) - \Lambda \mathbf{e}(t)). \tag{10}$$

The inverse of $\mathbf{C}g$ always exists and is represented by:

$$(\mathbf{C}g)^{-1} = \begin{bmatrix} -\mathcal{L}/L_r & 0 \\ 0 & -\mathcal{L}/L_r \end{bmatrix}. \quad (11)$$

3.1. Classic SMC

The controller based on the constant ratio range law is the simplest form of SMC implementation. In this method, the derivative of the sliding surface is expressed as follows:

$$\dot{S}(\mathbf{x}, t) = -\mathcal{K}_1 \text{sign}(S(\mathbf{x}, t)), \quad (12)$$

where the matrix $\mathcal{K}_1 = \text{diag}(k_{11}, k_{12})$ is a positive definite diagonal matrix. In addition, for $i = 1, 2$ the function $\text{sign}(S(\mathbf{x}, t)) = [\text{sign}(s_1), \text{sign}(s_2)]^T$ is defined as follows:

$$\text{sign}(s_i) = \begin{cases} 1, & \text{si } s_i > 0, \\ 0, & \text{si } s_i = 0, \\ -1, & \text{si } s_i < 0. \end{cases} \quad (13)$$

From (10) and (12), the control input is obtained:

$$\mathbf{u}(t) = (\mathbf{C}g)^{-1} (-\mathcal{K}_1 \text{sign}(S(\mathbf{x}, t)) - \mathbf{C}f(\mathbf{x}, t) + \dot{\mathbf{y}}^*(t) - \Lambda \mathbf{e}). \quad (14)$$

The stability of the system using this control law is assured, and the demonstration can be found in [36].

3.2. Current Controller Based on SMC-ERL

The exponential range law is used in the SMC design to reduce chattering [42]. The ERL selects an exponential term capable of adapting to variations in the switching function. Thus, the derivative of the sliding surface is expressed as:

$$\dot{S}(\mathbf{x}, t) = -\mathcal{K}_1 S(\mathbf{x}, t) - \mathcal{K}_2(S(\mathbf{x}, t)) \text{sign}(S(\mathbf{x}, t)), \quad (15)$$

where the function $\text{sign}(S(\mathbf{x}, t)) = [\text{sign}(s_1), \text{sign}(s_2)]^T$ is defined as in (13), the matrix $\mathcal{K}_1 = \text{diag}(k_{11}, k_{12})$ is a positive definite diagonal matrix and the matrix $\mathcal{K}_2(S(\mathbf{x}, t))$ is defined as follows:

$$\mathcal{K}_2(S(\mathbf{x}, t)) = \begin{bmatrix} k_{21}/N(s_1) & 0 \\ 0 & k_{22}/N(s_2) \end{bmatrix}, \quad (16)$$

where $N(s_i)$ is:

$$N(s_i) = \gamma_0 + (1 - \gamma_0)e^{-\alpha|s_i|^p}, \quad (17)$$

for $i = 1, 2$, with γ_0 being a positive constant less than one, p a positive integer and α a positive constant.

As for (10) and (15), the control input is obtained:

$$\mathbf{u}(t) = (\mathbf{C}g)^{-1} (-\mathcal{K}_1 S(\mathbf{x}, t) - \mathcal{K}_2(S(\mathbf{x}, t)) \text{sign}(S(\mathbf{x}, t)) - \mathbf{C}f(\mathbf{x}, t) + \dot{\mathbf{y}}^*(t) - \Lambda \mathbf{e}). \quad (18)$$

Stability using this control law is also assured, and a detailed demonstration is given in the following subsection. Both (10) and (18) then pass through the modulation stage, which is based on the space vector modulation (SVM) [43].

3.3. Stability Analysis

Consider the following Lyapunov function candidate:

$$V = \frac{1}{2} S^T S. \quad (19)$$

The system is stable if the variation of V is always decreasing:

$$\dot{V} = S^T \dot{S}. \quad (20)$$

Then, using (9) and (15), we obtain:

$$\dot{S} = \dot{e} + \Lambda e = -\mathcal{K}_1 S - \mathcal{K}_2 \text{sign}(S), \quad (21)$$

$$\begin{aligned} \dot{S} &= \mathbf{C}f(\mathbf{x}, t) + \mathbf{C}g(\mathbf{x}, t)\mathbf{u}(t) - \dot{\mathbf{y}}^*(t) + \Lambda \mathbf{e}(t) \\ &= -\mathcal{K}_1 S(\mathbf{x}, t) - \mathcal{K}_2(S(\mathbf{x}, t)) \text{sign}(S(\mathbf{x}, t)). \end{aligned} \quad (22)$$

The control law in (18) can be obtained using the above relation. Then,

$$\begin{aligned} \dot{V} &= S^T [-\mathcal{K}_1 S(\mathbf{x}, t) - \mathcal{K}_2(S(\mathbf{x}, t)) \text{sign}(S(\mathbf{x}, t))] \\ &= -S^T \mathcal{K}_1 S - S^T \mathcal{K}_2(S) \text{sign}(S) \\ &= -S^T \mathcal{K}_1 S - \sum_{i=1}^2 \frac{k_i}{N(s_i)} s_i \text{sign}(s_i). \end{aligned} \quad (23)$$

$\dot{V} < 0$ since the first term on the right $-S^T \mathcal{K}_1 S < 0$ and $-\frac{k_i}{N(s_i)} s_i \text{sign}(s_i) < 0$ for k_1 and k_2 greater than zero, and $0 < \gamma < 1$, a & $p > 0$.

4. Simulation Results

A simulation environment has been designed in the Matlab/Simulink program. Table 1 lists the parameters of the IM used in the simulation environment. The gains of the designed current controllers, all obtained heuristically, are $\lambda_1 = \lambda_2 = 100$, $k_{11} = k_{12} = 100$ and $k_{21} = k_{22} = 0.5$.

Table 1. IM parameters.

Parameter	Symbol	Value	Unit
Nominal power	P_n	6.875	VA
Supply voltage	V_s	380	V
Nominal frequency	f	50	Hz
Stator resistance	R_s	5.95	Ω
Rotor resistance	R_r	3.95	Ω
Stator loss inductance	L_{ls}	7.7	mH
Rotor loss inductance	L_{lr}	5.1	mH
Magnetising inductance	L_m	430	mH
Friction coefficient	B	0.000503	Nm·s
Moment of inertia	J	0.07	kg·m ²
Pole pairs	P	2	

4.1. Steady-State Analysis

The classic SMC and SMC-ERL behaviour is analysed using a reference frequency of 50 Hz and a reference current amplitude $i_{sa}^* = 4$ A. In Figure 4, the stator current is denoted i_{sa} . In the tests shown in Figure 4, the values 0.4950 A and 0.3266 A were computed for the root mean-square error (RMSE) of the classic SMC and SMC-ERL controllers, respectively. It can be observed that the SMC-ERL controller performs better tracking of the current reference compared to the classic SMC. Moreover, it produces less chattering in the stator current. Therefore, it can be observed that the SMC-ERL controller achieves better current tracking than the classic one.

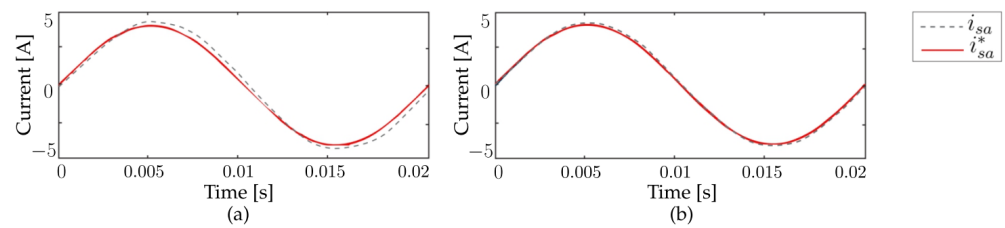


Figure 4. Simulation of the designed control algorithms. (a) Classic SMC controller. (b) SMC-ERL controller.

Next, both controllers' total harmonic distortion (THD) is analysed. For this purpose, $i_{sa}^* = 3$ A and a frequency of 50 Hz are established. The THD values obtained for the classic SMC and SMC-ERL were 2.52% and 1.28%, respectively.

Considering that the simulation results show that the SMC-ERL controller performs better than the classic SMC, the subsequent tests were conducted using only the proposed SMC-ERL controller.

4.2. SMC-ERL Gain Tuning

For the realisation of these tests, the gains \mathcal{K}_1 , \mathcal{K}_2 and Λ were varied individually to observe the effect on the stator current tracking for the values chosen in each case. It is possible to notice that the reference tracking was correctly performed in all cases. In Figure 5a,b, it is observed that for small values of the gains $k_{11} = k_{12}$, there is a more considerable difference between the measured value and the stator current reference value that becomes more noticeable as it approaches the peak values. In return, the increase in gain value is accompanied by the rise in chattering. Therefore, a trade-off is established when choosing the value of the gains $k_{11} = k_{12}$. A similar result is obtained by varying the values of the gains $k_{21} = k_{22}$, as can be seen in Figure 5c,d.

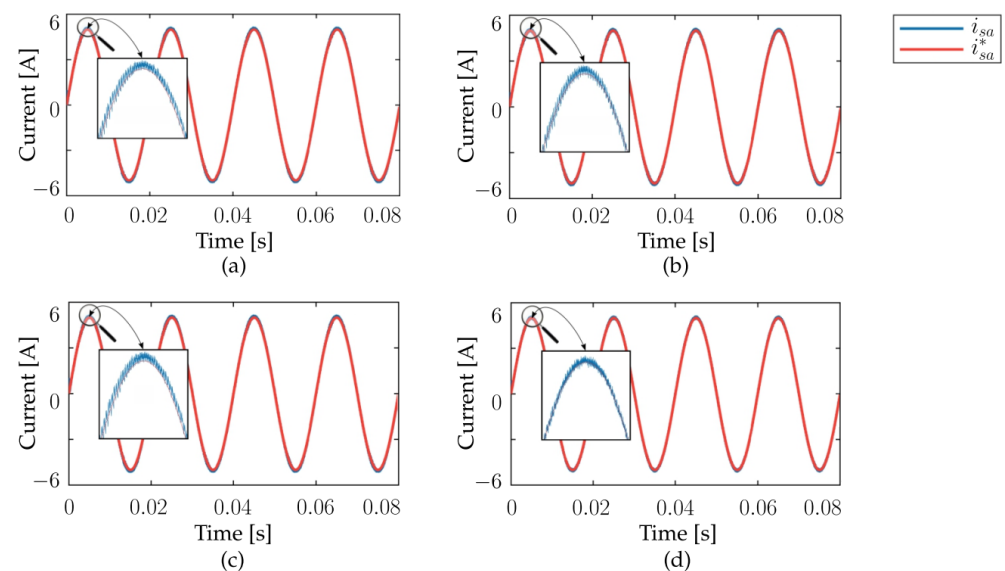


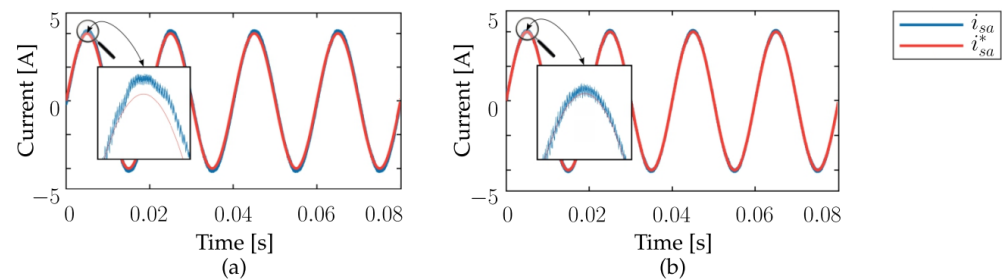
Figure 5. Gain adjustment results. (a) $\mathcal{K}_1 = 1$ and (b) $\mathcal{K}_1 = 1000$. (c) $\mathcal{K}_2 = 0.01$ and (d) $\mathcal{K}_2 = 100$.

The results obtained by varying the value of the gains $\lambda_1 = \lambda_2$ are shown in Figure 6. These show that for larger values of the studied gains, the stator current waveform fits better to the reference. However, unlike the gains so far analysed, the magnitude of the chattering is unaffected mainly by increasing the value of $\lambda_1 = \lambda_2$.

The statements made from the visual inspection were verified by calculating the RMSE for each test presented. The results shown in Table 2 ratify these statements, since it can be observed that for each case with a higher gain value, the RMSE decreases; therefore, the current tracking method is better.

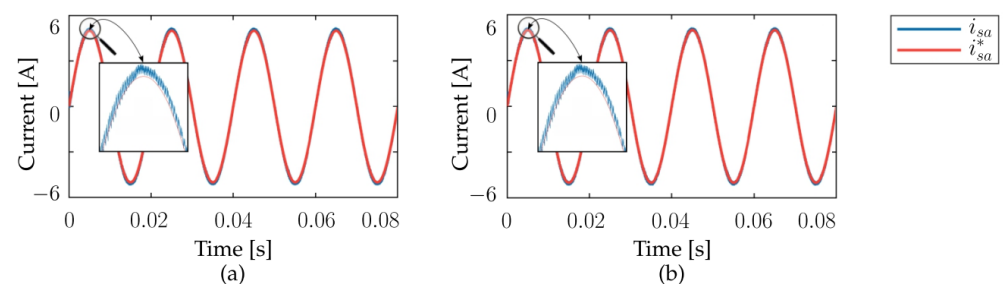
Table 2. RMSE in gain adjustment.

Gain	Values	RMSE (A)
$k_{11} = k_{12}$	1	0.0553
	1.000	0.0431
$k_{21} = k_{22}$	0.01	0.0549
	100	0.0311
$\lambda_1 = \lambda_2$	100	0.1378
	1.500	0.0463

**Figure 6.** Gain adjustment results. (a) $\Lambda = 0.0001$. (b) $\Lambda = 2000$.

4.3. Sensitivity Analysis to Parameter Variation

The datasheet provided by the manufacturer of the IM establishes 430 mH as the value of the mutual inductance. This test was carried out to observe the behaviour of the designed SMC-ERL controller in the presence of parametric uncertainties. First, a mutual inductance value lower than the one provided by the manufacturer's datasheet was chosen, and it was observed that the current tracking persisted. However, at peak values, the stator current briefly exceeded the reference current, adjusting to the same, as shown in Figure 7a. A similar result was obtained by choosing a mutual inductance value higher than that provided by the manufacturer's datasheet, as seen in Figure 7b. The RMSE values obtained were 0.0629 and 0.0468 A for mutual inductances of 230 and 630 mH, respectively. With these tests, it is possible to demonstrate that the designed controller behaves adequately concerning its immunity to the presence of parametric uncertainties.

**Figure 7.** Results obtained from the variation of the parameter L_m . (a) $L_m = 230$ mH. (b) $L_m = 630$ mH.

4.4. Analysis in Response to Frequency Variation of the Reference Current

The stator current tracking test for different frequency values of the reference current can be seen in Figure 8. Different frequency values were chosen to carry out this test. The gain values remained constant in all cases and were determined heuristically.

This test shows that for a given value of the current amplitude, as the current frequency increases, the differences between the measured and reference stator current values at the peaks increase.

These observations were again contrasted with the RMSE, obtaining values of 0.0455 and 0.0590 A for frequencies of 50 and 100 Hz, respectively. The RMSE values confirm that the differences between the measured and reference current increase for higher frequencies.

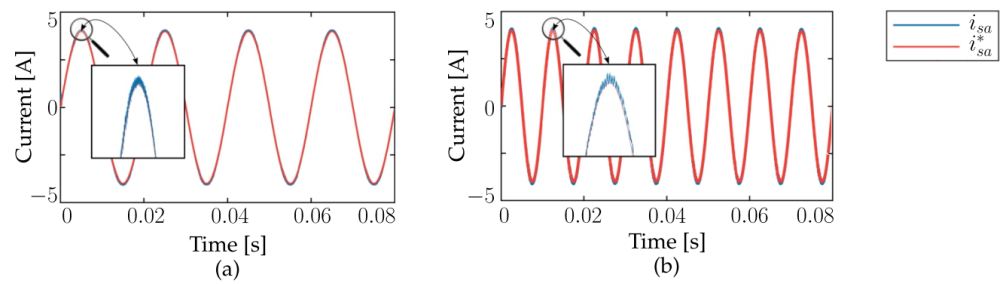


Figure 8. Current tracking results at different frequency values of the reference current. $i_{sa}^* = 4$ A. (a) $f = 50$ Hz. (b) $f = 100$ Hz.

4.5. Analysis of Electrical Frequency Variation

This test was performed to observe the stator current tracking upon an abrupt change in the frequency value (increase or decrease). As shown in Figure 9, the controller momentarily lost the reference tracking with an abrupt change in the frequency value. However, it recovered almost instantaneously. The same test could be repeated after an instant, obtaining the same results. Therefore, it was demonstrated that the designed controller has a fast response to transient changes.

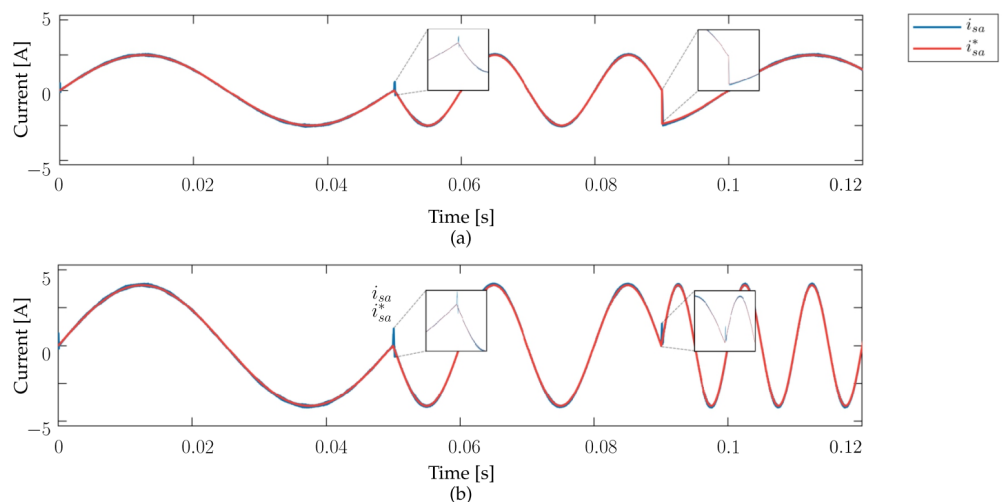


Figure 9. Current tracking results visualized as frequency changes. (a) Reference from 20 to 50 Hz and return to 20 Hz. (b) Reference from 20 to 50 and finally 100 Hz.

5. Experimental Results

This section presents the results of the experimental validation of the SMC-ERL applied to the current control of a three-phase IM fed by the DMC. For this purpose, an experimental platform whose main components are shown in Figure 10 was used. The DMC was based on SCH2080KE SiC-MOSFETs. The same figure shows the clamp circuit, which provides surge protection for the DMC. The voltage and current sensor boards obtained the magnitudes of the signals and delivered them to the MicroLabBox dSPACE in charge of executing the control algorithms. In turn, the NEXYS 3 field-programmable gate array (FPGA) was used to implement switching algorithms for the SiC-MOSFETs. The signals were transmitted to the bidirectional switches through fibre-optic cables. The IM acts as the load, and the encoder is used to measure the rotational speed of the machine.

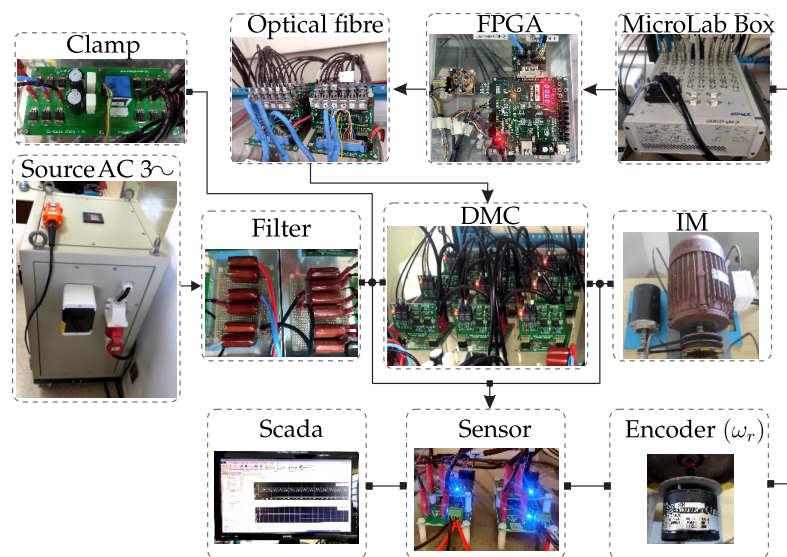


Figure 10. Experimental test bench.

5.1. Steady-State Analysis of SMC-ERL

For the steady-state analysis of the reference stator current tracking i_{sa}^* , a frequency of 50 Hz and an amplitude of 4 A were used. The gains of both controllers were the same as those used in the simulation environment. In Figure 11 it is possible to observe the behaviour of the designed control algorithms, the classic SMC controller and the SMC-ERL controller, respectively. The experimental results agree with the simulated tests and show that the measured stator current is better matched to the reference value using the SMC-ERL controller. Furthermore, it can be observed that the voltage waveform applied on the load has an approximately sinusoidal shape using the SMC-ERL controller, whereas with the classic SMC controller, the voltage waveform is noisier and less sinusoidal. The same results were seen when calculating the RMSE. The classic SMC gave a value of 0.4950 A, and the SMC-ERL controller, 0.3266 A.

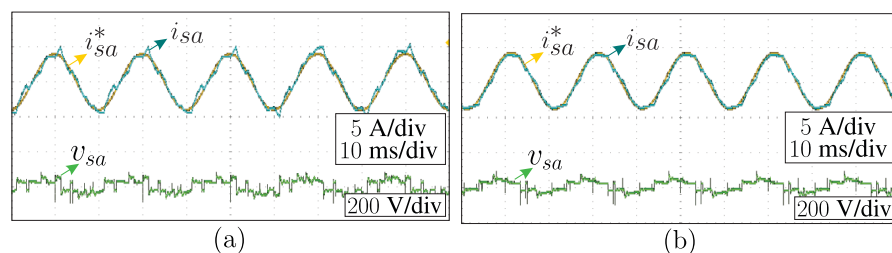


Figure 11. Experimental results of designed algorithms: (a) Classic SMC. (b) SMC-ERL.

5.2. SMC-ERL Gain Adjustments

The experimental validation was carried out identically to the test performed through simulations. For this purpose, the controller gains were adjusted, starting with small values, and one of them was increased, leaving the others constant. The results obtained for the gain adjustment K_1 are shown in Figure 12a,b. It is possible to quantify the RMSE values obtained in Table 3. Similar results were obtained by varying the values of the gains K_2 and Λ , as can be seen in Figure 12c,d and Figure 13, respectively.

Table 3. RMSE in the gain adjustment.

Gain	Value	RMSE (A)
$k_{11} = k_{12}$	1	0.4699
	1.000	0.3826
$k_{21} = k_{22}$	0.01	0.5257
	100	0.4663
$\lambda_1 = \lambda_2$	100	0.4467
	1.500	0.2683

While it has been shown that the stator current tracking is better at higher gain values, there is a trade-off between gain value and chattering magnitude. In that context, it is not recommended to increase indefinitely any of the gains of the SMC-ERL-based controllers.

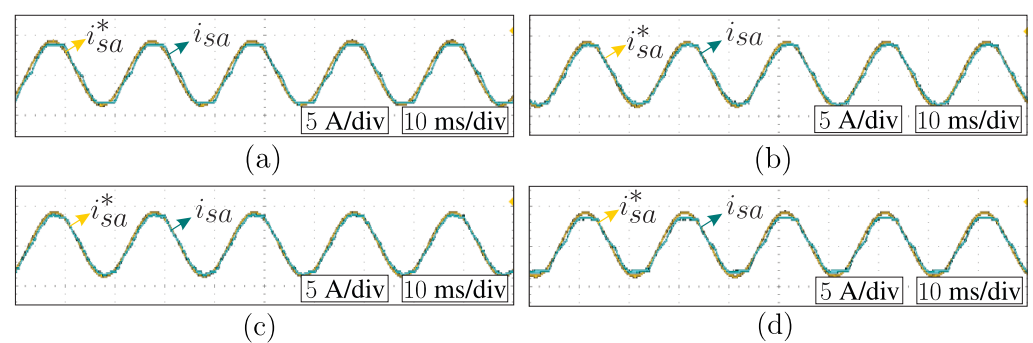


Figure 12. Gain adjustment validation, K_1 and K_2 . (a) $K_1 = 1$. (b) $K_1 = 1000$ (c) $K_2 = 0.01$. (d) $K_2 = 100$.

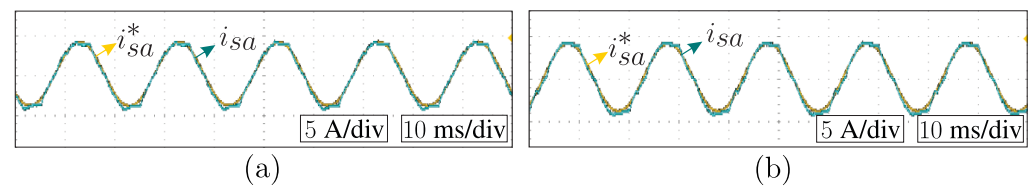


Figure 13. Gain adjustment validation, Λ . (a) $\Lambda = 0.0001$. (b) $\Lambda = 2000$.

5.3. Sensitivity Analysis to Parameter Variation

The controller’s immunity to parametric uncertainties is a desirable feature of the SMC. Tests were performed by varying the value of the magnetisation inductance to validate this feature, thereby obtaining the results shown in Figure 14. The RMSE values calculated in this case were 0.3454 and 0.3396 A for inductances of 230 and 630 mH, respectively. Therefore, even though the value used for the magnetisation inductance parameter was not exact, the reference tracking was established and maintained over time. Note that the variation in L_m implies variation in the whole dynamics, since $f(x, t)$ and g are in terms of this inductance [44]. The simulation and experimental results proved the robustness of the developed SMC-ERL method against parameter variations.

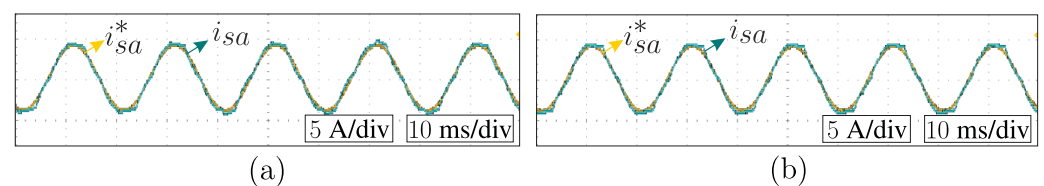


Figure 14. Results of L_m parameter variation. (a) $L_m = 230$ mH. (b) $L_m = 630$ mH.

5.4. Analysis against the Variation of Frequency of the Reference Current

Figure 15 shows the analysis of the follow-up of the stator current when varying its frequency from 50 to 100 Hz. The RMSE values obtained were 0.3066 A and 0.5604 A for frequencies of 50 and 100 Hz, respectively. Good current tracking was observed in both cases.

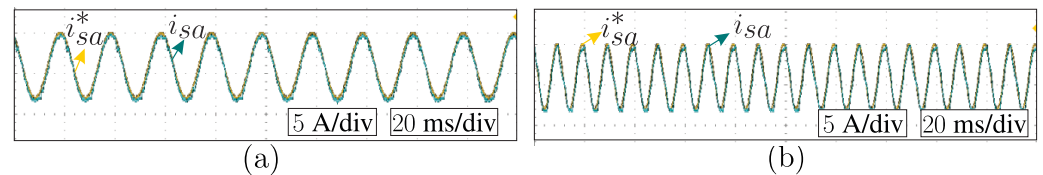


Figure 15. Current tracking performance. $i_{sa}^* = 4$ A, (a) $f = 50$ Hz (b) $f = 100$ Hz.

5.5. Analysis against Variation in the Electrical Frequency

Abrupt changes in the value of the frequency of the current reference signal were applied to analyse the designed controller's behaviour under electrical frequency changes, and the controller's response to these changes was observed. The results are presented in Figure 16. It is possible to observe that when an abrupt change in the frequency of the reference signal occurred (increase or decrease), the measured stator current lost track for a short period of time. However, tracking was again achieved and maintained for the remainder of the test.

The results obtained in the experimental validation present the expected behaviour, since they are similar to those obtained with the simulated tests, even when the quantitative metrics present differences. These differences are entirely attributable to unavoidable measurement errors and inaccuracies in the model of the plant under study. Therefore, the results highlight that the controller's performance was as expected under the operating circumstances imposed in each case.

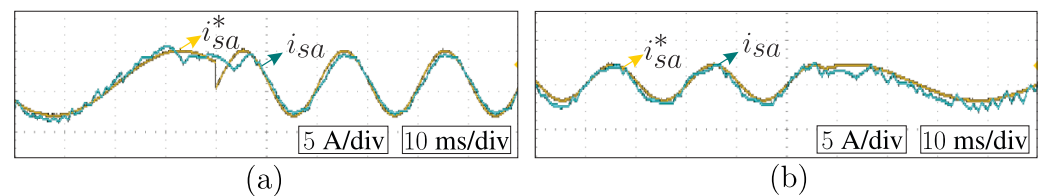


Figure 16. Current tracking performance compared to reference frequency changes. (a) Reference from 20 to 50 Hz. (b) Reference from 50 to 20 Hz.

6. Conclusions

In this paper, a theoretical study based on computational simulations has been presented, and subsequently, the experimental validation of nonlinear control algorithms based on the sliding mode technique applied to a direct matrix converter with a three-phase IM as a load has been considered. The method uses the exponential reaching law technique to reduce the chattering present in sliding mode-based controllers.

From the results obtained, it can be confirmed that the proposed control strategy is robust to variations in machine parameters and has a fast transient response. In this sense, it is concluded that the control technique presented in this work is attractive as an alternative to the current control techniques usually implemented for three-phase electrical drives powered by matrix converters.

This paper demonstrated that with modifications, the SMC can include more terms to reduce chattering. The comparison between SMC and SMC-ERL gave us the motivation to address an exhaustive comparison of the proposed methods against others, such as FOC, DTC and FCS-MPC, as a near-future research topic. Moreover, this paper opens the door for a niche applications of other nonlinear control techniques, such as higher-order SMC, fuzzy logic and backstepping, in this exciting system.

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Abbreviations

The following abbreviations are used in this manuscript:

BTB	Back-to-back
DMC	Direct matrix converter
DTC	Direct torque control
ERL	Exponential reaching law
FCS-MPC	Finite-control-set model predictive control
FOC	Field oriented control
FPGA	Field-programmable gate array
IGBT	Insulated gate bipolar transistor
IM	Induction machine
NPC	Neutral point clamped
PCC	Predictive current control
PTC	Predictive torque control
RMSE	Root mean square error
SiC-MOSFETs	Silicon carbide-metal-oxide-semiconductor field-effect transistors
SMC	Sliding mode control
SVM	Space vector modulation
THD	Total harmonic distortion
VSI	Voltage source inverter

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